Type introduction illustrated

for casual haskellers

to get over the Foldable

Takenobu T.

"What is this description?!"

foldr :: Foldable t => (a -> b -> b) -> b -> t a -> b

NOTE

- This document shows one of the mental model.
- Please see also references.
- This is written for Haskell, especially ghc7.10/8.0 and later.

Contents

- 1. Introduction
 - Values, Types, Type classes
 - Polymorphic types
 - Type constructors
 - Polymorphic and type constructors
- 2. more, Types and Type classes
 - Function types
 - Type class operations
- 3. What is this?

Appendix I - Various types

- Bool, Char, Int, Float
- Maybe, List, Either, Tuple

Appendix II - Various type classes

- Eq, Ord
- Num
- Foldable
- Functor, Applicative, Monad
- Monoid
- Traversable

Appendix III - Advanced topics

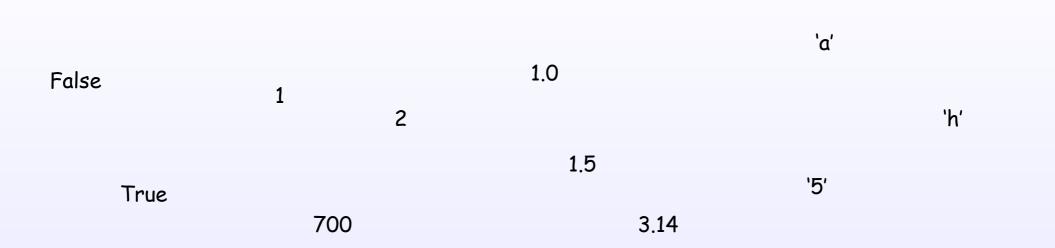
References

1. Introduction

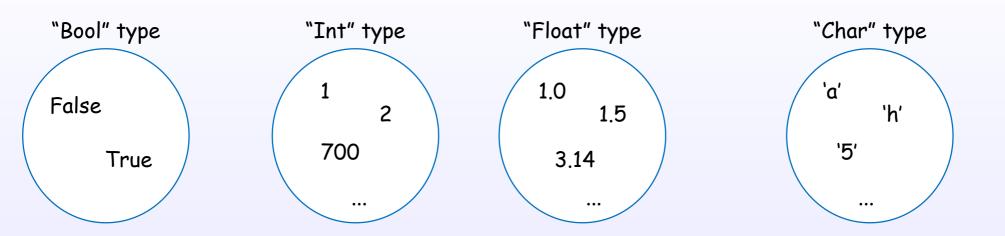
1. Introduction

Values, Types, Type classes

Values



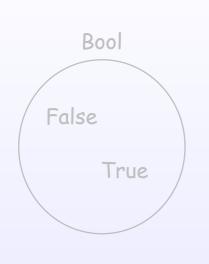
Types

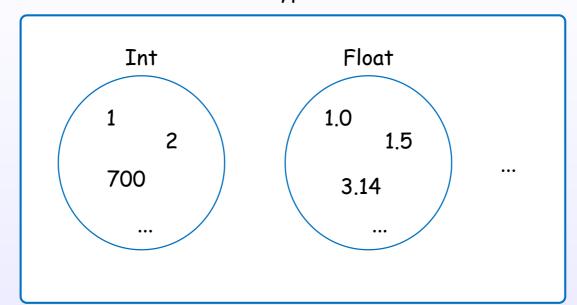


A type is a collection of values which have common property.

Type classes

"Num" type class





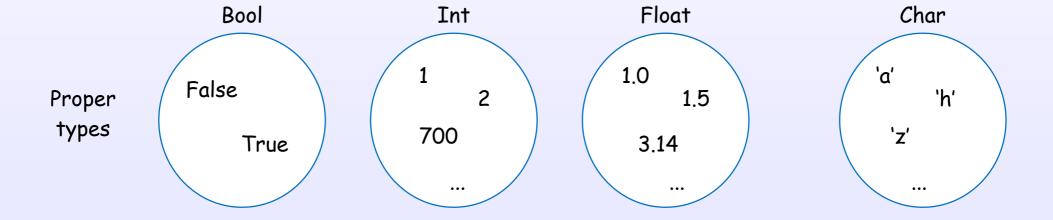


A type class is a collection of types which have common operations.

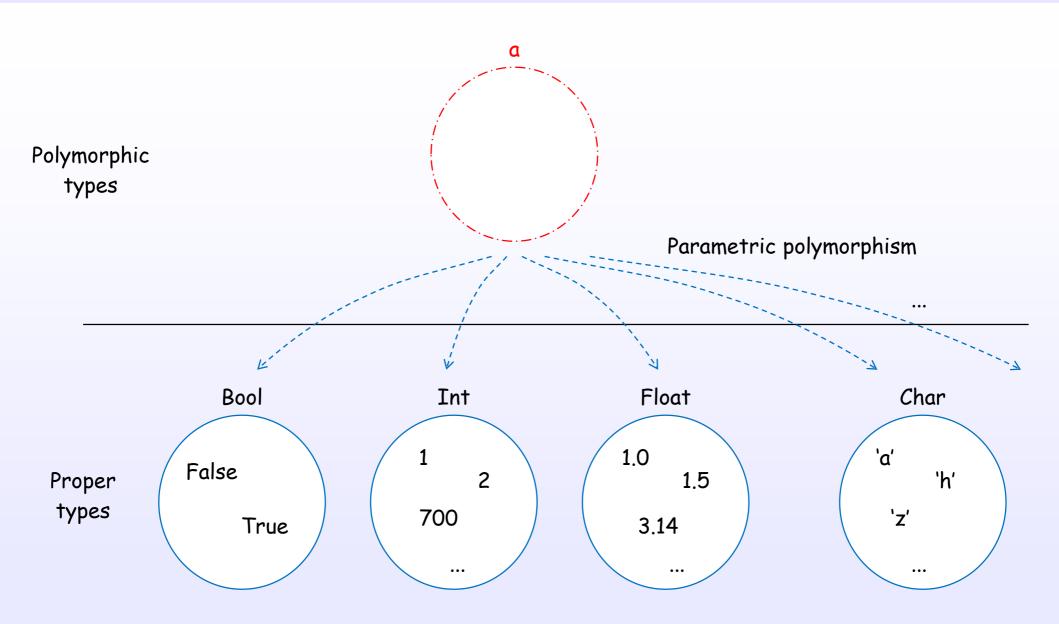
1. Introduction

Polymorphic types

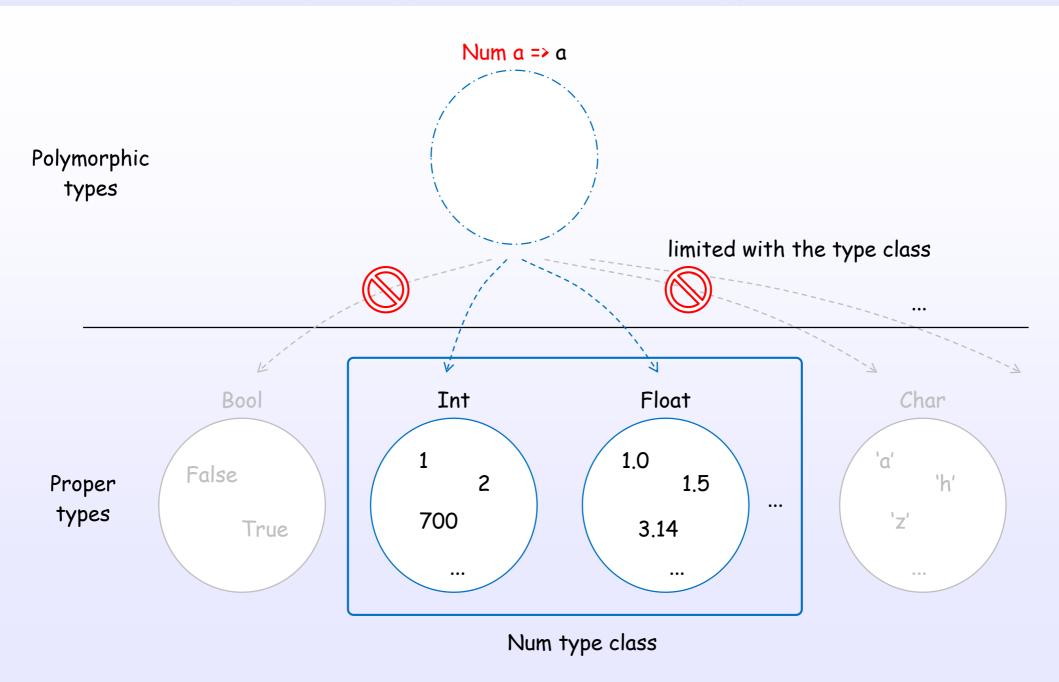
Proper types



Polymorphic types



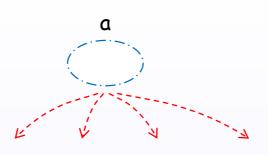
Polymorphic types restricted with type classes



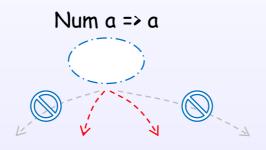
References: [B1] Ch.2, [B2] Ch.2, [B3] Ch.3, [B4] Ch.6, [D1] Week 4

