

# Lazy evaluation in Haskell

*exploring some mental models and implementations*

Takenobu T.

Lazy,... zzz

..., It's fun.

## NOTE

- Meaning of terms are different by communities.
- There are a lot of good documents. Please see also references.
- This is written for GHC's Haskell.

# Contents

## Overview

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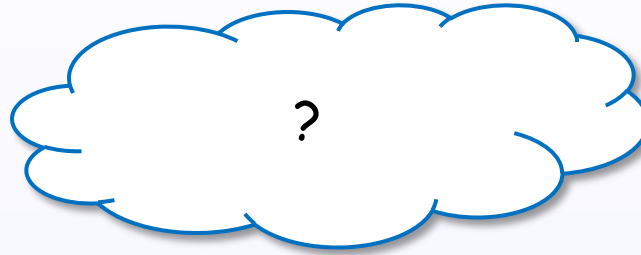
## Appendix

- References

# Introduction

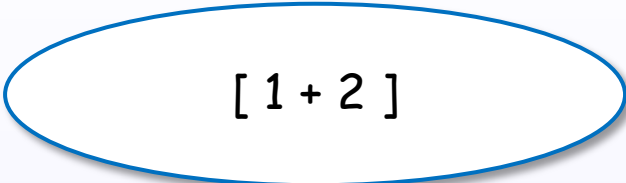
# What is an expression?

An expression



# An expression denotes a value

An expression



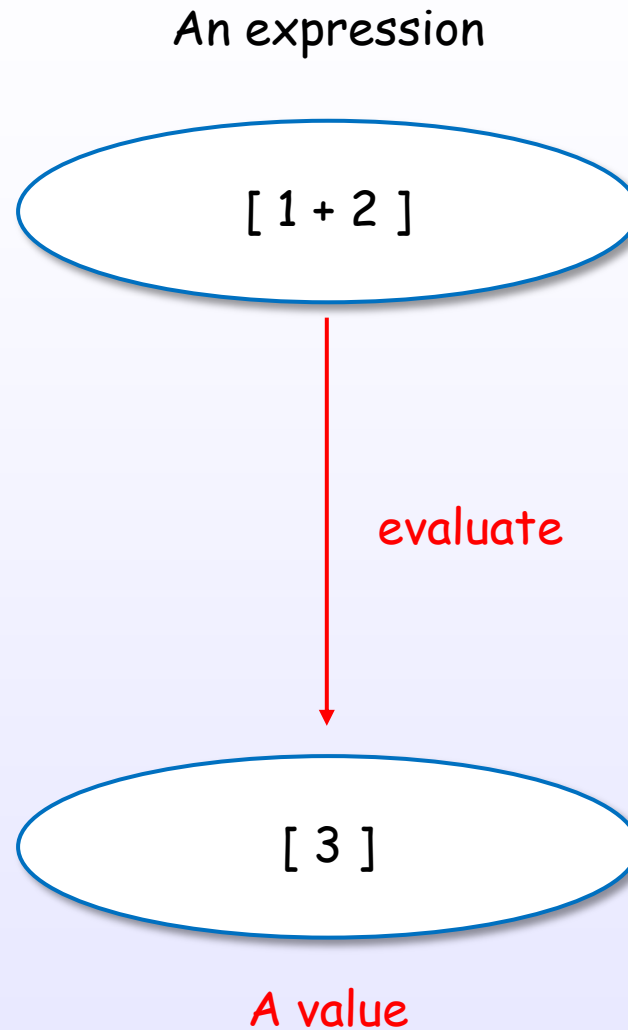
[ 1 + 2 ]

[HR2010]

[Bird, Chapter 2]

References : [1]

# An expression evaluates to a value

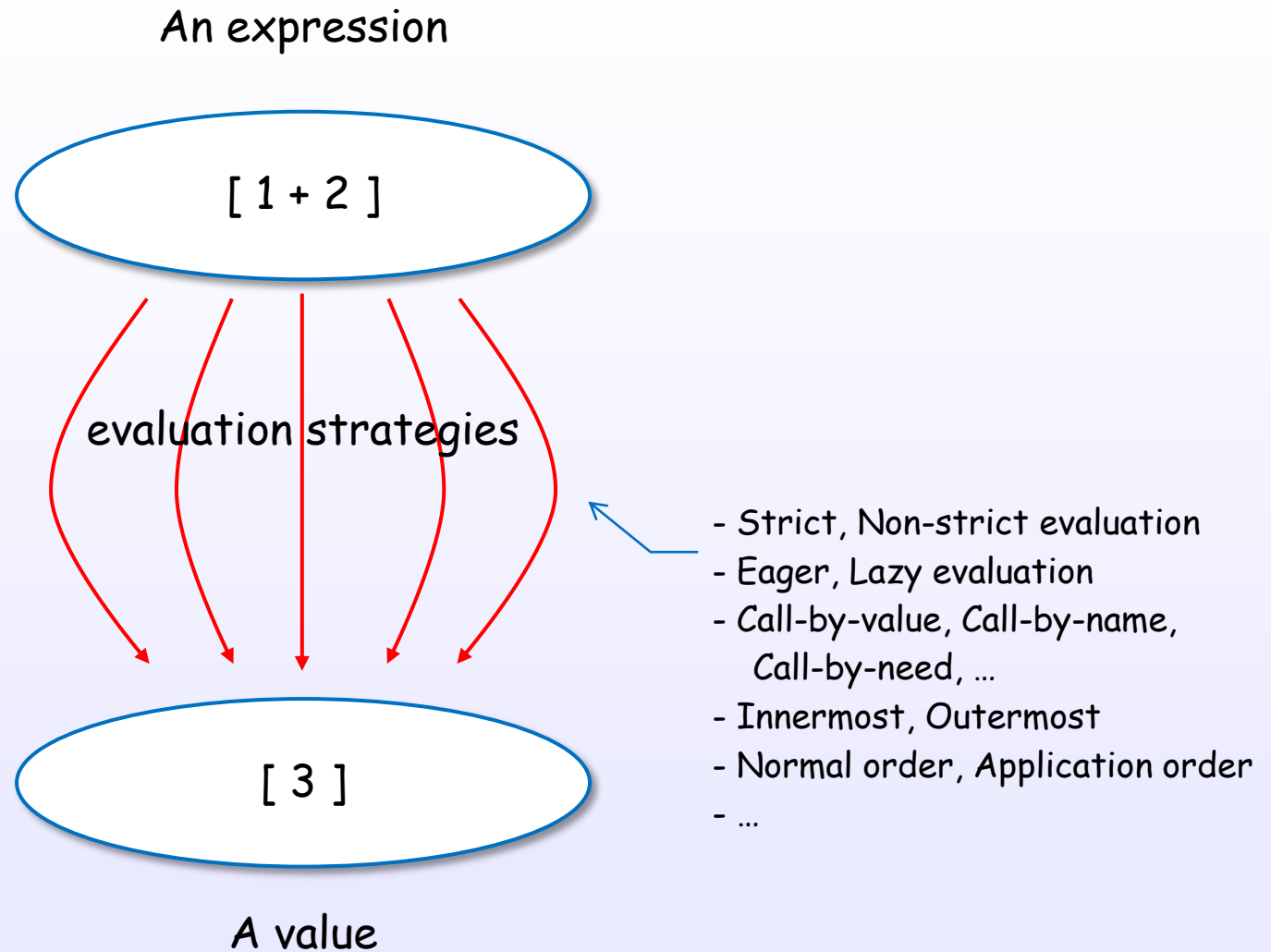


[HR2010]

[Bird, Chapter 2]



