

Step W : $clientp1(l_1tsl \ ())(p1,1)(p1,200)(p1,1)(p1,1)(p1,2)))))servermyVNum2p2(l_2$
typing context:

Step W : $p1(l_1tsl \ ())(p1,1)(p1,200)(p1,1)(p1,1)(p1,2)))))$
typing context:

Step W : $(l_1tsl \ ())$
typing context:

Step W : l_1tsl
typing context:

Step W': l_1tsl
type: $\xrightarrow{\beta_7} \rho_6$
beha: τ
cons:

- $tsl^{l_1} \sim \psi_5$
- $l_1\psi_5 \subseteq \beta_7$
- $l_1 \sim \rho_6$

subs: $\square\square\square\square\square$

Step F: l_1tsl
cons:

- $tsl^{l_1} \sim \psi_5$
- $l_1\psi_5 \subseteq \beta_7$
- $l_1 \sim \rho_6$

subs: $\square\square\square\square\square$

Step R: l_1tsl
type: $\xrightarrow{\beta_7} \rho_6$
beha: τ
cons:

- $tsl^{l_1} \sim \psi_5$
- $l_1\psi_5 \subseteq \beta_7$
- $l_1 \sim \rho_6$

Step W : ()
typing context:

Step W': ()
type:
beha: τ
cons:

•

subs: $\square\square\square\square\square$

Step F: ()
cons:

•

subs: $\square\square\square\square\square$

Step R: ()
type:
beha: τ
cons:

•

Step W': (l_1tsl ())
type: α_3
beha: $\tau; \tau; \beta_4$
cons:

- $\xrightarrow{\beta_\tau} \rho_6 \subseteq \xrightarrow{\beta_4} \alpha_3$
- $tsl^{l_1} \sim \psi_5$

- $l_1\psi_5 \subseteq \beta_7$

- $l_1 \sim \rho_6$

subs: $\square\square\square\square\square$

Step F: $(l_1tsl \ ())$

cons:

- $tsl^{l_1} \sim \psi_5$

- $\beta_7 \subseteq \beta_4$

- $l_1\psi_5 \subseteq \beta_7$

- $\rho_8 \sim \rho_6$

- $l_1 \sim \rho_6$

subs: $[\alpha_3 \mapsto \rho_8]\square\square\square\square$

Step R: $(l_1tsl \ ())$

type: ρ_8

beha: $\tau; \tau; \beta_4$

cons:

- $tsl^{l_1} \sim \psi_5$

- $l_1\psi_5 \subseteq \beta_4$

- $l_1 \sim \rho_8$

Step W : $((p1, 1)((p1, 200)((p1, 1)((p1, 1)((p1, 2))))))$

typing context: $p1 : \forall(\rho_8 : l_1 \sim \rho_8).\rho_8$

Step W :

typing context: $p1 : \forall(\rho_8 : l_1 \sim \rho_8).\rho_8$

Step W':

type: $(\rho_{12} \times \alpha_{13}) \xrightarrow{\beta_{11}}$

beha: τ

cons:

- $\rho_{12}!\alpha_{13} \subseteq \beta_{11}$

subs: $\square\square\square\square\square$

Step F:

cons:

- $\rho_{12}!\alpha_{13} \subseteq \beta_{11}$

subs: $\square\square\square\square\square$

Step R:

type: $(\rho_{12} \times \alpha_{13}) \xrightarrow{\beta_{11}}$

beha: τ

cons:

- $\rho_{12}!\alpha_{13} \subseteq \beta_{11}$
-

Step W : $(p1, 1)((p1, 200)((p1, 1)((p1, 1)((p1, 2))))))$

typing context: $p1 : \forall(\rho_8 : l_1 \sim \rho_8).\rho_8$

Step W : $(p1, 1)$

typing context: $p1 : \forall(\rho_8 : l_1 \sim \rho_8).\rho_8$

Step W : $p1$

typing context: $p1 : \forall(\rho_8 : l_1 \sim \rho_8).\rho_8$

Step W': $p1$

type: ρ_{17}

beha: τ

cons:

- $l_1 \sim \rho_{17}$

subs: $\square\square\square\square\square$

Step F: $p1$

cons:

- $l_1 \sim \rho_{17}$

subs: $\square\square\square\square$

Step R: $p1$

type: ρ_{17}

beha: τ

cons:

- $l_1 \sim \rho_{17}$

Step W : 1

typing context: $p1 : \forall(\rho_8 : l_1 \sim \rho_8).\rho_8$

Step W': 1

type:

beha: τ

cons:

-

subs: $\square\square\square\square$

Step F: 1

cons:

-

subs: $\square\square\square\square$

Step R: 1

type:

beha: τ

cons:

-

Step W': $(p1, 1)$

type: α_{16}

beha: $\tau; \tau$

cons:

- $\alpha_{14} \rightarrow \alpha_{15} \rightarrow (\alpha_{14} \times \alpha_{15}) \subseteq \rho_{17} \rightarrow \rightarrow \alpha_{16}$

- $l_1 \sim \rho_{17}$

subs: $\square\square\square\square\square$

Step F: $(p1, 1)$

cons:

- $\rho_{18} \sim \rho_{17}$

- $\rho_{19} \sim \rho_{18}$

- $l_1 \sim \rho_{17}$

subs: $[\alpha_{14} \mapsto \rho_{18}, \alpha_{15} \mapsto, \alpha_{16} \mapsto (\rho_{19} \times)]\square\square\square\square\square$

Step R: $(p1, 1)$

type: $(\rho_{19} \times)$

beha: $\tau; \tau$

cons:

- $l_1 \sim \rho_{19}$

Step W : $((p1, 200)((p1, 1)((p1, 1)((p1, 2))))$

typing context: $:\forall(\rho_{19} : l_1 \sim \rho_{19}).(\rho_{19} \times), p1 : \forall(\rho_8 : l_1 \sim \rho_8).\rho_8$

Step W :

typing context: $:\forall(\rho_{19} : l_1 \sim \rho_{19}).(\rho_{19} \times), p1 : \forall(\rho_8 : l_1 \sim \rho_8).\rho_8$

Step W':

type: $(\rho_{23} \times \alpha_{24}) \xrightarrow{\beta_{22}}$

beha: τ

cons:

- $\rho_{23}! \alpha_{24} \subseteq \beta_{22}$

subs: $\square\square\square\square\square$

Step F:

cons:

- $\rho_{23}!\alpha_{24} \subseteq \beta_{22}$

subs: $\square\square\square\square\square$

Step R:

type: $(\rho_{23} \times \alpha_{24}) \xrightarrow{\beta_{22}}$

beha: τ

cons:

- $\rho_{23}!\alpha_{24} \subseteq \beta_{22}$
-

Step W : $(p1, 200)((p1, 1)((p1, 1)((p1, 2))))$

typing context: $: \forall(\rho_{19} : l_1 \sim \rho_{19}).(\rho_{19} \times), p1 : \forall(\rho_8 : l_1 \sim \rho_8).\rho_8$

Step W : $(p1, 200)$

typing context: $: \forall(\rho_{19} : l_1 \sim \rho_{19}).(\rho_{19} \times), p1 : \forall(\rho_8 : l_1 \sim \rho_8).\rho_8$

Step W : $p1$

typing context: $: \forall(\rho_{19} : l_1 \sim \rho_{19}).(\rho_{19} \times), p1 : \forall(\rho_8 : l_1 \sim \rho_8).\rho_8$

Step W': $p1$

type: ρ_{28}

beha: τ

cons:

- $l_1 \sim \rho_{28}$

subs: $\square\square\square\square\square$

Step F: $p1$

cons:

- $l_1 \sim \rho_{28}$

subs: $\square\square\square\square\square$

Step R: $p1$

type: ρ_{28}

beha: τ

cons:

- $l_1 \sim \rho_{28}$

Step W : 200

typing context: $:\forall(\rho_{19} : l_1 \sim \rho_{19}).(\rho_{19} \times), p1 : \forall(\rho_8 : l_1 \sim \rho_8).\rho_8$

Step W': 200

type:

beha: τ

cons:

-

subs: $\square\square\square\square\square$

Step F: 200

cons:

-

subs: $\square\square\square\square\square$

Step R: 200

type:

beha: τ

cons:

-

Step W': $(p1, 200)$

type: α_{27}

beha: $\tau; \tau$

cons:

- $\alpha_{25} \rightarrow \alpha_{26} \rightarrow (\alpha_{25} \times \alpha_{26}) \subseteq \rho_{28} \rightarrow \rightarrow \alpha_{27}$

- $l_1 \sim \rho_{28}$

subs: $\square\square\square\square\square$

Step F: $(p1, 200)$

cons:

- $\rho_{29} \sim \rho_{28}$
- $\rho_{30} \sim \rho_{29}$
- $l_1 \sim \rho_{28}$

subs: $[\alpha_{25} \mapsto \rho_{29}, \alpha_{26} \mapsto, \alpha_{27} \mapsto (\rho_{30} \times)] \square \square \square \square$

Step R: $(p1, 200)$

type: $(\rho_{30} \times)$

beha: $\tau; \tau$

cons:

- $l_1 \sim \rho_{30}$

Step W : $((p1, 1)(p1, 1)(p1, 2)))$

typing context: $:\forall(\rho_{30} : l_1 \sim \rho_{30}).(\rho_{30} \times), :\forall(\rho_{19} : l_1 \sim \rho_{19}).(\rho_{19} \times), p1 : \forall(\rho_8 : l_1 \sim \rho_8).\rho_8$

Step W :

typing context: $:\forall(\rho_{30} : l_1 \sim \rho_{30}).(\rho_{30} \times), :\forall(\rho_{19} : l_1 \sim \rho_{19}).(\rho_{19} \times), p1 : \forall(\rho_8 : l_1 \sim \rho_8).\rho_8$

Step W':

type: $(\rho_{34} \times \alpha_{35}) \xrightarrow{\beta_{33}}$

beha: τ

cons:

- $\rho_{34}! \alpha_{35} \subseteq \beta_{33}$

subs: $\square \square \square \square$

Step F:

cons:

- $\rho_{34}! \alpha_{35} \subseteq \beta_{33}$

subs: $\square \square \square \square$

Step R:

type: $(\rho_{34} \times \alpha_{35}) \xrightarrow{\beta_{33}}$

beha: τ

cons:

- $\rho_{34}! \alpha_{35} \subseteq \beta_{33}$

Step W : $(p1, 1)((p1, 1)((p1, 2)))$

typing context: $: \forall(\rho_{30} : l_1 \sim \rho_{30}).(\rho_{30} \times), : \forall(\rho_{19} : l_1 \sim \rho_{19}).(\rho_{19} \times), p1 : \forall(\rho_8 : l_1 \sim \rho_8).\rho_8$

Step W : $(p1, 1)$

typing context: $: \forall(\rho_{30} : l_1 \sim \rho_{30}).(\rho_{30} \times), : \forall(\rho_{19} : l_1 \sim \rho_{19}).(\rho_{19} \times), p1 : \forall(\rho_8 : l_1 \sim \rho_8).\rho_8$

Step W : $p1$

typing context: $: \forall(\rho_{30} : l_1 \sim \rho_{30}).(\rho_{30} \times), : \forall(\rho_{19} : l_1 \sim \rho_{19}).(\rho_{19} \times), p1 : \forall(\rho_8 : l_1 \sim \rho_8).\rho_8$

Step W': $p1$

type: ρ_{39}

beha: τ

cons:

- $l_1 \sim \rho_{39}$

subs: $\square\square\square\square\square$

Step F: $p1$

cons:

- $l_1 \sim \rho_{39}$

subs: $\square\square\square\square\square$

Step R: $p1$

type: ρ_{39}

beha: τ

cons:

- $l_1 \sim \rho_{39}$

Step W : 1

typing context: $:\forall(\rho_{30} : l_1 \sim \rho_{30}).(\rho_{30} \times), :\forall(\rho_{19} : l_1 \sim \rho_{19}).(\rho_{19} \times), p1 : \forall(\rho_8 : l_1 \sim \rho_8).\rho_8$

