# House Rent Analysis

- Project Report -

## Data Preparation

I have introduced the dataset munichrent03 which is integrated in the R package LinRegInteractive, available at **README.md** file. Therefore, I can simply load this dataset to begin the subsequent steps of the analysis.

```
library(LinRegInteractive)
data(munichrent03)
data <- munichrent03</pre>
```

I began by examining the variable types to understand the structure of the dataset.

```
> str(data)
              2053 obs. of 12 variables:
'data.frame':
$ rent : num 741 716 528 554 698 ...
$ rentsqm : num 10.9 11.01 8.38 8.52 6.98 ...
          : int 68 65 63 65 100 81 55 79 52 77 ...
$ rooms : int 2 2 3 3 4 4 2 3 1 3 ...
$ yearc : num 1918 1995 1918 1983 1995
$ bathextra: Factor w/ 2 levels "no", "yes": 1 1 1 2 2 1 2 1 1 1 ...
$ bathtile : Factor w/ 2 levels "yes", "no": 1 1 1 1 1 1 1 1 1 1 ...
$ cheating : Factor w/ 2 levels "yes","no": 1 1 1 1 1 1 1 1 1 1 ...
$ district : Factor w/ 25 levels "All-Umenz", "Alt-Le",..: 10 10 10 17 17 17 21 21 21 21 ...
$ location : Ord.factor w/ 3 levels "normal"<"good"<...: 2 2 2 1 2 1 1 1 1 1 ...
$ upkitchen: Factor w/ 2 levels "no","yes": 1 1 1 1 2 1 1 1 1 1 ...
$ wwater : Factor w/ 2 levels "yes","no": 1 1 1 1 1 1 1 1 1 1 ...
> names(data)
'rent''rentsqm''area''rooms''yearc''bathextra''bathtile''cheating''district''location''upkitchen''wwater'
```

After that, I reviewed the distributions, value ranges, and identified any potential missing values.

```
> summary(data)
     rent
                   rentsqm
                                   area
                                                rooms
              Min. : 1.470 Min. : 17.0 Min. :1.000
Min. : 77.31
1st Qu.: 389.95
               1st Qu.: 6.800
                             1st Qu.: 53.0
                                           1st Qu.:2.000
Median : 534.30
               Median : 8.470
                             Median: 67.0
                                            Median :3.000
                             Mean : 69.6
Mean : 570.09
               Mean : 8.394
                                            Mean :2.598
3rd Qu.: 700.48
               3rd Qu.:10.090
                             3rd Qu.: 83.0
                                            3rd Qu.:3.000
Max. :1789.55 Max. :20.090 Max. :185.0
                                            Max. :6.000
        bathextra bathtile cheating
                                          district
                                                       location
vearc
Min. :1918 no :1862 yes:1673 yes:1878
                                         Neuh-Nymp: 177
                                                       normal:1205
1st Qu.:1948 yes: 191 no: 380 no: 175
                                         Lud-Isar : 161
                                                         good : 803
                                          Au-Haid : 139
Median:1960
                                                       top : 45
                                          SchwWest: 137
Mean :1958
3rd Qu.:1973
                                          Maxvor : 132
Max. :2001
                                          Laim
                                                : 117
(Other) :1190
upkitchen wwater
no:1903 yes:1981
yes: 150 no: 72
```

Note that the variables rentsqm, rent and area are related by the equation: rent = rentsqm  $\times$  area. For example, at row 100, we have:

```
> round(data$rent[100]/data$area[100],2) #compute rentsqm
11.3
> data$rentsqm[100]
11.3
```

Since rentsqm is a derived variable, I chose to exclude it and instead focus on total rent, which may better capture the underlying relationships with other features.

```
> data$rentsqm <- NULL
```

## **Exploratory Data Analysis**

Subsequently, I conducted an Exploratory Data Analysis (EDA) to gain initial insights into the dataset. A few key findings from this phase include:

• The 7 districts with the largest number of houses

Neun-Nymp	Lud-Isar	Au-Haid	SchwWest	Maxvor	Laim	Ram-Per
177	161	139	137	132	117	115