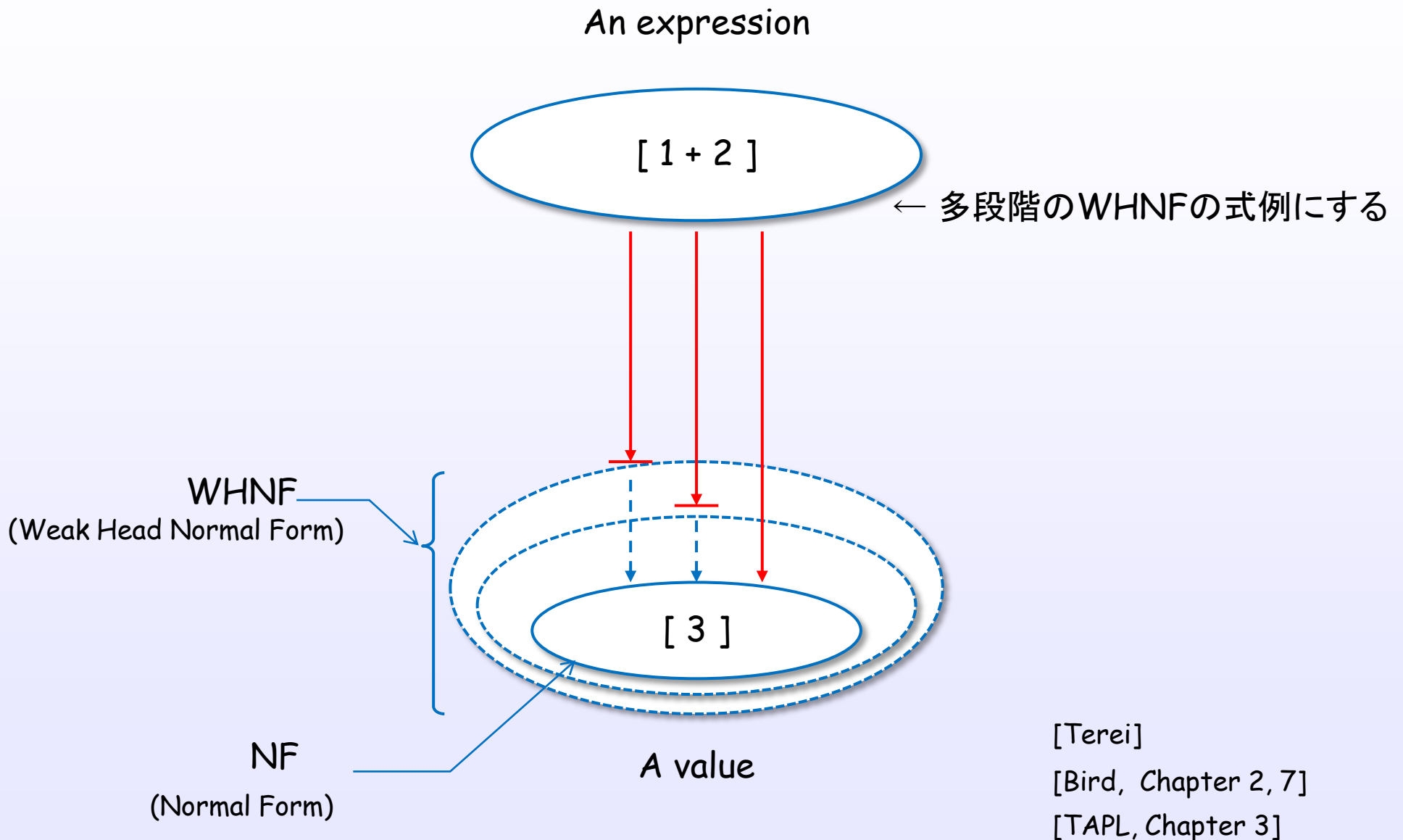
# There are many evaluation approaches



[Bird, Chapter 2, 7]

[TAPL, Chapter 3]

# There are some evaluation levels

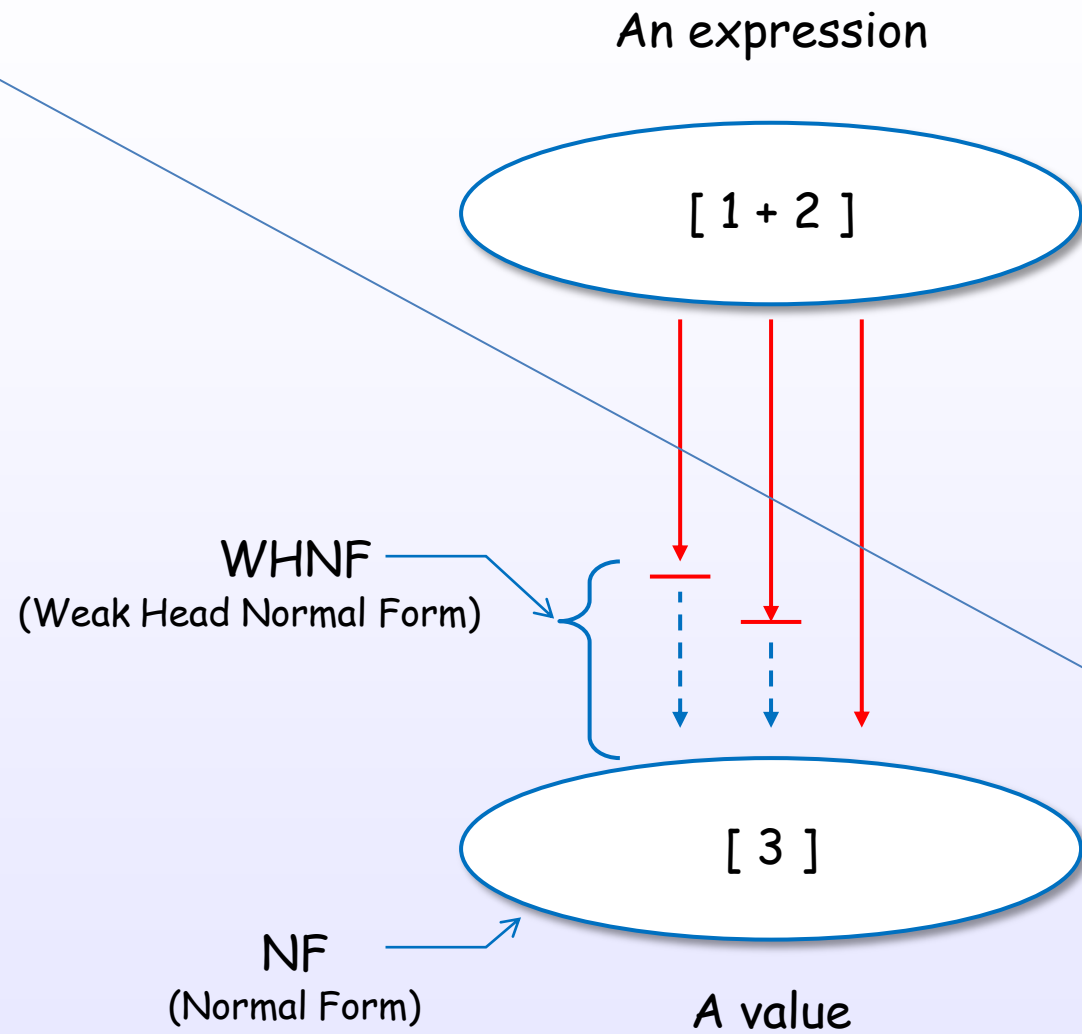


[Terei]

[Bird, Chapter 2, 7]

[TAPL, Chapter 3]

# There are some evaluation levels



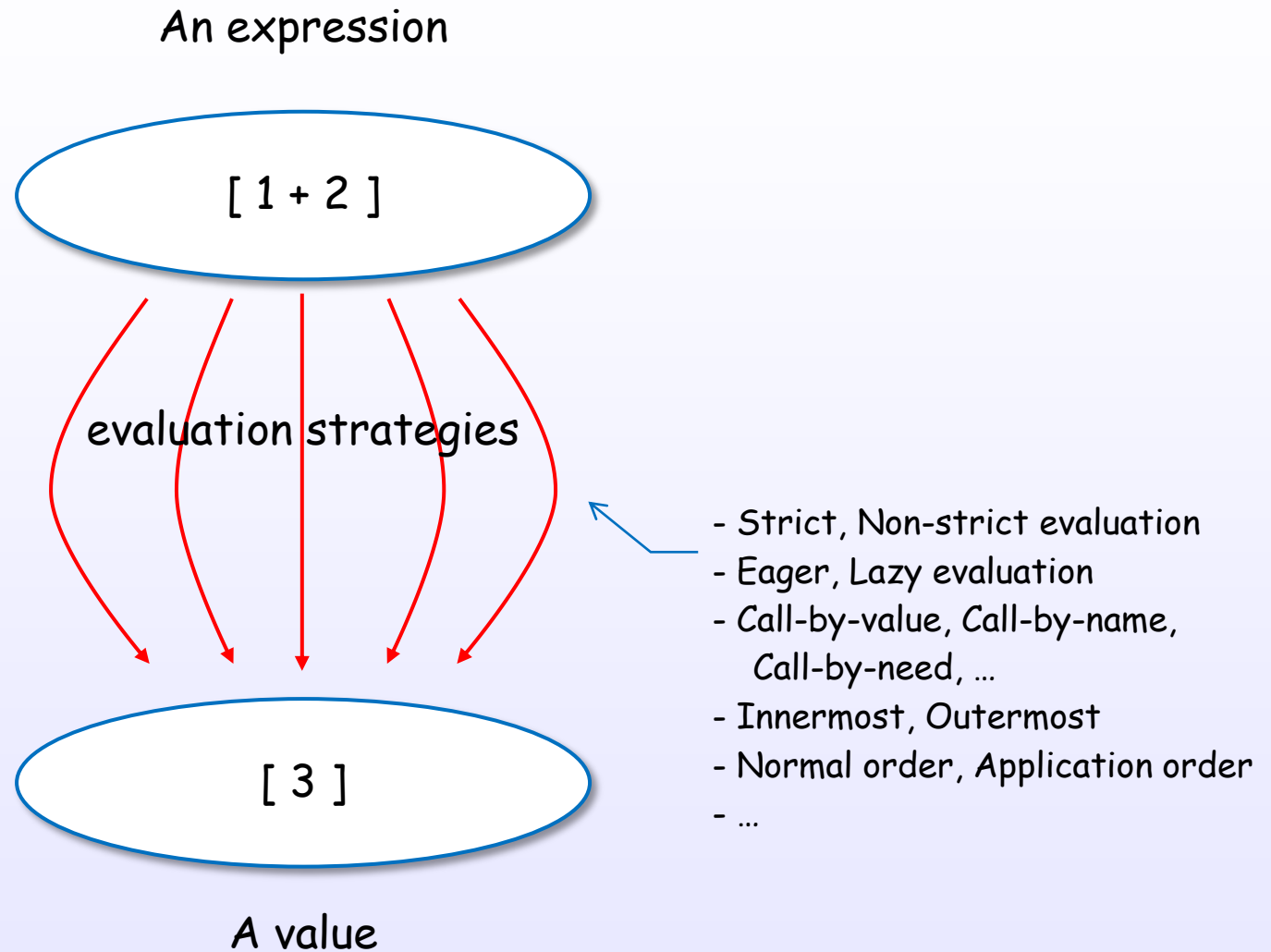
[Terei]

[Bird, Chapter 2, 7]

[TAPL, Chapter 3]

# Evaluation strategies

# There are many evaluation approaches



[Bird, Chapter 2, 7]

[TAPL, Chapter 3]

# Evaluation layers

denotational semantics

evaluation strategies

implementation techniques

[Bird, Chapter 7]

[Hutton, Chapter 8]

[TAPL, Chapter 3]

References : [1]

# Evaluation layers

denotational  
semantics

Strict semantics

Non-strict semantics

evaluation  
strategies

Eager evaluation  
(Strict evaluation)

Nondeterministic  
evaluation

Lazy evaluation  
(Non-strict evaluation)

...

