

Visualization (Exploring Co-variation)

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Introduction

Skills hopefully acquired at the end of lecture

Take a two variables in a dataset. Visualize to learn more about how they co-vary.

Key cases of interest:

- Categorical variable and a continuous variable
- Two categorical variables
- Two continuous variables

Categorical variable and continuous variable

Categorical vs. continuous: roadmap

- `penguins` dataset
- Boxplots
- Densities
- Small multiples

penguins dataset

```
1 url = ("https://raw.githubusercontent.com/mcnakhaee/palmerpenguins/master/p  
2 penguins = pd.read_csv(url)  
3 penguins.head()
```

| | species | island | bill_length_mm | bill_depth_mm | flipper_length_mm | boc |
|---|---------|-----------|----------------|---------------|-------------------|-----|
| 0 | Adelie | Torgersen | 39.1 | 18.7 | 181.0 | 375 |
| 1 | Adelie | Torgersen | 39.5 | 17.4 | 186.0 | 380 |
| 2 | Adelie | Torgersen | 40.3 | 18.0 | 195.0 | 325 |
| 3 | Adelie | Torgersen | NaN | NaN | NaN | NaN |
| 4 | Adelie | Torgersen | 36.7 | 19.3 | 193.0 | 345 |

penguins dataset

`species` appears to be a categorical variable

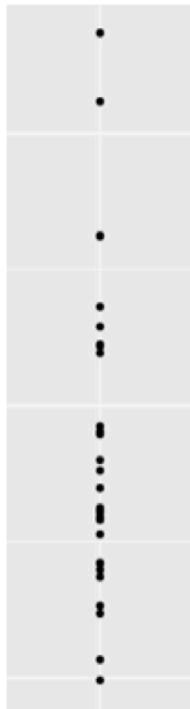
```
1 penguins['species'].value_counts()
```

```
species
Adelie      152
Gentoo     124
Chinstrap    68
Name: count, dtype: int64
```

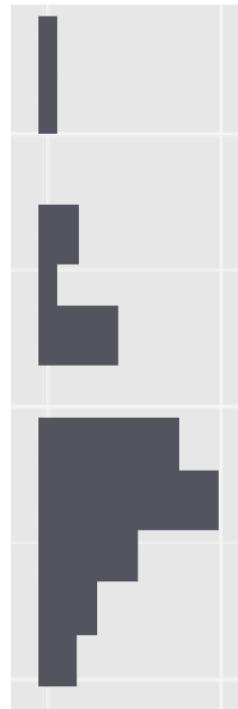
Discussion question: is it a Nominal or Ordinal variable?

Categorical & continuous: box plot

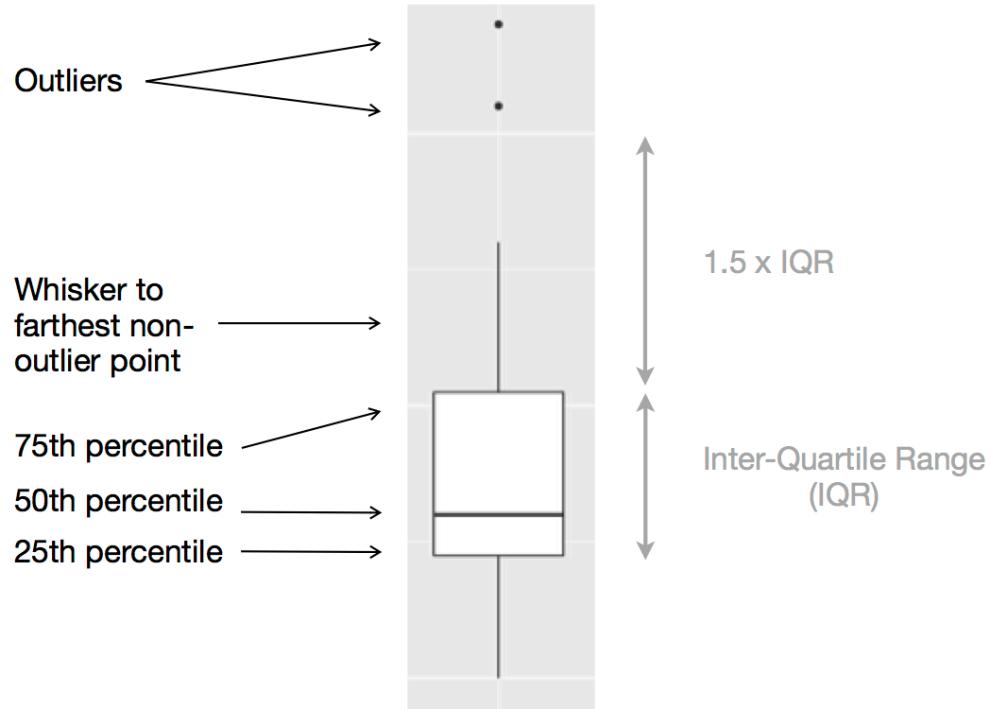
The actual values in a distribution



How a histogram would display the values (rotated)

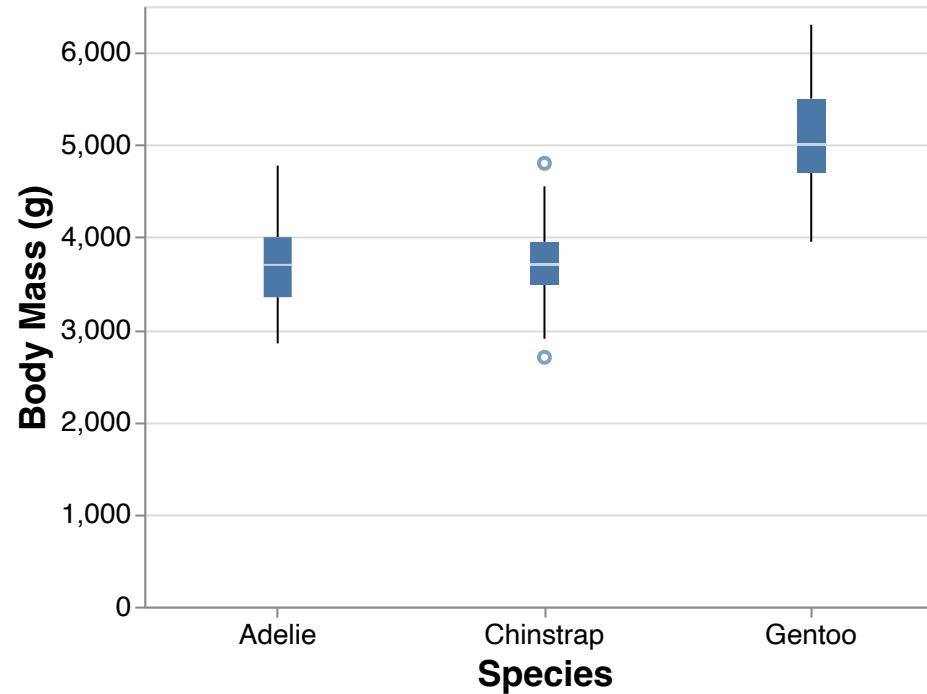


How a boxplot would display the values



mark_boxplot()

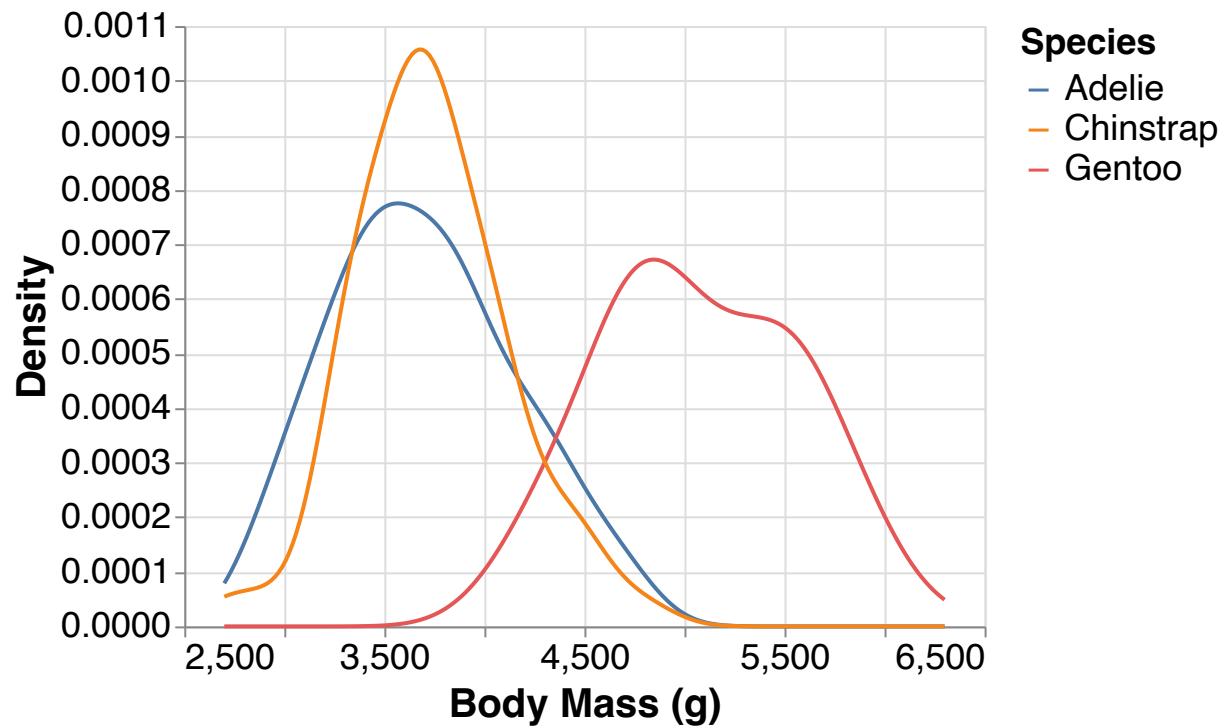
```
1 alt.Chart(penguins).mark_boxplot().encode(  
2     alt.X('species:N', title="Species"),  
3     alt.Y('body_mass_g:Q', title="Body Mass (g)"),  
4 )
```



Discussion question: what is the headline message from this graph?
Submessages?

