

The physics of black hole binaries: geodesic properties, quasinormal modes and interaction with fundamental fields

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2. Construction of BH binary spacetime
3. Our results
 - a. global closed null geodesic
 - b. global QNM
 - c. superradiant like instability (ongoing work)
4. Summary

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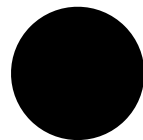
4. Summary

Black hole binary

- Compared with single BH, BH binary spacetime is not deeply understood.

Black Hole

- closed null geodesic
- Quasi normal mode
- Superradiance



Black Hole Binary

- “Global ” closed null geodesic ?
- “Global” Quasi normal mode ?
- Superradiance like mechanism ?



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Approximate BHB spacetime

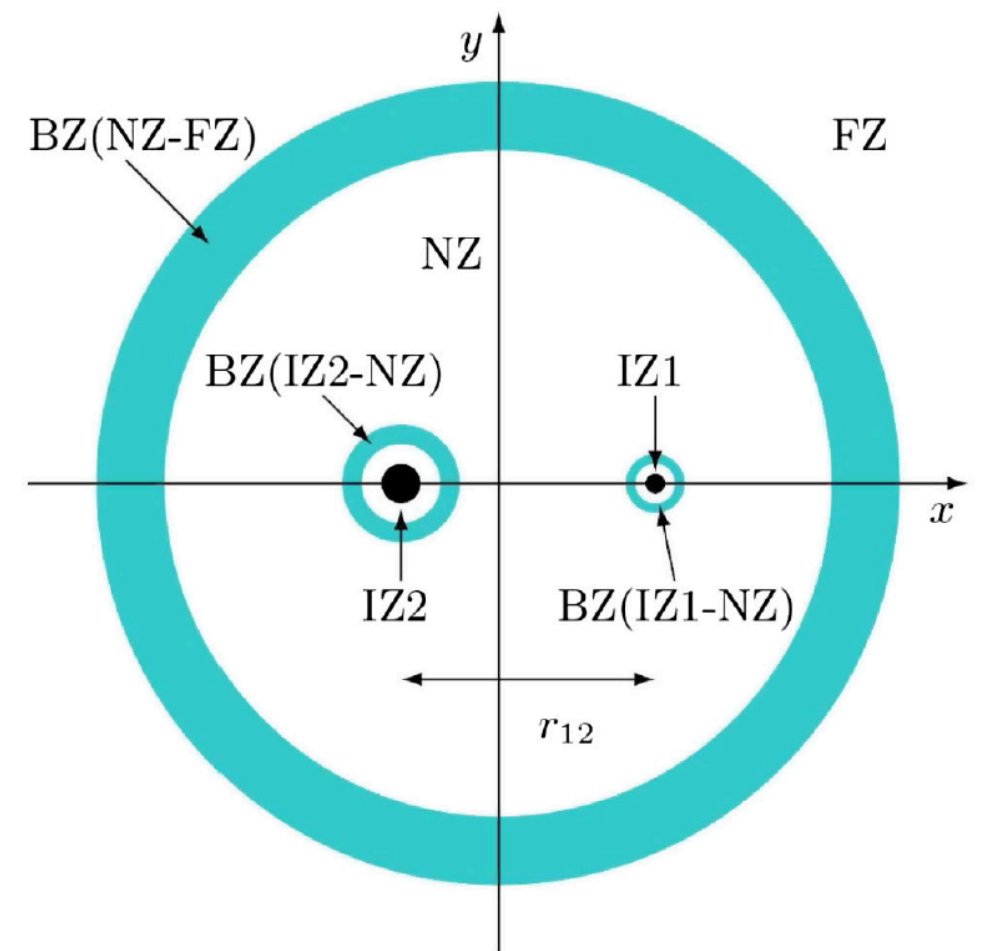
- Long time simulation is needed.

➡ We use approximate BHB metric.

ref) PRD89,084008(2014)

- Construction of the metric $A = 1,2$

- ▶ Inner Zones (IZ) : $0 < r_A \ll r_{12}$
 - a perturbed Schwarzschild BH
- ▶ Near Zone (NZ) : $m_A \ll r_A \ll \lambda$
 - PN approximation
- ▶ Far Zone (FZ) : $\lambda \ll r < \infty$
 - PM approximation
- ▶ Buffer Zone (BZ)
 - Asymptotic matching



BHB spacetime (BH1, BH2)