Call-by-Value

Call-by-Name

Call-by-Need

...

implementation  
techniques

Lazy graph reduction

...

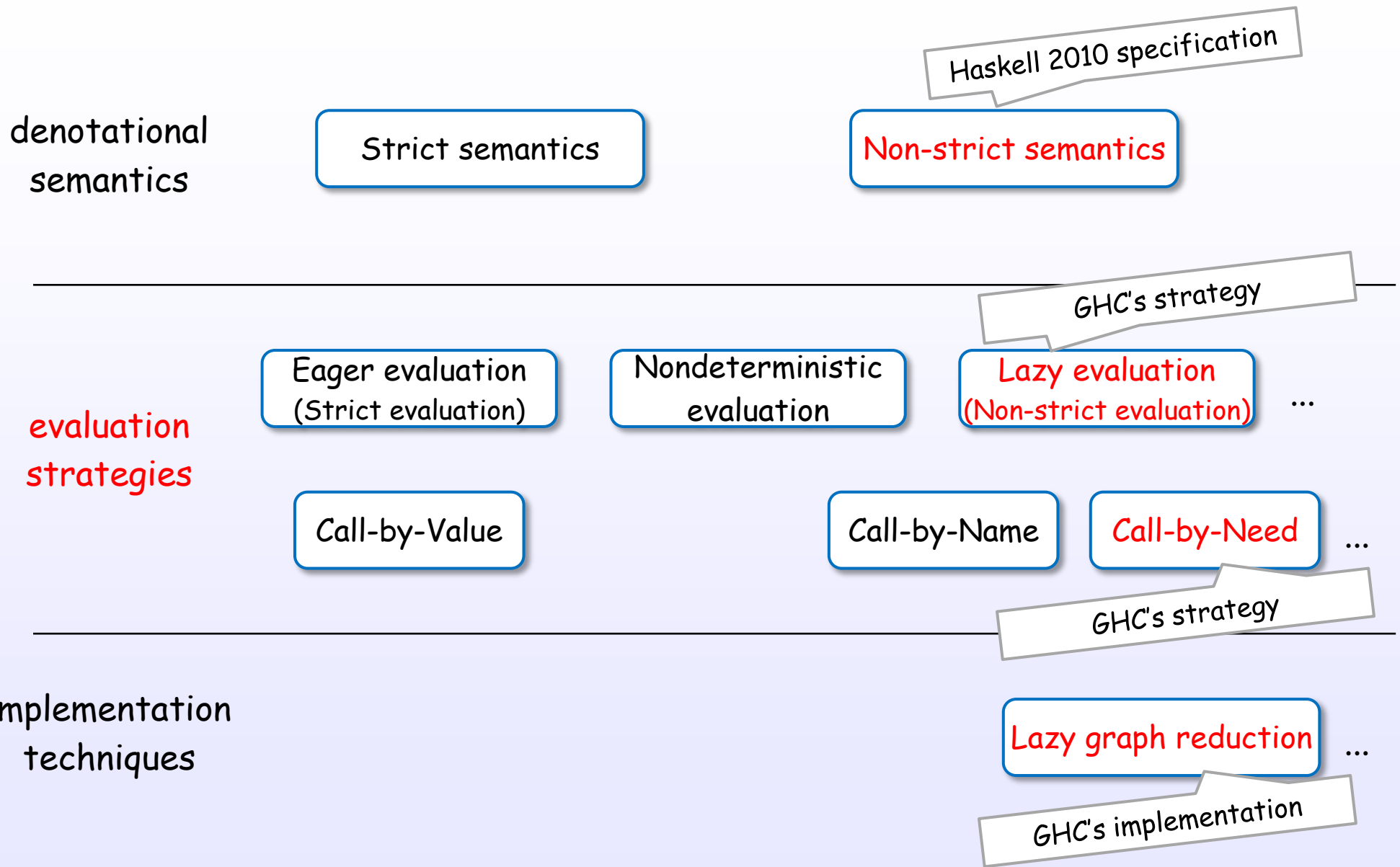
[Bird, Chapter 7]

[Hutton, Chapter 8]

[TAPL, Chapter 3]

References : [1]

# Evaluation layers for GHC's Haskell





# Evaluation strategies and order

$a(b\ c) + d(e\ (f\ g))$

order

[Bird]  
[Hutton]

References : [1]

# Simple example of both evaluations

## Eager evaluation (Strict evaluation)

default  
C, Java, JavaScript,  
Python, OCaml, Scheme, ...

square ( 1 + 2 )



argument  
evaluation  
first

square ( 3 )



3 \* 3



9

## Lazy evaluation (Non-strict evaluation)

default  
Haskell (GHC), ...

square ( 1 + 2 )



apply  
first

( 1 + 2 ) \* ( 1 + 2 )



( 3 ) \* ( 3 )



9

[Bird]  
[Hutton]

# Simple example of both evaluations

Eager evaluation  
(Strict evaluation)

square ( 1 + 2 )



square ( 3 )



3 \* 3



9

argument  
evaluated

Lazy evaluation  
(Non-strict evaluation)

square ( 1 + 2 )



( 1 + 2 ) \* ( 1 + 2 )



( 3 ) \* ( 3 )



9

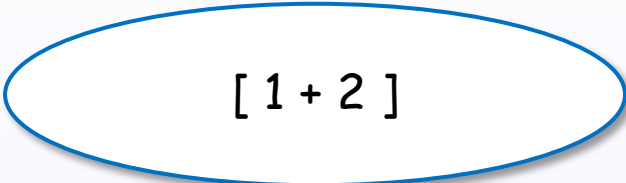
argument  
evaluation  
**delayed !**

[Bird]  
[Hutton]

# Expressions in Haskell

# An expression denotes a value

An expression



[ 1 + 2 ]

[HR2010]

[Bird, Chapter 2]

References : [1]

# There are many expressions in Haskell

## Expressions

Just 5

$1 + 2$

$(1, 2)$

take 5 xs

$[1, 2, 3]$

let  $x = 1$  in  $x + y$

'a'

map f xs

if b then 1 else 0

7

$\forall x \rightarrow x + 1$

$x : xs$

fun arg

case x of  $\_ \rightarrow 0$

$(\forall x \rightarrow x + 1) 3$

do { $x \leftarrow$  get; put x}



categorizing

[HR2010]

[Bird, Chapter 2]

References : [1]

# Expression categories in Haskell

## lambda abstraction

$\forall x \rightarrow x + 1$

## let expression

let  $x = 1$  in  $x + y$

## conditional

if  $b$  then 1 else 0

## case expression

case  $x$  of  $\_ \rightarrow 0$

## do expression

do { $x \leftarrow \text{get}$ ; put  $x$ }

## general constructor, literal and some forms

7

[1, 2, 3]

(1, 2)

'a'

$x : xs$

Just 5

## function application

take 5  $xs$

$(\forall x \rightarrow x + 1)$  3

1 + 2

map  $f$   $xs$

fun arg

[HR2010]  
[Bird, Chapter 2]