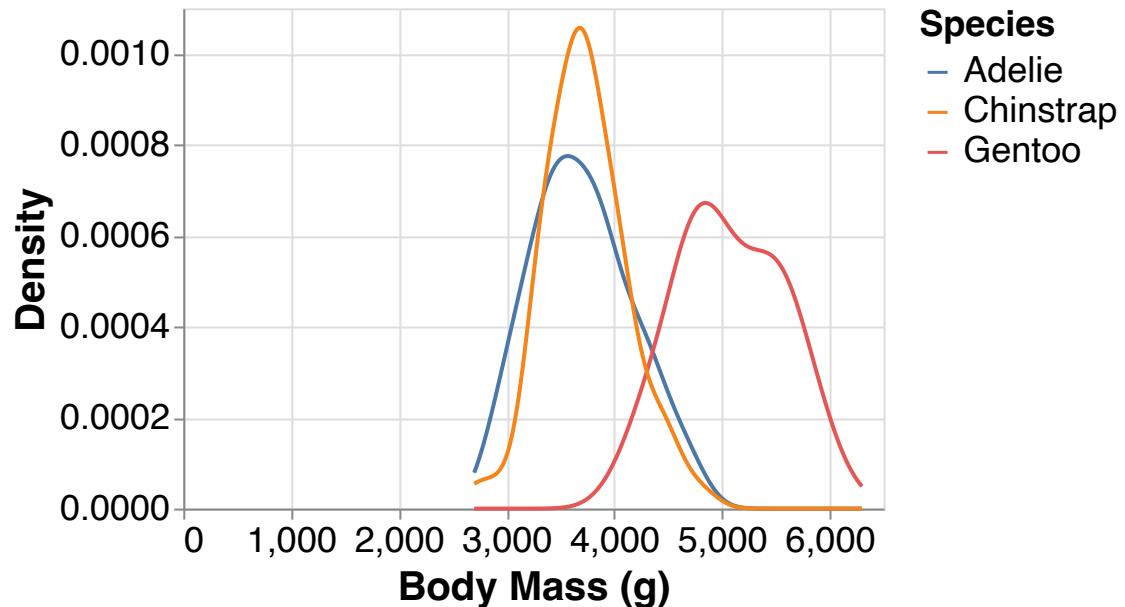
transform_density()

```
1 alt.Chart(penguins).transform_density(  
2     'body_mass_g',  
3     groupby=['species'],  
4     as_=['body_mass_g2', 'density'])  
5     .mark_line().encode(  
6         alt.X('body_mass_g2:Q', title = "Body Mass (g)"),  
7         alt.Y('density:Q', title = "Density"),  
8         alt.Color('species:N', title = "Species")  
9     )
```



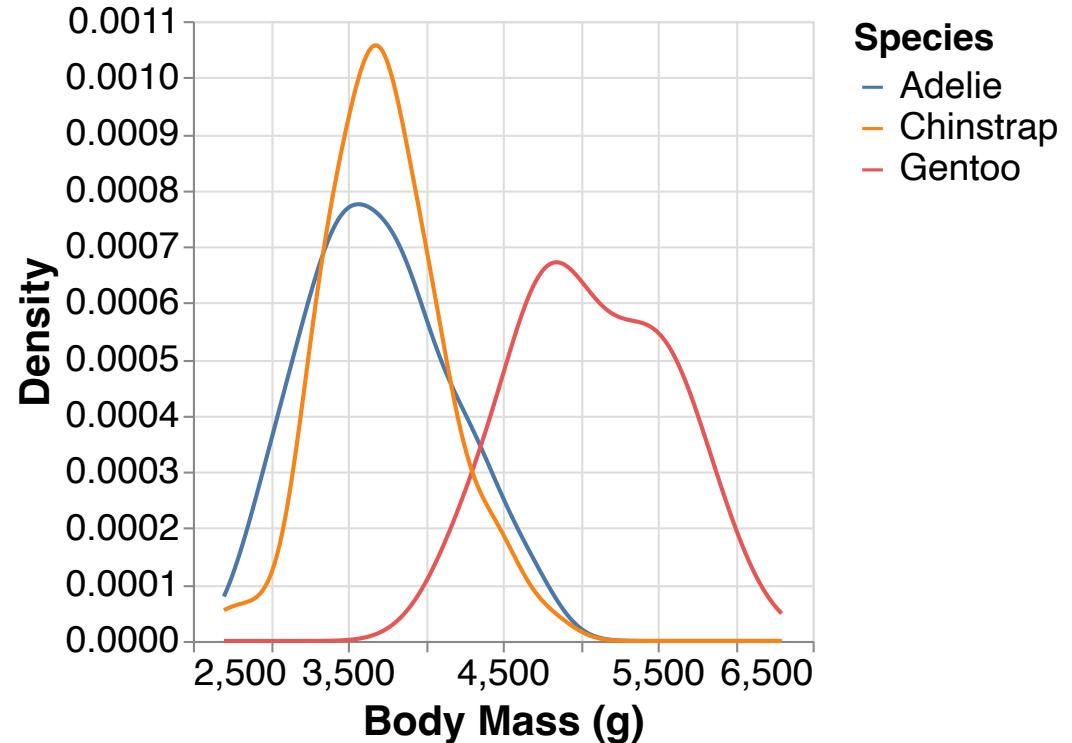
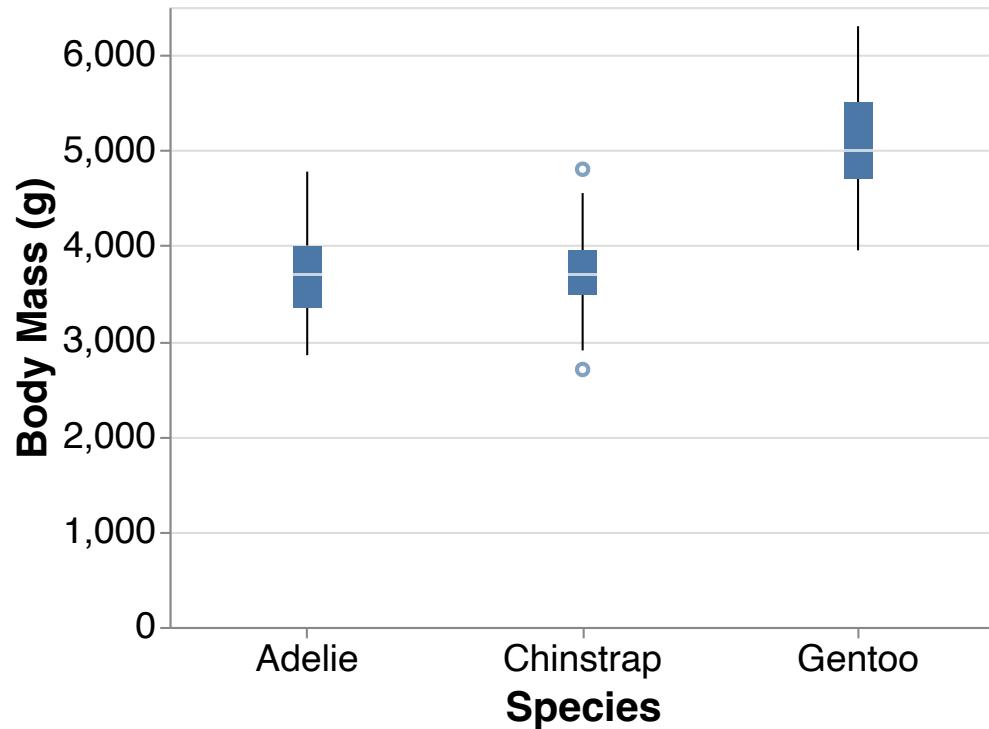
`transform_density()`, scale to 0

```
1 alt.Chart(penguins).transform_density(  
2     'body_mass_g',  
3     groupby=['species'],  
4     as_=['body_mass_g', 'density']  
5 ).mark_line().encode(  
6     alt.X('body_mass_g:Q', scale=alt.Scale(zero=True), title = "Body Mass (g)",  
7     alt.Y('density:Q', title = "Density"),  
8     alt.Color('species:N', title = "Species")  
9 )
```



Discussion question: what if we required the x-axis range to include zero?
Would that improve or reduce clarity? Why?