Polymorphic types

Polymorphic types



polymorphic types with type class



Proper types

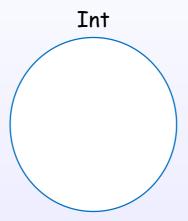


1. Introduction

Type constructors

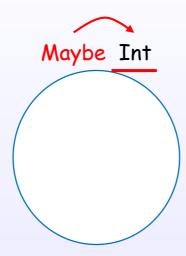
Type constructors

nullary type constructor



Type constructors

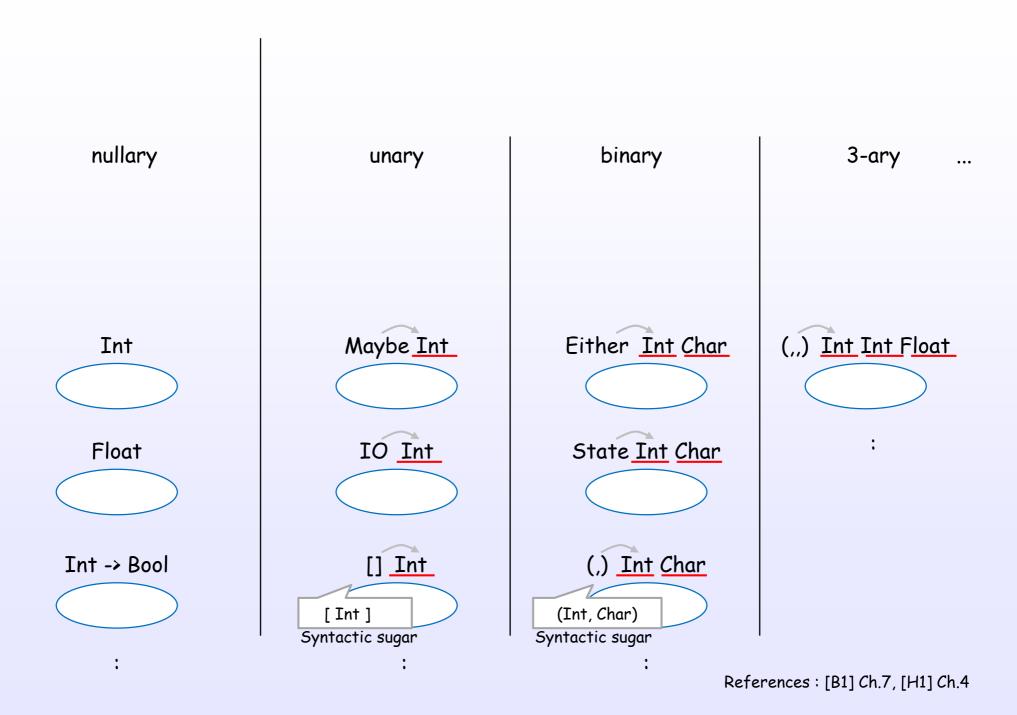
unary type constructor



"Maybe" type constructor takes one type argument (unary).