# Specification is defined in Haskell 2010 Language Report

## Haskell 2010 Language Report, Chapter 3 Expressions [1]

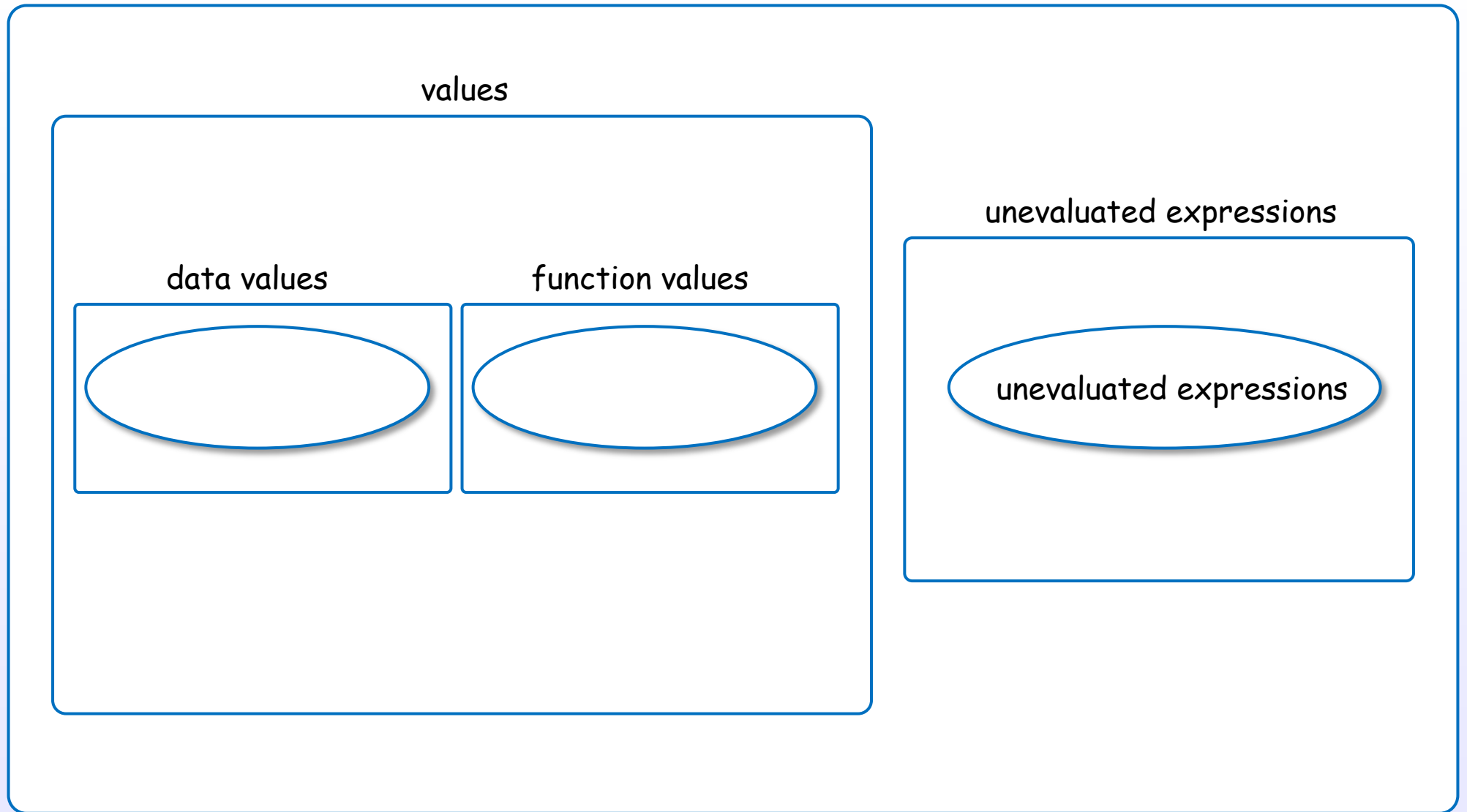
<i>exp</i>	→	<i>infixexp</i> :: [context =>] type   <i>infixexp</i>	(expression type signature)
<i>infixexp</i>	→	<i>lexp</i> <i>qop</i> <i>infixexp</i>   - <i>infixexp</i>   <i>lexp</i>	(infix operator application) (prefix negation)
<i>lexp</i>	→	\ <i>apat</i> <sub>1</sub> ... <i>apat</i> <sub><i>n</i></sub> -> <i>exp</i>   let <i>decls</i> in <i>exp</i>   if <i>exp</i> [ <i>i</i> ] then <i>exp</i> [ <i>i</i> ] else <i>exp</i>   case <i>exp</i> of { <i>alts</i> }   do { <i>stmts</i> }   <i>fexp</i>	(lambda abstraction, $n \geq 1$ ) (let expression) (conditional) (case expression) (do expression)
<i>fexp</i>	→	[ <i>fexp</i> ] <i>aexp</i>	(function application)
<i>aexp</i>	→	<i>qvar</i>   <i>gcon</i>   <i>literal</i>   ( <i>exp</i> )   ( <i>exp</i> <sub>1</sub> , ... , <i>exp</i> <sub><i>k</i></sub> )   [ <i>exp</i> <sub>1</sub> , ... , <i>exp</i> <sub><i>k</i></sub> ]   [ <i>exp</i> <sub>1</sub> [, <i>exp</i> <sub>2</sub> ] .. [ <i>exp</i> <sub>3</sub> ] ]   [ <i>exp</i>   <i>qual</i> <sub>1</sub> , ... , <i>qual</i> <sub><i>n</i></sub> ]   ( <i>infixexp</i> <i>qop</i> )   ( <i>qop</i> { - } <i>infixexp</i> )   <i>qcon</i> { <i>fbind</i> <sub>1</sub> , ... , <i>fbind</i> <sub><i>n</i></sub> }   <i>aexp</i> <sub>{<i>qcon</i>}</sub> { <i>fbind</i> <sub>1</sub> , ... , <i>fbind</i> <sub><i>n</i></sub> }	(variable) (general constructor)  (parenthesized expression) (tuple, $k \geq 2$ ) (list, $k \geq 1$ ) (arithmetic sequence) (list comprehension, $n \geq 1$ ) (left section) (right section)  (labeled construction, $n \geq 0$ ) (labeled update, $n \geq 1$ )



# Classification of expressions

# A value or an unevaluated expression

## Expressions

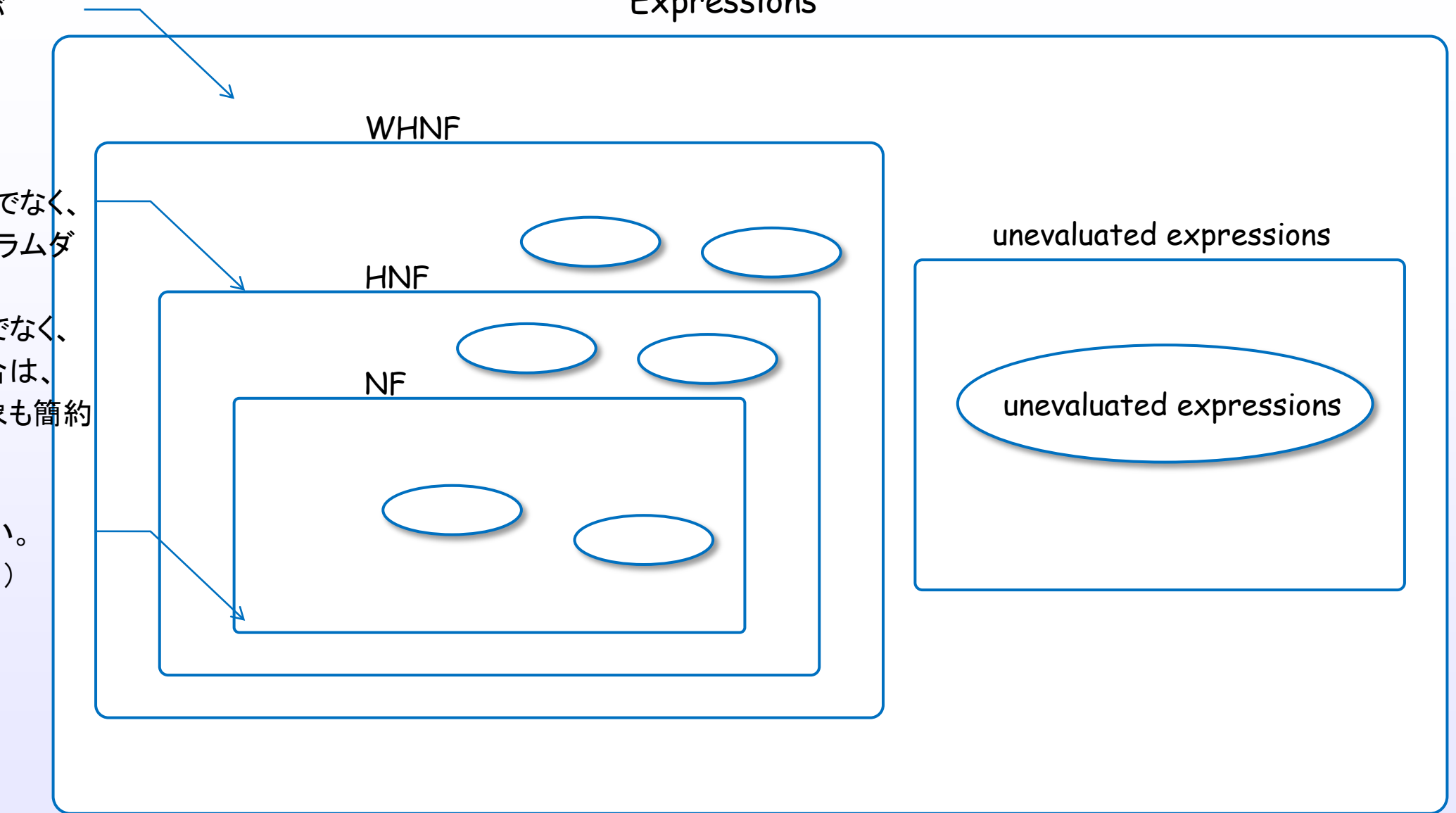


値か否か。値は2種。

[STG]

# evaluation level

## Expressions



値には、評価レベルがある。

[STG]

# 実例との対応付け

[STG]

References : [1]

# Constructor

# Constructor

Constructor is one of the key elements to understand WHNF and lazy evaluation.