r_{12} : BH separation

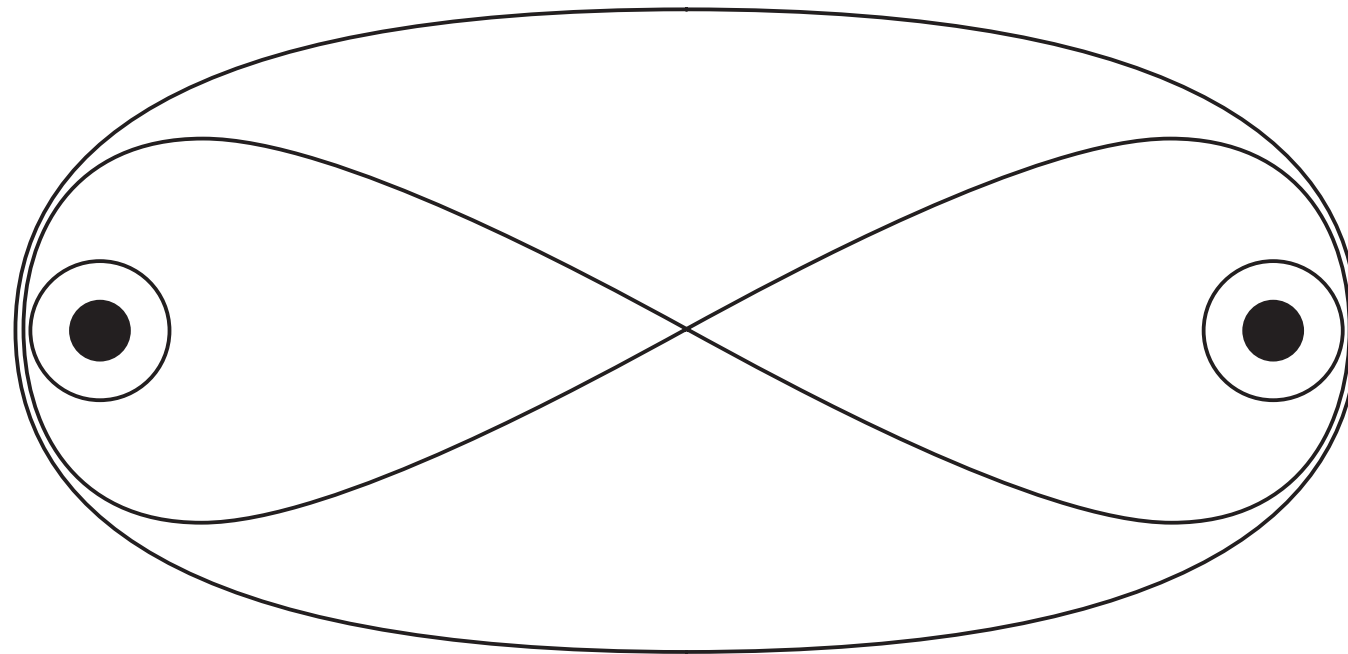
$m_1 = m_2 = M/2$

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Global closed null geodesic

- We solved null geodesic on the BHB metric.
- And, we found three types of “nearly” closed null geodesics.
 - ▶ Geodesic surrounding each BH
 - ▶ A global non-intersecting geodesic
 - ▶ An eight-shaped geodesic



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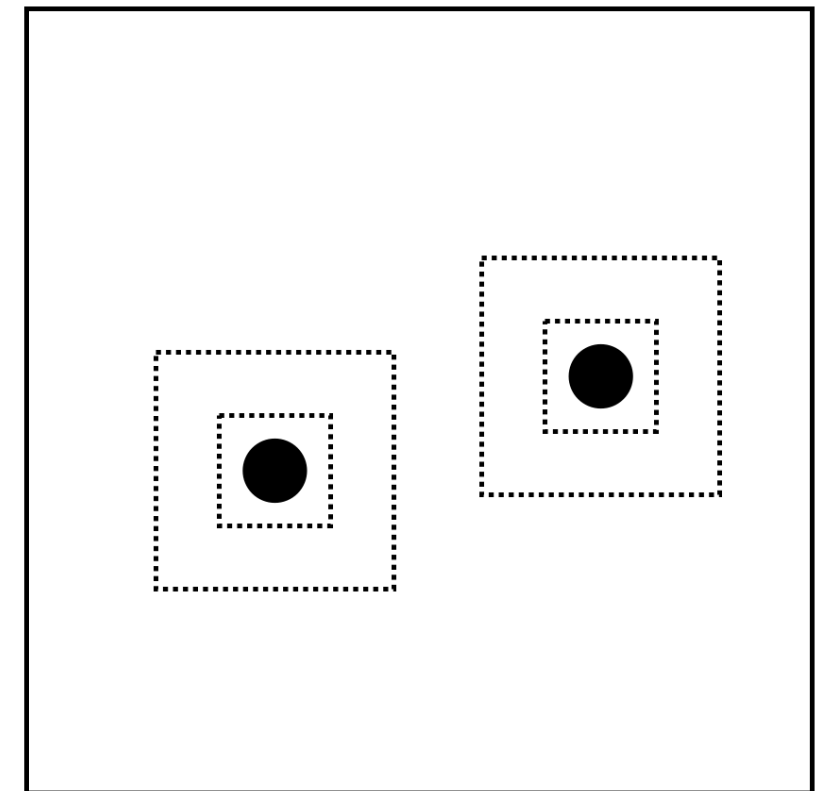
Our numerical code



- QNM appears in late time behavior of wave equation.
- ➡ We solve the Klein-Gordon eq. around BHB numerically.
- We developed new thorns on EinsteinToolkit.
 - ▶ Approximate BHB background.
 - ▶ Massless scalar field on the BHB spacetime with excision.
 - $\square \Phi = 0$
 - Ingoing spherically symmetric initial data.

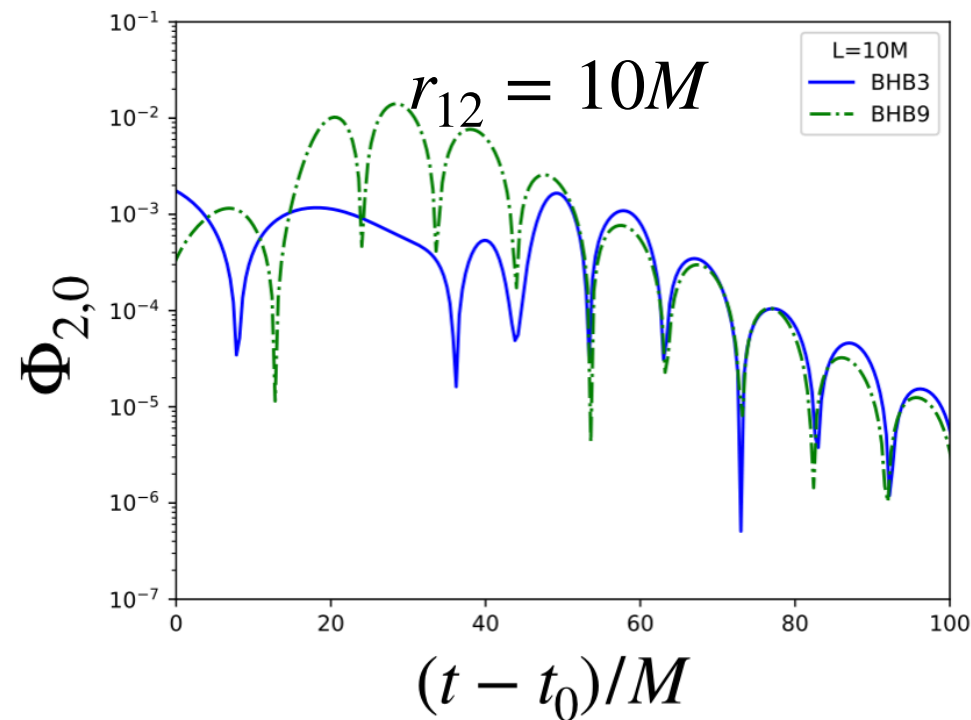
$$\left\{ \begin{array}{l} \Phi(0, \vec{x}) \equiv \Phi_0 = \frac{\sin \omega r W(r)}{r} e^{-(r-r_0)^2/\sigma^2} \\ \partial_t \Phi(0, \vec{x}) = \partial_r \Phi_0 + \frac{\Phi_0}{r} \end{array} \right.$$