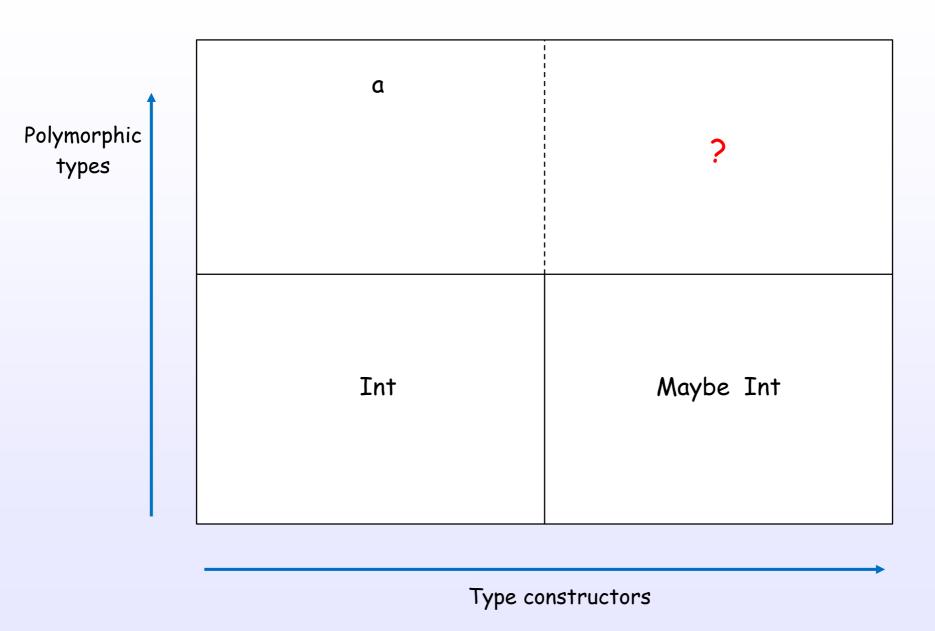
References: [B1] Ch.7

Type constructors

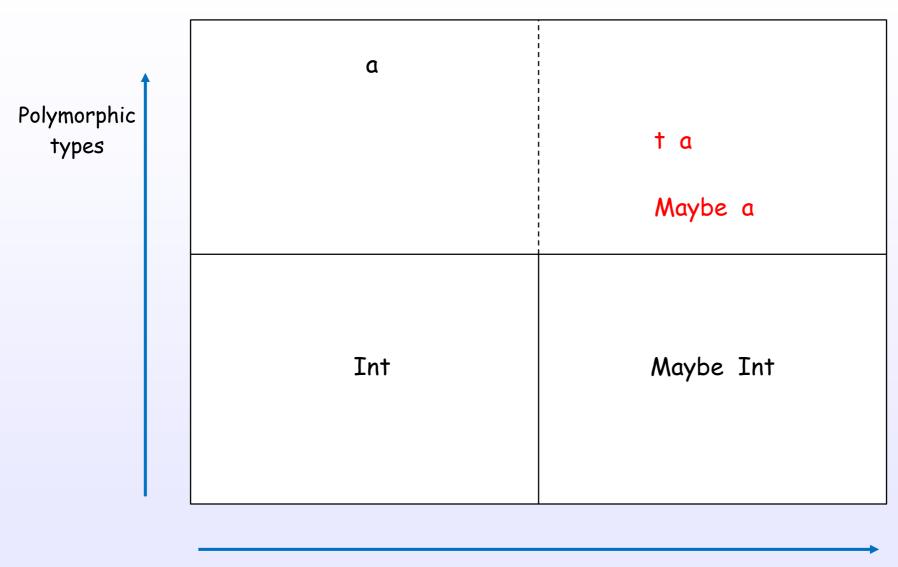


1. Introduction

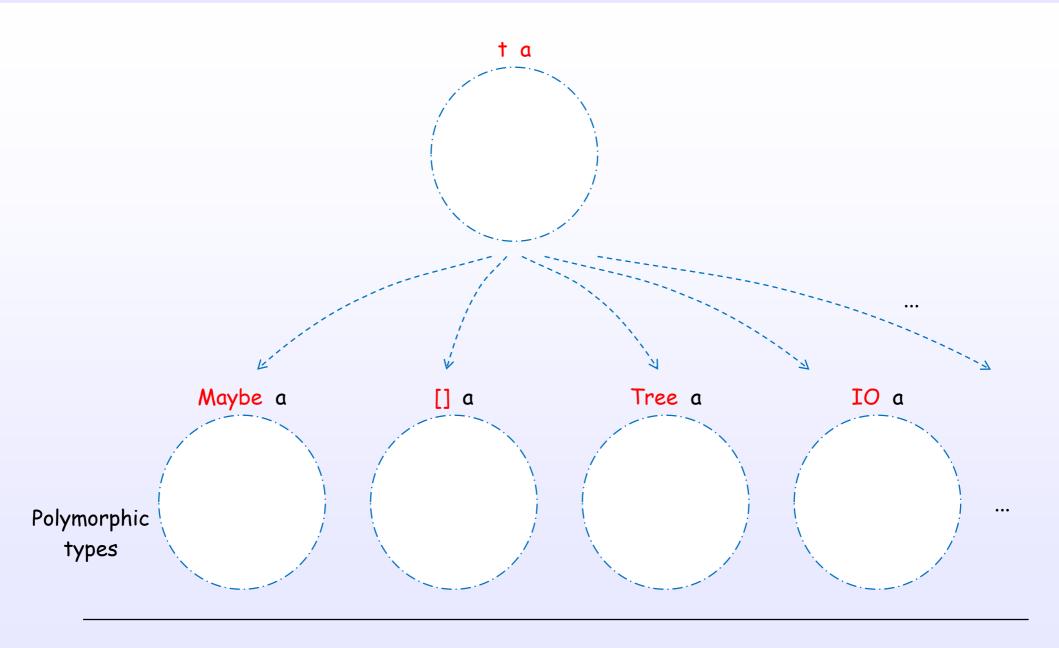
Polymorphic types and type constructors

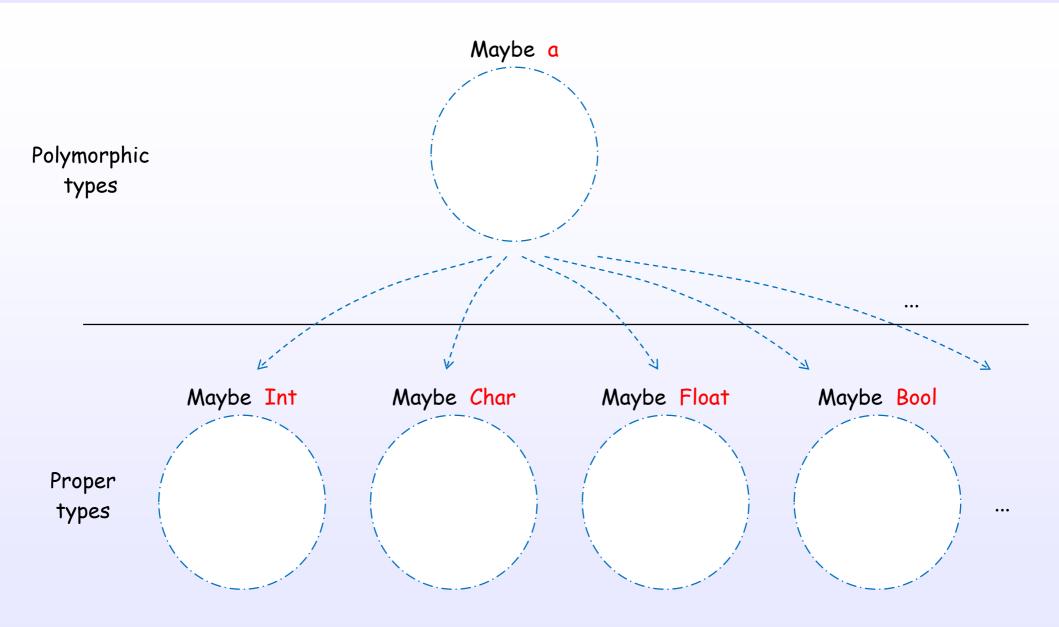


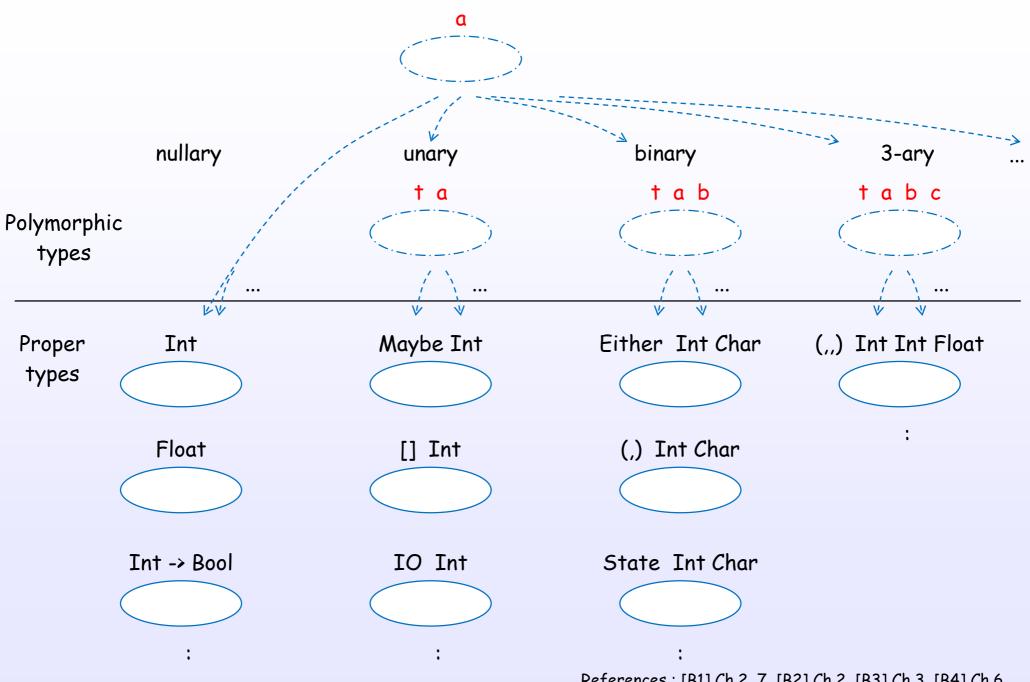
References: [B1] Ch.2, 7, [B2] Ch.2, [B3] Ch.3, [B4] Ch.6



Type constructors







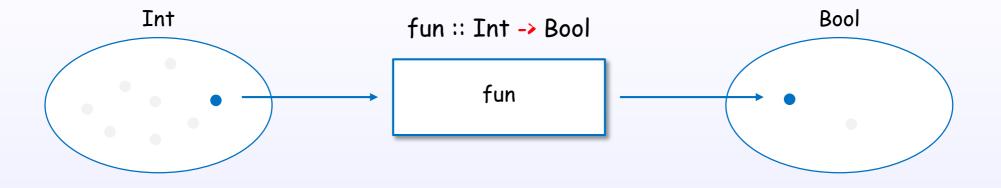
References: [B1] Ch.2, 7, [B2] Ch.2, [B3] Ch.3, [B4] Ch.6

2. more, Types and Type classes

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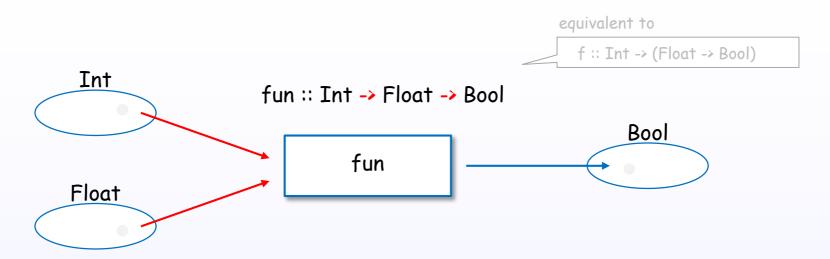
Function types

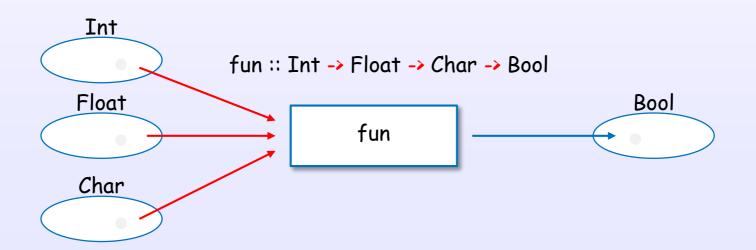
Function type



The "->" represents the function type.

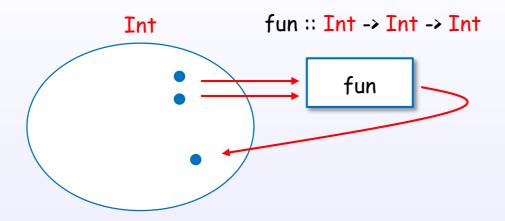
Function type with multiple arguments





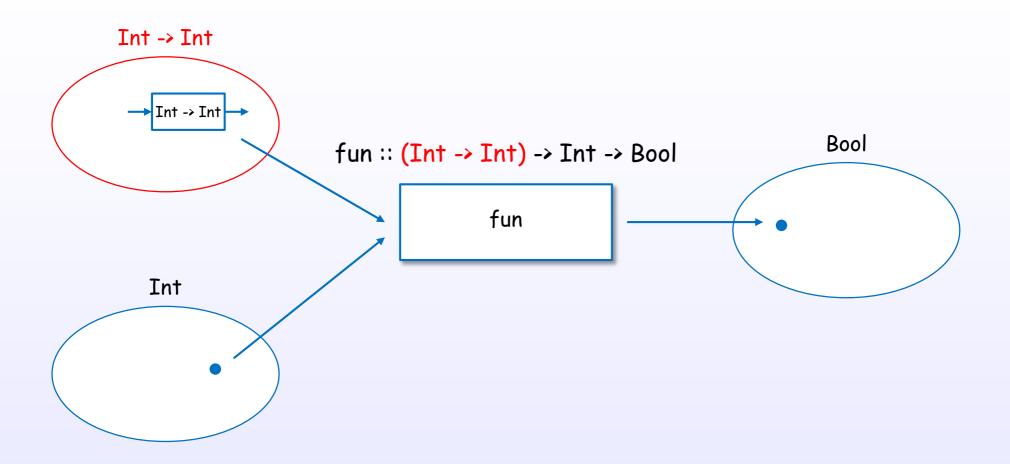
References: [B2] Ch.2, [B1] Ch.5, [B3] Ch.7

Function type with same type

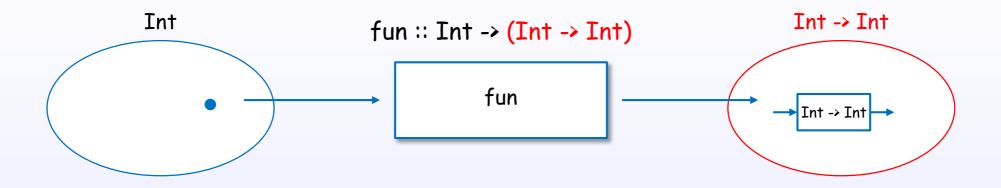


References: [B2] Ch.2, [B1] Ch.5, [B3] Ch.7

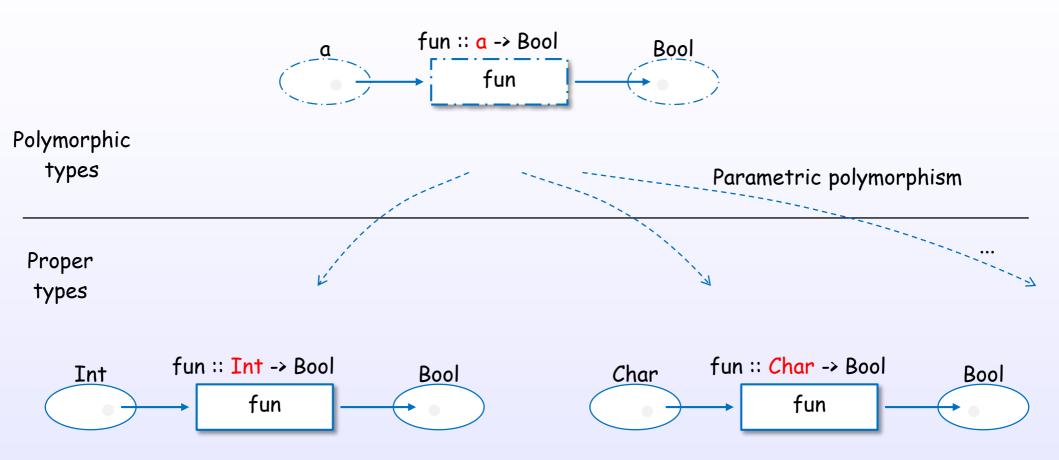
Function type with function as argument



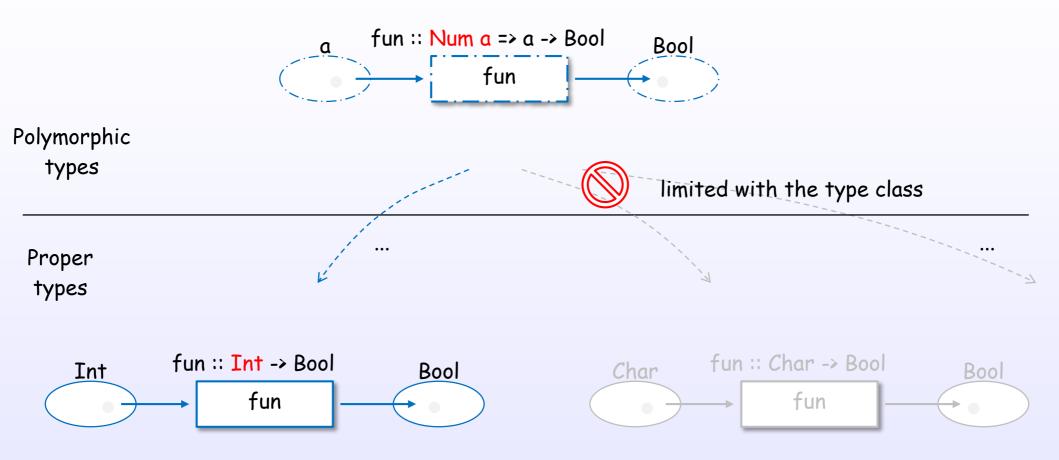
Function type with function as result



Function type with polymorphic function



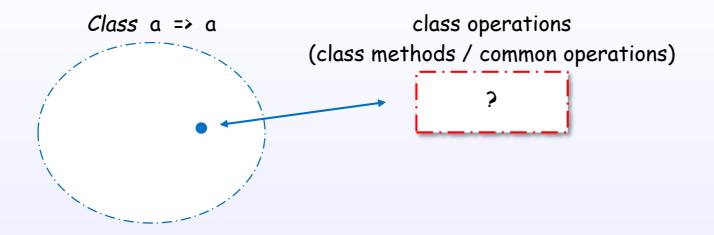
Function type for polymorphic function with type class