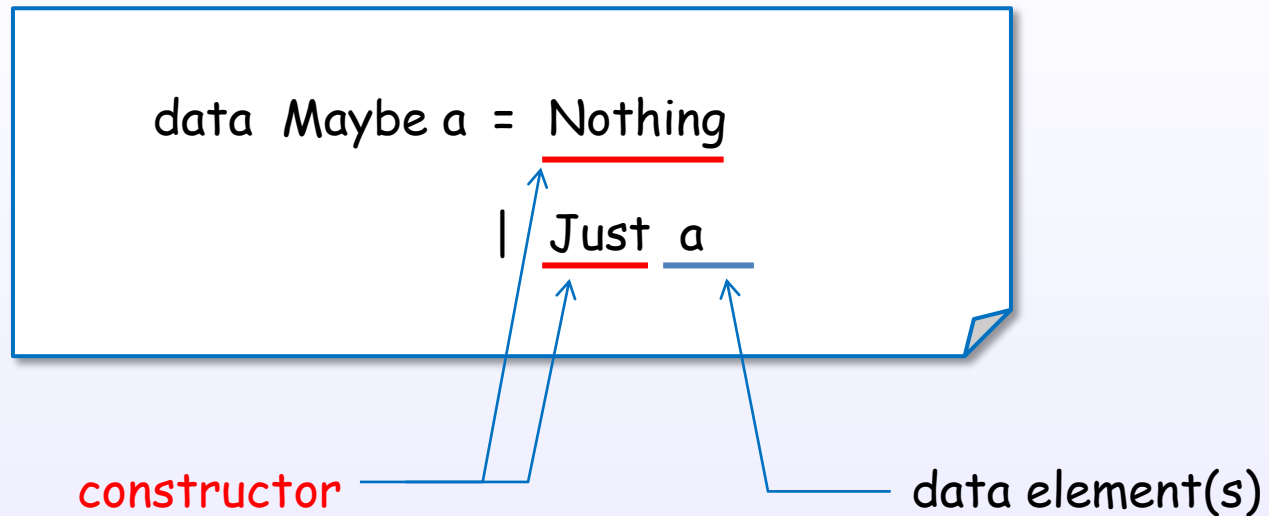
# data文で宣言する代数的データ型とその値

```
data Maybe a = Nothing  
              | Just a
```