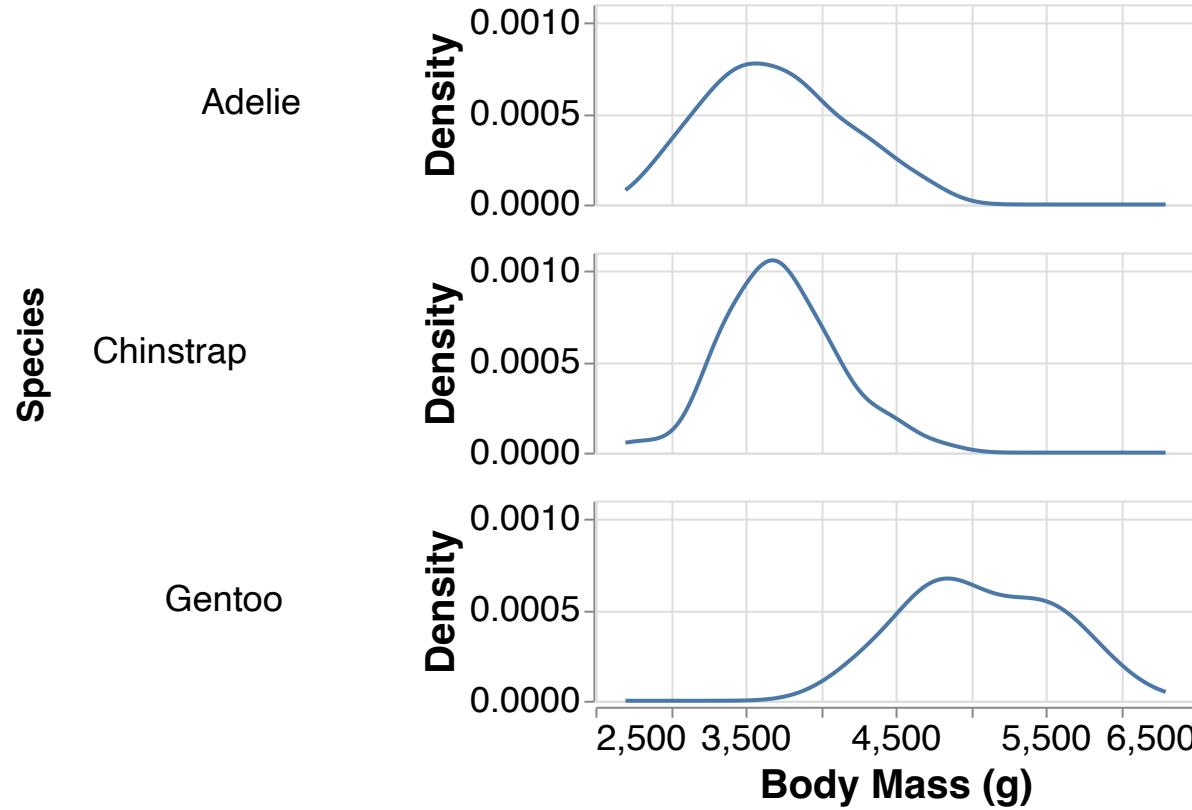
Boxplot or density plots?



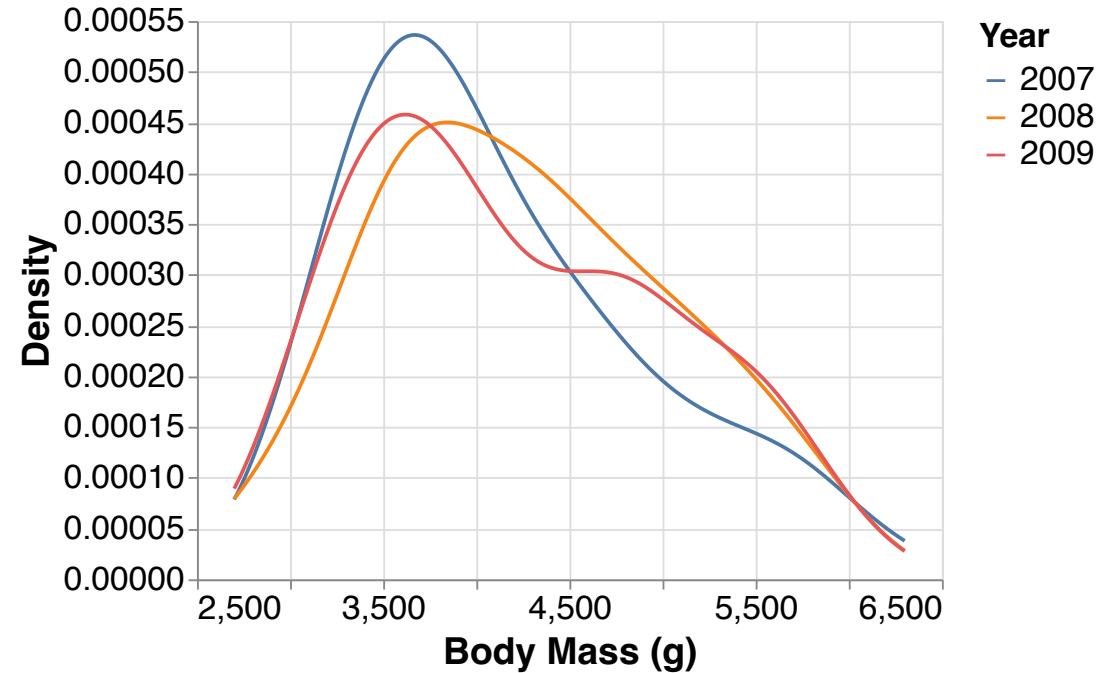
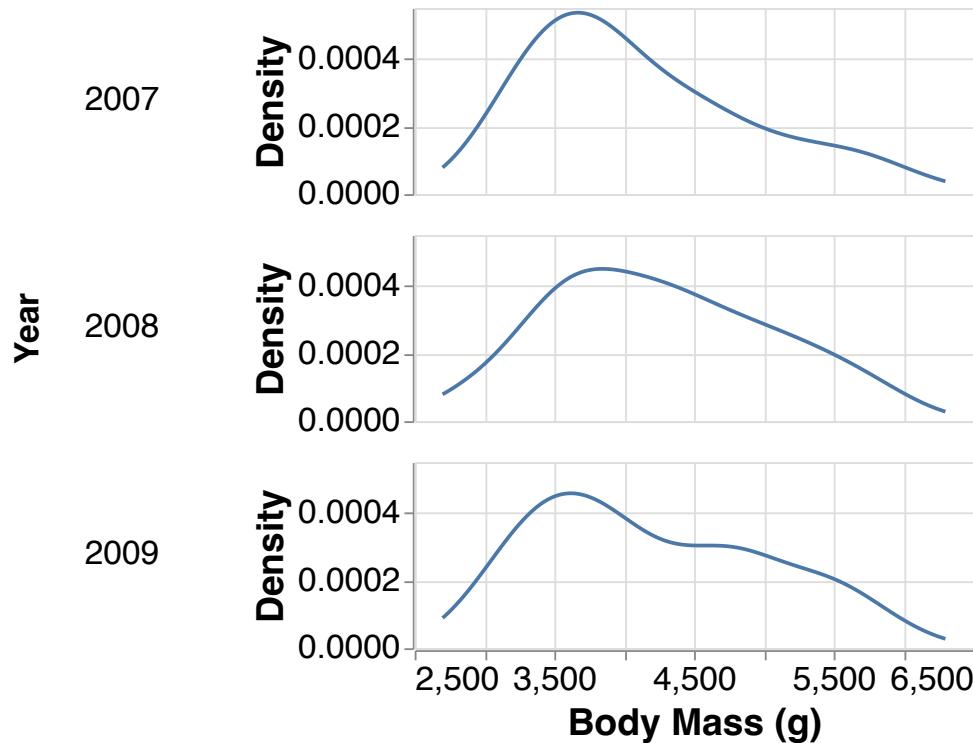
Discussion question: what messages come through more with the box plot? Through the density plot?

alt.Row: small multiples

```
1 alt.Chart(penguins).transform_density(  
2     'body_mass_g',  
3     groupby=['species'],  
4     as_=['body_mass_g', 'density'])  
5 ).mark_line().encode(  
6     alt.X('body_mass_g:Q', title = "Body Mass (g)",  
7     alt.Y('density:Q', title = "Density"),  
8     alt.Row('species:N', header=alt.Header(labelAngle=0), title = "Species")  
9 )
```



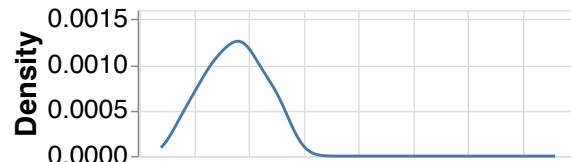
By year: colors or small multiples?