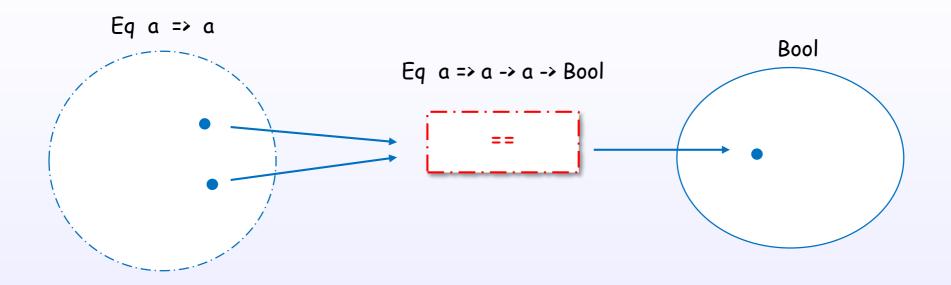
2. more, Types and Type classes

Type class operations

A type class has the class operations

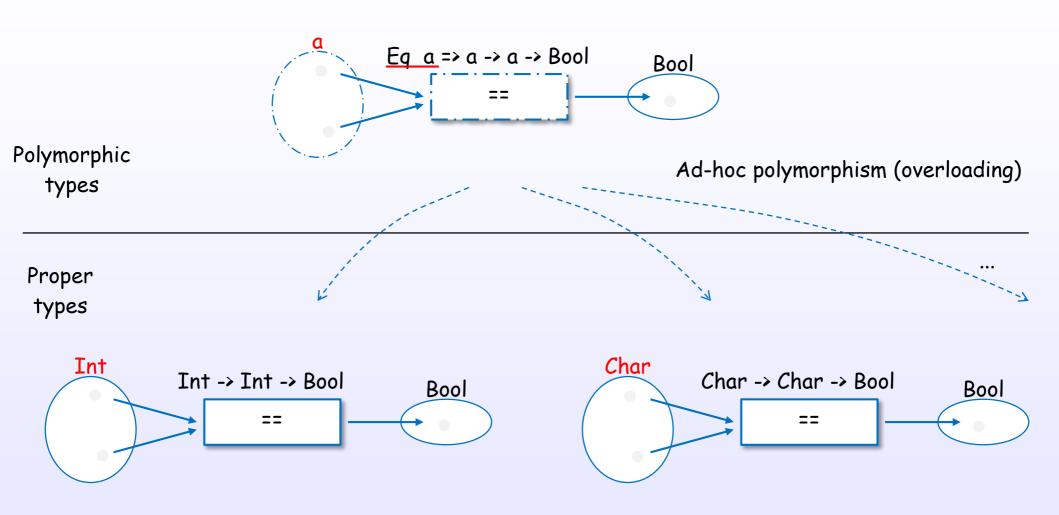


A type class has the class operations



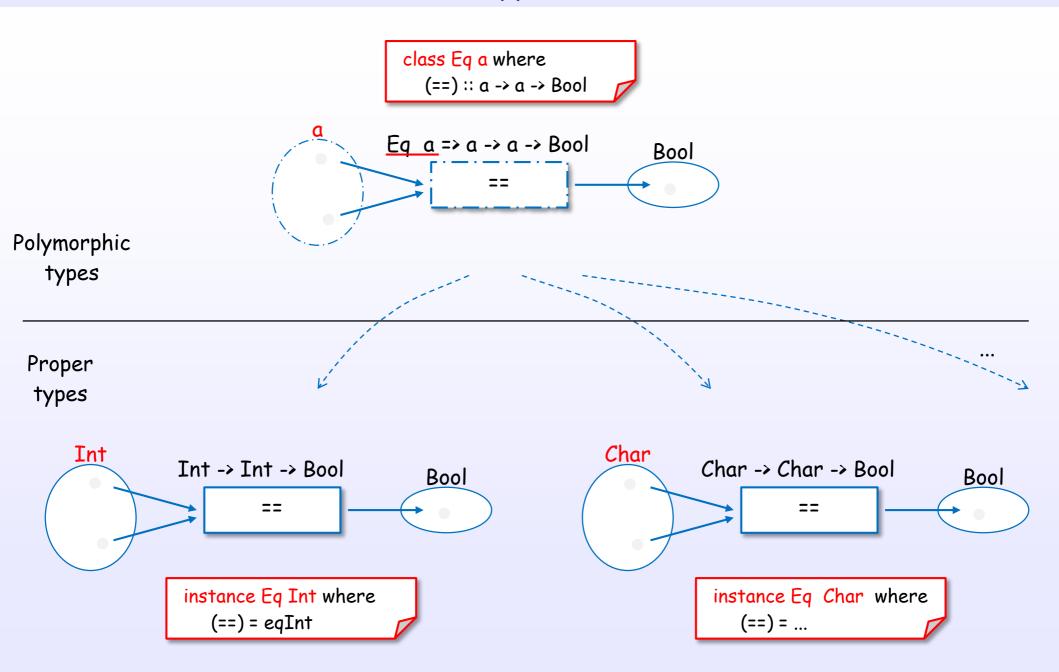
Eq class has "==" (equality) operation.

A type class has the class operations



Each type, that belongs to the type class, must be support the overloaded operations.

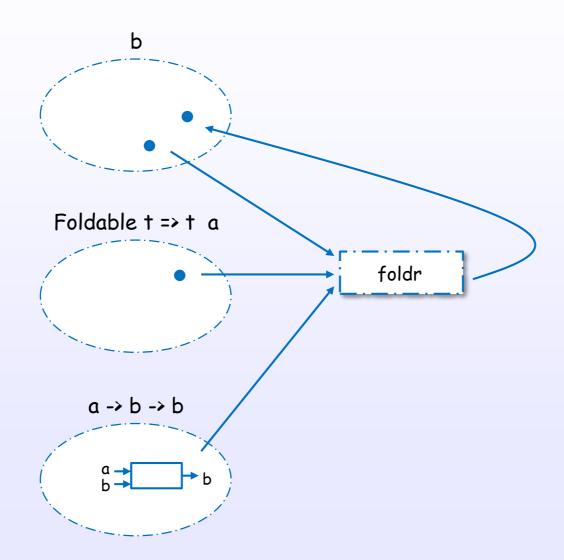
Declaration of a type class and instances

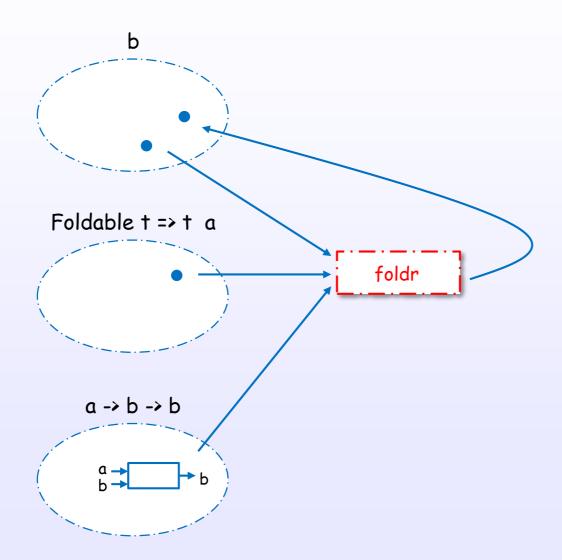


3. What is this?

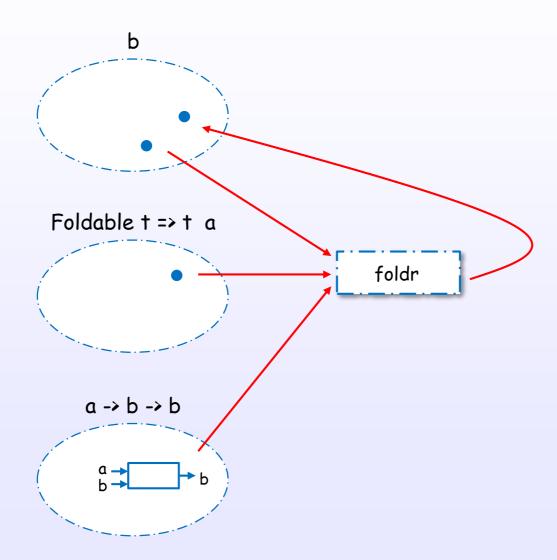
```
foldr:: Foldable t => (a \rightarrow b \rightarrow b) \rightarrow b \rightarrow t a \rightarrow b
foldr = ...
```

foldr:: Foldable $t \Rightarrow (a \rightarrow b \rightarrow b) \rightarrow b \rightarrow t a \rightarrow b$