BBH

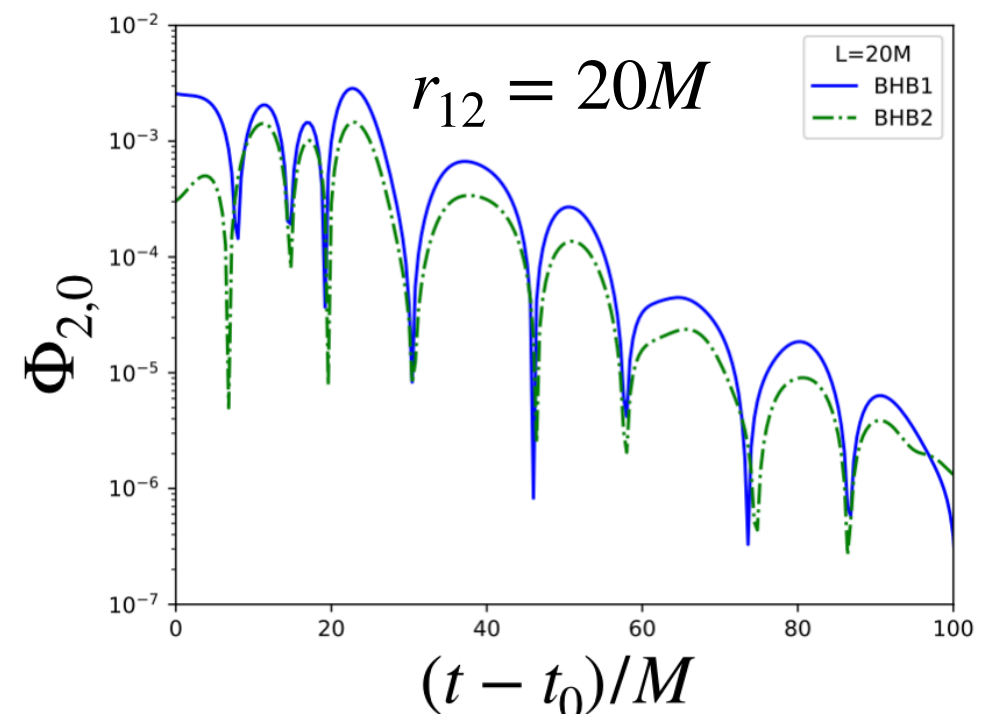


Global QNM

- The late behavior does not depend on the initial data.



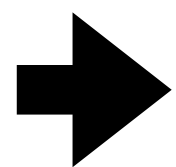
$$T \simeq 18M$$



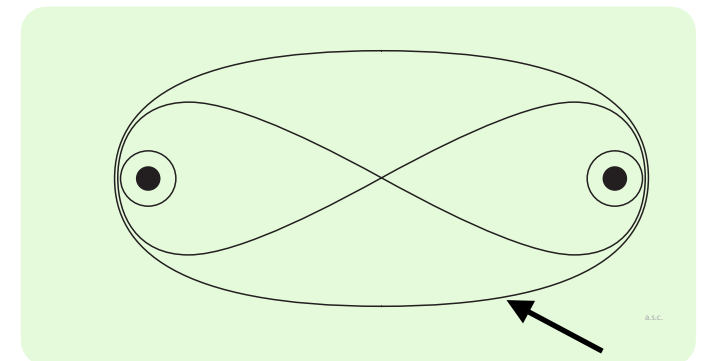
$$T \simeq 28M$$

- The periods of QNM are consistent with the expected period from global null closed geodesic.

$$T_{\text{QNM}} \simeq L + 8M$$



This is “global QNM”



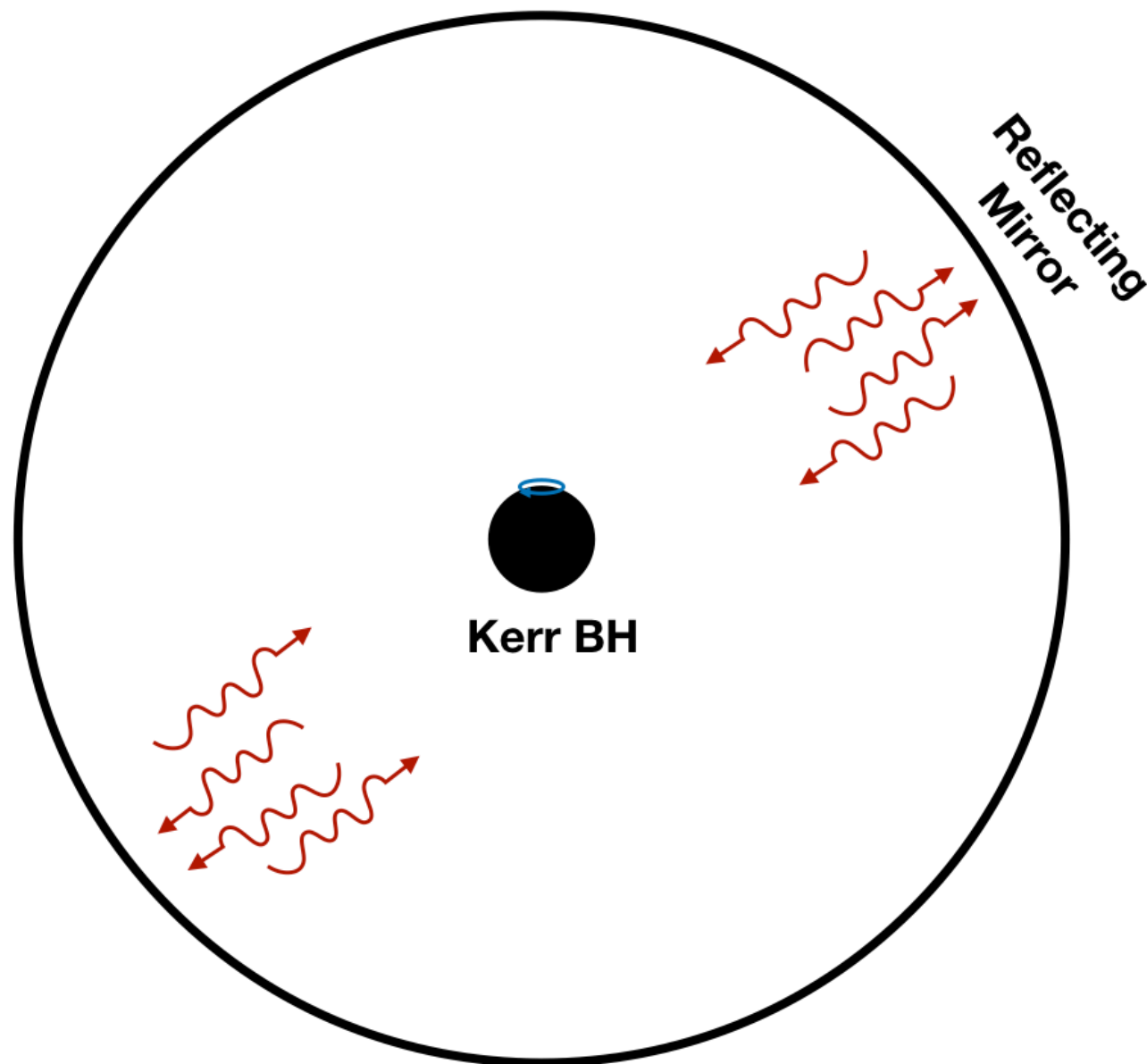
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Super-radiant like instability