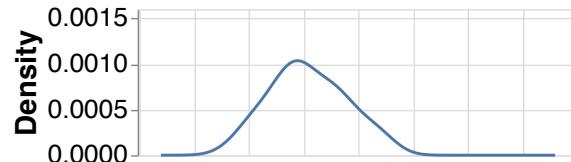
Discussion question: these two graphs show identical information. Which do you prefer, and why?

Colors or small multiples?

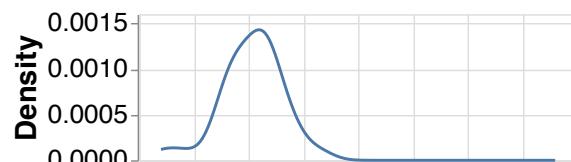
Adelie - female



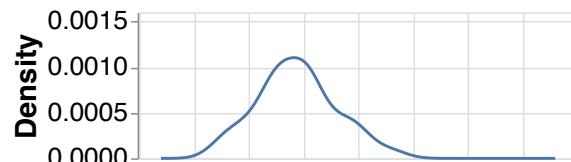
Adelie - male



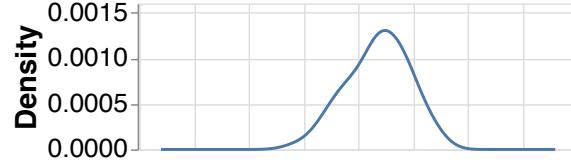
Chinstrap - female



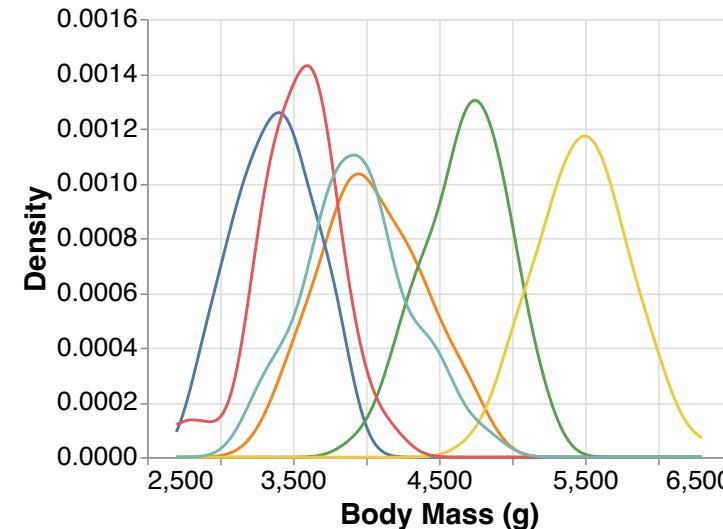
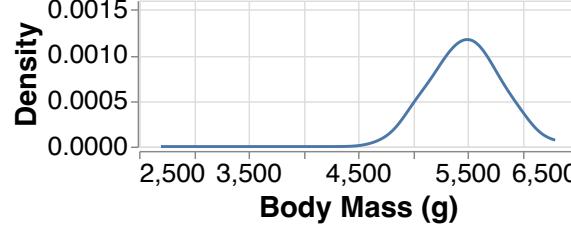
Chinstrap - male



Gentoo - female



Gentoo - male



Species & Sex

- Adelie - female
- Adelie - male
- Chinstrap - female
- Chinstrap - male
- Gentoo - female
- Gentoo - male

Two Categorical Variables

Two categorical variables: roadmap

- Two ways to encode frequency as a third dimension:
diamonds
 - **size**
 - **color**
- A word of caution against 3D graphs

How is cut related to color? Size

In `diamonds` dataset, `color` and `cut` are both categorical

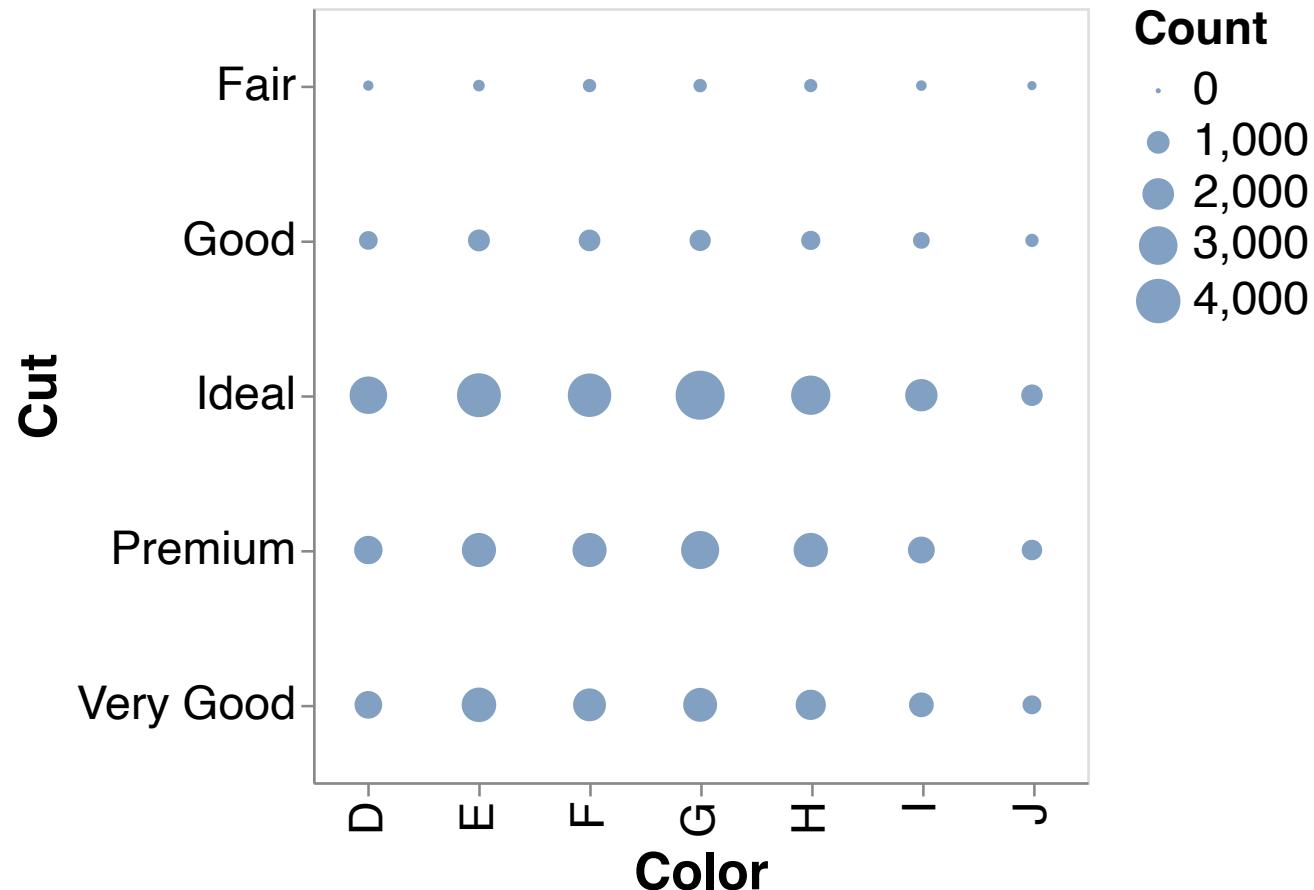
```
1 diamonds_grouped = diamonds.groupby(['color','cut']).size().reset_index().rename(columns={0:'N'})
2 diamonds_grouped
```

| | color | cut | N |
|----|-------|-----------|------|
| 0 | D | Fair | 163 |
| 1 | D | Good | 662 |
| 2 | D | Very Good | 1513 |
| 3 | D | Premium | 1603 |
| 4 | D | Ideal | 2834 |
| 5 | E | Fair | 224 |
| 6 | E | Good | 933 |
| 7 | E | Very Good | 2400 |
| 8 | E | Premium | 2337 |
| 9 | E | Ideal | 3903 |
| 10 | F | Fair | 312 |
| 11 | F | Good | 909 |
| 12 | F | Very Good | 2164 |
| 13 | F | Premium | 2331 |

| | color | cut | N |
|----|-------|-----------|------|
| 14 | F | Ideal | 3826 |
| 15 | G | Fair | 314 |
| 16 | G | Good | 871 |
| 17 | G | Very Good | 2299 |
| 18 | G | Premium | 2924 |
| 19 | G | Ideal | 4884 |
| 20 | H | Fair | 303 |
| 21 | H | Good | 702 |
| 22 | H | Very Good | 1824 |
| 23 | H | Premium | 2360 |
| 24 | H | Ideal | 3115 |
| 25 | I | Fair | 175 |
| 26 | I | Good | 522 |
| 27 | I | Very Good | 1204 |
| 28 | I | Premium | 1428 |
| 29 | I | Ideal | 2093 |
| 30 | J | Fair | 119 |
| 31 | J | Good | 307 |
| 32 | J | Very Good | 678 |
| 33 | J | Premium | 808 |
| 34 | J | Ideal | 896 |