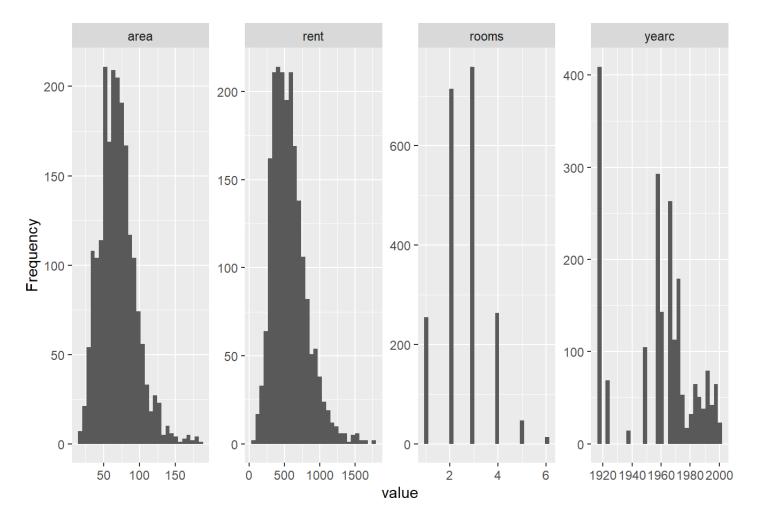
• The 7 districts with the highest number of houses where the location is classified as either "top" or "good":

118 116 97 96 81 50 37	Maxvor	Neuh-Nymp	Lud-Isar	SchwWest	Au-Haid S	chwab-Frei	Trud-Rie
	118	116	97	96	81	50	37

• The proportion of houses equipped with each feature:

	Feature	Count	Percent
1	bathextra	191	9.3
2	2 bathtile	1673	81.5
3	3 cheating	1878	91.5
4	upkitchen	150	7.3
5	wwater	1981	96.5

• The distribution of the numerical variables in the dataset



• The variable yearc represents discrete individual years, and the number of rooms(room)ranges only from 1 to 6.

```
> table(data$room) #Count for each number of room
             4
         3
                  5
255 715 759 263 47 14
> table(data$yearc) #Count for each year
1918
        1924
                1939
                        1948
                                1957 1957.5
                                                1960
                                                        1966
                                                                1967
                                                                        1968
409
         69
                 14
                        105
                                225
                                         68
                                                143
                                                        228
                                                                 35
                                                                         23
                                                                        1978
1969
        1970
                1971
                        1972
                                1973
                                        1974
                                                1975
                                                        1976
                                                                1977
44
        46
                35
                        89
                                55
                                        30
                                                16
                                                         7
                                                                 6
                                                                         5
1979
        1980
                1981
                        1982
                                1983
                                        1984
                                                1985
                                                        1986
                                                                1987
                                                                        1988
6
      17
               15
                        8
                               40
                                       17
                                               20
                                                       11
                                                               20
                                                                       13
1989
        1990
                1991
                        1992
                                1993
                                        1994
                                                1995
                                                        1996
                                                                1997
                                                                        1998
                                        13
                                                 9
        10
                14
                        24
                                41
                                                        20
                                                                12
15
                                                                        14
1998.5
         1999
                  2000
                          2001
32
         7
                18
                         5
```

## **Graphical Model Learning**

#### More Data Preparation

To learn a model from the data, some additional preprocessing steps are required. From the earlier exploration, I observed that the dataset contains many categorical variables, and only two variables, namely rent and area, are truly continuous. A Directed Graphical Model can be used to model data under two common distributional assumptions:

- Multinomial (each variable is categorical)
- Multivariate Normal

Since the dataset contains mostly categorical variables, I decided to model the data assuming a Multinomial distribution. Therefore, several variables needed to be transformed accordingly. Below is a summary of the preprocessing tasks (see the R code file for more details):

• For the variable years, there are two values with decimals: 1957.5 and 1998.5. I removed the decimal part to keep only the integer year. After that, I created a new variable called year\_group to extract information from years with fewer levels. Specifically, the years were grouped into the following periods: 1918–1959, 1960–1969, 1970–1989, and 1990–2001.

```
# Count for each periods
1918-1959 1960-1969 1970-1989 1990-2001
890 473 471 219
```

• The variable district represents the 25 districts of Munich. If treated directly as a categorical variable, it would result in 25 levels, which would make computation extremely complex. To address this, I created a new variable called district\_group, which clusters the 25 districts into 3 broader areas. The grouping is based on the density of houses and geographical location. The figure below illustrates this grouping: the districts are sorted in descending order based on the number of houses. Region 1 includes the districts marked with a bold dot. Region 2 includes those marked with an "x", and Region 3 consists of the remaining districts.



