# 5 Exercise solutions – Evaluation of alignment scores

## 1. Non-parametric test

A non-parametric test is used to determine a p-value for the optimal score of a global alignment. Assume we randomly generated 9 sequences and calculated the alignment scores as follows.

q: AACG

Seq No.	1	2	3	4	5	6	7	8	9
Score	0.2	0.4	0.5	1.2	1.2	1.5	1.9	2.2	2.1

(a) What are  $H_0$  (null hypothesis) and  $H_1$  (alternative hypothesis) if you want to use a statistical hypothesis test to evaluate a global pairwise alignment in terms of finding homologues?

**Solution:**  $H_0$ : Sequences are not homologous,  $H_1$ : Sequences are homologous

(b) Calculate the p-value for the alignment below.

q: AACG d: AGTG

Score: 2

The p-value can be calculated as:

$$p = (b+1)/(n+1)$$

where b is the number of randomly generated scores above the score of the original alignment, and n is the sample size.

Solution: p-value: 0.3

(c) Is the test result statistically significant when  $\alpha = 0.05$ ?

Solution: No.

(d) What is the conclusion of the test in terms of finding homologues?

Solution:  ${\bf q}$  and  ${\bf d}$  are not homologous.

### 2. Gumbel distribution

Use the alignment scores between q and 5 randomly generated sequences below to answer the following questions.

q: ACGTA

Randomly generated sequence	Alignment score
ACGTA	4
TTACG	5
CGCGA	6
ATTAT	4
CGATC	6

(a) What is the mean of the scores?

$$\bar{x} = \frac{1}{n} \sum_{i=1}^{n} x_i$$

Solution: 5

(b) What is the standard deviation of the scores?

$$s = \sqrt{\frac{\sum_{i=1}^{n} (x_i - \bar{x})^2}{n-1}}$$

Solution: 1

(c) The parameters  $\mu$  and  $\lambda$  of the Gumbel distribution can be estimated from the mean and the variance of a sample. Calculate lambda and mu.

$$lamda \approx \frac{1.282}{s}$$
$$mu \approx \bar{x} - \frac{0.577}{lamda}$$

**Solution:** lamda: 1.282, mu: 4.55

(d) What is the p-value when the score of an alignment is 4.55?

X	$\exp(x)$
0	1
-1	0.3679
-2	0.1353
-3	0.0497

$$P[Y > 4.55] = 1 - F_Y(4.55) = 1 - \exp(-e^{-\lambda(4.55 - \mu)})$$

**Solution:** 1 - 0.3679 = 0.6321

(e) What is the conclusion of the test in terms of finding homologues?

**Solution:** The sequences of the alignment with score 4.55 are not homologous.

#### 3. Bit score

BLAST reports bit scores, which are equivalent to the information content that are calculated from raw scores.

• Bit score:  $S' = \frac{(\lambda S - \ln K)}{\ln 2}$ 

• S: raw score

• K and  $\lambda$ : Karlin-Altschul statistics

X	$\ln x$
1	0
2	0.693
3	1.099

Assume K: 3 and  $\lambda$ : 0.1 and use the table above to answer the following questions.

(a) What is the bit score when the raw score is 80.29?

**Solution:** 
$$\frac{0.1 \times 80.29 - 1.099}{0.693} = \frac{6.93}{0.693} = 10$$

(b)  $2^{S'}$  indicates the expected search space size that one can find an alignment with score at least S by chance alone. What is the  $2^{S'}$  value when the raw score is 17.92?

**Solution:** 
$$S' = \frac{0.1 \times 17.92 - 1.099}{0.693} = \frac{0.693}{0.693} = 1;$$
  $2^1 = 2$ 

### 4. Bit score to e-value

The e-value represents the expected number of hits when homologous sequence are searched on a database of a particular size. It can be calculated from a bit score as follows.

$$E = \frac{\text{Size of search space}}{2^{\text{bit-score}}}$$

(a) What is the e-value when the size of search space is 3200 and the bit score is 4?

**Solution:** 
$$\frac{3200}{2^4} = \frac{3200}{16} = 200$$

(b) Assume we can calculate a search space size as  $m \times n$  where m is the query sequence size and n is the total character size of a database. What is the e-value when m is 20, n is 4000, and the bit score is 3?

**Solution:** 
$$\frac{20 \times 4000}{2^3} = \frac{80000}{8} = 10000$$

- 5. Raw score to e-value The e-value can be directly caudated from a raw score as  $E(S) = Kmne^{-\lambda S}$ . Use the values below to answer the following questions.
  - K: 2
  - $\bullet$   $\lambda$ : 0.1

X	$\exp(x)$
0	1
-1	0.3679
-10	0.000045

(a) What is E(10) when m is 10 and n is 100?

**Solution:** 
$$E(10) = 210100e^{-1} = 7358$$

(b) What is E(100) when m is 10 and n is 100?

**Solution:** 
$$E(100) = 210100e^{-10} = 0.09$$

(c) What is E(100) when m is 100 and n is 1000?

**Solution:** 
$$E(100) = 21001000e^{-10} = 9$$