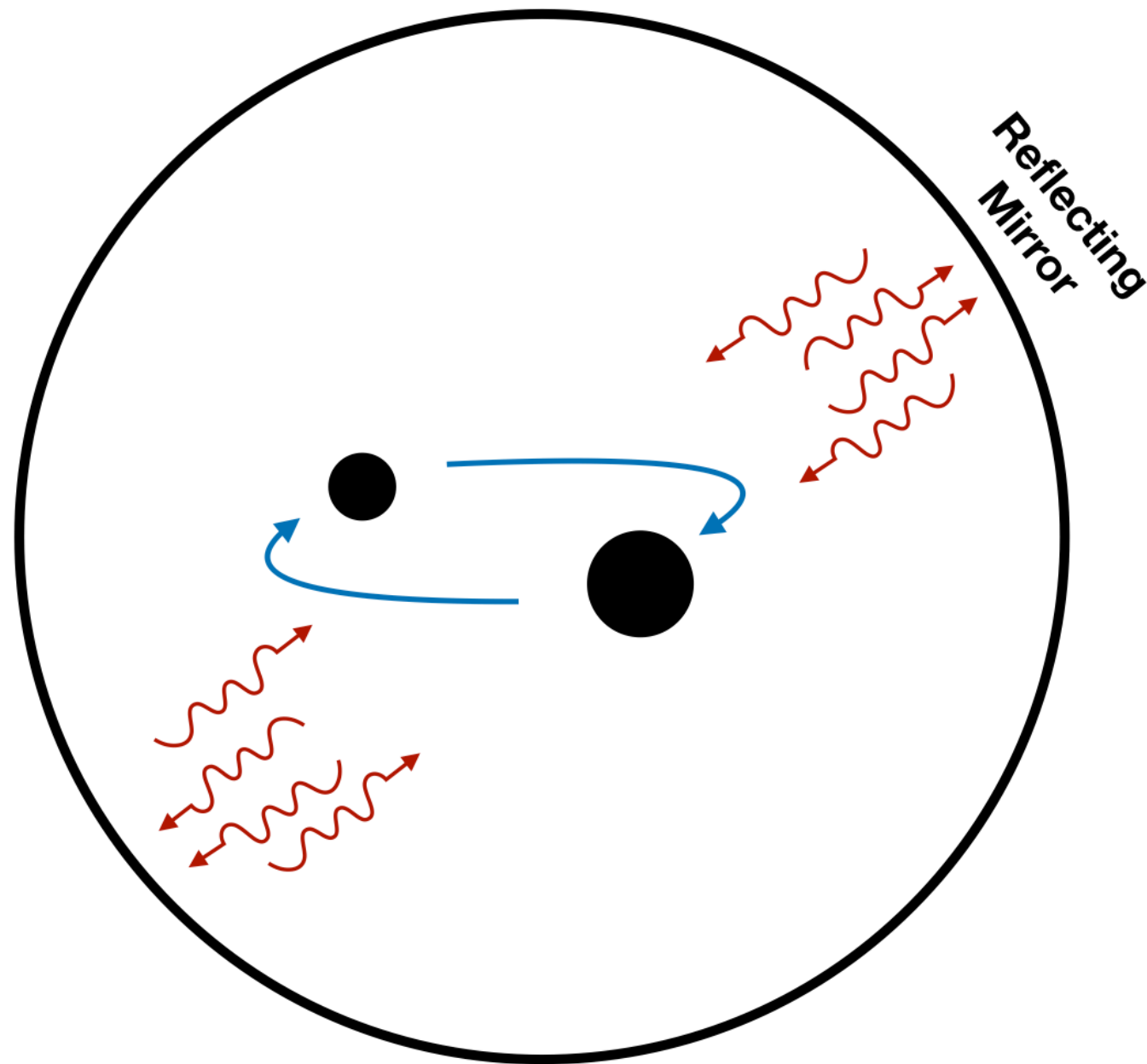
Black hole bomb

cf: super-radiant
instability



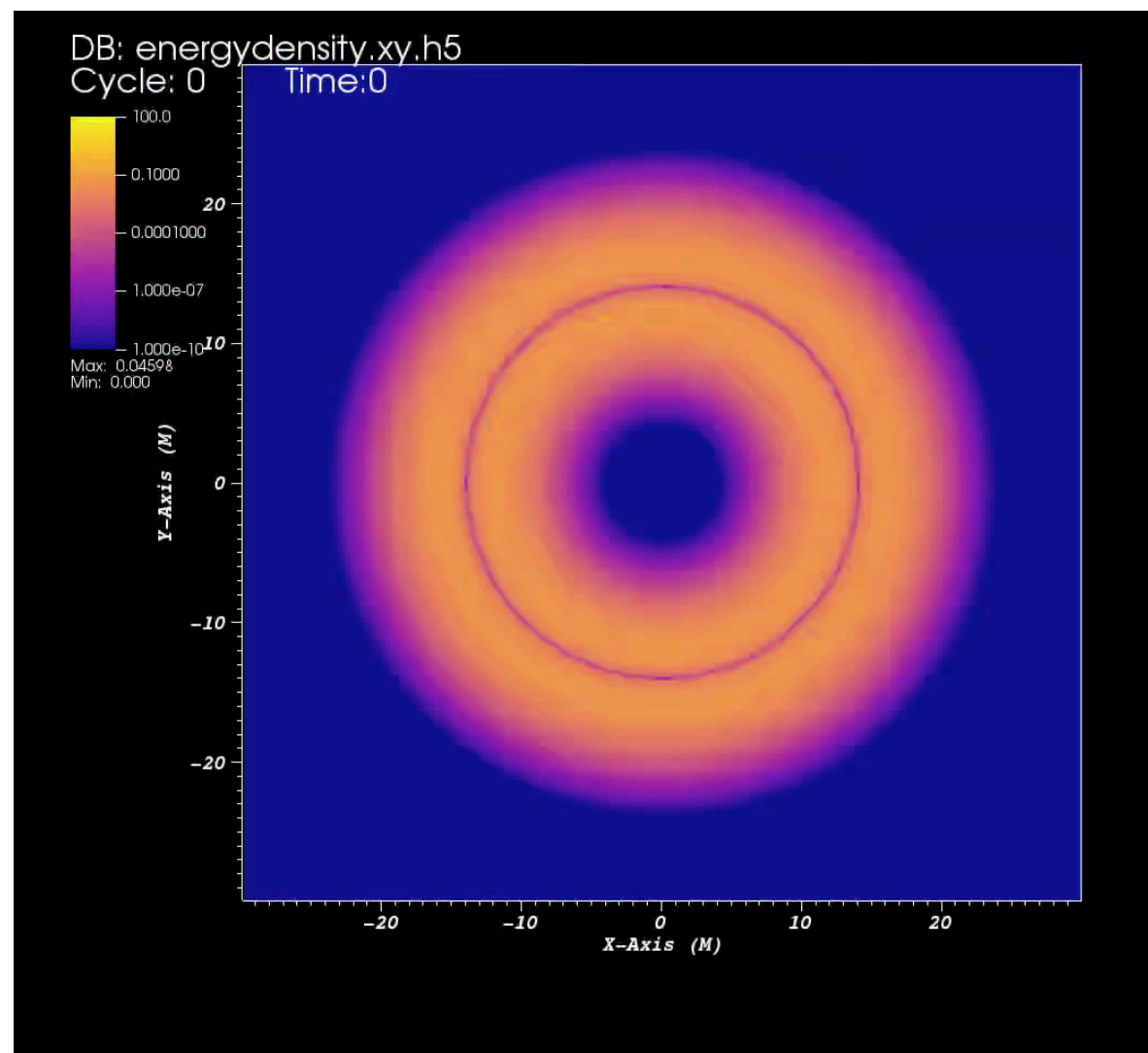
Super-radiant like instability

Black hole binary bomb (?)
