

1. 1) total permutations =  $\frac{7!}{4!} = 210$

innovative, analytical  $\rightarrow 2$  ia \_ \_ ia

empathetic, innovative  $\rightarrow 6$  ei \_ e-i ie \_ i-e \_ei \_ie

blanks =  $\binom{5}{1}$

$(2 \cdot 5) + (5 \cdot 6) = 40$

Duplicates: eia iae  $\rightarrow 40 - 2 = 38$

$\frac{38}{210} = \frac{19}{105}$

2) Bernoulli Trial

$\binom{10}{4} \cdot \left(\frac{19}{105}\right)^4 \cdot \left(\frac{86}{105}\right)^6 = 210 \left(\frac{19}{105}\right)^4 \left(\frac{86}{105}\right)^6 \approx 6.8\%$

2. 1)  $P(A) = \frac{1}{2}$   $P(B) = \frac{3}{4}$   $P(A \cap B) = \frac{5}{16}$  use chart below

If independent,  $P(A \cap B) = P(A) \cdot P(B)$

$\frac{1}{2} \cdot \frac{3}{4} = \frac{3}{8}$   $\frac{3}{8} \neq \frac{5}{16}$

NOT INDEPENDENT

2)  $P(x=0) = \frac{1}{2}$

$P(x=1) = \frac{5}{16}$

$P(x=2) = \frac{1}{8}$

$P(x=3) = \frac{1}{16}$

THTH HTHT HTTH TTHT TTHT HTTT TTTH TTTT

HTTT HTTH TTHT TTTH HTTH

HHHT THHH

HHHH

$$E(x) = 0\left(\frac{1}{2}\right) + 1\left(\frac{5}{16}\right) + 2\left(\frac{1}{4}\right) + 3\left(\frac{1}{16}\right) = \frac{5}{16} + \frac{4}{16} + \frac{3}{16} = \frac{12}{16} = \boxed{\frac{3}{4}}$$

3. NASTY  $P(x=1) = \frac{1}{5}$

NASTY

$$P(x=2) = \frac{3}{5}$$

HASTY MATHS BOARD

$$P(x=3) = \frac{1}{5}$$

HOARD  $\leftrightarrow$  Equal chance of it being board or hoard

$$E(x) = 1\left(\frac{1}{5}\right) + 2\left(\frac{3}{5}\right) + 3\left(\frac{1}{5}\right) = \frac{1}{5} + \frac{6}{5} + \frac{3}{5} = \frac{10}{5} = \boxed{2}$$

HASTY

$$P(x=1) = \frac{1}{5}$$

HASTY

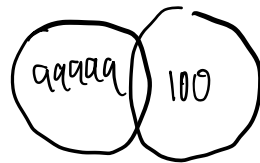
$$P(x=2) = \frac{4}{5}$$

NASTY MATHS HOARD BOARD

$$E(x) = 1\left(\frac{1}{5}\right) + 2\left(\frac{4}{5}\right) = \frac{1}{5} + \frac{8}{5} = \boxed{\frac{9}{5}}$$

4. 1)  $P(M) = 1/1000$  matches description

$P(I \cap M) = \frac{99}{100000}$  innocent



$$P(I|M) = \frac{99}{100000} \div \frac{1}{1000} = \frac{99000}{100000} = \boxed{\frac{99}{100}}$$

2)  $P(I) = \frac{99999}{100000}$

$$P(M|I) = \frac{99}{100000} \div \frac{99999}{100000} = \frac{9900000}{999990000} = \frac{99}{99999} = \boxed{\frac{11}{11111}}$$

3)

$$1 - \frac{\binom{99900}{1000}}{\binom{100000}{1000}}$$

not matching

reviewed residents

No one in the 1000 matches description

$1 - (\text{none of the 1000 matches}) = \text{at least 1 matches}$

5.

$$0.7 \cdot 0.8 = 0.56 \rightarrow 56\%$$

↑ chance of 3 planets

↑ chance Earth not detected