Algebraic Data Type

Data **Values**

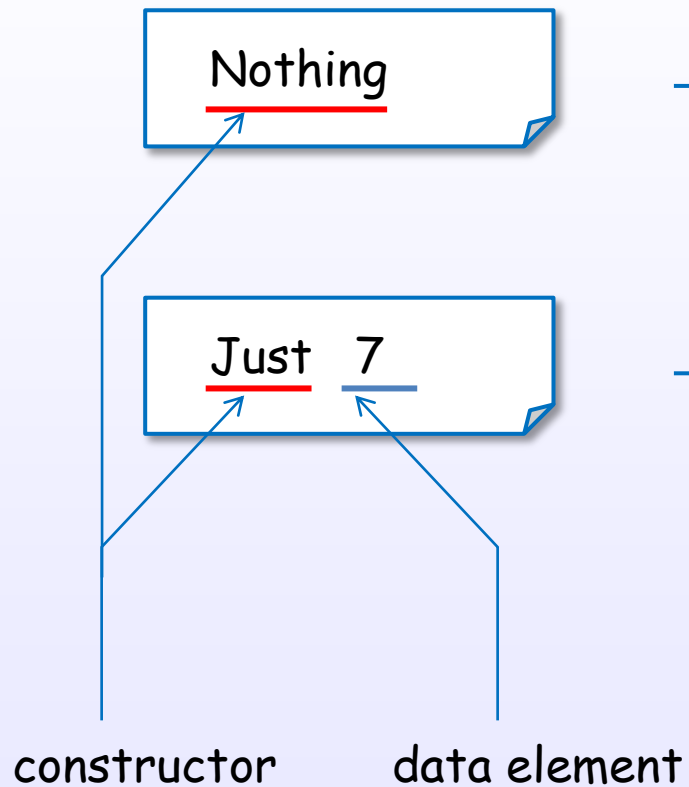
# Constructorはdata文で宣言する代数的データ値



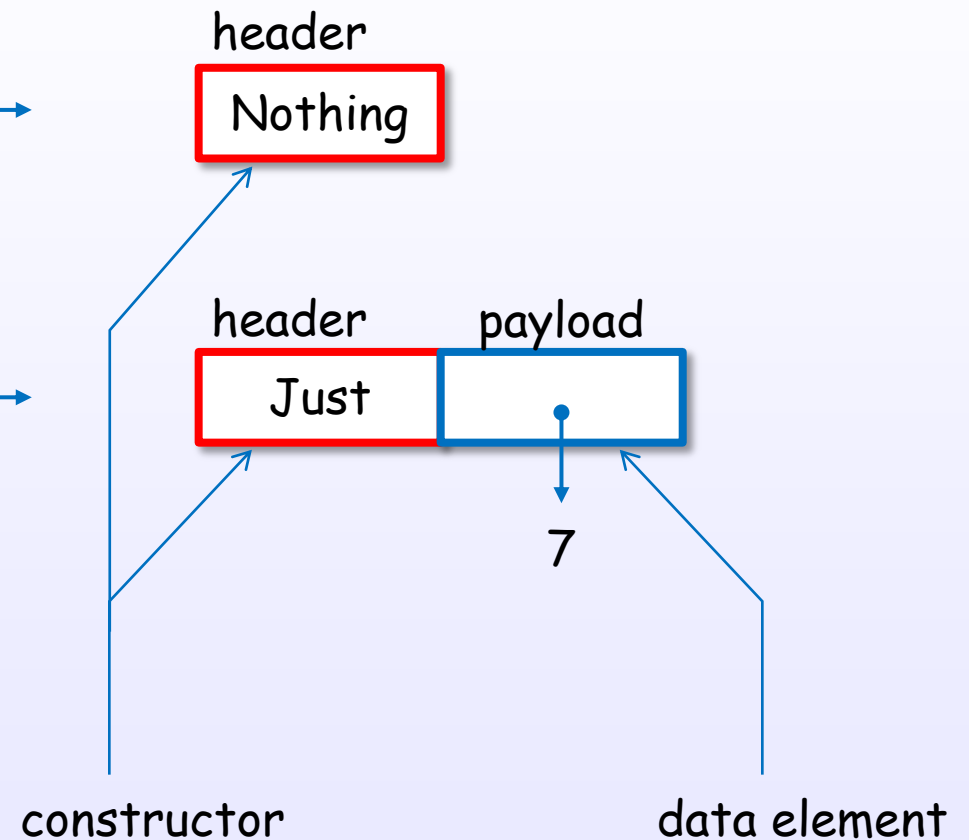


# Constructorの内部表現

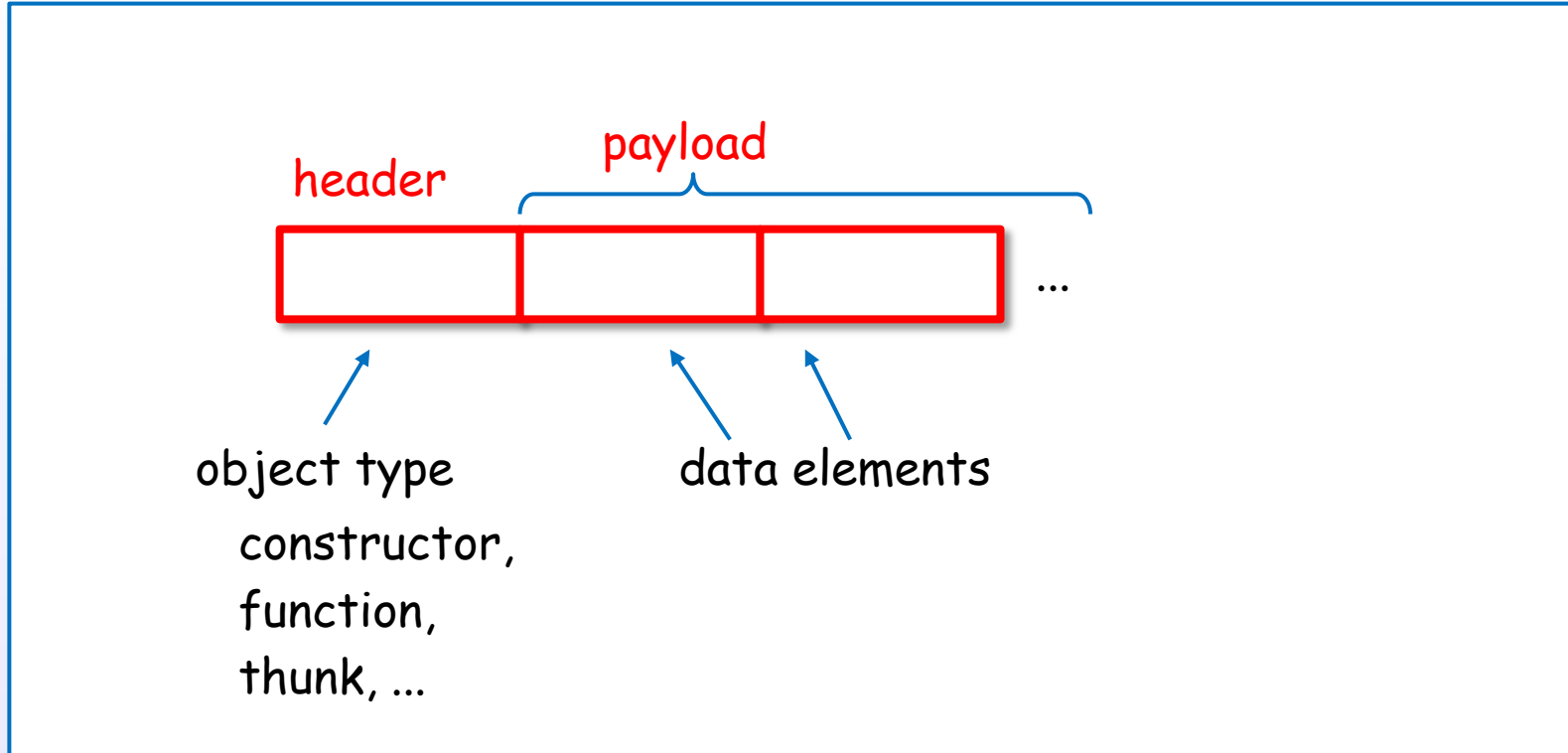
Haskell code



GHC's internal representation  
in heap memory

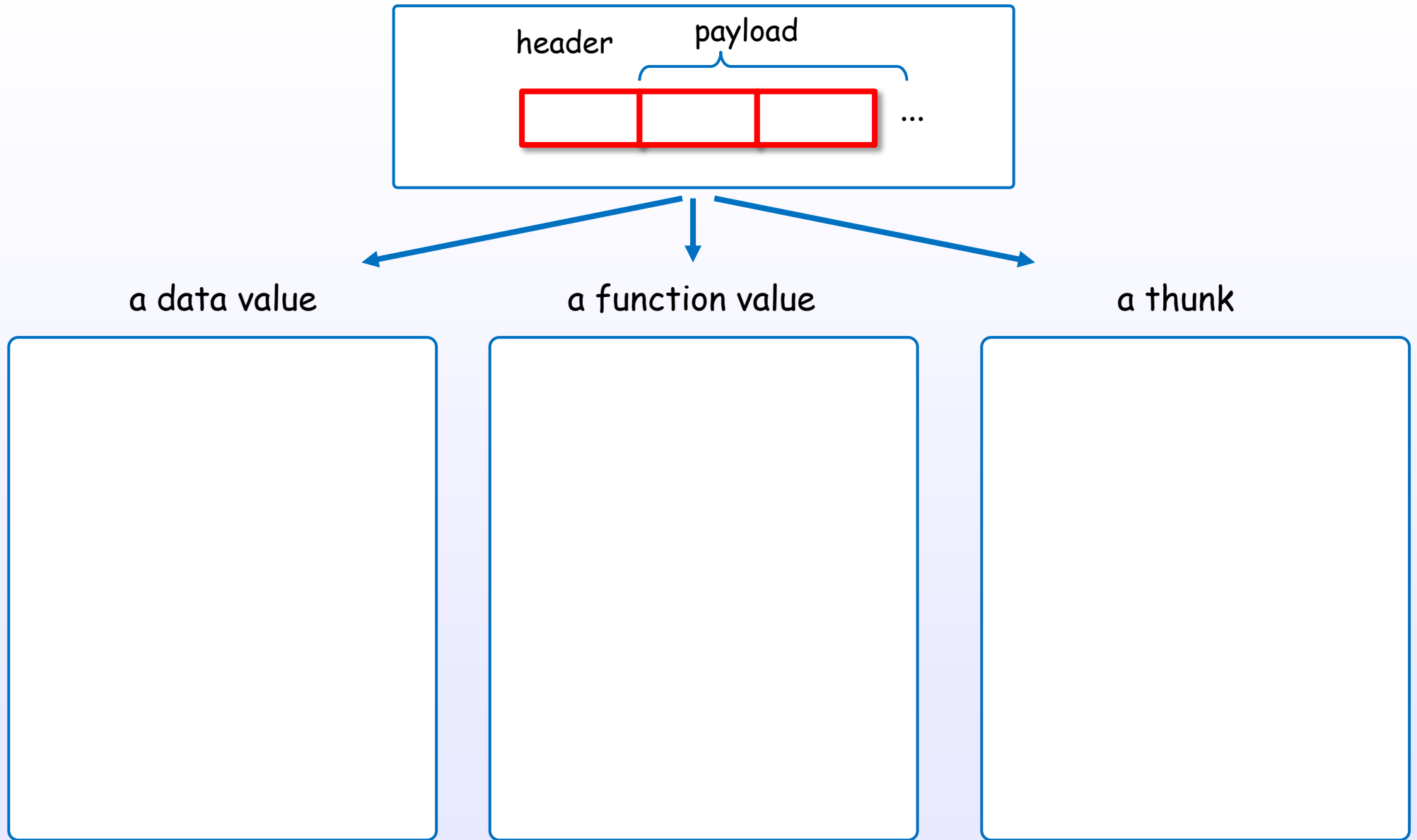


# Constructorは統一内部表現で表現される

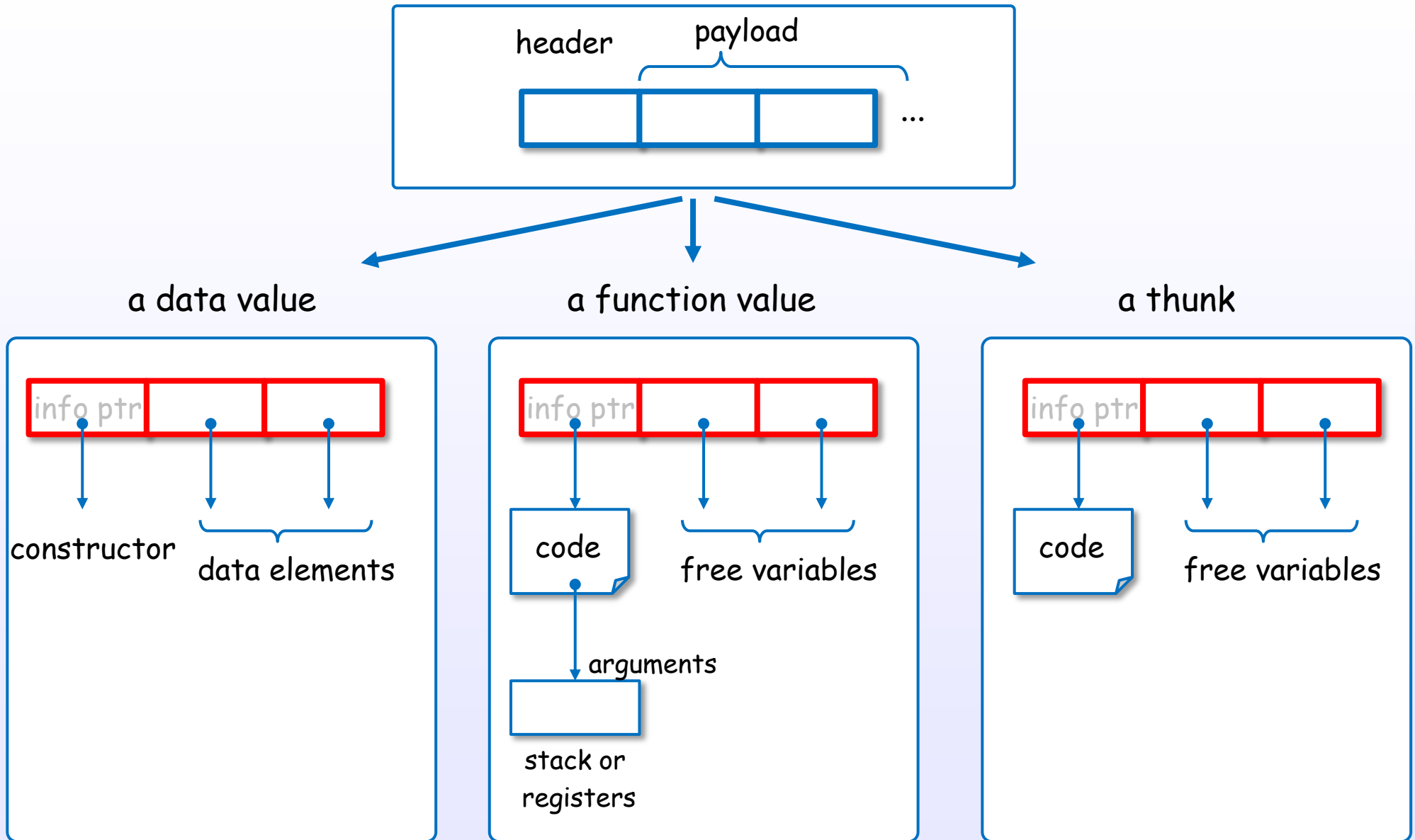


in heap memory, stack, registers or static memory

# 統一内部表現



# 統一内部表現



# いろいろなコンストラクタと内部表現

Haskell code

```
data Bool = False  
          | True
```

```
data Maybe a = Nothing  
              | Just a
```

```
data Either a b = Left a  
                 | Right b
```

GHC's internal representation

False

True

Nothing

Just

a

Left

a

Right

b

# 基本データ型も実はコンストラクタで構成されている

Haskell code

```
data Int = Int# 0#  
        | Int# 1#  
        | ...
```

```
data Char = Char# 'a'#  
          | Char# 'b'#  
          | ...
```