super-radiant like instability (?)



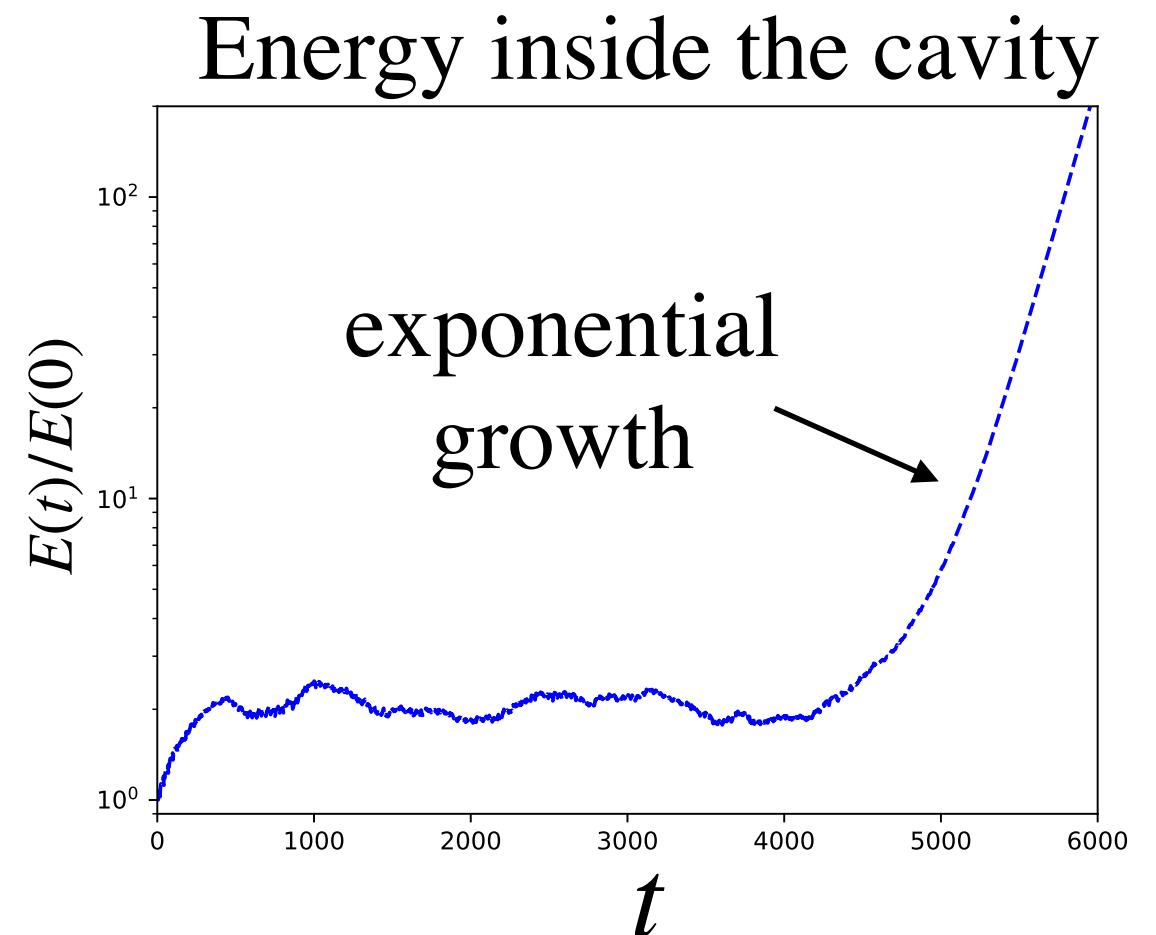
Toy model

- Massless scalar field inside a cavity with a binary of two reflecting objects in 2+1 Minkowski