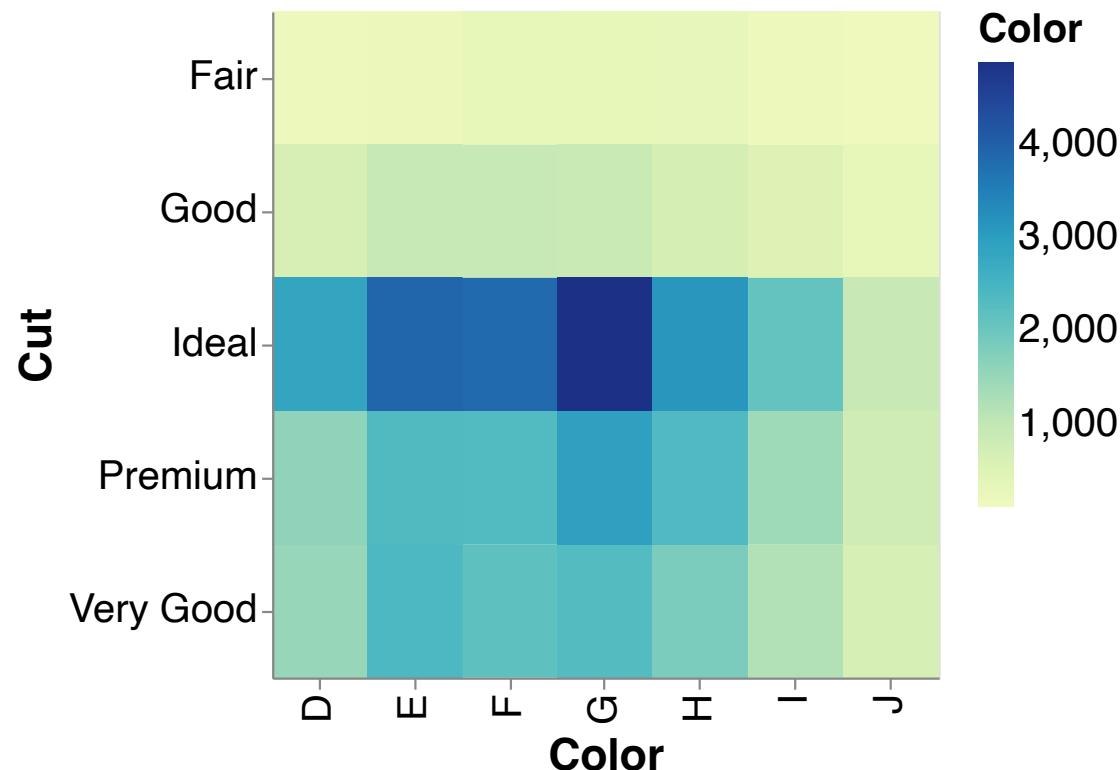
How is cut related to color? Color

```
1 alt.Chart(diamonds_grouped).mark_circle().encode(  
2     alt.X('color:N', title = "Color"),  
3     alt.Y('cut:N', title = "Cut"),  
4     alt.Size('N:Q', title = "Count"))
```



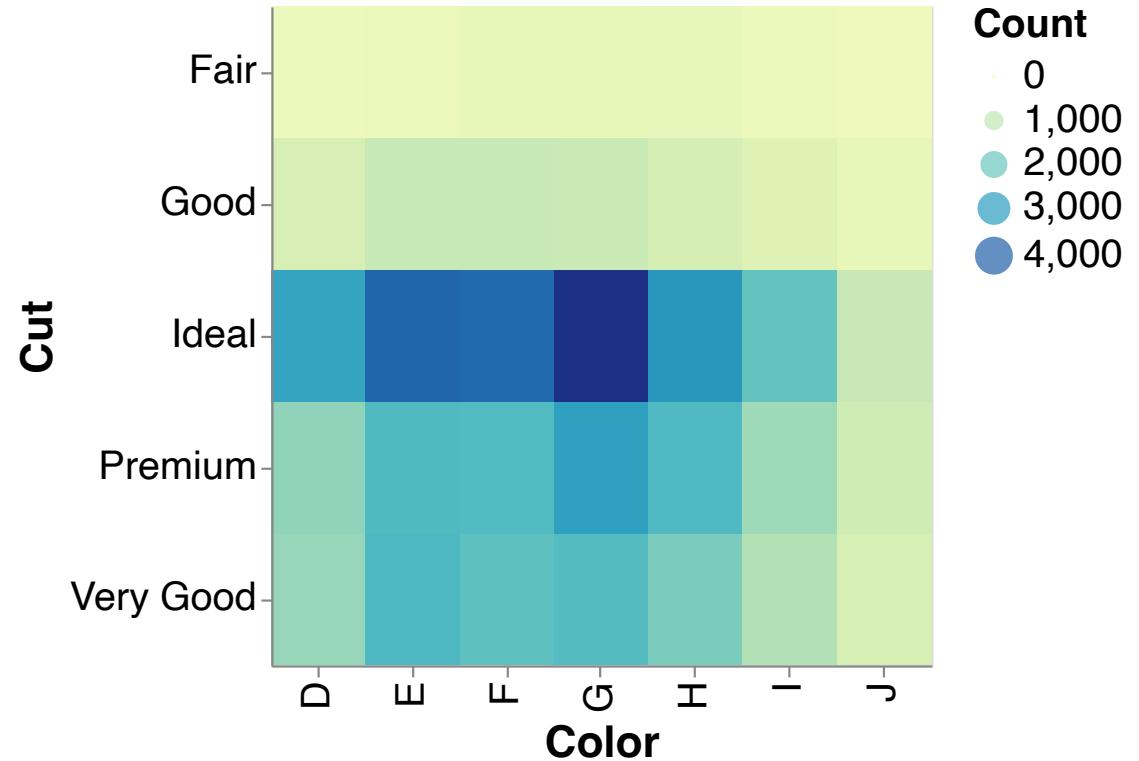
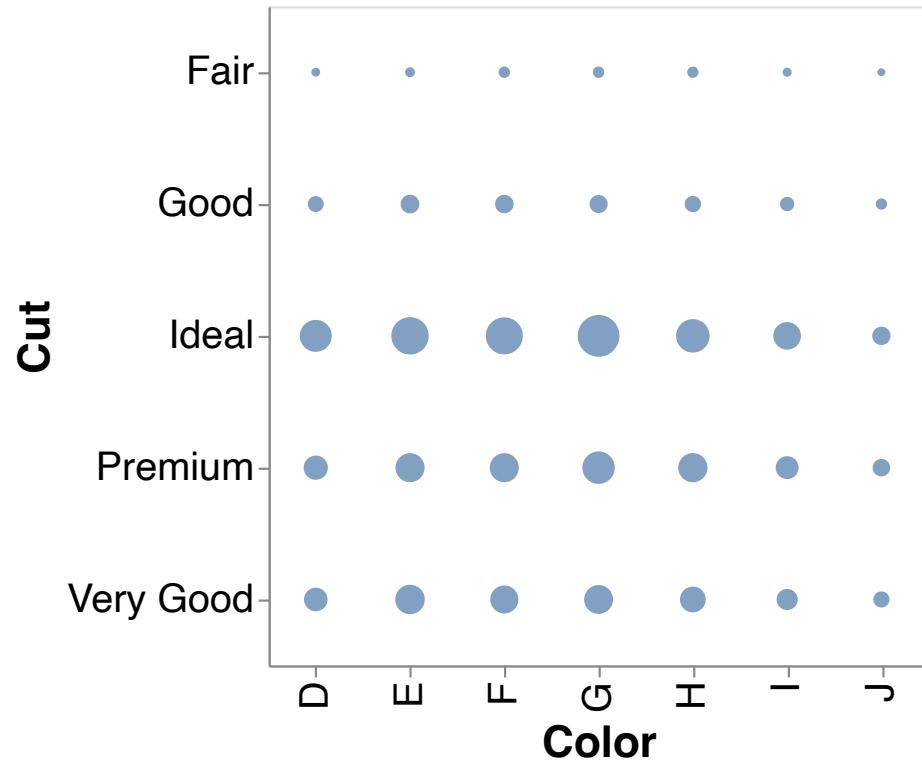
How is cut related to color?

```
1 alt.Chart(diamonds_grouped).mark_rect().encode(  
2     alt.X('color:N', title = "Color"),  
3     alt.Y('cut:N', title = "Cut"),  
4     alt.Color('N:Q', title = "Color"))
```



Discussion question: what diamond types are most common?

How is cut related to color?



Discussion question: these two plots display the same information, but encoded differently. Which do you prefer?

A word of caution: 3D graphs

You may have seen covariation between two variables depicted as a 3D plot before

Two Categorical Variables: summary

- Encode frequency as `color` or `size`
- Avoid 3D representations!