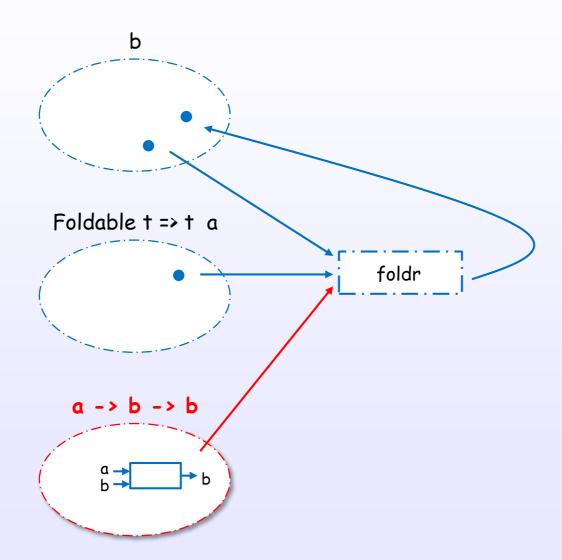




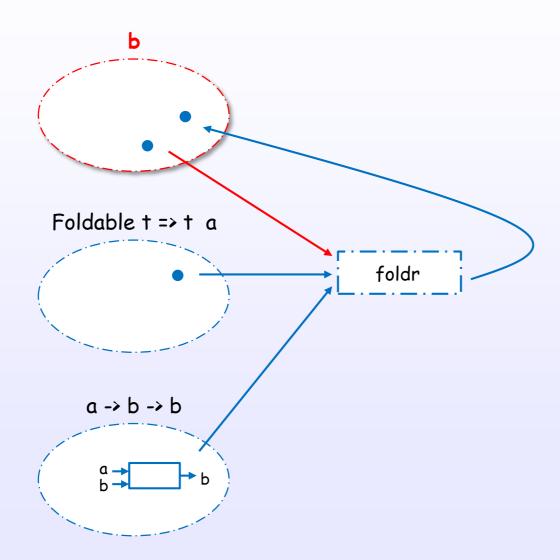
foldr:: Foldable
$$t \Rightarrow (a \rightarrow b \rightarrow b) \rightarrow b \rightarrow t a \rightarrow b$$



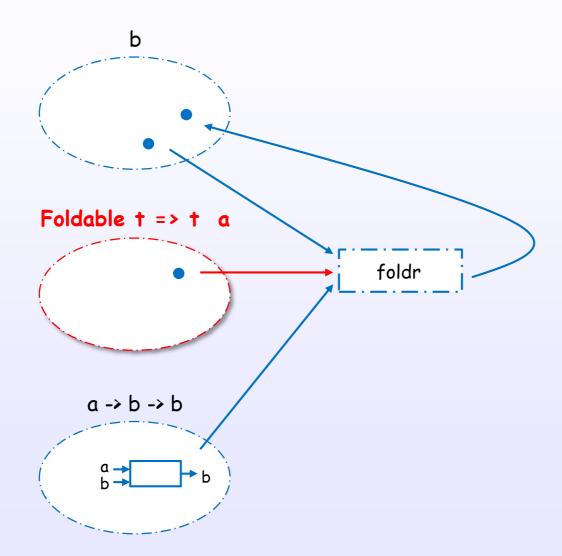
foldr:: Foldable
$$t \Rightarrow (a \rightarrow b \rightarrow b) \rightarrow b \rightarrow t a \rightarrow b$$



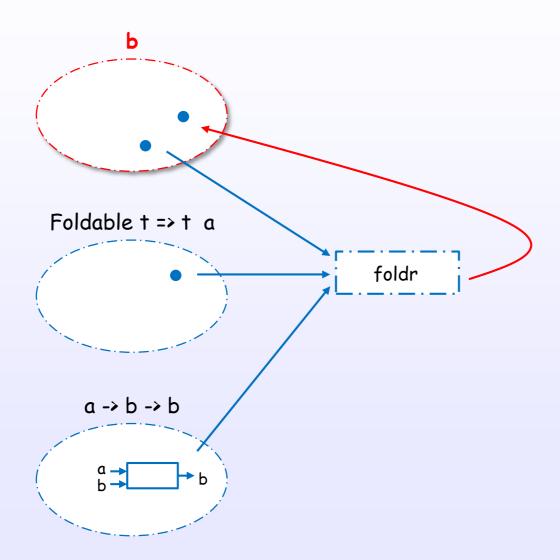
foldr:: Foldable
$$t \Rightarrow (a \rightarrow b \rightarrow b) \rightarrow b \rightarrow t a \rightarrow b$$



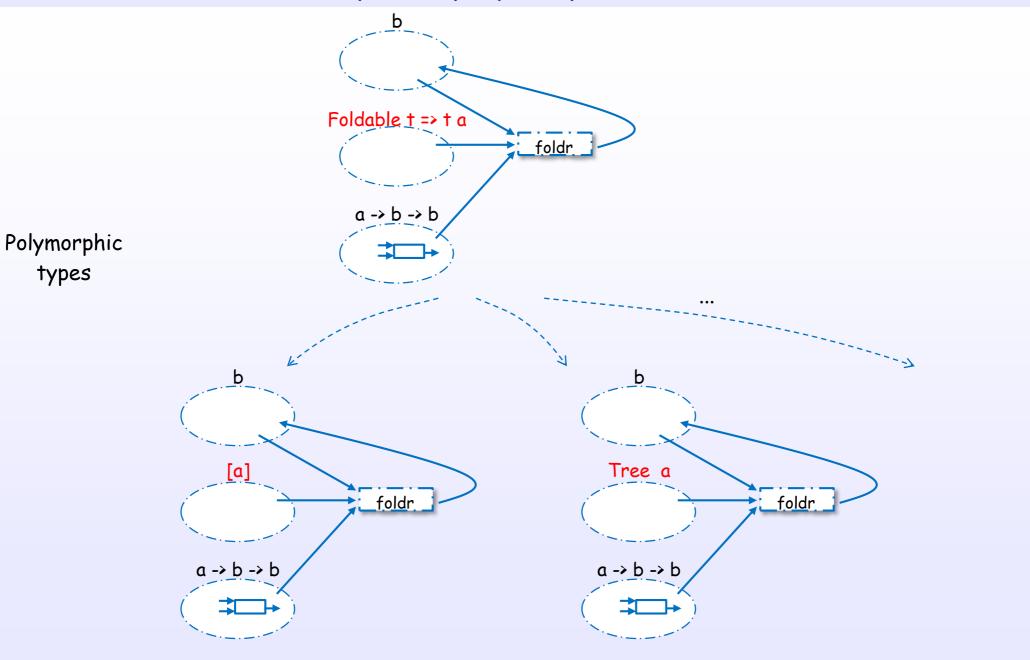
foldr:: Foldable
$$t \Rightarrow (a \rightarrow b \rightarrow b) \rightarrow b \rightarrow t a \rightarrow b$$



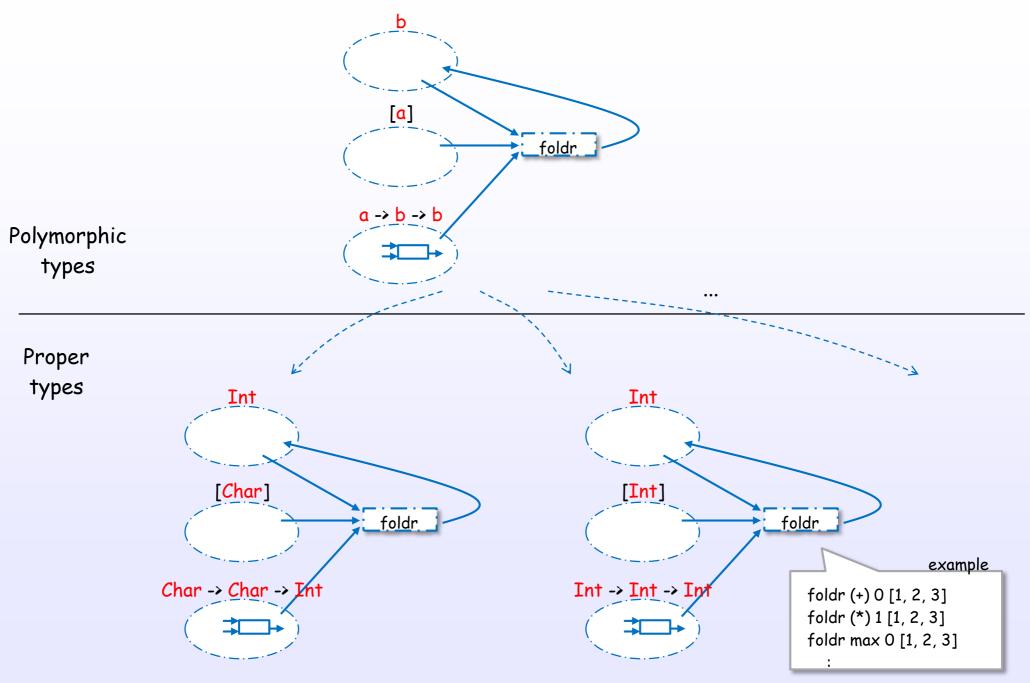
foldr:: Foldable
$$t \Rightarrow (a \rightarrow b \rightarrow b) \rightarrow b \rightarrow t a \rightarrow b$$