GHC's internal representation

→

Int#	0#
Int#	1#
⋮	

→

Char#	'a'#
Char#	'b'#
⋮	

# リストも実はコンストラクタで構成されている

List

```
[ 1, 2, 3 ]
```

syntactic desugar

```
1 : ( 2 : ( 3 : [] ) )
```

prefix notation by section

```
(:) 1 ( (:) 2 ( (:) 3 [] ) )
```

equivalent data constructor

```
Cons 1 ( Cons 2 ( Cons 3 Nil ) )
```

constructor

# リストも実はコンストラクタで構成されている

List

```
[ 1, 2, 3 ]
```

syntactic desugar

```
1 : ( 2 : ( 3 : [] ) )
```

prefix notation by section

```
(:) 1 ( (:) 2 ( (:) 3 [] ) )
```

equivalent data constructor

```
Cons 1 ( Cons 2 ( Cons 3 Nil ) )
```

*\* pseudo code*

```
data List a = []  
             | : a (List a)
```

```
data List a = Nil  
             | Cons a (List a)
```



# リストも実はコンストラクタで構成されている

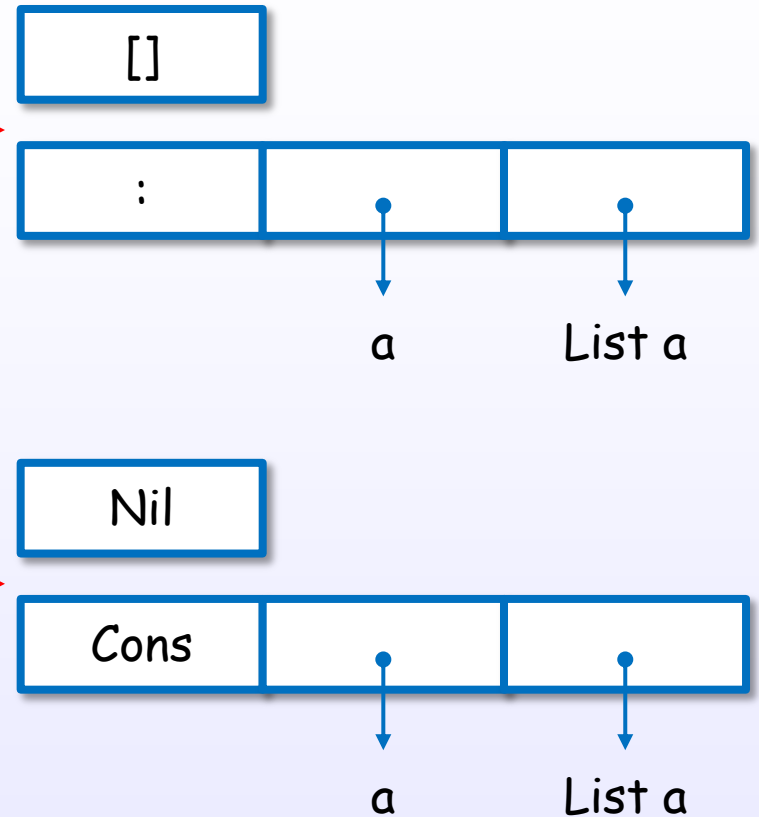
Haskell code

```
data List a = []  
           | : a (List a)
```

↕ equivalent data constructor

```
data List a = Nil  
           | Cons a (List a)
```

GHC's internal representation



# リストも実はコンストラクタで構成されている

Haskell code

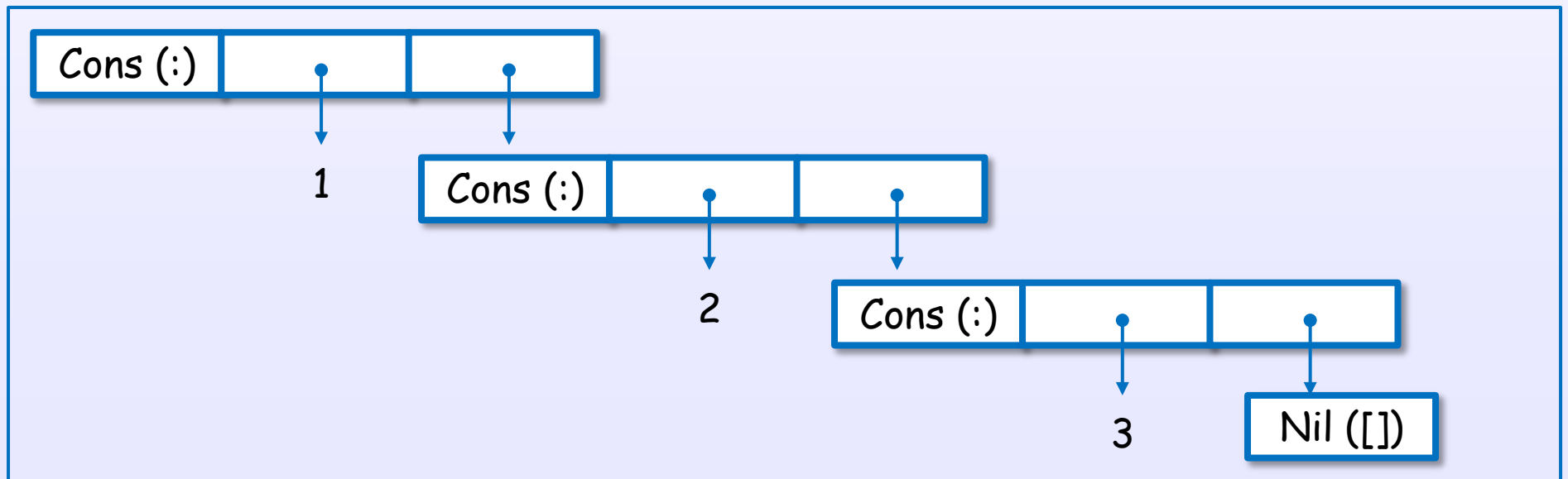
```
[ 1, 2, 3 ]
```

```
1 : ( 2 : ( 3 : [] ) )
```

```
(:) 1 ( (:) 2 ( (:) 3 [] ) )
```

```
Cons 1 ( Cons 2 ( Cons 3 Nil ) )
```

GHC's internal representation



# タプルも実はコンストラクタで構成されている

Tuple (Pair)

( 7 , 8 )

prefix notation by section

(,) 7 8

equivalent data constructor

Pair 7 8

constructor

*\* pseudo code*

data Pair a = (,) a a

data Pair a = Pair a a

# タプルも実はコンストラクタで構成されている

Haskell code

`(7, 8)`



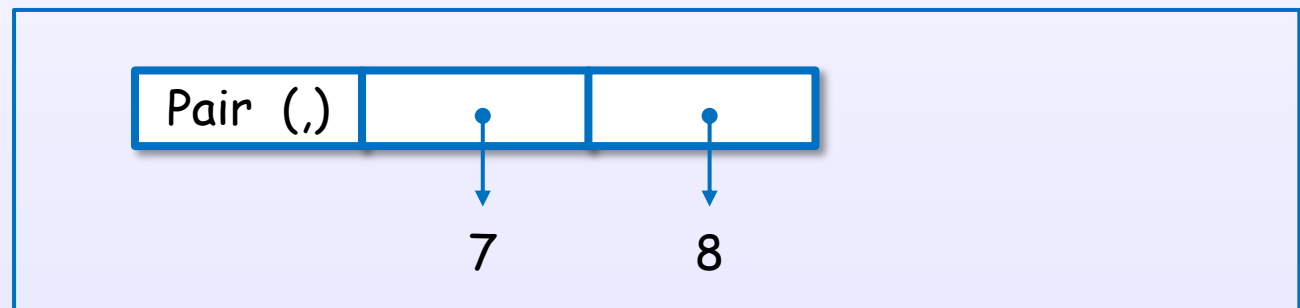
`(,) 7 8`



`Pair 7 8`



GHC's internal representation



Thunk

# Thunk

think  
(unevaluated expression/  
suspended computation)

A thunk is an **unevaluated** expression in heap memory.

# Thunk

An unevaluated expression

take x ys



create/allocate

thunk  
(unevaluated expression/  
suspended computation)

in heap memory

A thunk is created for an unevaluated expression.