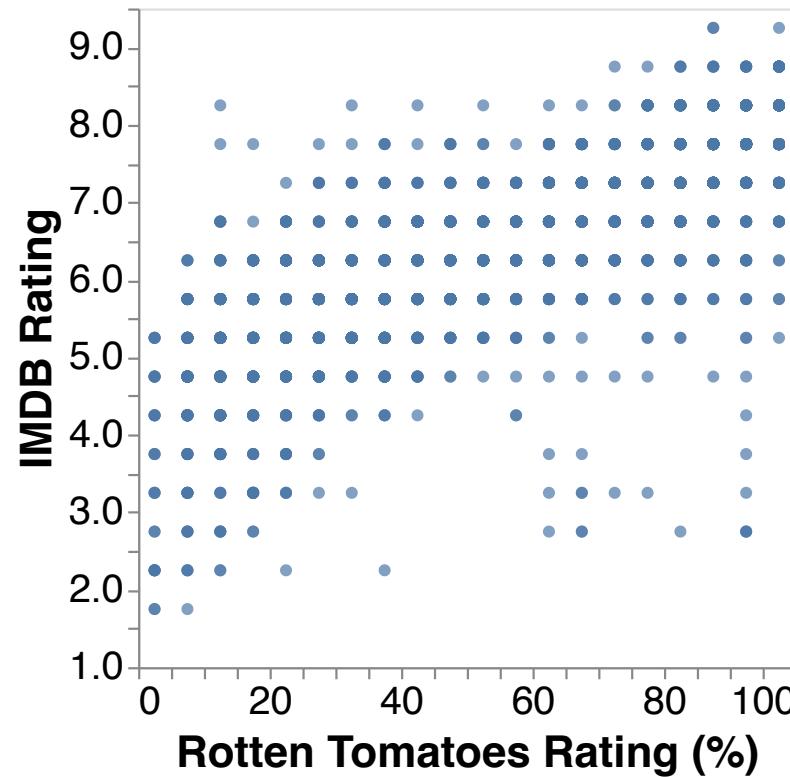
Two Continuous Variables

Two continuous variables: roadmap

- `movies` ratings from Rotten Tomatoes and IMDB
- `diamonds`: carat vs price

How are RT and IMDB ratings related?

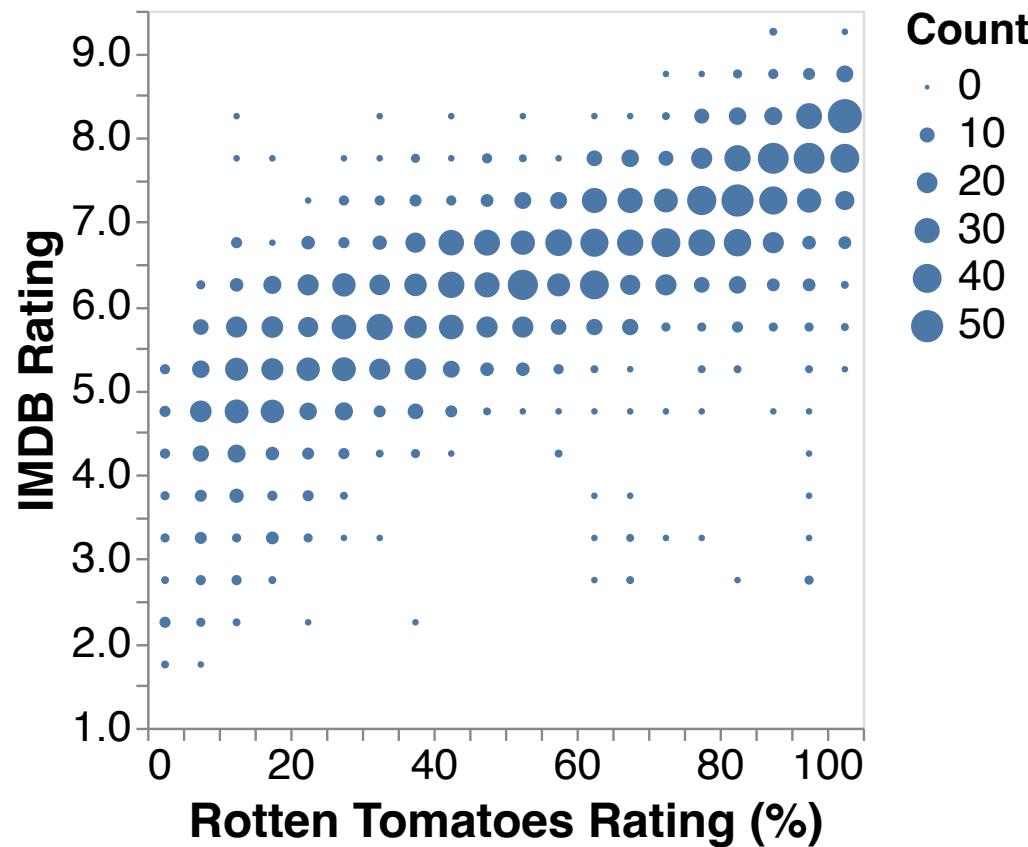
```
1 alt.Chart(movies).mark_circle().encode(  
2     alt.X('Rotten_Tomatoes_Rating:Q', bin=alt.BinParams(maxbins=20), title  
3     alt.Y('IMDB_Rating:Q', bin=alt.BinParams(maxbins=20), title = "IMDB Rat  
4 )
```



Suffers from overplotting!

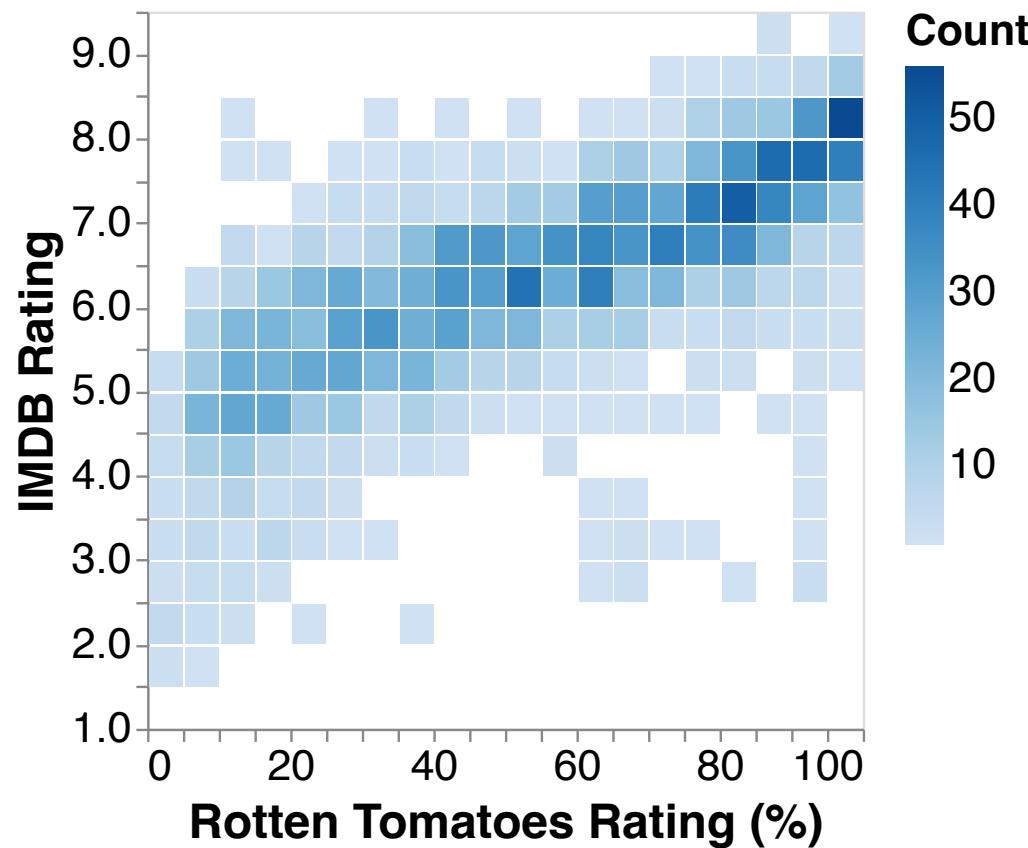
use alt.Size('count()')

```
1 alt.Chart(movies_url).mark_circle().encode(  
2     alt.X('Rotten_Tomatoes_Rating:Q', bin=alt.BinParams(maxbins=20)),  
3     alt.Y('IMDB_Rating:Q', bin=alt.BinParams(maxbins=20)),  
4     alt.Size('count())'  
5 )
```