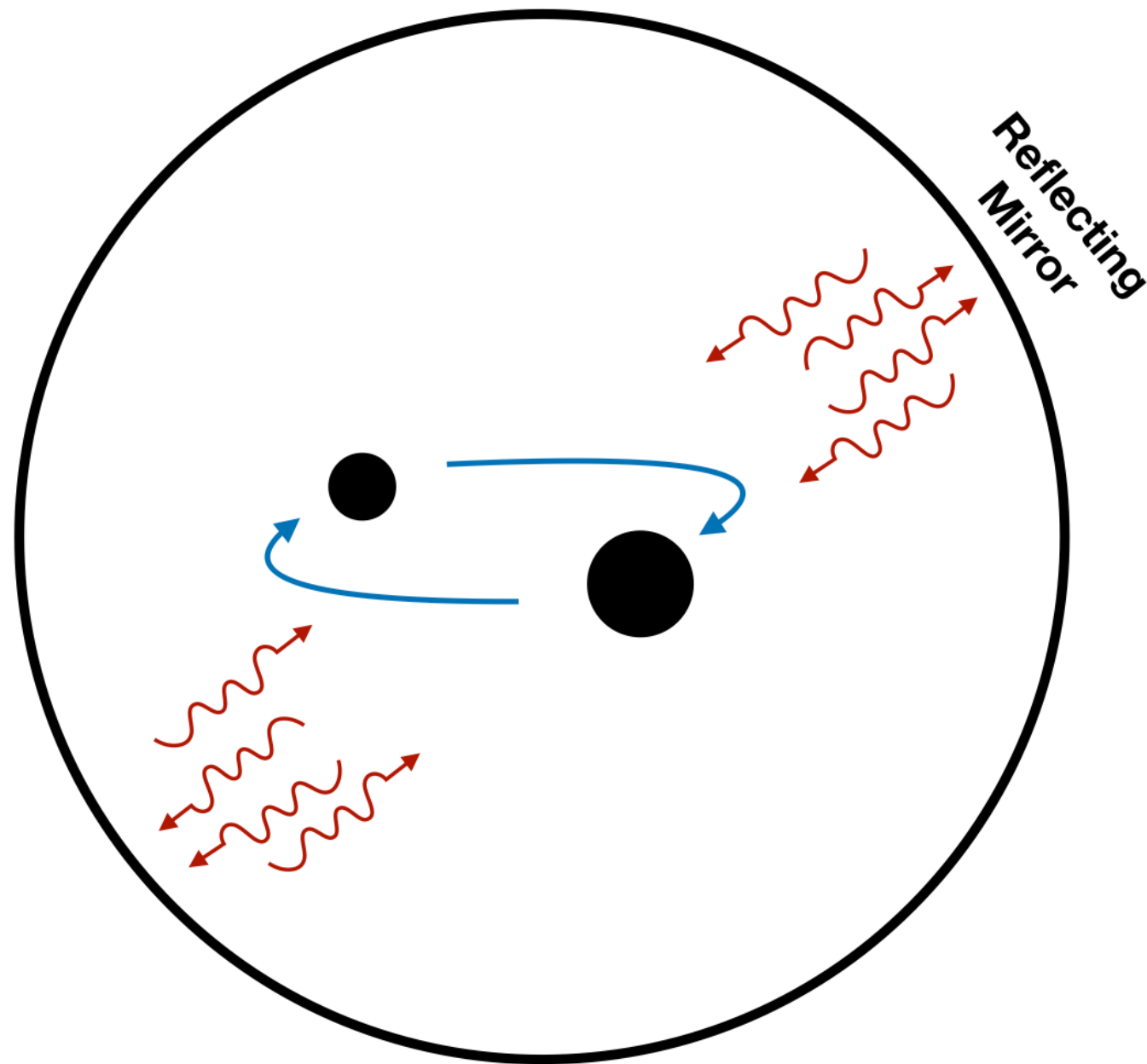
y

x $R_{\text{ext}} = 30, \Omega = 0.14, r_b = 0.5$



Super-radiant like instability

Black hole binary bomb (?)
super-radiant like instability (?)

