11 Exercises – Construction of scoring matrix

1. Scoring schemes for protein alignments

Calculate the score of the alignment by using different scoring schemes.

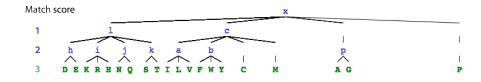
Seq1 R-HIC Seq2 RDDCC

- (a) Use the identity with a simple scoring scheme as match: 1, mismatch: 0, and gap penalty: 0.
- (b) Use the genetic code.

First		Third			
position	Т	С	A	G	position
Т	F	S	Y	С	Т
	F	\mathbf{S}	Y	\mathbf{C}	C
	$_{ m L}$	\mathbf{S}	Stop	Stop	A
	L	\mathbf{S}	Stop	W	G
С	L	Р	Н	R	Т
	${ m L}$	Р	Η	\mathbf{R}	C
	$_{ m L}$	Ρ	Q	\mathbf{R}	A
	L	Р	Q	\mathbf{R}	G
A	I	Τ	N	S	Т
	I	${ m T}$	N	\mathbf{S}	C
	I	${ m T}$	K	\mathbf{R}	A
	M	${ m T}$	K	\mathbf{R}	G
G	V	A	D	G	Т
	V	A	D	G	C
	V	A	\mathbf{E}	G	A
	V	A	E	G	G

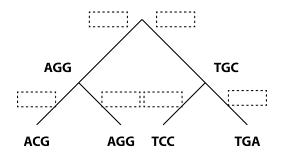
Α Ala Alanine \mathbf{C} Cysteine Cys ${\bf D}$ Aspartic acid Asp Glutamic acid Glu F Phe Phenylalanine GGly Glycine Η Histidine His Ι IleIsoleucine \mathbf{K} Lysine Lys \mathbf{L} Leu Leucine Μ Met Methionine Ν Asparagine Asn Ρ Pro Proline Q Gln Glutamine \mathbf{R} Arginine Arg \mathbf{S} Ser Serine \mathbf{T} Threonine Thr V Valine Val W Trp Tryptophan Tyr Tyrosine

(c) Use the AACH.



2. Probabilities of accepted mutations

Use a phylogenetic tree below to calculate the probabilities of accepted mutations. The tree contains sequences of four OTUs.



- (a) Estimate the mutations and fill them in the boxes next to the edges.
- (b) Count the occurrences of mutations and fill them in the matrix. Note that a mutation $A \to B$ is equivalent with a mutation $B \to A$.

	A	С	G	Т
A				
С				
G				
Т				

(c) Use the following definitions and calculate f_{CG} , f_C and f.

 f_{ab} : The number of mutations from a to b or from b to a

 f_a : Total number of mutations in which a takes part

f: Twice the total number of mutations

 f_{CG} :

 f_C :

f:

(d) Use the following definition and calculate p_C .

 p_a : The relative occurrence of a in the observed sequences

 p_C :

3. Relative mutability of PAM

Relative mutability is calculated from frequencies of estimated mutilation and background probabilities.

$$m_a: \frac{1}{100p_a} \times \frac{f_a}{f}$$

 f_a : Total number of point mutations in which a takes part

f: Twice the total number of point mutations

 p_a : Relative occurrence of a in the observed sequences

Assume that the frequencies are pre-calculated as follows.

• Frequencies of estimated mutations

$$f_A: 2, \quad f_G: 3, \quad f_C: 3, \quad f_T: 2$$

 $f: 10$

• Background probabilities

$$p_A: 3/10, \quad p_G: 2/10, \quad p_C: 4/10, \quad p_T: 1/10$$

(a) Calculate the probabilities of point mutations by $\frac{f_a}{f}$.

$$\frac{f_A}{f}$$
: $\frac{f_G}{f}$: $\frac{f_C}{f}$:

(b) Calculate $100p_a$.

$$100p_A: 100p_G: 100p_C: 100p_T:$$

(c) Calculate the relative mutability m_a .

$$m_A: \qquad m_G: \qquad m_C: \qquad m_T:$$

4. Mutation probabilities of PAM

Mutation probabilities are calculated from relative mutability.

$$m_{ab}: m_a \times \frac{f_{ab}}{f_a}, \qquad m_{aa}: 1 - m_a$$

 f_{ab} : Total number of point mutations in which a takes part

 f_a : Twice the total number of point mutations

 m_a : Relative mutability of a

Assume that the frequencies are pre-calculated as follows.

• Frequencies of estimated mutations

 $f_{AC}: 8, \quad f_A: 32$

• Relative mutability

 $m_A:0.004$

- (a) Calculate M_{AC} .
- (b) Calculate M_{AA} .

5. Odds ratios of PAM

Odds ratios are calculated from mutation probabilities and background probabilities.

$$O_{ab} = \frac{M_{ab}}{p_b} = m_a \times \frac{f_{ab}}{f_a} \times \frac{1}{f_b} = \frac{1}{100} \times \frac{f_{ab}}{f} \times \frac{1}{p_a p_b}$$

Assume that the frequencies are pre-calculated as follows.

$$f_{AC}: 16, \quad f: 400, \quad p_A: 0.2, \quad p_c: 0.4$$

- (a) Calculate O_{AC} .
- (b) Calculate O_{CA} .