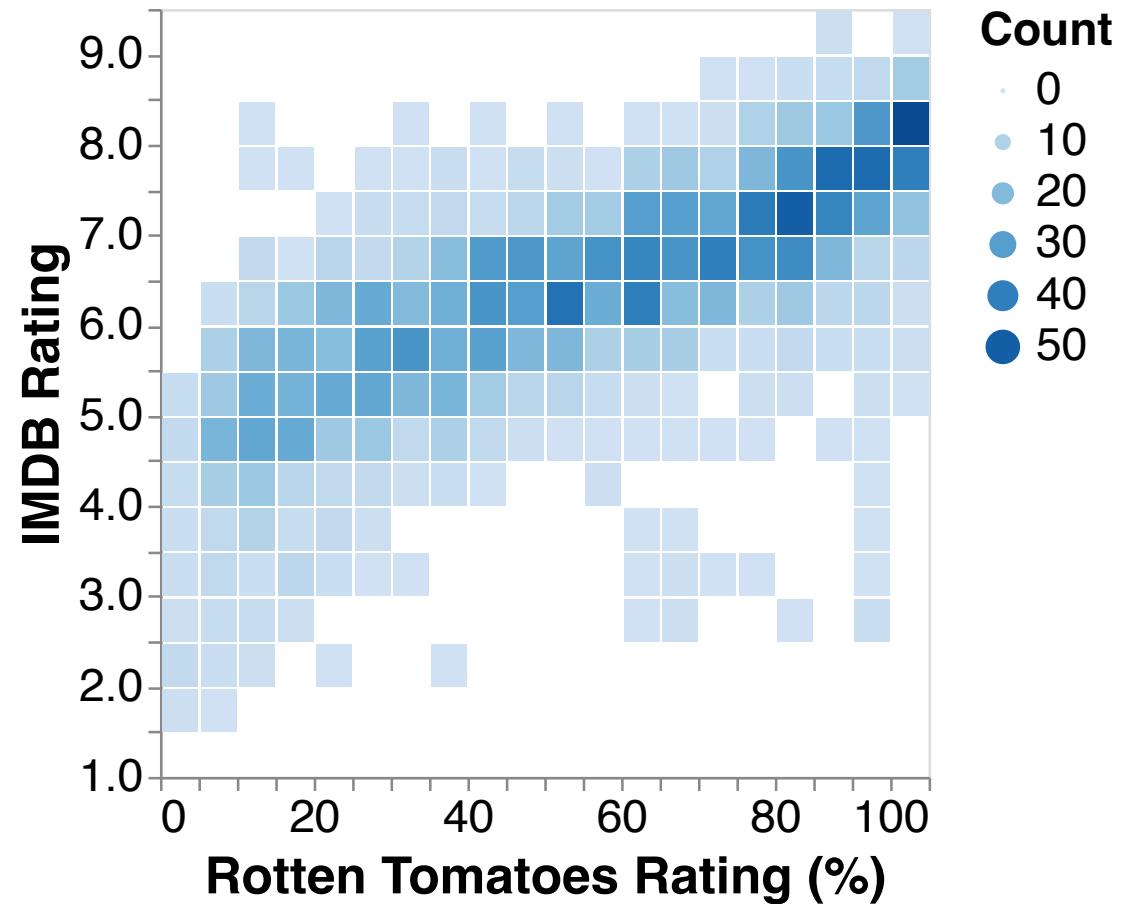
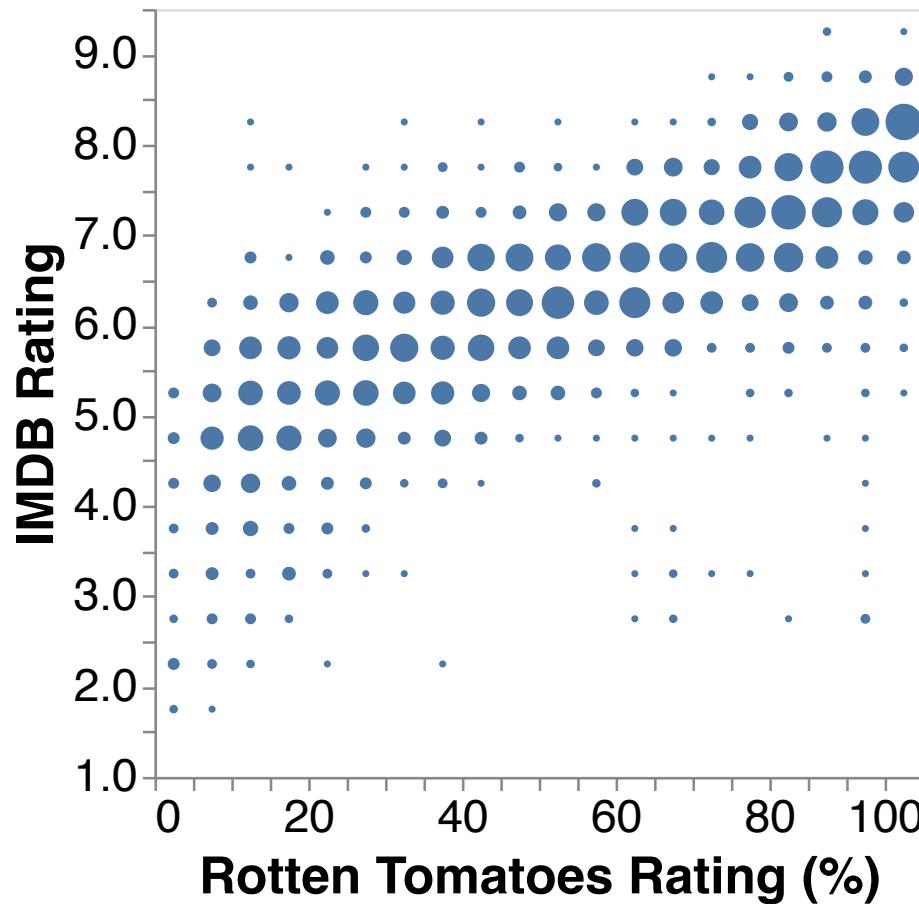


use alt.Color('count()')

```
1 alt.Chart(movies_url).mark_bar().encode(  
2     alt.X('Rotten_Tomatoes_Rating:Q', bin=alt.BinParams(maxbins=20), title  
3     alt.Y('IMDB_Rating:Q', bin=alt.BinParams(maxbins=20), title = "IMDB Rat  
4     alt.Color('count()', title = "Count")  
5 )
```



Discussion question



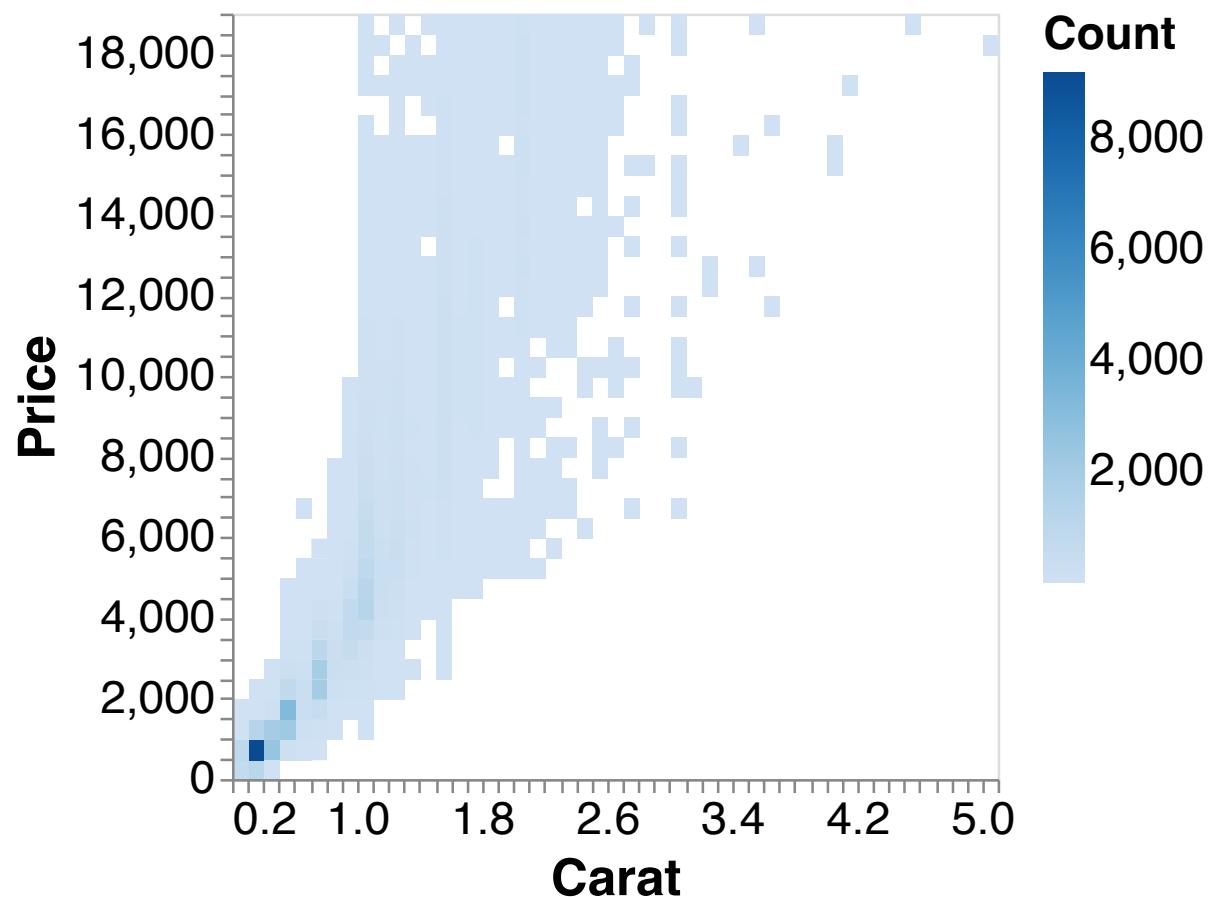
Compare the size and color-based 2D histograms above. Which encoding do you prefer? Why?