Once the districts were grouped into three areas, the following shows the distribution of houses across the areas.

```
> table(data$district_group)
Area1 Area2 Area3
1214 658 181
```

• Next, the variable rooms, which indicates the number of rooms in each house and only takes values from 1 to 6, was converted into a factor and treated as a categorical variable. The variable location is an ordered factor by default, so I converted it into a regular (unordered) factor to ensure compatibility with the modeling functions.

```
> data$rooms <- as.factor(data$rooms)
> data$location <- as.factor(as.character(data$location))</pre>
```

• Now, only two continuous variables remain: rent and area. To model the data under the Multinomial distribution, I applied a discretization method to convert these variables into discrete ones, aiming to preserve as much information as possible. Specifically, the discretization technique used is called information-preserving discretization, also known as the Hartemink method. The details of this transformation are presented in the code file. For the sake of brevity, the method itself will not be discussed in this report.

The function that performs this task from the package bnlearn directly transforms the two mentioned continuous variables into discrete ones, without creating new variables. The rent and area variables have now been transformed into discrete variables, each divided into a set of intervals.

```
> table(data_disc$rent)

[77.31,406.132] (406.132,687.072] (687.072,1789.55]

582 923 548

> table(data_disc$area)

[17,44] (44,78] (78,185]

307 1086 660
```

The dataset after applying all the transformations described above is named data\_disc, and its structure is as follows:

```
> str(data_disc)
'data.frame':
                2053 obs. of 11 variables:
                : Factor w/ 3 levels "[77.31,406.132]",...: 3 3 2 2 3 3 1 2 2 1 ...
$ rent
                : Factor w/ 3 levels "[17,44]","(44,78]",...: 2 2 2 2 3 3 2 3 2 2 ...
$ area
                : Factor w/ 6 levels "1","2","3","4",...: 2 2 3 3 4 4 2 3 1 3 ...
$ rooms
               : Factor w/ 2 levels "no", "yes": 1 1 1 2 2 1 2 1 1 1 ...
$ bathextra
               : Factor w/ 2 levels "yes", "no": 1 1 1 1 1 1 1 1 1 1 ...
$ bathtile
               : Factor w/ 2 levels "yes", "no": 1 1 1 1 1 1 1 1 1 1 ...
$ cheating
                : Factor w/ 3 levels "good", "normal", ..: 1 1 1 2 1 2 2 2 2 2 ...
$ location
                : Factor w/ 2 levels "no", "yes": 1 1 1 1 2 1 1 1 1 1 ...
$ upkitchen
                : Factor w/ 2 levels "yes", "no": 1 1 1 1 1 1 1 1 1 1 ...
$ wwater
               : Factor w/ 4 levels "1918-1959","1960-1969",..: 1 4 1 3 4 3 1 1 1 1 ...
$ vear group
$ district_group: Factor w/ 3 levels "Area1", "Area2",...: 1 1 1 2 2 2 2 2 2 2 ...
```

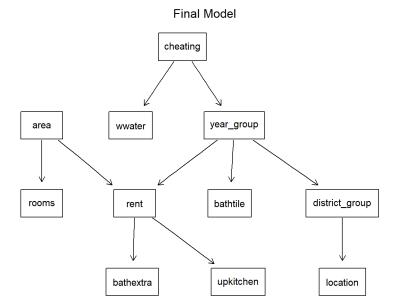
#### Model Learning

The detailed implementation for learning models from the data and selecting the most appropriate one can be found in the accompanying R code file. Additionally, understanding the modeling process requires background knowledge in topics related to Directed Graphical Models, such as learning methods, model learning algorithms, and more. A full discussion of these topics is beyond the scope of this report. Therefore, I will only present the final result. For a deeper understanding of Directed Graphical Models, one may refer to the book: **Bayesian Networks With Examples in R**.