Example of polymorphism on foldr

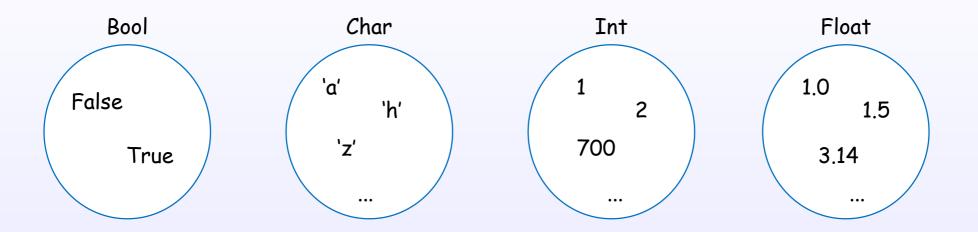


Example of polymorphism on foldr

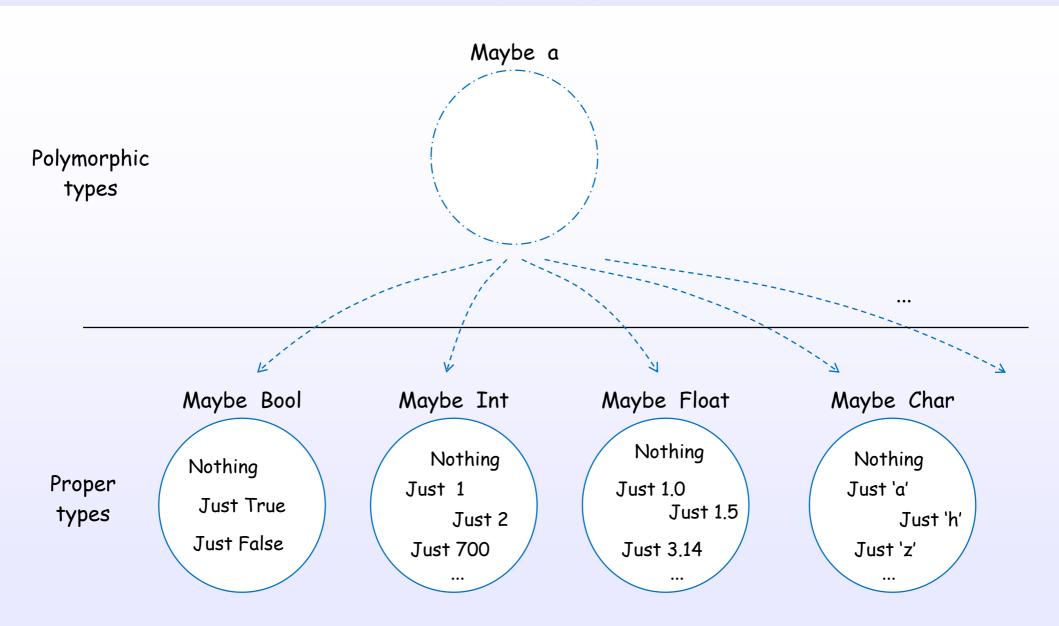


Appendix I - Various types

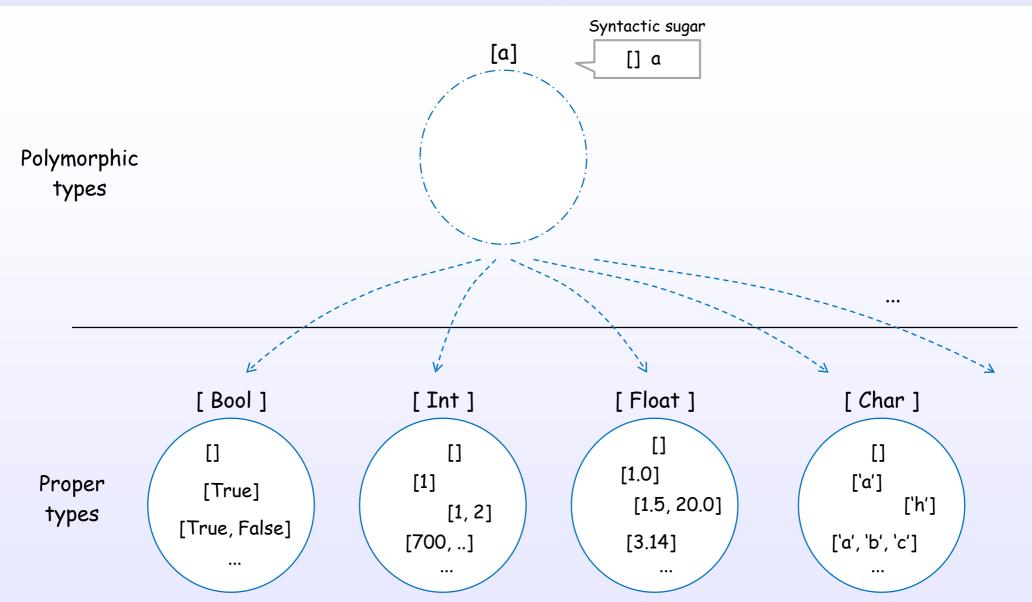
Bool, Char, Int, Float types



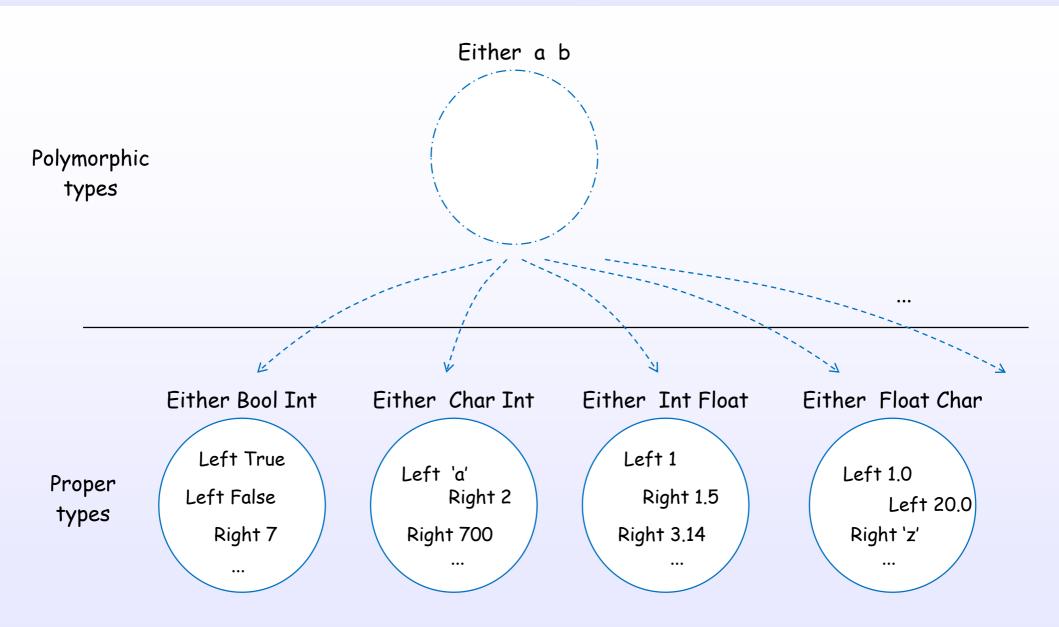
Maybe type



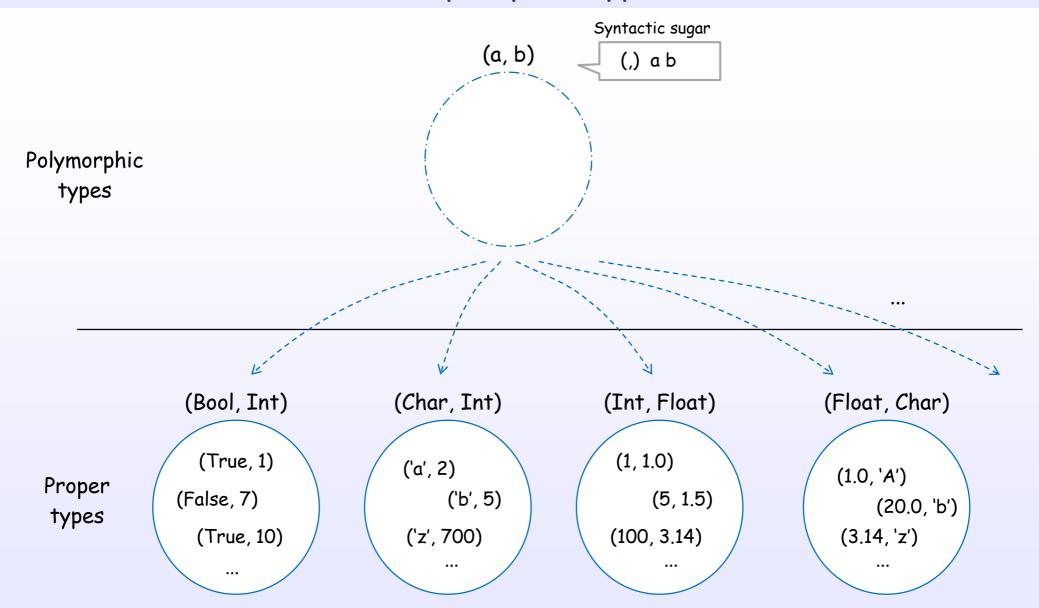
List type



Either type

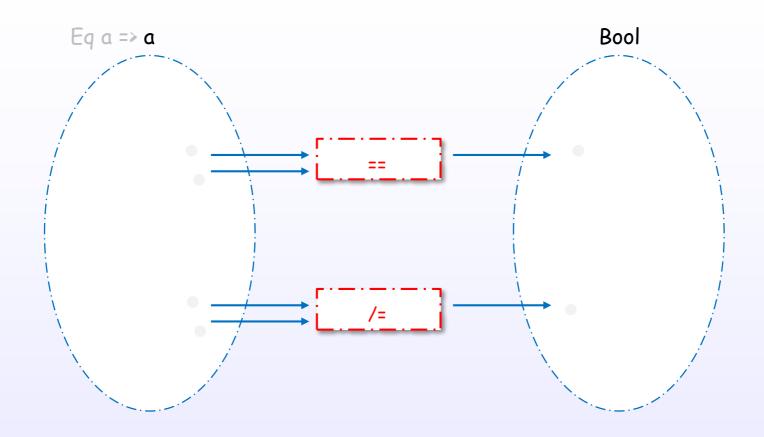


Tuple (pair) type



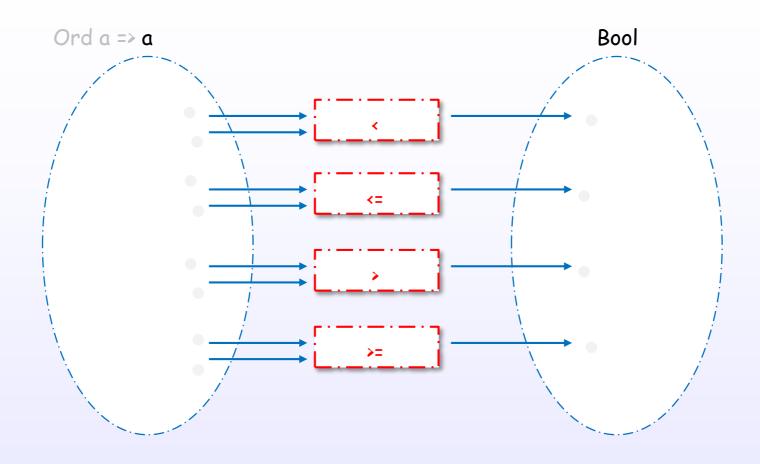
Appendix II - Various type classes

Eq class's characteristic operations



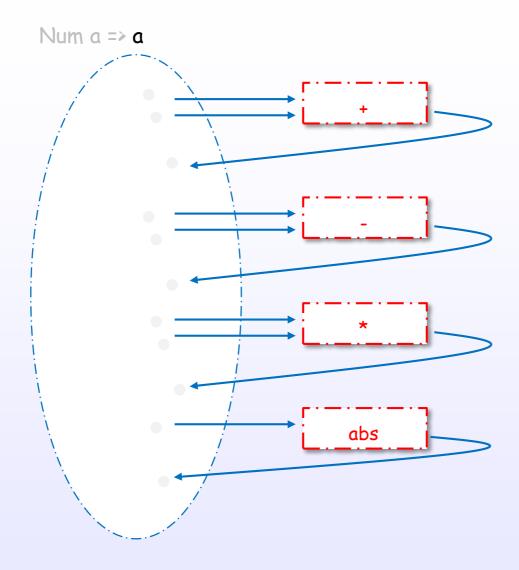
The Eq class has equality operations.