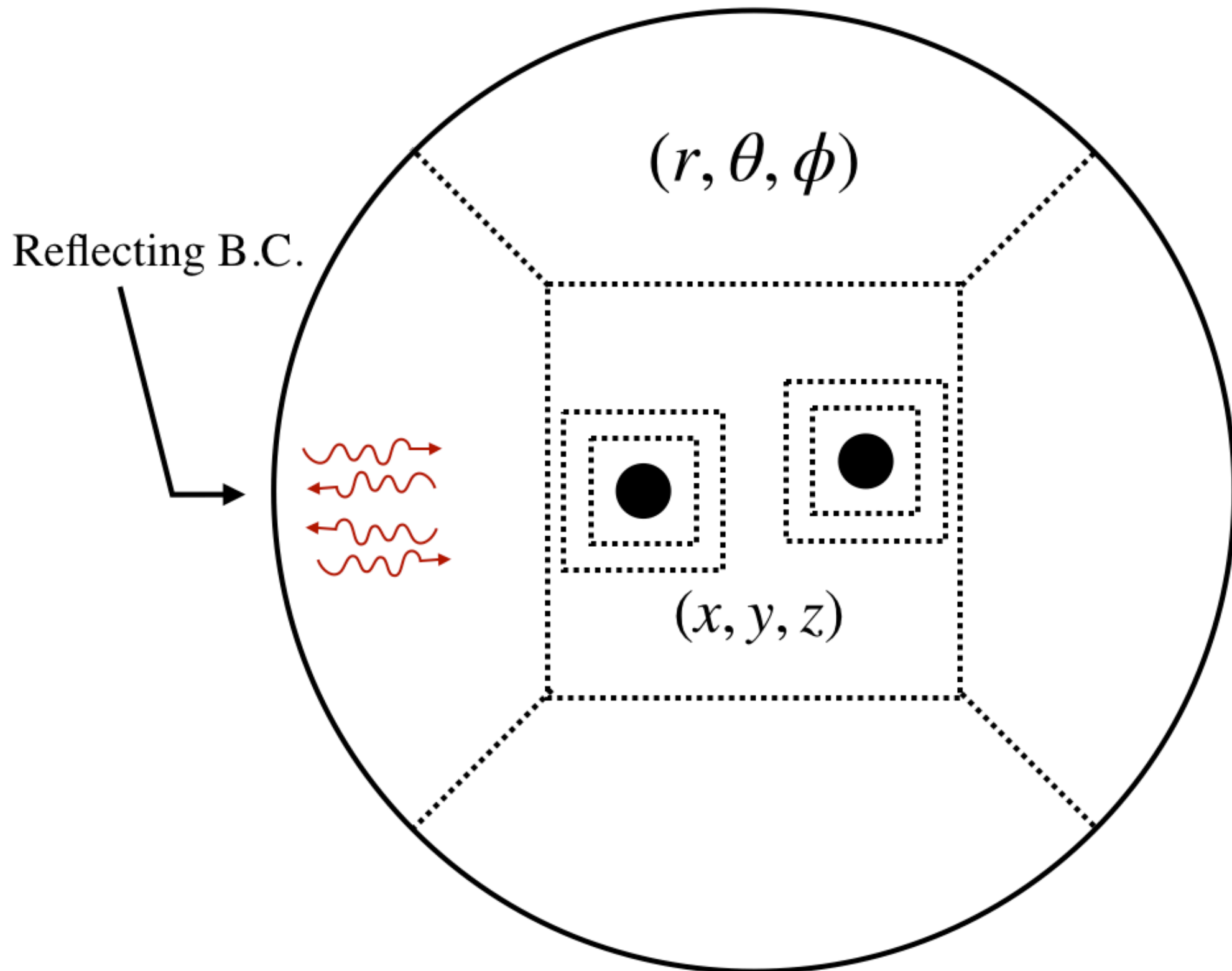


Our numerical code



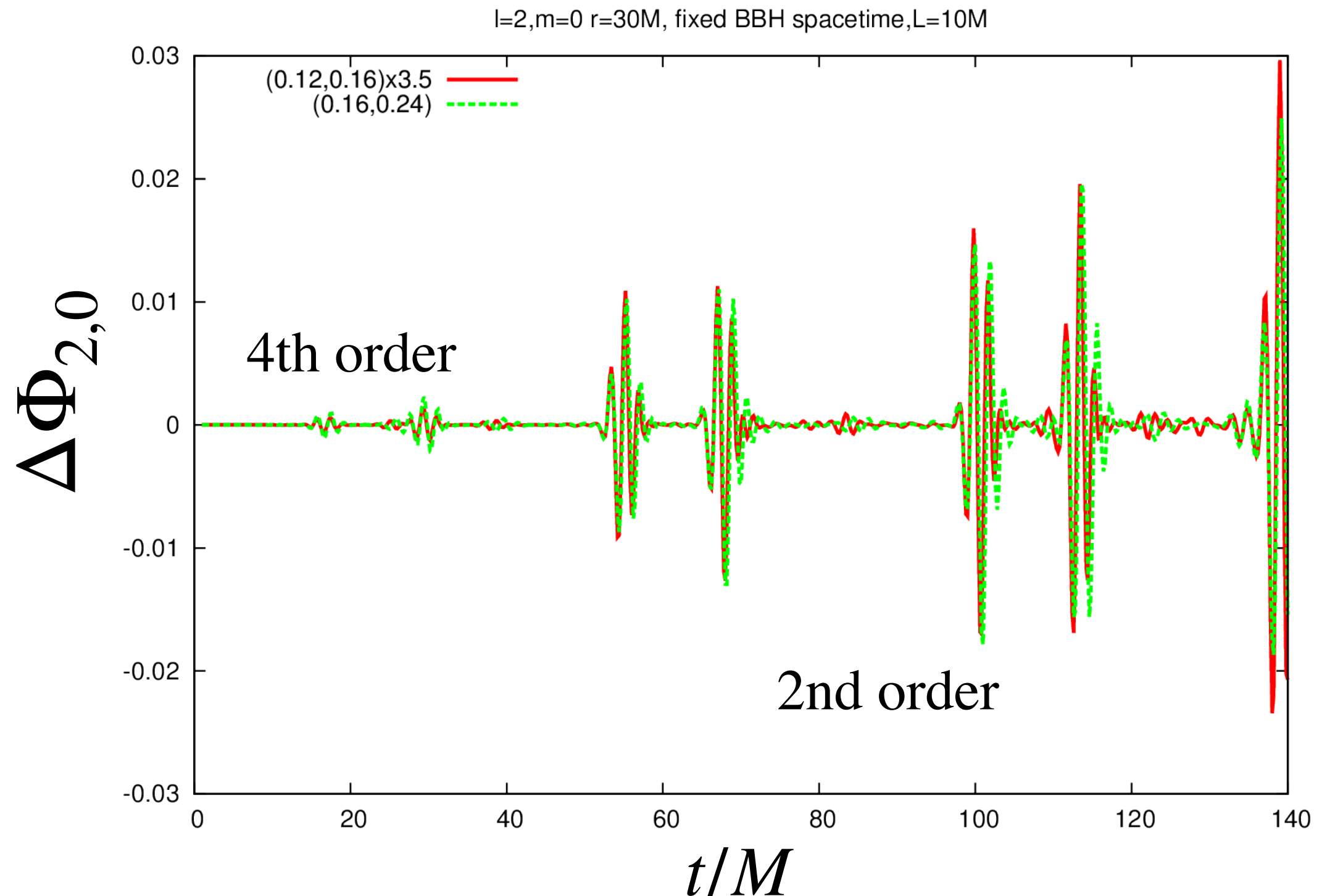
- Set up
 - ▶ Massless scalar field around BHB in cavity (3+1 dim).
- We developed our thorns on EinsteinToolkit.
 - ▶ Giving Approximate BHB background.
 - ▶ Solving massless scalar field on the BHB spacetime with excision.
 - $\square \Phi = 0$
 - Reflecting boundary condition on the spherical boundary.
- The llama thorn gives multi-patch structure.