After the model learning process and the selection of the most appropriate model, we arrive at the following result:

### Model Directed Acylic Graph

As mentioned earlier, in a Directed Graphical Model, the joint probability distribution of all variables factorizes according to a directed acyclic graph (DAG). The Final Model has the following DAG structure:



The joint distribution is:

```
p(\text{cheating}).p(\text{wwater}|\text{cheating}).p(\text{year\_group}|\text{cheating}).p(\text{district\_group}|\text{year\_group}).p(\text{location}|\text{district\_group}) \times p(\text{bathtile}).p(\text{rent}|\text{year\_group}, \text{ area}).p(\text{bathextra}|\text{rent}).p(\text{upkitchen}|\text{rent}).p(\text{rooms}|\text{rent}).
```

#### **Model Parameters**

The parameters are conditional probabilities. I will present only a few conditional probability tables for selected variables, rather than displaying all of them, in order to keep the report concise and readable. For example, conditional probability tables of rooms and location are:

```
> fit$rooms
Parameters of node rooms (multinomial distribution)
Conditional probability table:
area
          [17,44]
                      (44,78]
                                 (78,185]
rooms
1 0.736156352 0.025782689 0.001515152
2 0.263843648 0.565377532 0.030303030
3 0.000000000 0.390423573 0.507575758
4 0.000000000 0.018416206 0.368181818
5 0.000000000 0.000000000 0.071212121
6 0.000000000 0.000000000 0.021212121
> fit$location
Parameters of node location (multinomial distribution)
Conditional probability table:
district_group
                                       Area3
location
               Area1
                           Area2
       0.514827018 0.224924012 0.165745856
normal 0.464579901 0.746200608 0.828729282
      0.020593081 0.028875380 0.005524862
```

#### **Model Interpretation**

The rent is directly related to the property's area (area), year of construction (year\_group), and the presence of high-quality bathroom and upscale kitchen equipment (bathextra and upkitchen). The remaining factors are indirectly related to the rental price through these direct factors. Given information about the direct factors, the indirect factors become conditionally independent of the rental price.

## Model Applications

Once the model has been learned from the data, it is used for several purposes, including the following:

### **Analyzing Conditional Independencies**

It can be simply understood that when variables X and Y are conditionally independent given Z, this means that once the information about Z is known, knowing X provides no additional information about Y, and vice versa.

Directed Graphical Models can help analyze such relationships. Once again, the precise theoretical details can be quite complex to present in full. Fortunately, the R package bnlearn provides a function dsep() that can be used to test the conditional independence between any three variables.

For example, once the area of a house is known, the number of rooms (rooms) and the rent become conditionally independent.

```
> dsep(fit,x="rooms",y="rent",z="area")
[1] TRUE
```

## **Approximating Conditional Probabilities**

The bnlearn library also supports efficient approximation of conditional probabilities. As an example, I estimated the likelihood that a house located in Area1 is equipped with High quality equipment in the bathroom:

```
\mathbb{P}(\text{bathextra} = \text{yes} \mid \text{district group} = \text{Area1})
```

```
> cpquery(fit,event = (bathextra=="yes"),evidence = (district_group == "Area1"),n=10^6)
[1] 0.09121026
> cpquery(fit,event = (bathextra=="yes"),evidence = (district_group == "Area1"),n=10^6)
[1] 0.09108432
```

Note that this probability approximation function is based on a randomized algorithm, so the result may vary with each run. The argument  ${\tt n}$  controls the number of samples: the larger its value, the more accurate the result will be, but at the cost of increased computational time.

## Querying and Predicting

Based on the previous applications, I will now perform queries to extract useful insights and also make some predictions. The results will be presented here, while the corresponding code can be found in the accompanying R script.

#### Insights

- Area and number of rooms are not directly influenced by location, year of construction, or the heating and hot water systems. However, once the price segment is fixed, these factors become relevant and should be considered jointly.
- According to the model, when filtering houses by year of construction, the location and heating/hot water systems do not need to be considered in rental price analysis.
- Area alone is sufficient to determine the rental price, without the need to consider the number of rooms (as shown in the previous example).
- Within each price segment, there are no additional factors that influence whether a house is equipped with high-quality bathroom features (bathextra) or upscale kitchen equipment (upkitchen).

#### Prediction