Ord class's characteristic operations



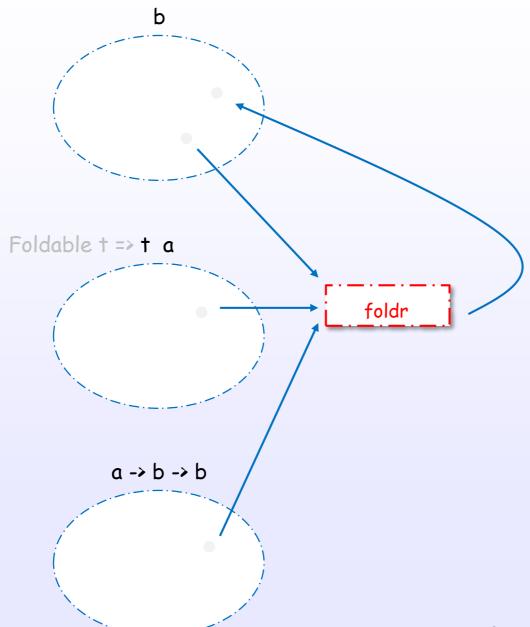
The Ord class has comparison operations.

Num class's characteristic operations



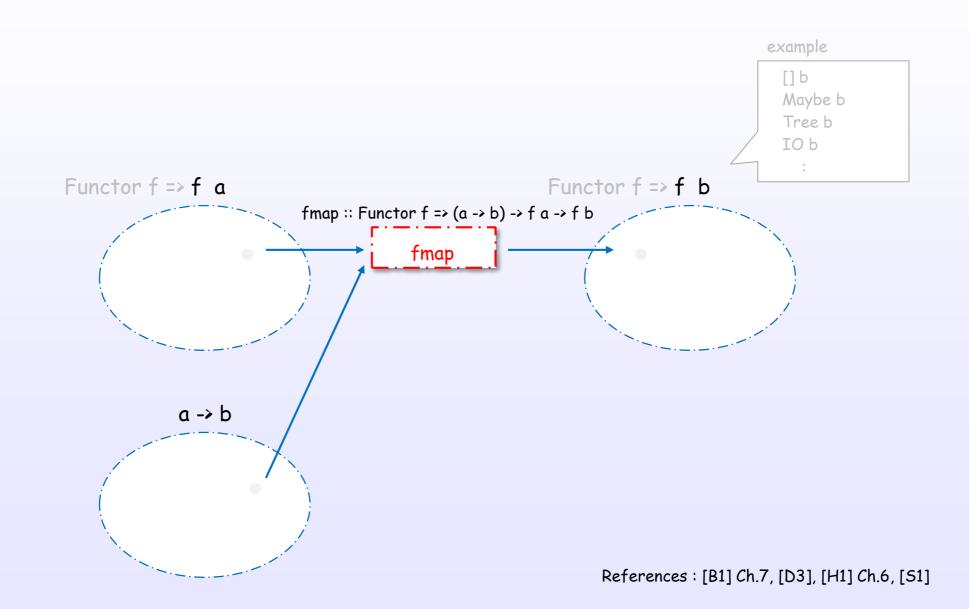
The Num class has arithmetic operations.

Foldable class's characteristic operations

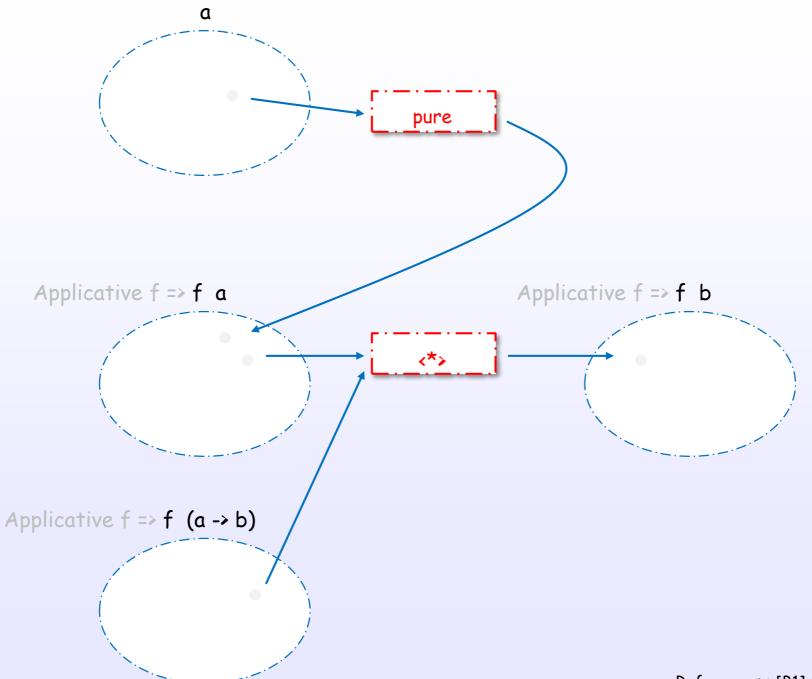


References: [B1] Ch.12, [B2] Ch.6, [B3] Ch.7, [D3], [S1]

Functor class's characteristic operations

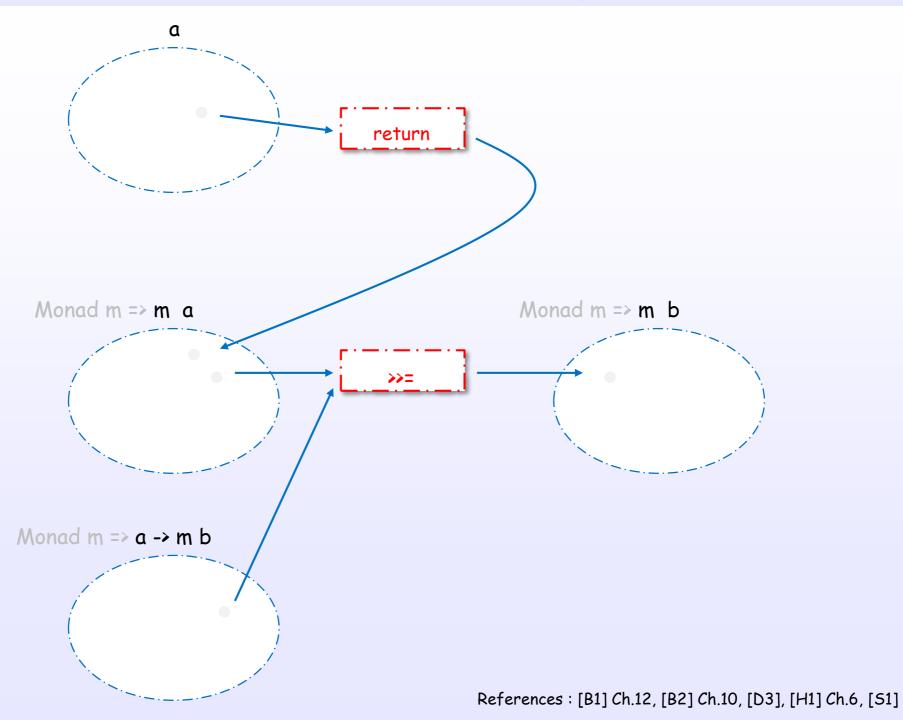


Applicative class's characteristic operations

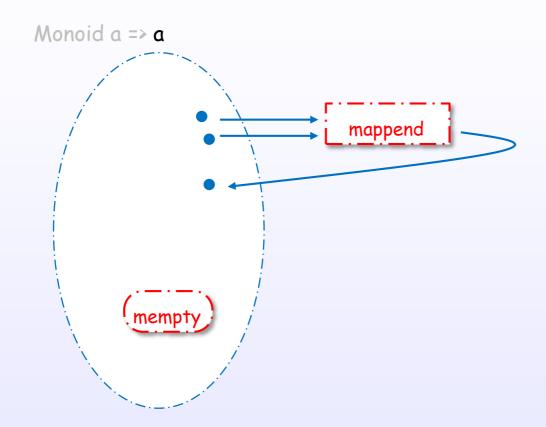


References: [B1] Ch.11, [D3], [S1]

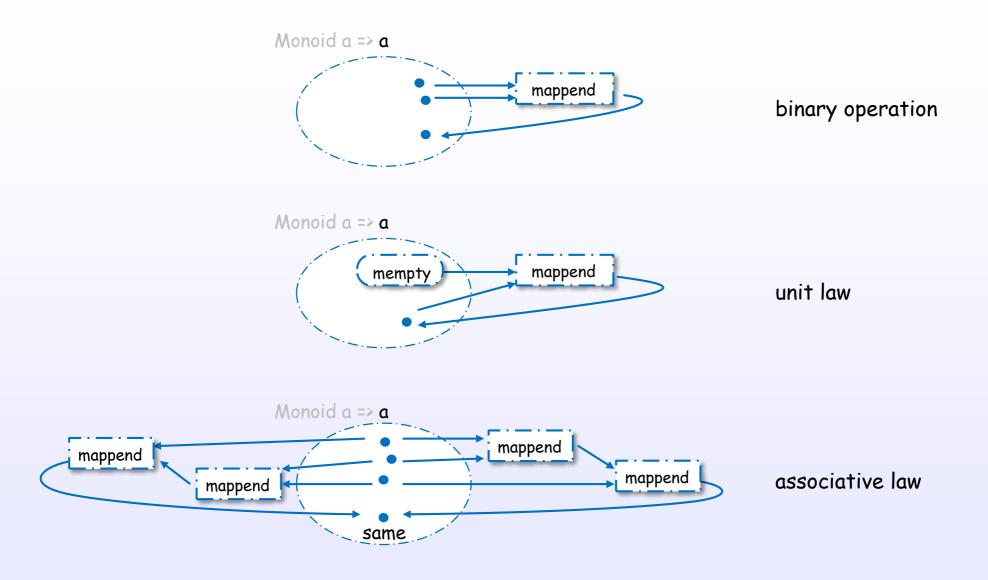
Monad class's characteristic operations



Monoid class's characteristic operations



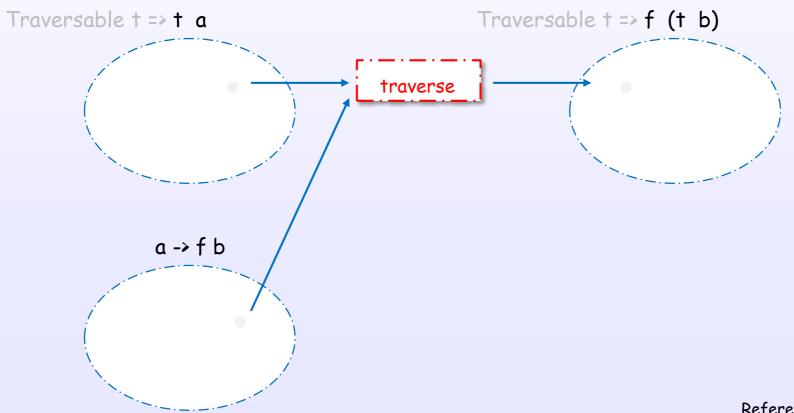
Related topics: monoid laws



Programmers should satisfy the monoid laws.