Step W': 1

type:

beha: τ

cons:

•

subs: $\square\square\square\square\square$

Step F: 1

cons:

•

subs: $\square\square\square\square\square$

Step R: 1

type:

beha: τ

cons:

•

Step W': $(p1, 1)$

type: α_{38}

beha: $\tau; \tau$

cons:

• $\alpha_{36} \rightarrow \alpha_{37} \rightarrow (\alpha_{36} \times \alpha_{37}) \subseteq \rho_{39} \rightarrow \rightarrow \alpha_{38}$

• $l_1 \sim \rho_{39}$

subs: $\square\square\square\square\square$

Step F: $(p1, 1)$

cons:

- $\rho_{40} \sim \rho_{39}$
- $\rho_{41} \sim \rho_{40}$
- $l_1 \sim \rho_{39}$

subs: $[\alpha_{36} \mapsto \rho_{40}, \alpha_{37} \mapsto, \alpha_{38} \mapsto (\rho_{41} \times)] \square \square \square \square$

Step R: $(p1, 1)$

type: $(\rho_{41} \times)$

beha: $\tau; \tau$

cons:

- $l_1 \sim \rho_{41}$

Step W : $((p1, 1)(p1, 2))$

typing context: $:\forall(\rho_{41} : l_1 \sim \rho_{41}).(\rho_{41} \times), : \forall(\rho_{30} : l_1 \sim \rho_{30}).(\rho_{30} \times), : \forall(\rho_{19} : l_1 \sim \rho_{19}).(\rho_{19} \times), p1 : \forall(\rho_8 : l_1 \sim \rho_8).\rho_8$

Step W :

typing context: $:\forall(\rho_{41} : l_1 \sim \rho_{41}).(\rho_{41} \times), : \forall(\rho_{30} : l_1 \sim \rho_{30}).(\rho_{30} \times), : \forall(\rho_{19} : l_1 \sim \rho_{19}).(\rho_{19} \times), p1 : \forall(\rho_8 : l_1 \sim \rho_8).\rho_8$

Step W':

type: $(\rho_{45} \times \alpha_{46}) \xrightarrow{\beta_{44}}$

beha: τ

cons:

- $\rho_{45}! \alpha_{46} \subseteq \beta_{44}$

subs: $\square \square \square \square$

Step F:

cons:

- $\rho_{45}! \alpha_{46} \subseteq \beta_{44}$

subs: $\square \square \square \square$

Step R:

type: $(\rho_{45} \times \alpha_{46}) \xrightarrow{\beta_{44}}$

beha: τ

cons:

- $\rho_{45}! \alpha_{46} \subseteq \beta_{44}$

Step W : $(p1, 1)(p1, 2)$

typing context: $: \forall(\rho_{41} : l_1 \sim \rho_{41}).(\rho_{41} \times), : \forall(\rho_{30} : l_1 \sim \rho_{30}).(\rho_{30} \times), : \forall(\rho_{19} : l_1 \sim \rho_{19}).(\rho_{19} \times), p1 : \forall(\rho_8 : l_1 \sim \rho_8). \rho_8$

Step W : $(p1, 1)$

typing context: $: \forall(\rho_{41} : l_1 \sim \rho_{41}).(\rho_{41} \times), : \forall(\rho_{30} : l_1 \sim \rho_{30}).(\rho_{30} \times), : \forall(\rho_{19} : l_1 \sim \rho_{19}).(\rho_{19} \times), p1 : \forall(\rho_8 : l_1 \sim \rho_8). \rho_8$

Step W : $p1$

typing context: $: \forall(\rho_{41} : l_1 \sim \rho_{41}).(\rho_{41} \times), : \forall(\rho_{30} : l_1 \sim \rho_{30}).(\rho_{30} \times), : \forall(\rho_{19} : l_1 \sim \rho_{19}).(\rho_{19} \times), p1 : \forall(\rho_8 : l_1 \sim \rho_8). \rho_8$

Step W': $p1$

type: ρ_{50}

beha: τ

cons:

- $l_1 \sim \rho_{50}$

subs: $\square\square\square\square\square$

Step F: $p1$

cons:

- $l_1 \sim \rho_{50}$

subs: $\square\square\square\square\square$

Step R: $p1$

type: ρ_{50}

beha: τ

cons:

- $l_1 \sim \rho_{50}$

Step W : 1

typing context: $\vdash \forall(\rho_{41} : l_1 \sim \rho_{41}).(\rho_{41} \times), \vdash \forall(\rho_{30} : l_1 \sim \rho_{30}).(\rho_{30} \times), \vdash \forall(\rho_{19} : l_1 \sim \rho_{19}).(\rho_{19} \times), p1 : \forall(\rho_8 : l_1 \sim \rho_8).\rho_8$

Step W': 1

type:

beha: τ

cons:

•

subs: $\square\square\square\square\square$

Step F: 1

cons:

•

subs: $\square\square\square\square\square$

Step R: 1

type:

beha: τ

cons:

•

Step W': $(p1, 1)$

type: α_{49}

beha: $\tau; \tau$

cons:

• $\alpha_{47} \rightarrow \alpha_{48} \rightarrow (\alpha_{47} \times \alpha_{48}) \subseteq \rho_{50} \rightarrow \rightarrow \alpha_{49}$

• $l_1 \sim \rho_{50}$

subs: $\square\square\square\square\square$

Step F: $(p1, 1)$

cons:

- $\rho_{51} \sim \rho_{50}$
- $\rho_{52} \sim \rho_{51}$
- $l_1 \sim \rho_{50}$

subs: $[\alpha_{47} \mapsto \rho_{51}, \alpha_{48} \mapsto, \alpha_{49} \mapsto (\rho_{52} \times)] \square \square \square \square$

Step R: $(p1, 1)$

type: $(\rho_{52} \times)$

beha: $\tau; \tau$

cons:

- $l_1 \sim \rho_{52}$

Step W : $((p1, 2))$

typing context: $:\forall(\rho_{52} : l_1 \sim \rho_{52}).(\rho_{52} \times), :\forall(\rho_{41} : l_1 \sim \rho_{41}).(\rho_{41} \times), :\forall(\rho_{30} : l_1 \sim \rho_{30}).(\rho_{30} \times), :\forall(\rho_{19} : l_1 \sim \rho_{19}).(\rho_{19} \times), p1 : \forall(\rho_8 : l_1 \sim \rho_8). \rho_8$

Step W :

typing context: $:\forall(\rho_{52} : l_1 \sim \rho_{52}).(\rho_{52} \times), :\forall(\rho_{41} : l_1 \sim \rho_{41}).(\rho_{41} \times), :\forall(\rho_{30} : l_1 \sim \rho_{30}).(\rho_{30} \times), :\forall(\rho_{19} : l_1 \sim \rho_{19}).(\rho_{19} \times), p1 : \forall(\rho_8 : l_1 \sim \rho_8). \rho_8$

Step W':

type: $(\rho_{56} \times \alpha_{57}) \xrightarrow{\beta_{55}}$

beha: τ

cons:

- $\rho_{56}! \alpha_{57} \subseteq \beta_{55}$

subs: $\square \square \square \square \square$

Step F:

cons:

- $\rho_{56}! \alpha_{57} \subseteq \beta_{55}$

subs: $\square \square \square \square \square$

Step R:

type: $(\rho_{56} \times \alpha_{57}) \xrightarrow{\beta_{55}}$

beha: τ

cons:

- $\rho_{56}! \alpha_{57} \subseteq \beta_{55}$

Step W : $(p1, 2)$

typing context: $: \forall(\rho_{52} : l_1 \sim \rho_{52}).(\rho_{52} \times), : \forall(\rho_{41} : l_1 \sim \rho_{41}).(\rho_{41} \times), : \forall(\rho_{30} : l_1 \sim \rho_{30}).(\rho_{30} \times), : \forall(\rho_{19} : l_1 \sim \rho_{19}).(\rho_{19} \times), p1 : \forall(\rho_8 : l_1 \sim \rho_8). \rho_8$

Step W : $p1$

typing context: $: \forall(\rho_{52} : l_1 \sim \rho_{52}).(\rho_{52} \times), : \forall(\rho_{41} : l_1 \sim \rho_{41}).(\rho_{41} \times), : \forall(\rho_{30} : l_1 \sim \rho_{30}).(\rho_{30} \times), : \forall(\rho_{19} : l_1 \sim \rho_{19}).(\rho_{19} \times), p1 : \forall(\rho_8 : l_1 \sim \rho_8). \rho_8$

Step W': $p1$

type: ρ_{61}

beha: τ

cons:

- $l_1 \sim \rho_{61}$

subs: $\square \square \square \square \square$

Step F: $p1$

cons:

- $l_1 \sim \rho_{61}$

subs: $\square \square \square \square \square$

Step R: $p1$

type: ρ_{61}

beha: τ

cons:

- $l_1 \sim \rho_{61}$

Step W : 2

typing context: $\vdash \forall(\rho_{52} : l_1 \sim \rho_{52}).(\rho_{52} \times), \vdash \forall(\rho_{41} : l_1 \sim \rho_{41}).(\rho_{41} \times), \vdash \forall(\rho_{30} : l_1 \sim \rho_{30}).(\rho_{30} \times), \vdash \forall(\rho_{19} : l_1 \sim \rho_{19}).(\rho_{19} \times), p1 : \forall(\rho_8 : l_1 \sim \rho_8).\rho_8$

Step W': 2

type:

beha: τ

cons:

•

subs: $\square \square \square \square$

Step F: 2

cons:

•

subs: $\square \square \square \square$

Step R: 2

type:

beha: τ

cons:

•

Step W': $(p1, 2)$

type: α_{60}

beha: $\tau; \tau$

cons:

• $\alpha_{58} \rightarrow \alpha_{59} \rightarrow (\alpha_{58} \times \alpha_{59}) \subseteq \rho_{61} \rightarrow \rightarrow \alpha_{60}$

• $l_1 \sim \rho_{61}$

subs: $\square \square \square \square$

Step F: $(p1, 2)$

cons:

• $\rho_{62} \sim \rho_{61}$

- $\rho_{63} \sim \rho_{62}$

- $l_1 \sim \rho_{61}$

subs: $[\alpha_{58} \mapsto \rho_{62}, \alpha_{59} \mapsto, \alpha_{60} \mapsto (\rho_{63} \times)] \square \square \square \square$

Step R: $(p1, 2)$

type: $(\rho_{63} \times)$

beha: $\tau; \tau$

cons:

- $l_1 \sim \rho_{63}$

Step W': $((p1, 2))$

type: α_{53}

beha: $\tau; \tau; \tau; \beta_{54}$

cons:

- $(\rho_{56} \times \alpha_{57}) \xrightarrow{\beta_{55}} \subseteq (\rho_{63} \times) \xrightarrow{\beta_{54}} \alpha_{53}$

- $\rho_{56}! \alpha_{57} \subseteq \beta_{55}$

- $l_1 \sim \rho_{63}$

subs: $[\alpha_{58} \mapsto \rho_{62}, \alpha_{59} \mapsto, \alpha_{60} \mapsto (\rho_{63} \times)] \square \square \square \square$

Step F: $((p1, 2))$

cons:

- $\beta_{55} \subseteq \beta_{54}$

- $\rho_{56}! \subseteq \beta_{55}$

- $\rho_{56} \sim \rho_{63}$

- $l_1 \sim \rho_{63}$

subs: $[\alpha_{53} \mapsto, \alpha_{57} \mapsto] \square \square \square \square$

Step R: $((p1, 2))$

type:

beha: $\tau; \tau; \tau; \beta_{54}$

cons:

- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

Step W': $(p1, 1)(p1, 2)$

type:

beha: $\tau; \tau; \tau; \tau; \tau; \beta_{54}$

cons:

- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

subs: $[\alpha_{47} \mapsto \rho_{51}, \alpha_{48} \mapsto, \alpha_{49} \mapsto (\rho_{52} \times), \alpha_{53} \mapsto, \alpha_{57} \mapsto, \alpha_{58} \mapsto \rho_{62}, \alpha_{59} \mapsto, \alpha_{60} \mapsto (\rho_{63} \times)] \square \square \square \square$

Step F: $(p1, 1)(p1, 2)$

cons:

- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

subs: $\square \square \square \square \square$

Step R: $(p1, 1)(p1, 2)$

type:

beha: $\tau; \tau; \tau; \tau; \tau; \beta_{54}$

cons:

- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

Step W': $((p1, 1)(p1, 2))$

type: α_{42}

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \beta_{54}; \beta_{43}$

cons:

- $(\rho_{45} \times \alpha_{46}) \xrightarrow{\beta_{44}} \subseteq \xrightarrow{\beta_{43}} \alpha_{42}$

- $\rho_{45}!\alpha_{46} \subseteq \beta_{44}$
- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

subs: $[\alpha_{47} \mapsto \rho_{51}, \alpha_{48} \mapsto, \alpha_{49} \mapsto (\rho_{52} \times), \alpha_{53} \mapsto, \alpha_{57} \mapsto, \alpha_{58} \mapsto \rho_{62}, \alpha_{59} \mapsto, \alpha_{60} \mapsto (\rho_{63} \times)] \square \square \square \square$

Step F: $((p1, 1)(p1, 2))$

cons:

- $\subseteq (\rho_{45} \times \alpha_{46})$
- $\beta_{44} \subseteq \beta_{43}$
- $\rho_{45}!\alpha_{46} \subseteq \beta_{44}$
- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

subs: $[\alpha_{42} \mapsto] \square \square \square \square$

Step R: $((p1, 1)(p1, 2))$

type:

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{54}; \beta_{43}$

cons:

- $\subseteq (\rho_{45} \times \alpha_{46})$
- $\rho_{45}!\alpha_{46} \subseteq \beta_{43}$
- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

Step W': $((p1, 1)(p1, 1)(p1, 2))$

type:

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{54}; \beta_{43}$

cons:

- $\subseteq (\rho_{45} \times \alpha_{46})$
- $\rho_{45}! \alpha_{46} \subseteq \beta_{43}$
- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

subs: $[\alpha_{36} \mapsto \rho_{40}, \alpha_{37} \mapsto, \alpha_{38} \mapsto (\rho_{41} \times), \alpha_{42} \mapsto, \alpha_{47} \mapsto \rho_{51}, \alpha_{48} \mapsto, \alpha_{49} \mapsto (\rho_{52} \times), \alpha_{53} \mapsto, \alpha_{57} \mapsto, \alpha_{58} \mapsto \rho_{62}, \alpha_{59} \mapsto, \alpha_{60} \mapsto (\rho_{63} \times)] \square \square \square \square$

Step F: $(p1, 1)((p1, 1)((p1, 2)))$
 cons:

- $\subseteq (\rho_{45} \times \alpha_{46})$
- $\rho_{45}! \alpha_{46} \subseteq \beta_{43}$
- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

subs: $\square \square \square \square$

Step R: $(p1, 1)((p1, 1)((p1, 2)))$

type:

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{54}; \beta_{43}$

cons:

- $\subseteq (\rho_{45} \times \alpha_{46})$
- $\rho_{45}! \alpha_{46} \subseteq \beta_{43}$
- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

Step W': $((p1, 1)((p1, 1)((p1, 2))))$

type: α_{31}

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{54}; \beta_{43}; \beta_{32}$

cons:

- $\subseteq (\rho_{45} \times \alpha_{46})$
- $(\rho_{34} \times \alpha_{35}) \xrightarrow{\beta_{33}} \subseteq \xrightarrow{\beta_{32}} \alpha_{31}$
- $\rho_{34}! \alpha_{35} \subseteq \beta_{33}$
- $\rho_{45}! \alpha_{46} \subseteq \beta_{43}$
- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

subs: $[\alpha_{36} \mapsto \rho_{40}, \alpha_{37} \mapsto, \alpha_{38} \mapsto (\rho_{41} \times), \alpha_{42} \mapsto, \alpha_{47} \mapsto \rho_{51}, \alpha_{48} \mapsto, \alpha_{49} \mapsto (\rho_{52} \times), \alpha_{53} \mapsto, \alpha_{57} \mapsto, \alpha_{58} \mapsto \rho_{62}, \alpha_{59} \mapsto, \alpha_{60} \mapsto (\rho_{63} \times)] \square \square \square \square$

Step F: $((p1, 1)(p1, 1)(p1, 2)))$

cons:

- $\subseteq (\rho_{34} \times \alpha_{35})$
- $\subseteq (\rho_{45} \times \alpha_{46})$
- $\beta_{33} \subseteq \beta_{32}$
- $\rho_{34}! \alpha_{35} \subseteq \beta_{33}$
- $\rho_{45}! \alpha_{46} \subseteq \beta_{43}$
- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

subs: $[\alpha_{31} \mapsto] \square \square \square \square$

Step R: $((p1, 1)(p1, 1)(p1, 2)))$

type:

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{54}; \beta_{43}; \beta_{32}$

cons:

- $\subseteq (\rho_{34} \times \alpha_{35})$
- $\subseteq (\rho_{45} \times \alpha_{46})$

- $\rho_{34}!\alpha_{35} \subseteq \beta_{32}$
- $\rho_{45}!\alpha_{46} \subseteq \beta_{43}$
- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

Step W': $(p1, 200)((p1, 1)((p1, 1)((p1, 2))))$

type:

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{54}; \beta_{43}; \beta_{32}$

cons:

- $\subseteq (\rho_{34} \times \alpha_{35})$
- $\subseteq (\rho_{45} \times \alpha_{46})$
- $\rho_{34}!\alpha_{35} \subseteq \beta_{32}$
- $\rho_{45}!\alpha_{46} \subseteq \beta_{43}$
- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

subs: $[\alpha_{25} \mapsto \rho_{29}, \alpha_{26} \mapsto, \alpha_{27} \mapsto (\rho_{30} \times), \alpha_{31} \mapsto, \alpha_{36} \mapsto \rho_{40}, \alpha_{37} \mapsto, \alpha_{38} \mapsto$
 $(\rho_{41} \times), \alpha_{42} \mapsto, \alpha_{47} \mapsto \rho_{51}, \alpha_{48} \mapsto, \alpha_{49} \mapsto (\rho_{52} \times), \alpha_{53} \mapsto, \alpha_{57} \mapsto, \alpha_{58} \mapsto \rho_{62}, \alpha_{59} \mapsto$
 $, \alpha_{60} \mapsto (\rho_{63} \times)] \square \square \square \square$

Step F: $(p1, 200)((p1, 1)((p1, 1)((p1, 2))))$

cons:

- $\subseteq (\rho_{34} \times \alpha_{35})$
- $\subseteq (\rho_{45} \times \alpha_{46})$
- $\rho_{34}!\alpha_{35} \subseteq \beta_{32}$
- $\rho_{45}!\alpha_{46} \subseteq \beta_{43}$
- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

subs: $\square\square\square\square\square$

Step R: $(p1, 200)((p1, 1)((p1, 1)((p1, 2))))$

type:

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{54}; \beta_{43}; \beta_{32}$

cons:

- $\subseteq (\rho_{34} \times \alpha_{35})$
 - $\subseteq (\rho_{45} \times \alpha_{46})$
 - $\rho_{34}! \alpha_{35} \subseteq \beta_{32}$
 - $\rho_{45}! \alpha_{46} \subseteq \beta_{43}$
 - $\rho_{56}! \subseteq \beta_{54}$
 - $l_1 \sim \rho_{56}$
-

Step W': $((p1, 200)((p1, 1)((p1, 1)((p1, 2))))$

type: α_{20}

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{54}; \beta_{43}; \beta_{32}; \beta_{21}$

cons:

- $\subseteq (\rho_{34} \times \alpha_{35})$
- $\subseteq (\rho_{45} \times \alpha_{46})$
- $(\rho_{23} \times \alpha_{24}) \xrightarrow{\beta_{22}} \subseteq \xrightarrow{\beta_{21}} \alpha_{20}$
- $\rho_{23}! \alpha_{24} \subseteq \beta_{22}$
- $\rho_{34}! \alpha_{35} \subseteq \beta_{32}$
- $\rho_{45}! \alpha_{46} \subseteq \beta_{43}$
- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

subs: $[\alpha_{25} \mapsto \rho_{29}, \alpha_{26} \mapsto, \alpha_{27} \mapsto (\rho_{30} \times), \alpha_{31} \mapsto, \alpha_{36} \mapsto \rho_{40}, \alpha_{37} \mapsto, \alpha_{38} \mapsto$
 $(\rho_{41} \times), \alpha_{42} \mapsto, \alpha_{47} \mapsto \rho_{51}, \alpha_{48} \mapsto, \alpha_{49} \mapsto (\rho_{52} \times), \alpha_{53} \mapsto, \alpha_{57} \mapsto, \alpha_{58} \mapsto \rho_{62}, \alpha_{59} \mapsto$
 $, \alpha_{60} \mapsto (\rho_{63} \times)] \square \square \square \square$

Step F: $((p1, 200)((p1, 1)((p1, 1)((p1, 2))))$

cons:

- $\subseteq (\rho_{23} \times \alpha_{24})$
- $\subseteq (\rho_{34} \times \alpha_{35})$
- $\subseteq (\rho_{45} \times \alpha_{46})$
- $\beta_{22} \subseteq \beta_{21}$
- $\rho_{23}! \alpha_{24} \subseteq \beta_{22}$
- $\rho_{34}! \alpha_{35} \subseteq \beta_{32}$
- $\rho_{45}! \alpha_{46} \subseteq \beta_{43}$
- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

subs: $[\alpha_{20} \mapsto] \square \square \square \square$

Step R: $((p1, 200)((p1, 1)((p1, 1)((p1, 2))))$

type:

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{54}; \beta_{43}; \beta_{32}; \beta_{21}$

cons:

- $\subseteq (\rho_{23} \times \alpha_{24})$
- $\subseteq (\rho_{34} \times \alpha_{35})$
- $\subseteq (\rho_{45} \times \alpha_{46})$
- $\rho_{23}! \alpha_{24} \subseteq \beta_{21}$
- $\rho_{34}! \alpha_{35} \subseteq \beta_{32}$
- $\rho_{45}! \alpha_{46} \subseteq \beta_{43}$

- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

Step W': $(p1, 1)((p1, 200)((p1, 1)((p1, 1)((p1, 2)))))$

type:

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{54}; \beta_{43}; \beta_{32}; \beta_{21}$

cons:

- $\subseteq (\rho_{23} \times \alpha_{24})$
- $\subseteq (\rho_{34} \times \alpha_{35})$
- $\subseteq (\rho_{45} \times \alpha_{46})$
- $\rho_{23}! \alpha_{24} \subseteq \beta_{21}$
- $\rho_{34}! \alpha_{35} \subseteq \beta_{32}$
- $\rho_{45}! \alpha_{46} \subseteq \beta_{43}$
- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

subs: $[\alpha_{14} \mapsto \rho_{18}, \alpha_{15} \mapsto, \alpha_{16} \mapsto (\rho_{19} \times), \alpha_{20} \mapsto, \alpha_{25} \mapsto \rho_{29}, \alpha_{26} \mapsto, \alpha_{27} \mapsto (\rho_{30} \times), \alpha_{31} \mapsto, \alpha_{36} \mapsto \rho_{40}, \alpha_{37} \mapsto, \alpha_{38} \mapsto (\rho_{41} \times), \alpha_{42} \mapsto, \alpha_{47} \mapsto \rho_{51}, \alpha_{48} \mapsto, \alpha_{49} \mapsto (\rho_{52} \times), \alpha_{53} \mapsto, \alpha_{57} \mapsto, \alpha_{58} \mapsto \rho_{62}, \alpha_{59} \mapsto, \alpha_{60} \mapsto (\rho_{63} \times)] \square \square \square \square$