How is carat related to price? Raw data

```
1 alt.Chart(diamonds).mark_point().encode(  
2     alt.X('carat:Q', title = "Carat"),  
3     alt.Y('price:Q', title = "Price")  
4 )
```

How is carat related to price? Color

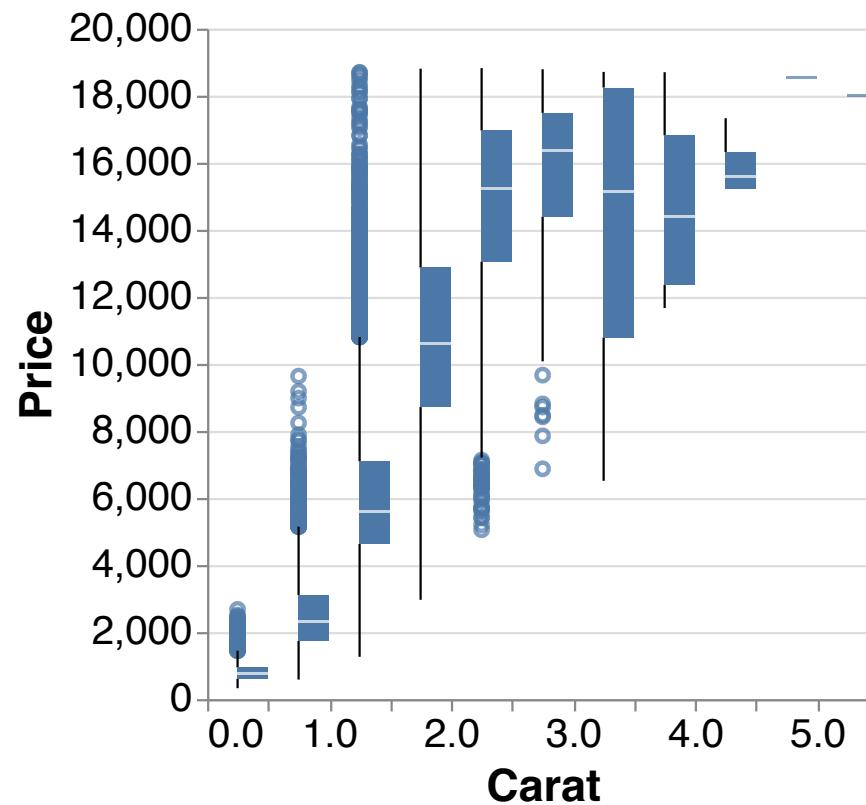
```
1 alt.Chart(diamonds).mark_rect().encode(  
2     alt.X('carat:Q', bin=alt.Bin(maxbins=70), title = "Carat"),  
3     alt.Y('price:Q', bin=alt.Bin(maxbins=70), title = "Price"),  
4     alt.Color('count()', scale=alt.Scale(scheme='blues'), title = "Count"))
```



How is carat related to price?

mark_boxplot()

```
1 alt.Chart(diamonds).mark_boxplot().encode(  
2     alt.X('carat:Q', bin=alt.Bin(maxbins=10), title = "Carat"),  
3     alt.Y('price:Q', title = "Price"))
```



How is carat related to price?

binscatter (code)

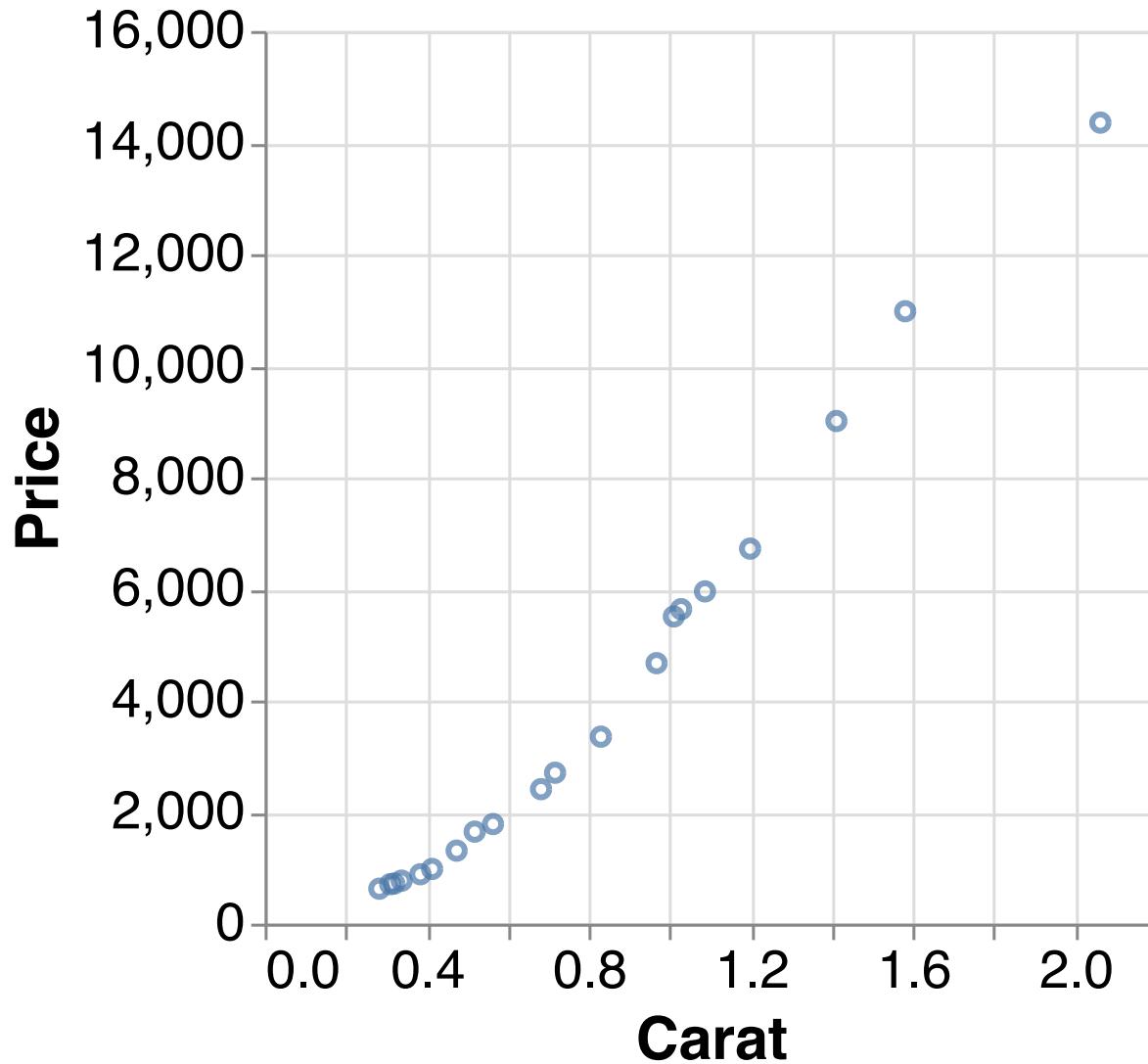
```
1 df = diamonds
2 df['carat_bin'] = pd.qcut(df['carat'], q=20, labels=(np.arange(1, 21, 1)))
3
4 df = df.groupby('carat_bin').agg(
5     carat = ('carat', 'mean'),
6     price = ('price', 'mean')).reset_index()
7
8 alt.Chart(df).mark_point().encode(
9     alt.X('carat:Q', title = "Carat"),
10    alt.Y('price:Q', title = "Price"))
11 )
```

How is carat related to price?

binscatter

- Can also create a binscatter: `binscatter` in stata and `binsreg` in R.
- Doesn't exist yet for `altair`, but easy to code up yourself
- What it does:
 1. Computes bins using quantiles of x
 2. Computes means of y within each bin

How is carat related to price? (plot)



Discussion question – “How is carat related to price?”

Review the `mark_rect()`, `mark_boxplot()`, and `binscatter` plots

- Headline?
- Sub-messages?

Exploring covariation: summary

| Scenario | Functions |
|-------------------------------------|---|
| Categorical and continuous variable | <code>mark_boxplot()</code> <code>transform_density()</code> <code>alt.Row()</code> |
| Two categorical variables | <code>size</code> <code>color</code> |
| Two continuous variables | <code>alt.Size('count()')</code> <code>alt.Color('count()')</code> <code>mark_boxplot()</code> <code>binscatter</code> |