References: [B1] Ch.12, [D3], [S1]

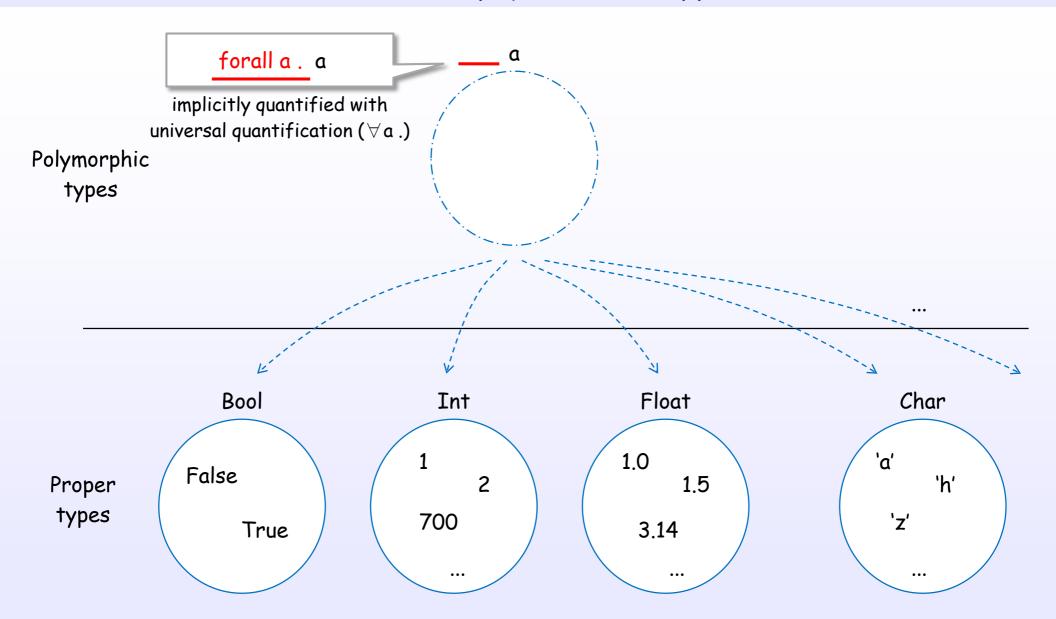
Traversable class's characteristic operations



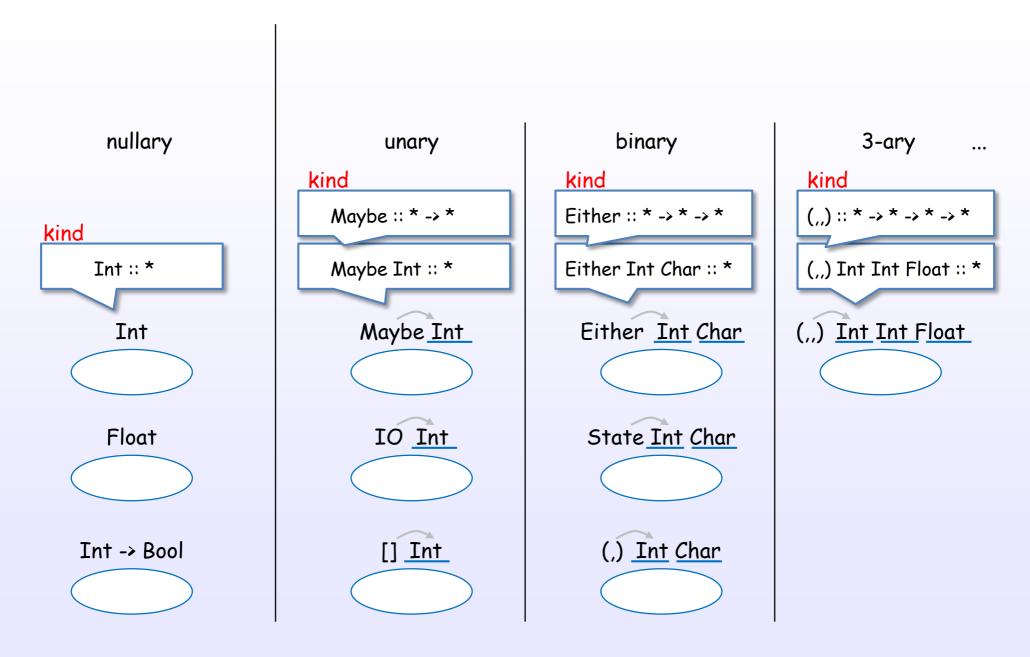
References: [D3], [S1]

Appendix III - Advanced topics

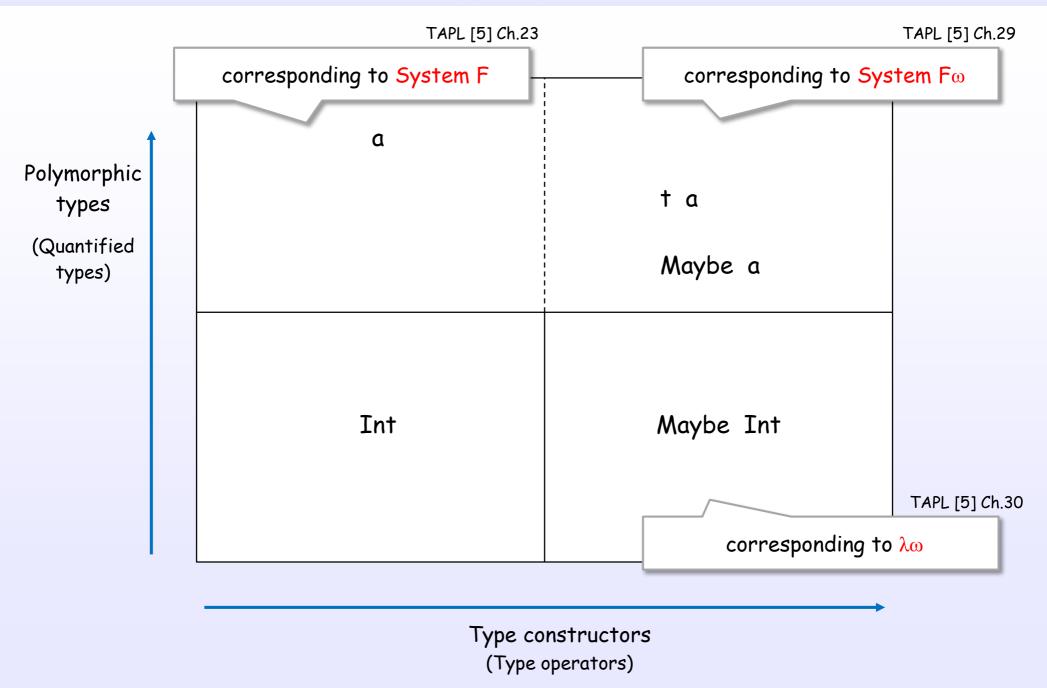
Universally quantified types



Kinds and type constructors



Type systems



References: [B5] Ch.23, 29, 30

Books

- [B1] Learn You a Haskell for Great Good! (LYAH) http://learnyouahaskell.com/
- [B2] Thinking Functionally with Haskell (IFPH 3rd edition) http://www.cs.ox.ac.uk/publications/books/functional/
- [B3] Programming in Haskell http://www.cs.nott.ac.uk/~pszgmh/book.html
- [B4] Real World Haskell (RWH) http://book.realworldhaskell.org/
- [B5] Types and Programming Languages (TAPL) https://mitpress.mit.edu/books/types-and-programming-languages

Documents

- [D1] CIS 194: Introduction to Haskell http://www.seas.upenn.edu/~cis194/lectures.html
- [D2] Type Systems http://dev.stephendiehl.com/fun/004_type_systems.html
- [D3] Typeclassopedia http://www.cs.tufts.edu/comp/150FP/archive/brent-yorgey/tc.pdf https://wiki.haskell.org/Typeclassopedia

Search

[S1] Hoogle https://www.haskell.org/hoogle

Specifications

- [H1] Haskell 2010 Language Report https://www.haskell.org/definition/haskell2010.pdf
- [H2] The Glorious Glasgow Haskell Compilation System (GHC user's guide) https://downloads.haskell.org/~ghc/latest/docs/html/users_guide/index.html https://downloads.haskell.org/~ghc/latest/docs/users_guide.pdf

Furthermore readings

- [A1] What I Wish I Knew When Learning Haskell http://dev.stephendiehl.com/hask/
- [A2] How to learn Haskell https://github.com/bitemyapp/learnhaskell
- [A3] Documentation https://www.haskell.org/documentation
- [A4] A Haskell Implementation Reading List http://www.stephendiehl.com/posts/essential_compilers.html
- [A5] The GHC reading list https://ghc.haskell.org/trac/ghc/wiki/ReadingList