Step F: $(p1, 1)((p1, 200)((p1, 1)((p1, 1)((p1, 2)))))$

cons:

- $\subseteq (\rho_{23} \times \alpha_{24})$
- $\subseteq (\rho_{34} \times \alpha_{35})$
- $\subseteq (\rho_{45} \times \alpha_{46})$
- $\rho_{23}! \alpha_{24} \subseteq \beta_{21}$
- $\rho_{34}! \alpha_{35} \subseteq \beta_{32}$
- $\rho_{45}! \alpha_{46} \subseteq \beta_{43}$

- $\rho_{56}! \subseteq \beta_{54}$

- $l_1 \sim \rho_{56}$

subs: $\square\square\square\square\square$

Step R: $(p1, 1)((p1, 200)((p1, 1)((p1, 1)((p1, 2))))))$

type:

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{54}; \beta_{43}; \beta_{32}; \beta_{21}$

cons:

- $\subseteq (\rho_{23} \times \alpha_{24})$

- $\subseteq (\rho_{34} \times \alpha_{35})$

- $\subseteq (\rho_{45} \times \alpha_{46})$

- $\rho_{23}!\alpha_{24} \subseteq \beta_{21}$

- $\rho_{34}!\alpha_{35} \subseteq \beta_{32}$

- $\rho_{45}!\alpha_{46} \subseteq \beta_{43}$

- $\rho_{56}! \subseteq \beta_{54}$

- $l_1 \sim \rho_{56}$

Step W': $((p1, 1)((p1, 200)((p1, 1)((p1, 1)((p1, 2))))))$

type: α_9

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{54}; \beta_{43}; \beta_{32}; \beta_{21}; \beta_{10}$

cons:

- $\subseteq (\rho_{23} \times \alpha_{24})$

- $\subseteq (\rho_{34} \times \alpha_{35})$

- $\subseteq (\rho_{45} \times \alpha_{46})$

- $(\rho_{12} \times \alpha_{13}) \xrightarrow{\beta_{11}} \subseteq \xrightarrow{\beta_{10}} \alpha_9$

- $\rho_{12}!\alpha_{13} \subseteq \beta_{11}$

- $\rho_{23}!\alpha_{24} \subseteq \beta_{21}$
- $\rho_{34}!\alpha_{35} \subseteq \beta_{32}$
- $\rho_{45}!\alpha_{46} \subseteq \beta_{43}$
- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

subs: $[\alpha_{14} \mapsto \rho_{18}, \alpha_{15} \mapsto, \alpha_{16} \mapsto (\rho_{19} \times), \alpha_{20} \mapsto, \alpha_{25} \mapsto \rho_{29}, \alpha_{26} \mapsto, \alpha_{27} \mapsto (\rho_{30} \times), \alpha_{31} \mapsto, \alpha_{36} \mapsto \rho_{40}, \alpha_{37} \mapsto, \alpha_{38} \mapsto (\rho_{41} \times), \alpha_{42} \mapsto, \alpha_{47} \mapsto \rho_{51}, \alpha_{48} \mapsto, \alpha_{49} \mapsto (\rho_{52} \times), \alpha_{53} \mapsto, \alpha_{57} \mapsto, \alpha_{58} \mapsto \rho_{62}, \alpha_{59} \mapsto, \alpha_{60} \mapsto (\rho_{63} \times)] \square \square \square \square$

Step F: $((p1, 1)(p1, 200)(p1, 1)(p1, 1)(p1, 2))))$

cons:

- $\subseteq (\rho_{12} \times \alpha_{13})$
- $\subseteq (\rho_{23} \times \alpha_{24})$
- $\subseteq (\rho_{34} \times \alpha_{35})$
- $\subseteq (\rho_{45} \times \alpha_{46})$
- $\beta_{11} \subseteq \beta_{10}$
- $\rho_{12}!\alpha_{13} \subseteq \beta_{11}$
- $\rho_{23}!\alpha_{24} \subseteq \beta_{21}$
- $\rho_{34}!\alpha_{35} \subseteq \beta_{32}$
- $\rho_{45}!\alpha_{46} \subseteq \beta_{43}$
- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

subs: $[\alpha_9 \mapsto] \square \square \square \square$

Step R: $((p1, 1)(p1, 200)(p1, 1)(p1, 1)(p1, 2))))$

type:

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{54}; \beta_{43}; \beta_{32}; \beta_{21}; \beta_{10}$

cons:

- $\subseteq (\rho_{12} \times \alpha_{13})$
- $\subseteq (\rho_{23} \times \alpha_{24})$
- $\subseteq (\rho_{34} \times \alpha_{35})$
- $\subseteq (\rho_{45} \times \alpha_{46})$
- $\rho_{12}! \alpha_{13} \subseteq \beta_{10}$
- $\rho_{23}! \alpha_{24} \subseteq \beta_{21}$
- $\rho_{34}! \alpha_{35} \subseteq \beta_{32}$
- $\rho_{45}! \alpha_{46} \subseteq \beta_{43}$
- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

Step W': $p1(l_1 t s l \ ()) ((p1, 1) ((p1, 200) ((p1, 1) ((p1, 1) ((p1, 2)))))))$

type:

beha: $\tau; \tau; \beta_4; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{54}; \beta_{43}; \beta_{32}; \beta_{21}; \beta_{10}$

cons:

- $\subseteq (\rho_{12} \times \alpha_{13})$
- $\subseteq (\rho_{23} \times \alpha_{24})$
- $\subseteq (\rho_{34} \times \alpha_{35})$
- $\subseteq (\rho_{45} \times \alpha_{46})$
- $t s l^{l_1} \sim \psi_5$
- $l_1 \psi_5 \subseteq \beta_4$
- $\rho_{12}! \alpha_{13} \subseteq \beta_{10}$
- $\rho_{23}! \alpha_{24} \subseteq \beta_{21}$
- $\rho_{34}! \alpha_{35} \subseteq \beta_{32}$

- $\rho_{45}!\alpha_{46} \subseteq \beta_{43}$
- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

subs: $[\alpha_3 \mapsto \rho_8, \alpha_9 \mapsto, \alpha_{14} \mapsto \rho_{18}, \alpha_{15} \mapsto, \alpha_{16} \mapsto (\rho_{19} \times), \alpha_{20} \mapsto, \alpha_{25} \mapsto \rho_{29}, \alpha_{26} \mapsto, \alpha_{27} \mapsto (\rho_{30} \times), \alpha_{31} \mapsto, \alpha_{36} \mapsto \rho_{40}, \alpha_{37} \mapsto, \alpha_{38} \mapsto (\rho_{41} \times), \alpha_{42} \mapsto, \alpha_{47} \mapsto \rho_{51}, \alpha_{48} \mapsto, \alpha_{49} \mapsto (\rho_{52} \times), \alpha_{53} \mapsto, \alpha_{57} \mapsto, \alpha_{58} \mapsto \rho_{62}, \alpha_{59} \mapsto, \alpha_{60} \mapsto (\rho_{63} \times)] \square \square \square \square$

Step F: $p1(l_1 tsl ()) ((p1, 1) ((p1, 200) ((p1, 1) ((p1, 1) ((p1, 2)))))))$

cons:

- $\subseteq (\rho_{12} \times \alpha_{13})$
- $\subseteq (\rho_{23} \times \alpha_{24})$
- $\subseteq (\rho_{34} \times \alpha_{35})$
- $\subseteq (\rho_{45} \times \alpha_{46})$
- $tsl^{l_1} \sim \psi_5$
- $l_1 \psi_5 \subseteq \beta_4$
- $\rho_{12}!\alpha_{13} \subseteq \beta_{10}$
- $\rho_{23}!\alpha_{24} \subseteq \beta_{21}$
- $\rho_{34}!\alpha_{35} \subseteq \beta_{32}$
- $\rho_{45}!\alpha_{46} \subseteq \beta_{43}$
- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

subs: $\square \square \square \square \square$

Step R: $p1(l_1 tsl ()) ((p1, 1) ((p1, 200) ((p1, 1) ((p1, 1) ((p1, 2)))))))$

type:

beha: $\tau; \tau; \beta_4; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{54}; \beta_{43}; \beta_{32}; \beta_{21}; \beta_{10}$

cons:

- $\subseteq (\rho_{12} \times \alpha_{13})$
- $\subseteq (\rho_{23} \times \alpha_{24})$
- $\subseteq (\rho_{34} \times \alpha_{35})$
- $\subseteq (\rho_{45} \times \alpha_{46})$
- $tsl^{l_1} \sim \psi_5$
- $l_1\psi_5 \subseteq \beta_4$
- $\rho_{12}!\alpha_{13} \subseteq \beta_{10}$
- $\rho_{23}!\alpha_{24} \subseteq \beta_{21}$
- $\rho_{34}!\alpha_{35} \subseteq \beta_{32}$
- $\rho_{45}!\alpha_{46} \subseteq \beta_{43}$
- $\rho_{56}! \subseteq \beta_{54}$
- $l_1 \sim \rho_{56}$

Step W : $servermyVNum2p2(l_2tsl())((p2((p2((p2((p2(p2)))))))))(client)(server)$
 typing context: $client : \forall(:)$.

Step W : $myVNum2p2(l_2tsl())(p2((p2((p2((p2(p2))))))))$
 typing context: $client : \forall(\cdot)$.

Step W : 2
typing context: $client : \forall(\cdot)$.

```
Step W': 2
type:
beha:  $\tau$ 
cons:
```

-

subs: $\square\square\square\square$

Step F: 2

cons:

•

subs: $\square\square\square\square$

Step R: 2

type:

beha: τ

cons:

•

Step W : $p2(l_2tsl\ ())((p2\ ((p2\ ((p2\ (p2)))))))$

typing context: $myVNum : \forall(:)., client : \forall(:).$

Step W : $(l_2tsl\ ())$

typing context: $myVNum : \forall(:)., client : \forall(:).$

Step W : l_2tsl

typing context: $myVNum : \forall(:)., client : \forall(:).$

Step W': l_2tsl

type: $\xrightarrow{\beta_{68}} \rho_{66}$

beha: τ

cons:

- $\overline{tsl^{l_2}} \sim \psi_{67}$
- $l_2\psi_{67} \subseteq \beta_{68}$
- $l_2 \sim \rho_{66}$

subs: $\square\square\square\square$

Step F: l_2tsl

cons:

- $\overline{tsl^{l_2}} \sim \psi_{67}$
- $l_2\psi_{67} \subseteq \beta_{68}$
- $l_2 \sim \rho_{66}$

subs: $\square\square\square\square\square$

Step R: l_2tsl

type: $\xrightarrow{\beta_{68}} \rho_{66}$

beha: τ

cons:

- $\overline{tsl^{l_2}} \sim \psi_{67}$
- $l_2\psi_{67} \subseteq \beta_{68}$
- $l_2 \sim \rho_{66}$

Step W : $()$

typing context: $myVNum : \forall(:)., client : \forall(:).$

Step W': $()$

type:

beha: τ

cons:

•

subs: $\square\square\square\square\square$

Step F: $()$

cons:

•

subs: $\square\square\square\square\square$

Step R: $()$

type:

beha: τ

cons:

•

Step W': (l_2tsl ())

type: α_{64}

beha: $\tau; \tau; \beta_{65}$

cons:

- $\xrightarrow{\beta_{68}} \rho_{66} \subseteq \xrightarrow{\beta_{65}} \alpha_{64}$
- $\overline{tsl^{l_2}} \sim \psi_{67}$
- $l_2\psi_{67} \subseteq \beta_{68}$
- $l_2 \sim \rho_{66}$

subs: $\square\square\square\square\square$

Step F: (l_2tsl ())

cons:

- $\overline{tsl^{l_2}} \sim \psi_{67}$
- $\beta_{68} \subseteq \beta_{65}$
- $l_2\psi_{67} \subseteq \beta_{68}$
- $\rho_{69} \sim \rho_{66}$
- $l_2 \sim \rho_{66}$

subs: $[\alpha_{64} \mapsto \rho_{69}]\square\square\square\square$

Step R: (l_2tsl ())

type: ρ_{69}

beha: $\tau; \tau; \beta_{65}$

cons:

- $\overline{tsl^{l_2}} \sim \psi_{67}$
- $l_2\psi_{67} \subseteq \beta_{65}$
- $l_2 \sim \rho_{69}$

Step W : ((p2 ((p2 ((p2 ((p2 (p2))))))))))
 typing context: $p2 : \forall(\rho_{69} : l_2 \sim \rho_{69}).\rho_{69}, myVNum : \forall(:)., client : \forall(:).$

Step W :
 typing context: $p2 : \forall(\rho_{69} : l_2 \sim \rho_{69}).\rho_{69}, myVNum : \forall(:)., client : \forall(:).$

Step W':
 type: $\rho_{74} \xrightarrow{\beta_{73}} \alpha_{72}$
 beha: τ
 cons:

- $\rho_{74}?\alpha_{72} \subseteq \beta_{73}$

subs: $\square\square\square\square$

Step F:
 cons:

- $\rho_{74}?\alpha_{72} \subseteq \beta_{73}$

subs: $\square\square\square\square$

Step R:
 type: $\rho_{74} \xrightarrow{\beta_{73}} \alpha_{72}$
 beha: τ
 cons:

- $\rho_{74}?\alpha_{72} \subseteq \beta_{73}$
-

Step W : (p2 ((p2 ((p2 ((p2 (p2))))))))
 typing context: $p2 : \forall(\rho_{69} : l_2 \sim \rho_{69}).\rho_{69}, myVNum : \forall(:)., client : \forall(:).$

Step W : p2
 typing context: $p2 : \forall(\rho_{69} : l_2 \sim \rho_{69}).\rho_{69}, myVNum : \forall(:)., client : \forall(:).$

Step W': p2
 type: ρ_{77}
 beha: τ
 cons:

- $l_2 \sim \rho_{77}$

subs: $\square\square\square\square\square$

Step F: $p2$

cons:

- $l_2 \sim \rho_{77}$

subs: $\square\square\square\square\square$

Step R: $p2$

type: ρ_{77}

beha: τ

cons:

- $l_2 \sim \rho_{77}$
-

Step W : (($p2$ (($p2$ (($p2$ ($p2$))))))

typing context: $p2 : \forall(\rho_{69} : l_2 \sim \rho_{69}).\rho_{69}, myVNum : \forall(:)., client : \forall(:).$

Step W :

typing context: $p2 : \forall(\rho_{69} : l_2 \sim \rho_{69}).\rho_{69}, myVNum : \forall(:)., client : \forall(:).$

Step W':

type: $\rho_{82} \xrightarrow{\beta_{81}} \alpha_{80}$

beha: τ

cons:

- $\rho_{82}?\alpha_{80} \subseteq \beta_{81}$

subs: $\square\square\square\square\square$

Step F:

cons:

- $\rho_{82}?\alpha_{80} \subseteq \beta_{81}$

subs: $\square\square\square\square\square$

Step R:

type: $\rho_{82} \xrightarrow{\beta_{81}} \alpha_{80}$

beha: τ

cons:

- $\rho_{82}?\alpha_{80} \subseteq \beta_{81}$

Step W : $(p2 \ (\ (p2 \ (\ (p2 \ (\ p2))))))$

typing context: $p2 : \forall(\rho_{69} : l_2 \sim \rho_{69}).\rho_{69}, myVNum : \forall(:)., client : \forall(:).$

Step W : $p2$

typing context: $p2 : \forall(\rho_{69} : l_2 \sim \rho_{69}).\rho_{69}, myVNum : \forall(:)., client : \forall(:).$

Step W': $p2$

type: ρ_{85}

beha: τ

cons:

- $l_2 \sim \rho_{85}$

subs: $\square\square\square\square\square$

Step F: $p2$

cons:

- $l_2 \sim \rho_{85}$

subs: $\square\square\square\square\square$

Step R: $p2$

type: ρ_{85}

beha: τ

cons:

- $l_2 \sim \rho_{85}$

Step W : $(\ (p2 \ (\ (p2 \ (\ p2))))$

typing context: $p2 : \forall(\rho_{69} : l_2 \sim \rho_{69}).\rho_{69}, myVNum : \forall(:)., client : \forall(:).$

Step W :

typing context: $p2 : \forall(\rho_{69} : l_2 \sim \rho_{69}).\rho_{69}, myVNum : \forall(:)., client : \forall(:).$

Step W':

type: $\rho_{90} \xrightarrow{\beta_{89}} \alpha_{88}$

beha: τ

cons:

- $\rho_{90}?\alpha_{88} \subseteq \beta_{89}$

subs: $\square\square\square\square\square$

Step F:

cons:

- $\rho_{90}?\alpha_{88} \subseteq \beta_{89}$

subs: $\square\square\square\square\square$

Step R:

type: $\rho_{90} \xrightarrow{\beta_{89}} \alpha_{88}$

beha: τ

cons:

- $\rho_{90}?\alpha_{88} \subseteq \beta_{89}$
-

Step W : $(p2 ((p2 (p2))))$

typing context: $p2 : \forall(\rho_{69} : l_2 \sim \rho_{69}).\rho_{69}, myVNum : \forall(:)., client : \forall(:).$

Step W : $p2$

typing context: $p2 : \forall(\rho_{69} : l_2 \sim \rho_{69}).\rho_{69}, myVNum : \forall(:)., client : \forall(:).$

Step W': $p2$

type: ρ_{93}

beha: τ

cons:

- $l_2 \sim \rho_{93}$

subs: $\square\square\square\square$

Step F: $p2$

cons:

- $l_2 \sim \rho_{93}$

subs: $\square\square\square\square$

Step R: $p2$

type: ρ_{93}

beha: τ

cons:

- $l_2 \sim \rho_{93}$
-

Step W : (($p2$ ($p2$)))

typing context: $p2 : \forall(\rho_{69} : l_2 \sim \rho_{69}).\rho_{69}, myVNum : \forall(:)., client : \forall(:).$

Step W :

typing context: $p2 : \forall(\rho_{69} : l_2 \sim \rho_{69}).\rho_{69}, myVNum : \forall(:)., client : \forall(:).$

Step W':

type: $\rho_{98} \xrightarrow{\beta_{97}} \alpha_{96}$

beha: τ

cons:

- $\rho_{98}?\alpha_{96} \subseteq \beta_{97}$

subs: $\square\square\square\square$

Step F:

cons:

- $\rho_{98}?\alpha_{96} \subseteq \beta_{97}$

subs: $\square\square\square\square$

Step R:

type: $\rho_{98} \xrightarrow{\beta_{97}} \alpha_{96}$

beha: τ

cons:

- $\rho_{98}?\alpha_{96} \subseteq \beta_{97}$

Step W : ($p2$ ($p2$))

typing context: $p2 : \forall(\rho_{69} : l_2 \sim \rho_{69}).\rho_{69}, myVNum : \forall(:)., client : \forall(:).$

Step W : $p2$

typing context: $p2 : \forall(\rho_{69} : l_2 \sim \rho_{69}).\rho_{69}, myVNum : \forall(:)., client : \forall(:).$

Step W': $p2$

type: ρ_{101}

beha: τ

cons:

- $l_2 \sim \rho_{101}$

subs: $\square\square\square\square\square$

Step F: $p2$

cons:

- $l_2 \sim \rho_{101}$

subs: $\square\square\square\square\square$

Step R: $p2$

type: ρ_{101}

beha: τ

cons:

- $l_2 \sim \rho_{101}$

Step W : ($p2$)

typing context: $p2 : \forall(\rho_{69} : l_2 \sim \rho_{69}).\rho_{69}, myVNum : \forall(:)., client : \forall(:).$

Step W :

typing context: $p2 : \forall(\rho_{69} : l_2 \sim \rho_{69}).\rho_{69}, myVNum : \forall(:)., client : \forall(:).$

Step W':

type: $\rho_{106} \xrightarrow{\beta_{105}} \alpha_{104}$

beha: τ

cons:

- $\rho_{106}?\alpha_{104} \subseteq \beta_{105}$

subs: $\square\square\square\square\square$

Step F:

cons:

- $\rho_{106}?\alpha_{104} \subseteq \beta_{105}$

subs: $\square\square\square\square\square$

Step R:

type: $\rho_{106} \xrightarrow{\beta_{105}} \alpha_{104}$

beha: τ

cons:

- $\rho_{106}?\alpha_{104} \subseteq \beta_{105}$
-

Step W : $p2$

typing context: $p2 : \forall(\rho_{69} : l_2 \sim \rho_{69}).\rho_{69}, myVNum : \forall(:)., client : \forall(:).$

Step W': $p2$

type: ρ_{107}

beha: τ

cons:

- $l_2 \sim \rho_{107}$

subs: $\square\square\square\square\square$

Step F: $p2$

cons:

- $l_2 \sim \rho_{107}$

subs: $\square\square\square\square\square$

Step R: $p2$

type: ρ_{107}

beha: τ

cons:

- $l_2 \sim \rho_{107}$

Step W': ($p2$)

type: α_{102}

beha: $\tau; \tau; \beta_{103}$

cons:

- $\rho_{106} \xrightarrow{\beta_{105}} \alpha_{104} \subseteq \rho_{107} \xrightarrow{\beta_{103}} \alpha_{102}$
- $\rho_{106} ? \alpha_{104} \subseteq \beta_{105}$
- $l_2 \sim \rho_{107}$

subs: $\square\square\square\square\square$

Step F: ($p2$)

cons:

- $\alpha_{104} \subseteq \alpha_{108}$
- $\beta_{105} \subseteq \beta_{103}$
- $\rho_{106} ? \alpha_{104} \subseteq \beta_{105}$
- $\rho_{106} \sim \rho_{107}$
- $l_2 \sim \rho_{107}$

subs: $[\alpha_{102} \mapsto \alpha_{108}] \square\square\square\square$

Step R: ($p2$)

type: α_{104}

beha: $\tau; \tau; \beta_{103}$

cons:

- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{106}$

Step W': ($p2$ ($p2$))

type: α_{99}

beha: $\tau; \tau; \tau; \beta_{103}; \beta_{100}$

cons:

- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \alpha_{99}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

subs: $[\alpha_{102} \mapsto \alpha_{108}] \square \square \square \square$

Step F: ($p2$ ($p2$))

cons:

- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \alpha_{99}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

subs: $\square \square \square \square \square$

Step R: ($p2$ ($p2$))

type: α_{99}

beha: $\tau; \tau; \tau; \beta_{103}; \beta_{100}$

cons:

- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \alpha_{99}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{101}$

- $l_2 \sim \rho_{106}$

Step W': ((p2 (p2)))

type: α_{94}

beha: $\tau; \tau; \tau; \tau; \beta_{103}; \beta_{100}; \beta_{95}$

cons:

- $\rho_{98} \xrightarrow{\beta_{97}} \alpha_{96} \subseteq \alpha_{99} \xrightarrow{\beta_{95}} \alpha_{94}$
- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \alpha_{99}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{97}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

subs: $[\alpha_{102} \mapsto \alpha_{108}] \square \square \square \square$

Step F: ((p2 (p2)))

cons:

- $\alpha_{96} \subseteq \alpha_{110}$
- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{109}$
- $\beta_{97} \subseteq \beta_{95}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{97}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $\rho_{98} \sim \rho_{109}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

subs: $[\alpha_{94} \mapsto \alpha_{110}, \alpha_{99} \mapsto \rho_{109}] \square \square \square \square$

Step R: $((p2 \ (p2)))$

type: α_{96}

beha: $\tau; \tau; \tau; \tau; \beta_{103}; \beta_{100}; \beta_{95}$

cons:

- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
 - $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
 - $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
 - $l_2 \sim \rho_{101}$
 - $l_2 \sim \rho_{106}$
-

Step W': $(p2 \ ((p2 \ (p2))))$

type: α_{91}

beha: $\tau; \tau; \tau; \tau; \tau; \beta_{103}; \beta_{100}; \beta_{95}; \beta_{92}$

cons:

- $\rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \alpha_{91}$
- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{93}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

subs: $[\alpha_{94} \mapsto \alpha_{110}, \alpha_{99} \mapsto \rho_{109}, \alpha_{102} \mapsto \alpha_{108}] \square \square \square \square$

Step F: $(p2 \ ((p2 \ (p2))))$

cons:

- $\rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \alpha_{91}$

- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{93}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

subs: $\square\square\square\square\square$

Step R: $(p2 \ (\ (p2 \ (\ p2))))$

type: α_{91}

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \beta_{103}; \beta_{100}; \beta_{95}; \beta_{92}$

cons:

- $\rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \alpha_{91}$
- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{93}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

Step W': $(\ (p2 \ (\ (p2 \ (\ p2))))$

type: α_{86}

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \beta_{103}; \beta_{100}; \beta_{95}; \beta_{92}; \beta_{87}$

cons:

- $\rho_{90} \xrightarrow{\beta_{89}} \alpha_{88} \subseteq \alpha_{91} \xrightarrow{\beta_{87}} \alpha_{86}$
- $\rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \alpha_{91}$

- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\rho_{90}?\alpha_{88} \subseteq \beta_{89}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{93}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

subs: $[\alpha_{94} \mapsto \alpha_{110}, \alpha_{99} \mapsto \rho_{109}, \alpha_{102} \mapsto \alpha_{108}] \square \square \square \square$

Step F: $((p2 \ (\ (p2 \ (\ p2))))))$

cons:

- $\alpha_{88} \subseteq \alpha_{112}$
- $\rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{111}$
- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\beta_{89} \subseteq \beta_{87}$
- $\rho_{90}?\alpha_{88} \subseteq \beta_{89}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $\rho_{90} \sim \rho_{111}$
- $l_2 \sim \rho_{93}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

subs: $[\alpha_{86} \mapsto \alpha_{112}, \alpha_{91} \mapsto \rho_{111}] \square \square \square \square$

Step R: $((p2 \ (\ (p2 \ (\ p2))))))$

type: α_{88}

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \beta_{103}; \beta_{100}; \beta_{95}; \beta_{92}; \beta_{87}$

cons:

- $\rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
 - $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
 - $\rho_{90}?\alpha_{88} \subseteq \beta_{87}$
 - $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
 - $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
 - $l_2 \sim \rho_{93}$
 - $l_2 \sim \rho_{101}$
 - $l_2 \sim \rho_{106}$
-

Step W': $((p2 \ (\ (p2 \ (\ (p2 \ (\ p2)))))))$

type: α_{83}

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{103}; \beta_{100}; \beta_{95}; \beta_{92}; \beta_{87}; \beta_{84}$

cons:

- $\rho_{85} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \alpha_{83}$
- $\rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\rho_{90}?\alpha_{88} \subseteq \beta_{87}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{85}$

- $l_2 \sim \rho_{93}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

subs: $[\alpha_{86} \mapsto \alpha_{112}, \alpha_{91} \mapsto \rho_{111}, \alpha_{94} \mapsto \alpha_{110}, \alpha_{99} \mapsto \rho_{109}, \alpha_{102} \mapsto \alpha_{108}] \square \square \square \square$

Step F: $(p2 \ (\ (p2 \ (\ (p2 \ (\ p2))))))$

cons:

- $\rho_{85} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \alpha_{83}$
- $\rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\rho_{90}?\alpha_{88} \subseteq \beta_{87}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{85}$
- $l_2 \sim \rho_{93}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

subs: $\square \square \square \square \square$

Step R: $(p2 \ (\ (p2 \ (\ (p2 \ (\ p2))))))$

type: α_{83}

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{103}; \beta_{100}; \beta_{95}; \beta_{92}; \beta_{87}; \beta_{84}$

cons:

- $\rho_{85} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \alpha_{83}$
- $\rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$

- $\rho_{90}?\alpha_{88} \subseteq \beta_{87}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{85}$
- $l_2 \sim \rho_{93}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

Step W': ((p2 ((p2 ((p2 (p2)))))))

type: α_{78}

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{103}; \beta_{100}; \beta_{95}; \beta_{92}; \beta_{87}; \beta_{84}; \beta_{79}$

cons:

- $\rho_{82} \xrightarrow{\beta_{81}} \alpha_{80} \subseteq \alpha_{83} \xrightarrow{\beta_{79}} \alpha_{78}$
- $\rho_{85} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \alpha_{83}$
- $\rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\rho_{82}?\alpha_{80} \subseteq \beta_{81}$
- $\rho_{90}?\alpha_{88} \subseteq \beta_{87}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{85}$
- $l_2 \sim \rho_{93}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

subs: $[\alpha_{86} \mapsto \alpha_{112}, \alpha_{91} \mapsto \rho_{111}, \alpha_{94} \mapsto \alpha_{110}, \alpha_{99} \mapsto \rho_{109}, \alpha_{102} \mapsto \alpha_{108}] \square \square \square \square$

Step F: $((p2 \ ((p2 \ ((p2 \ (p2)))))))))$

cons:

- $\alpha_{80} \subseteq \alpha_{114}$
- $\rho_{85} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{113}$
- $\rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\beta_{81} \subseteq \beta_{79}$
- $\rho_{82}?\alpha_{80} \subseteq \beta_{81}$
- $\rho_{90}?\alpha_{88} \subseteq \beta_{87}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $\rho_{82} \sim \rho_{113}$
- $l_2 \sim \rho_{85}$
- $l_2 \sim \rho_{93}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

subs: $[\alpha_{78} \mapsto \alpha_{114}, \alpha_{83} \mapsto \rho_{113}] \square \square \square \square$

Step R: $((p2 \ ((p2 \ ((p2 \ (p2)))))))))$

type: α_{80}

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{103}; \beta_{100}; \beta_{95}; \beta_{92}; \beta_{87}; \beta_{84}; \beta_{79}$

cons:

- $\rho_{85} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$

- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\rho_{82}?\alpha_{80} \subseteq \beta_{79}$
- $\rho_{90}?\alpha_{88} \subseteq \beta_{87}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{85}$
- $l_2 \sim \rho_{93}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

Step W': $(p2 \ (\ (p2 \ (\ (p2 \ (\ p2))))))$

type: α_{75}

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{103}; \beta_{100}; \beta_{95}; \beta_{92}; \beta_{87}; \beta_{84}; \beta_{79}; \beta_{76}$

cons:

- $\rho_{77} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \alpha_{75}$
- $\rho_{85} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\rho_{82}?\alpha_{80} \subseteq \beta_{79}$
- $\rho_{90}?\alpha_{88} \subseteq \beta_{87}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{77}$
- $l_2 \sim \rho_{85}$

- $l_2 \sim \rho_{93}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

subs: $[\alpha_{78} \mapsto \alpha_{114}, \alpha_{83} \mapsto \rho_{113}, \alpha_{86} \mapsto \alpha_{112}, \alpha_{91} \mapsto \rho_{111}, \alpha_{94} \mapsto \alpha_{110}, \alpha_{99} \mapsto \rho_{109}, \alpha_{102} \mapsto \alpha_{108}] \square \square \square \square$

Step F: $(p2 \ (\ (p2 \ (\ (p2 \ (\ (p2 \ (\ p2))))))))$

cons:

- $\rho_{77} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \alpha_{75}$
- $\rho_{85} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\rho_{82}?\alpha_{80} \subseteq \beta_{79}$
- $\rho_{90}?\alpha_{88} \subseteq \beta_{87}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{77}$
- $l_2 \sim \rho_{85}$
- $l_2 \sim \rho_{93}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

subs: $\square \square \square \square \square$

Step R: $(p2 \ (\ (p2 \ (\ (p2 \ (\ (p2 \ (\ p2))))))))$

type: α_{75}

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{103}; \beta_{100}; \beta_{95}; \beta_{92}; \beta_{87}; \beta_{84}; \beta_{79}; \beta_{76}$

cons:

- $\rho_{77} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \alpha_{75}$
- $\rho_{85} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\rho_{82}?\alpha_{80} \subseteq \beta_{79}$
- $\rho_{90}?\alpha_{88} \subseteq \beta_{87}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{77}$
- $l_2 \sim \rho_{85}$
- $l_2 \sim \rho_{93}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

Step W': ((p2 ((p2 ((p2 ((p2 (p2))))))))))

type: α_{70}

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{103}; \beta_{100}; \beta_{95}; \beta_{92}; \beta_{87}; \beta_{84}; \beta_{79}; \beta_{76}; \beta_{71}$

cons:

- $\rho_{74} \xrightarrow{\beta_{73}} \alpha_{72} \subseteq \alpha_{75} \xrightarrow{\beta_{71}} \alpha_{70}$
- $\rho_{77} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \alpha_{75}$
- $\rho_{85} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$

- $\rho_{74}?\alpha_{72} \subseteq \beta_{73}$
- $\rho_{82}?\alpha_{80} \subseteq \beta_{79}$
- $\rho_{90}?\alpha_{88} \subseteq \beta_{87}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{77}$
- $l_2 \sim \rho_{85}$
- $l_2 \sim \rho_{93}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

subs: $[\alpha_{78} \mapsto \alpha_{114}, \alpha_{83} \mapsto \rho_{113}, \alpha_{86} \mapsto \alpha_{112}, \alpha_{91} \mapsto \rho_{111}, \alpha_{94} \mapsto \alpha_{110}, \alpha_{99} \mapsto \rho_{109}, \alpha_{102} \mapsto \alpha_{108}] \square \square \square \square$

Step F: $((p2 \ ((p2 \ ((p2 \ ((p2 \ (p2))))))))))$

cons:

- $\alpha_{72} \subseteq \alpha_{116}$
- $\rho_{77} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{115}$
- $\rho_{85} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\beta_{73} \subseteq \beta_{71}$
- $\rho_{74}?\alpha_{72} \subseteq \beta_{73}$
- $\rho_{82}?\alpha_{80} \subseteq \beta_{79}$
- $\rho_{90}?\alpha_{88} \subseteq \beta_{87}$

- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $\rho_{74} \sim \rho_{115}$
- $l_2 \sim \rho_{77}$
- $l_2 \sim \rho_{85}$
- $l_2 \sim \rho_{93}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

$$\text{subs: } [\alpha_{70} \mapsto \alpha_{116}, \alpha_{75} \mapsto \rho_{115}][] [] [] []$$

Step R: ((p2 ((p2 ((p2 ((p2 (p2))))))))))

type: α_{72}

beha: $\tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{103}; \beta_{100}; \beta_{95}; \beta_{92}; \beta_{87}; \beta_{84}; \beta_{79}; \beta_{76}; \beta_{71}$

cons:

- $\rho_{77} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}$
- $\rho_{85} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\rho_{74}?\alpha_{72} \subseteq \beta_{71}$
- $\rho_{82}?\alpha_{80} \subseteq \beta_{79}$
- $\rho_{90}?\alpha_{88} \subseteq \beta_{87}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{77}$

- $l_2 \sim \rho_{85}$
- $l_2 \sim \rho_{93}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

Step W': $p2(l_2tsl \ ()) ((p2 \ (\ (p2 \ (\ (p2 \ (\ p2)))))))$

type: α_{72}

beha: $\tau; \tau; \beta_{65}; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{103}; \beta_{100}; \beta_{95}; \beta_{92}; \beta_{87}; \beta_{84}; \beta_{79}; \beta_{76}; \beta_{71}$

cons:

- $\rho_{77} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}$
- $\rho_{85} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\overline{tsl^{l_2}} \sim \psi_{67}$
- $l_2\psi_{67} \subseteq \beta_{65}$
- $\rho_{74}?\alpha_{72} \subseteq \beta_{71}$
- $\rho_{82}?\alpha_{80} \subseteq \beta_{79}$
- $\rho_{90}?\alpha_{88} \subseteq \beta_{87}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{77}$
- $l_2 \sim \rho_{85}$
- $l_2 \sim \rho_{93}$
- $l_2 \sim \rho_{101}$

- $l_2 \sim \rho_{106}$

subs: $[\alpha_{64} \mapsto \rho_{69}, \alpha_{70} \mapsto \alpha_{116}, \alpha_{75} \mapsto \rho_{115}, \alpha_{78} \mapsto \alpha_{114}, \alpha_{83} \mapsto \rho_{113}, \alpha_{86} \mapsto \alpha_{112}, \alpha_{91} \mapsto \rho_{111}, \alpha_{94} \mapsto \alpha_{110}, \alpha_{99} \mapsto \rho_{109}, \alpha_{102} \mapsto \alpha_{108}] \square \square \square \square$

Step F: $p2(l_2 t s l \ ()) ((p2 ((p2 ((p2 ((p2 (p2))))))))$

cons:

- $\rho_{77} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}$
- $\rho_{85} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\overline{t s l^{l_2}} \sim \psi_{67}$
- $l_2 \psi_{67} \subseteq \beta_{65}$
- $\rho_{74} ? \alpha_{72} \subseteq \beta_{71}$
- $\rho_{82} ? \alpha_{80} \subseteq \beta_{79}$
- $\rho_{90} ? \alpha_{88} \subseteq \beta_{87}$
- $\rho_{98} ? \alpha_{96} \subseteq \beta_{95}$
- $\rho_{106} ? \alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{77}$
- $l_2 \sim \rho_{85}$
- $l_2 \sim \rho_{93}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

subs: $\square\square\square\square\square$

Step R: $p2(l_2tsl\ ())(\ (p2\ (\ (p2\ (\ (p2\ (\ (p2\ (\ p2))))))))$

type: α_{72}

beha: $\tau; \tau; \beta_{65}; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{103}; \beta_{100}; \beta_{95}; \beta_{92}; \beta_{87}; \beta_{84}; \beta_{79}; \beta_{76}; \beta_{71}$

cons:

- $\rho_{77} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}$
- $\rho_{85} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\overline{tsl^{l_2}} \sim \psi_{67}$
- $l_2\psi_{67} \subseteq \beta_{65}$
- $\rho_{74}?\alpha_{72} \subseteq \beta_{71}$
- $\rho_{82}?\alpha_{80} \subseteq \beta_{79}$
- $\rho_{90}?\alpha_{88} \subseteq \beta_{87}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{77}$
- $l_2 \sim \rho_{85}$
- $l_2 \sim \rho_{93}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

Step W': $myVNum2p2(l_2tsl\ ())(\ (p2\ (\ (p2\ (\ (p2\ (\ (p2\ (\ p2))))))))$

type: α_{72}

beha: $\tau; \tau; \tau; \beta_{65}; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{103}; \beta_{100}; \beta_{95}; \beta_{92}; \beta_{87}; \beta_{84}; \beta_{79}; \beta_{76}; \beta_{71}$

cons:

- $\rho_{77} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}$
- $\rho_{85} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\overline{tsl}^{l_2} \sim \psi_{67}$
- $l_2\psi_{67} \subseteq \beta_{65}$
- $\rho_{74}?\alpha_{72} \subseteq \beta_{71}$
- $\rho_{82}?\alpha_{80} \subseteq \beta_{79}$
- $\rho_{90}?\alpha_{88} \subseteq \beta_{87}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{77}$
- $l_2 \sim \rho_{85}$
- $l_2 \sim \rho_{93}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

subs: $[\alpha_{64} \mapsto \rho_{69}, \alpha_{70} \mapsto \alpha_{116}, \alpha_{75} \mapsto \rho_{115}, \alpha_{78} \mapsto \alpha_{114}, \alpha_{83} \mapsto \rho_{113}, \alpha_{86} \mapsto \alpha_{112}, \alpha_{91} \mapsto \rho_{111}, \alpha_{94} \mapsto \alpha_{110}, \alpha_{99} \mapsto \rho_{109}, \alpha_{102} \mapsto \alpha_{108}] \square \square \square \square$

Step F: $myVNum2p2(l_2tsl \ ()) ((p2 \ ((p2 \ ((p2 \ ((p2 \ (p2))))))))$

cons:

- $\rho_{77} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}$
- $\rho_{85} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$

- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\overline{tsl^{l_2}} \sim \psi_{67}$
- $l_2\psi_{67} \subseteq \beta_{65}$
- $\rho_{74}?\alpha_{72} \subseteq \beta_{71}$
- $\rho_{82}?\alpha_{80} \subseteq \beta_{79}$
- $\rho_{90}?\alpha_{88} \subseteq \beta_{87}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{77}$
- $l_2 \sim \rho_{85}$
- $l_2 \sim \rho_{93}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

subs: $\square\square\square\square\square$

Step R: $myVNum2p2(l_2tsl \ ())((p2 \ ((p2 \ ((p2 \ ((p2 \ (p2))))))))$

type: α_{72}

beha: $\tau; \tau; \tau; \beta_{65}; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{103}; \beta_{100}; \beta_{95}; \beta_{92}; \beta_{87}; \beta_{84}; \beta_{79}; \beta_{76}; \beta_{71}$

cons:

- $\rho_{77} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}$
- $\rho_{85} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\overline{tsl^{l_2}} \sim \psi_{67}$

- $l_2\psi_{67} \subseteq \beta_{65}$
- $\rho_{74}?\alpha_{72} \subseteq \beta_{71}$
- $\rho_{82}?\alpha_{80} \subseteq \beta_{79}$
- $\rho_{90}?\alpha_{88} \subseteq \beta_{87}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{77}$
- $l_2 \sim \rho_{85}$
- $l_2 \sim \rho_{93}$
- $l_2 \sim \rho_{101}$
- $l_2 \sim \rho_{106}$

Step W : (*client*)(*server*)

typing context: $server : \forall(\rho_{77}, \rho_{85}, \rho_{93}, \rho_{101} : \rho_{77} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}, \rho_{85} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}, \rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}, \rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}, l_2 \sim \rho_{77}, l_2 \sim \rho_{85}, l_2 \sim \rho_{93}, l_2 \sim \rho_{101}).\alpha_{72}, client : \forall(\cdot).$

Step W : (*client*)

typing context: $server : \forall(\rho_{77}, \rho_{85}, \rho_{93}, \rho_{101} : \rho_{77} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}, \rho_{85} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}, \rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}, \rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}, l_2 \sim \rho_{77}, l_2 \sim \rho_{85}, l_2 \sim \rho_{93}, l_2 \sim \rho_{101}).\alpha_{72}, client : \forall(\cdot).$

Step W : *client*

typing context: $server : \forall(\rho_{77}, \rho_{85}, \rho_{93}, \rho_{101} : \rho_{77} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}, \rho_{85} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}, \rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}, \rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}, l_2 \sim \rho_{77}, l_2 \sim \rho_{85}, l_2 \sim \rho_{93}, l_2 \sim \rho_{101}).\alpha_{72}, client : \forall(\cdot).$

Step W': *client*

type:

beha: τ
 cons:

•

subs: $\square\square\square\square$

Step F: *client*
 cons:

•

subs: $\square\square\square\square$

Step R: *client*
 type:
 beha: τ
 cons:

•

Step W': (*client*)
 type:
 beha: $\tau; (\beta_{117})$
 cons:

• $\xrightarrow{\beta_{117}} \subseteq$

subs: $\square\square\square\square$

Step F: (*client*)
 cons:

• $\xrightarrow{\beta_{117}} \subseteq$

subs: $\square\square\square\square$

Step R: (*client*)
 type:
 beha: $\tau; (\beta_{117})$
 cons:

$$\bullet \xrightarrow{\beta_{117}} \subseteq$$

Step W : (*server*)

typing context: $\vdash \forall(\cdot).$, $server : \forall(\rho_{77}, \rho_{85}, \rho_{93}, \rho_{101} : \rho_{77} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}, \rho_{85} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}, \rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}, \rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}, l_2 \sim \rho_{77}, l_2 \sim \rho_{85}, l_2 \sim \rho_{93}, l_2 \sim \rho_{101}).\alpha_{72}, client : \forall(\cdot).$

Step W : *server*

typing context: $\vdash \forall(\cdot).$, $server : \forall(\rho_{77}, \rho_{85}, \rho_{93}, \rho_{101} : \rho_{77} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}, \rho_{85} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}, \rho_{93} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}, \rho_{101} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}, l_2 \sim \rho_{77}, l_2 \sim \rho_{85}, l_2 \sim \rho_{93}, l_2 \sim \rho_{101}).\alpha_{72}, client : \forall(\cdot).$

Step W': *server*

type: α_{72}

beha: τ

cons:

- $\rho_{119} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}$
- $\rho_{120} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{121} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{122} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $l_2 \sim \rho_{119}$
- $l_2 \sim \rho_{120}$
- $l_2 \sim \rho_{121}$
- $l_2 \sim \rho_{122}$

subs: $\square\square\square\square\square$

Step F: *server*

cons:

- $\rho_{119} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}$

- $\rho_{120} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{121} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{122} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $l_2 \sim \rho_{119}$
- $l_2 \sim \rho_{120}$
- $l_2 \sim \rho_{121}$
- $l_2 \sim \rho_{122}$

subs: $\square\square\square\square\square$

Step R: *server*

type: α_{72}

beha: τ

cons:

- $\rho_{119} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}$
- $\rho_{120} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{121} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{122} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $l_2 \sim \rho_{119}$
- $l_2 \sim \rho_{120}$
- $l_2 \sim \rho_{121}$
- $l_2 \sim \rho_{122}$

Step W': (*server*)

type:

beha: $\tau; (\beta_{118})$

cons:

- $\xrightarrow{\beta_{118}} \subseteq \alpha_{72}$
- $\rho_{119} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}$
- $\rho_{120} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{121} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{122} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $l_2 \sim \rho_{119}$
- $l_2 \sim \rho_{120}$
- $l_2 \sim \rho_{121}$
- $l_2 \sim \rho_{122}$

subs: $\square\square\square\square\square$

Step F: (*server*)

cons:

- $\rho_{119} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}$
- $\rho_{120} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{121} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{122} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\beta_{118} \subseteq \beta_{123}$
- $l_2 \sim \rho_{119}$
- $l_2 \sim \rho_{120}$
- $l_2 \sim \rho_{121}$
- $l_2 \sim \rho_{122}$

subs: $[\alpha_{72} \mapsto \xrightarrow{\beta_{123}}] \square \square \square \square$

Step R: (*server*)

type:

beha: $\tau; (\beta_{118})$

cons:

- $\rho_{119} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}$
 - $\rho_{120} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
 - $\rho_{121} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
 - $\rho_{122} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
 - $\beta_{118} \subseteq \beta_{123}$
 - $l_2 \sim \rho_{119}$
 - $l_2 \sim \rho_{120}$
 - $l_2 \sim \rho_{121}$
 - $l_2 \sim \rho_{122}$
-

Step W': (*client*)(*server*)

type:

beha: $\tau; (\beta_{117}); \tau; (\beta_{118})$

cons:

- $\xrightarrow{\beta_{117}} \subseteq$
- $\rho_{119} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}$
- $\rho_{120} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{121} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{122} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\beta_{118} \subseteq \beta_{123}$

- $l_2 \sim \rho_{119}$
- $l_2 \sim \rho_{120}$
- $l_2 \sim \rho_{121}$
- $l_2 \sim \rho_{122}$

subs: $[\alpha_{72} \mapsto \xrightarrow{\beta_{123}}] \square \square \square \square$

Step F: $(client)(server)$

cons:

- $\xrightarrow{\beta_{117}} \subseteq$
- $\rho_{119} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}$
- $\rho_{120} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{121} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{122} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\beta_{118} \subseteq \beta_{123}$
- $l_2 \sim \rho_{119}$
- $l_2 \sim \rho_{120}$
- $l_2 \sim \rho_{121}$
- $l_2 \sim \rho_{122}$

subs: $\square \square \square \square \square$

Step R: $(client)(server)$

type:

beha: $\tau; (\beta_{117}); \tau; (\beta_{118})$

cons:

- $\xrightarrow{\beta_{117}} \subseteq$
- $\rho_{119} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}$

- $\rho_{120} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{121} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{122} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\beta_{118} \subseteq \beta_{123}$
- $l_2 \sim \rho_{119}$
- $l_2 \sim \rho_{120}$
- $l_2 \sim \rho_{121}$
- $l_2 \sim \rho_{122}$

Step W': $servermyVNum2p2(l_2tsl())((p2((p2((p2((p2((p2)))))))))(client)(server)$
type:

beha: $\tau; \tau; \tau; \beta_{65}; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{103}; \beta_{100}; \beta_{95}; \beta_{92}; \beta_{87}; \beta_{84}; \beta_{79}; \beta_{76}; \beta_{71}; \tau; (\beta_{117}); \tau; (\beta_{118})$
cons:

- $\xrightarrow{\beta_{117}} \subseteq$
- $\rho_{119} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}$
- $\rho_{120} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{121} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{122} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\overline{tsl}^{l_2} \sim \psi_{67}$
- $\beta_{118} \subseteq \beta_{123}$
- $l_2\psi_{67} \subseteq \beta_{65}$
- $\rho_{74}? \xrightarrow{\beta_{123}} \subseteq \beta_{71}$
- $\rho_{82}? \alpha_{80} \subseteq \beta_{79}$

- $\rho_{90}?\alpha_{88} \subseteq \beta_{87}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{106}$
- $l_2 \sim \rho_{119}$
- $l_2 \sim \rho_{120}$
- $l_2 \sim \rho_{121}$
- $l_2 \sim \rho_{122}$

subs: $[\alpha_{64} \mapsto \rho_{69}, \alpha_{70} \mapsto \alpha_{116}, \alpha_{72} \mapsto \xrightarrow{\beta_{123}}, \alpha_{75} \mapsto \rho_{115}, \alpha_{78} \mapsto \alpha_{114}, \alpha_{83} \mapsto \rho_{113}, \alpha_{86} \mapsto \alpha_{112}, \alpha_{91} \mapsto \rho_{111}, \alpha_{94} \mapsto \alpha_{110}, \alpha_{99} \mapsto \rho_{109}, \alpha_{102} \mapsto \alpha_{108}] \square \square \square \square$

Step F: $servermyVNum2p2(l_2tsl \ ()) (p2 \ (p2 \ (p2 \ (p2 \ (p2)))))) (client)(server)$
 cons:

- $\xrightarrow{\beta_{117}} \subseteq$
- $\rho_{119} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}$
- $\rho_{120} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{121} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{122} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\overline{tsl^{l_2}} \sim \psi_{67}$
- $\beta_{118} \subseteq \beta_{123}$
- $l_2\psi_{67} \subseteq \beta_{65}$
- $\rho_{74}?\xrightarrow{\beta_{123}} \subseteq \beta_{71}$
- $\rho_{82}?\alpha_{80} \subseteq \beta_{79}$
- $\rho_{90}?\alpha_{88} \subseteq \beta_{87}$

- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{106}$
- $l_2 \sim \rho_{119}$
- $l_2 \sim \rho_{120}$
- $l_2 \sim \rho_{121}$
- $l_2 \sim \rho_{122}$

subs: $\square\square\square\square\square$

Step R: $servermyVNum2p2(l_2tsl\ ())(p2\ ((p2\ ((p2\ ((p2\ ((p2\ ())))))))(client)(server)$

type:

beha: $\tau; \tau; \tau; \beta_{65}; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{103}; \beta_{100}; \beta_{95}; \beta_{92}; \beta_{87}; \beta_{84}; \beta_{79}; \beta_{76}; \beta_{71}; \tau; (\beta_{117}); \tau; (\beta_{118})$

cons:

- $\xrightarrow{\beta_{117}} \subseteq$
- $\rho_{119} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}$
- $\rho_{120} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{121} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{122} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $\overline{tsl^{l_2}} \sim \psi_{67}$
- $l_2\psi_{67} \subseteq \beta_{65}$
- $\rho_{74}?\xrightarrow{\beta_{118}} \subseteq \beta_{71}$
- $\rho_{82}?\alpha_{80} \subseteq \beta_{79}$
- $\rho_{90}?\alpha_{88} \subseteq \beta_{87}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$

- $\rho_{106} \alpha_{104} \subseteq \beta_{103}$
- $l_2 \sim \rho_{106}$
- $l_2 \sim \rho_{119}$
- $l_2 \sim \rho_{120}$
- $l_2 \sim \rho_{121}$
- $l_2 \sim \rho_{122}$

Step W': $clientp1(l_1tsl \ ())(p1, 1)(p1, 200)(p1, 1)(p1, 1)(p1, 2)))))servermyVNum2p2(l_2tsl$
type:

beha: $\tau; \tau; \beta_4; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{54}; \beta_{43}; \beta_{32}; \beta_{21}; \beta_{10}; \tau; \tau; \tau; \beta_{65}; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau;$
cons:

- $\subseteq (\rho_{12} \times \alpha_{13})$
- $\subseteq (\rho_{23} \times \alpha_{24})$
- $\subseteq (\rho_{34} \times \alpha_{35})$
- $\subseteq (\rho_{45} \times \alpha_{46})$
- $\xrightarrow{\beta_{117}} \subseteq$
- $\rho_{119} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}$
- $\rho_{120} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{121} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{122} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $tsl^{l_1} \sim \psi_5$
- $\overline{tsl^{l_2}} \sim \psi_{67}$
- $l_1\psi_5 \subseteq \beta_4$
- $l_2\psi_{67} \subseteq \beta_{65}$

- $\rho_{12}!\alpha_{13} \subseteq \beta_{10}$
- $\rho_{23}!\alpha_{24} \subseteq \beta_{21}$
- $\rho_{34}!\alpha_{35} \subseteq \beta_{32}$
- $\rho_{45}!\alpha_{46} \subseteq \beta_{43}$
- $\rho_{56}! \subseteq \beta_{54}$
- $\rho_{74}? \xrightarrow{\beta_{118}} \subseteq \beta_{71}$
- $\rho_{82}?\alpha_{80} \subseteq \beta_{79}$
- $\rho_{90}?\alpha_{88} \subseteq \beta_{87}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_1 \sim \rho_{56}$
- $l_2 \sim \rho_{106}$
- $l_2 \sim \rho_{119}$
- $l_2 \sim \rho_{120}$
- $l_2 \sim \rho_{121}$
- $l_2 \sim \rho_{122}$

subs: $[\alpha_3 \mapsto \rho_8, \alpha_9 \mapsto, \alpha_{14} \mapsto \rho_{18}, \alpha_{15} \mapsto, \alpha_{16} \mapsto (\rho_{19} \times), \alpha_{20} \mapsto, \alpha_{25} \mapsto \rho_{29}, \alpha_{26} \mapsto, \alpha_{27} \mapsto (\rho_{30} \times), \alpha_{31} \mapsto, \alpha_{36} \mapsto \rho_{40}, \alpha_{37} \mapsto, \alpha_{38} \mapsto (\rho_{41} \times), \alpha_{42} \mapsto, \alpha_{47} \mapsto \rho_{51}, \alpha_{48} \mapsto, \alpha_{49} \mapsto (\rho_{52} \times), \alpha_{53} \mapsto, \alpha_{57} \mapsto, \alpha_{58} \mapsto \rho_{62}, \alpha_{59} \mapsto, \alpha_{60} \mapsto (\rho_{63} \times), \alpha_{64} \mapsto \rho_{69}, \alpha_{70} \mapsto \alpha_{116}, \alpha_{72} \mapsto \xrightarrow{\beta_{123}}, \alpha_{75} \mapsto \rho_{115}, \alpha_{78} \mapsto \alpha_{114}, \alpha_{83} \mapsto \rho_{113}, \alpha_{86} \mapsto \alpha_{112}, \alpha_{91} \mapsto \rho_{111}, \alpha_{94} \mapsto \alpha_{110}, \alpha_{99} \mapsto \rho_{109}, \alpha_{102} \mapsto \alpha_{108}] \square \square \square \square$

Step F: $clientp1(l_1tsl \ ()) (p1, 1) (p1, 200) (p1, 1) (p1, 1) (p1, 2))) servermyVNum2p2(l_2tsl \ ($
cons:

- $\subseteq (\rho_{12} \times \alpha_{13})$

- $\subseteq (\rho_{23} \times \alpha_{24})$
- $\subseteq (\rho_{34} \times \alpha_{35})$
- $\subseteq (\rho_{45} \times \alpha_{46})$
- $\xrightarrow{\beta_{117}} \subseteq$
- $\rho_{119} \subseteq \alpha_{80} \xrightarrow{\beta_{76}} \rho_{74}$
- $\rho_{120} \subseteq \alpha_{88} \xrightarrow{\beta_{84}} \rho_{82}$
- $\rho_{121} \subseteq \alpha_{96} \xrightarrow{\beta_{92}} \rho_{90}$
- $\rho_{122} \subseteq \alpha_{104} \xrightarrow{\beta_{100}} \rho_{98}$
- $tsl^{l_1} \sim \psi_5$
- $\overline{tsl^{l_2}} \sim \psi_{67}$
- $l_1\psi_5 \subseteq \beta_4$
- $l_2\psi_{67} \subseteq \beta_{65}$
- $\rho_{12}!\alpha_{13} \subseteq \beta_{10}$
- $\rho_{23}!\alpha_{24} \subseteq \beta_{21}$
- $\rho_{34}!\alpha_{35} \subseteq \beta_{32}$
- $\rho_{45}!\alpha_{46} \subseteq \beta_{43}$
- $\rho_{56}! \subseteq \beta_{54}$
- $\rho_{74}? \xrightarrow{\beta_{118}} \subseteq \beta_{71}$
- $\rho_{82}?\alpha_{80} \subseteq \beta_{79}$
- $\rho_{90}?\alpha_{88} \subseteq \beta_{87}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$

- $l_2 \sim \rho_{122}$

subs: ☐ ☐ ☐ ☐ ☐

beha: $\tau; \tau; \beta_4; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \beta_{54}; \beta_{43}; \beta_{32}; \beta_{21}; \beta_{10}; \tau; \tau; \tau; \beta_{65}; \tau; \tau; \tau; \tau; \tau; \tau; \tau; \tau;$
cons:

- $l_1\psi_5 \subseteq \beta_4$

- $l_2\psi_{67} \subseteq \beta_{65}$
- $\rho_{12}!\alpha_{13} \subseteq \beta_{10}$
- $\rho_{23}!\alpha_{24} \subseteq \beta_{21}$
- $\rho_{34}!\alpha_{35} \subseteq \beta_{32}$
- $\rho_{45}!\alpha_{46} \subseteq \beta_{43}$
- $\rho_{56}! \subseteq \beta_{54}$
- $\rho_{74}? \xrightarrow{\beta_{118}} \subseteq \beta_{71}$
- $\rho_{82}?\alpha_{80} \subseteq \beta_{79}$
- $\rho_{90}?\alpha_{88} \subseteq \beta_{87}$
- $\rho_{98}?\alpha_{96} \subseteq \beta_{95}$
- $\rho_{106}?\alpha_{104} \subseteq \beta_{103}$
- $l_1 \sim \rho_{56}$
- $l_2 \sim \rho_{106}$
- $l_2 \sim \rho_{119}$
- $l_2 \sim \rho_{120}$
- $l_2 \sim \rho_{121}$
- $l_2 \sim \rho_{122}$

SessionTypeInference: unbound beta variable β_{100}