Grid structure



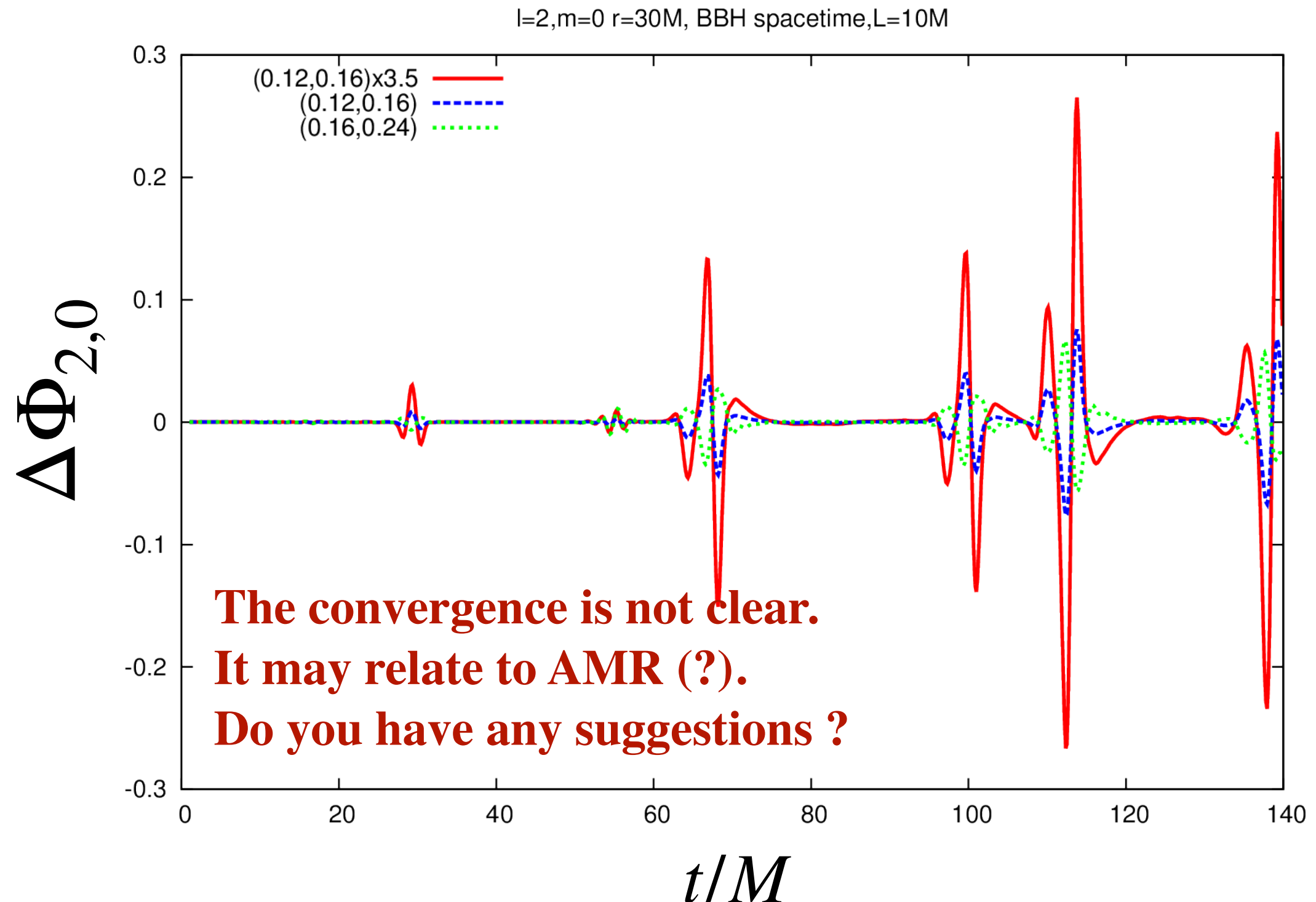
Convergence Check

- Fixed BHs (fixed mesh refinement) ➡ OK

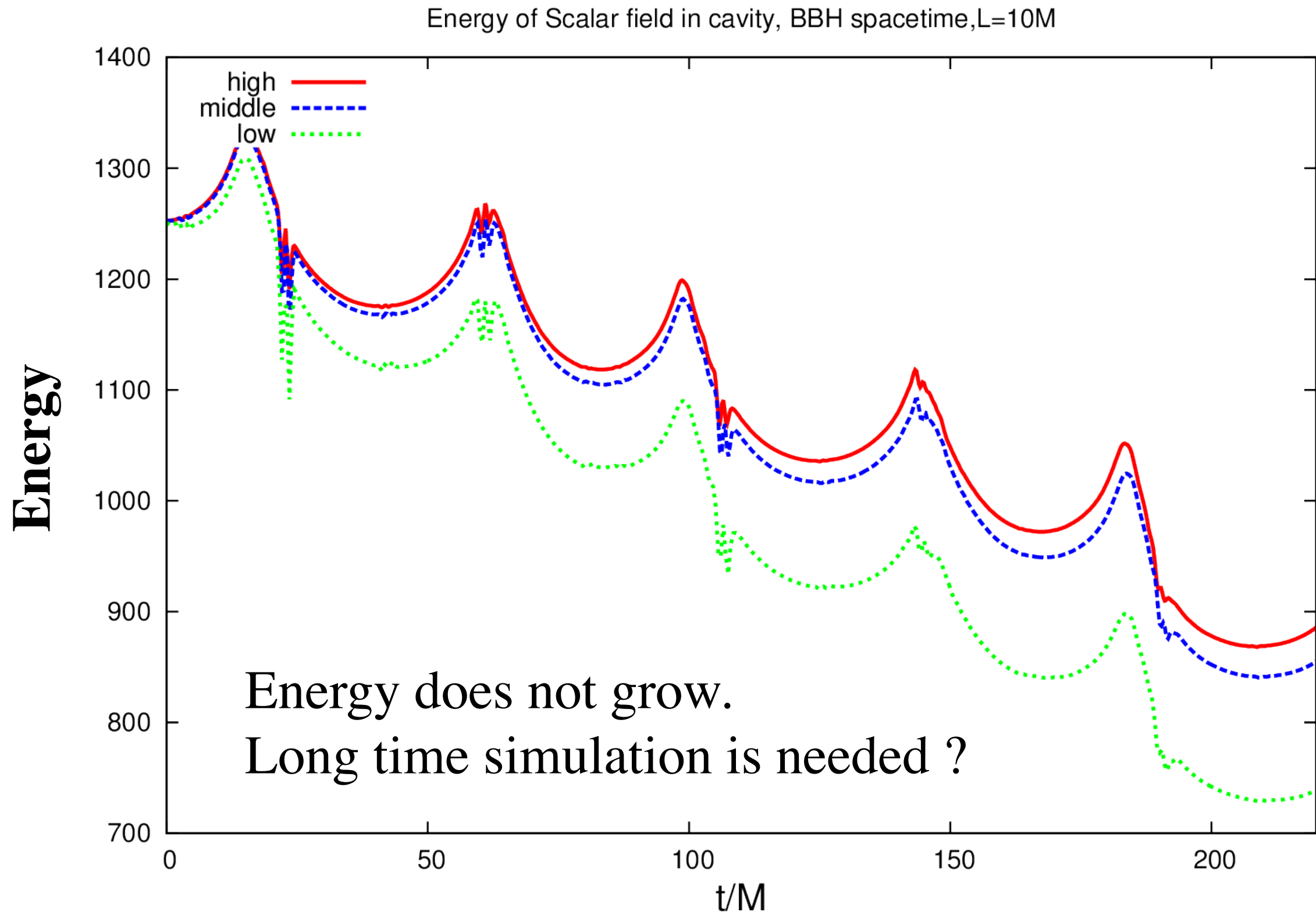


Convergence Check

- Binary BHs (adaptive mesh refinement)



Preliminary Result



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Summary

- Result

- ▶ closed null geodesic around BHB.
- ▶ global QNM in BHB spacetime.
- ▶ Energy extraction (in toy model)

- Ongoing work (BHB bomb)

- ▶ We could check the numerical convergence on fixed BHs spacetime.
- ▶ The convergence on BHB spacetime is not clear.
 - ➡ If you have good suggestions, let me know.

Thank you for your attention.