# Thunkの内部表現

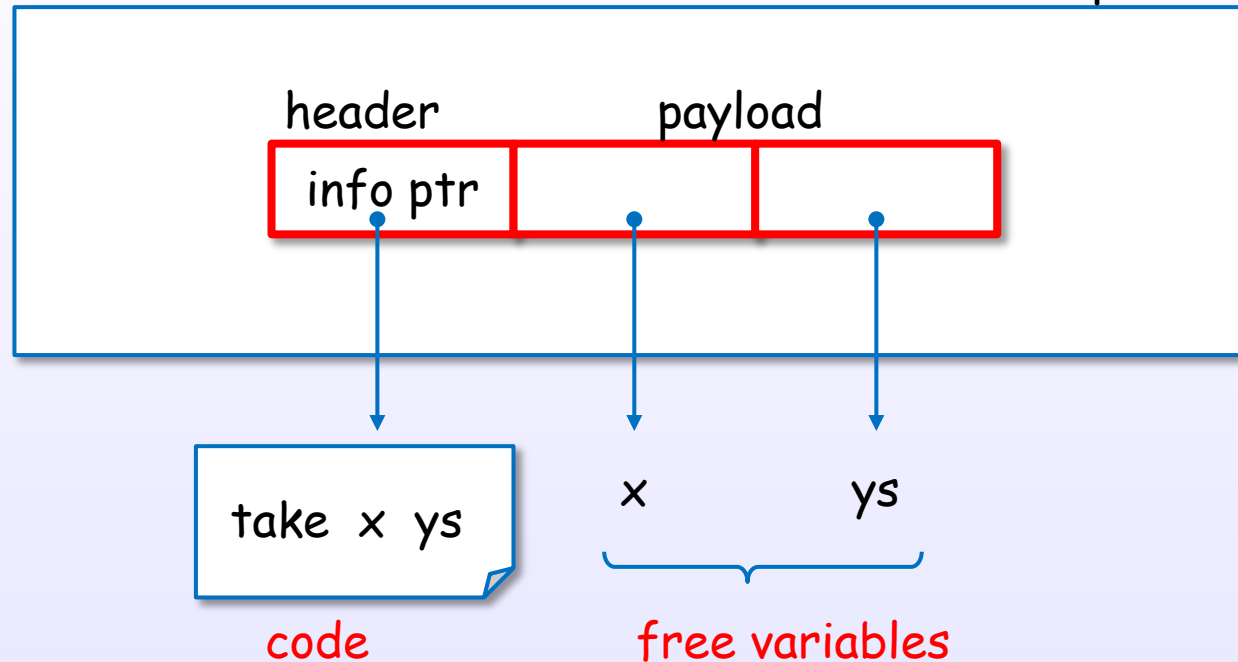
An unevaluated expression

take x ys



thunk

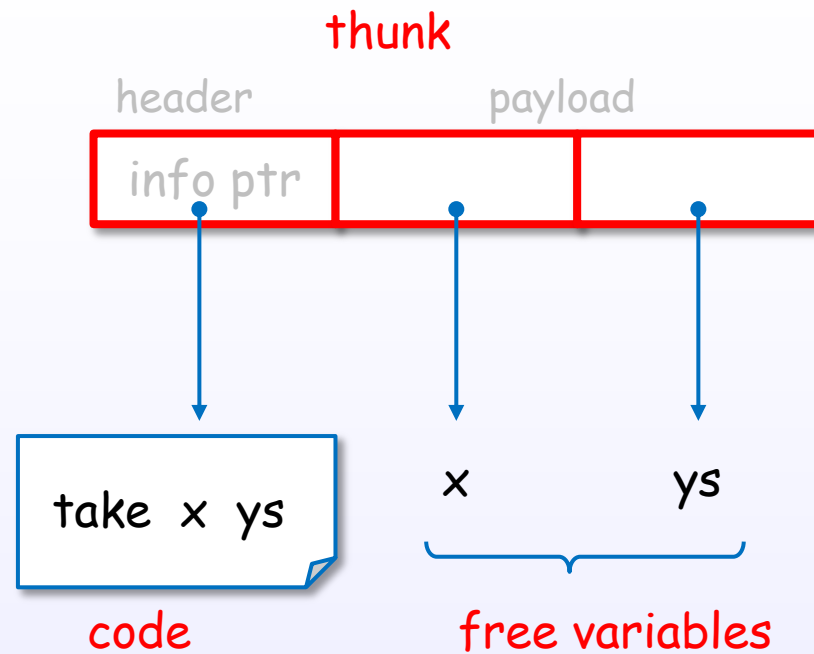
GHC's internal representation



A thunk is represented with header(code) + payload(free variables).

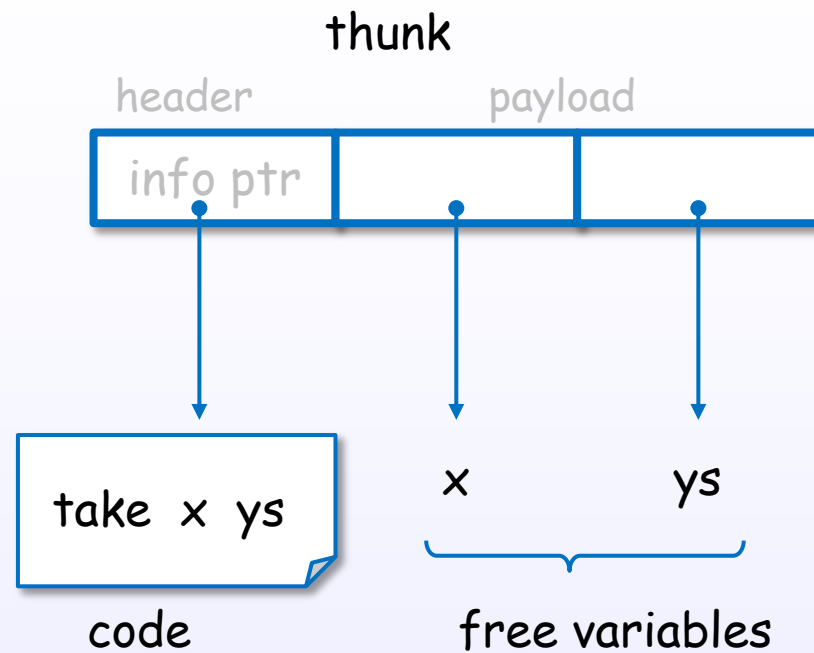


# Thunkは、codeとfree variablesをパッケージ化したもの



A thunk is a package of code + free variables.

# Thunkは、forcing要求により評価される



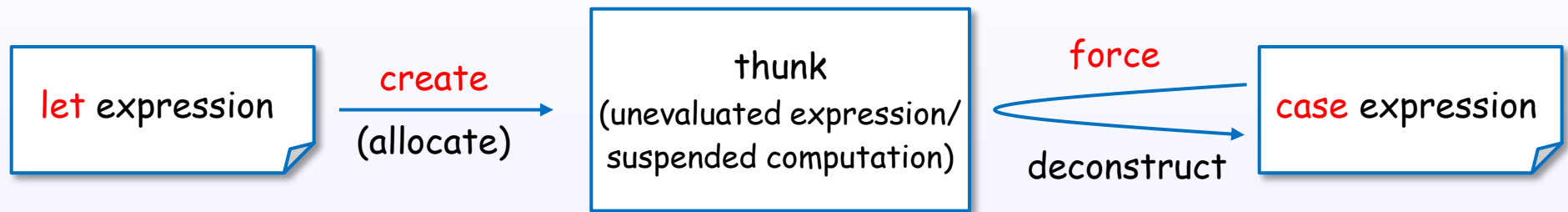
↓ forcing

[ 1, 2, 3 ]

A evaluated expression

let, case expression

# let/case expressions and thunk



A let expression may create a thunk.

A case expression forces and deconstructs the thunk.

# A let expression creates a thunk

let expression

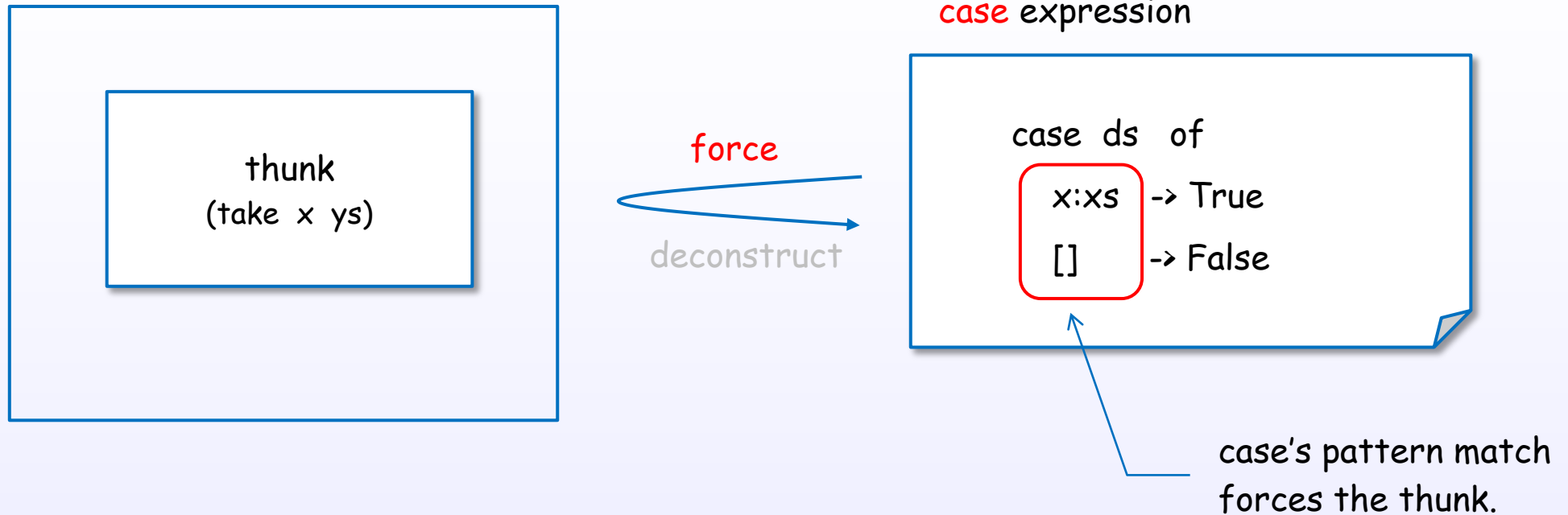
let ds = take x ys

create  
(allocate)

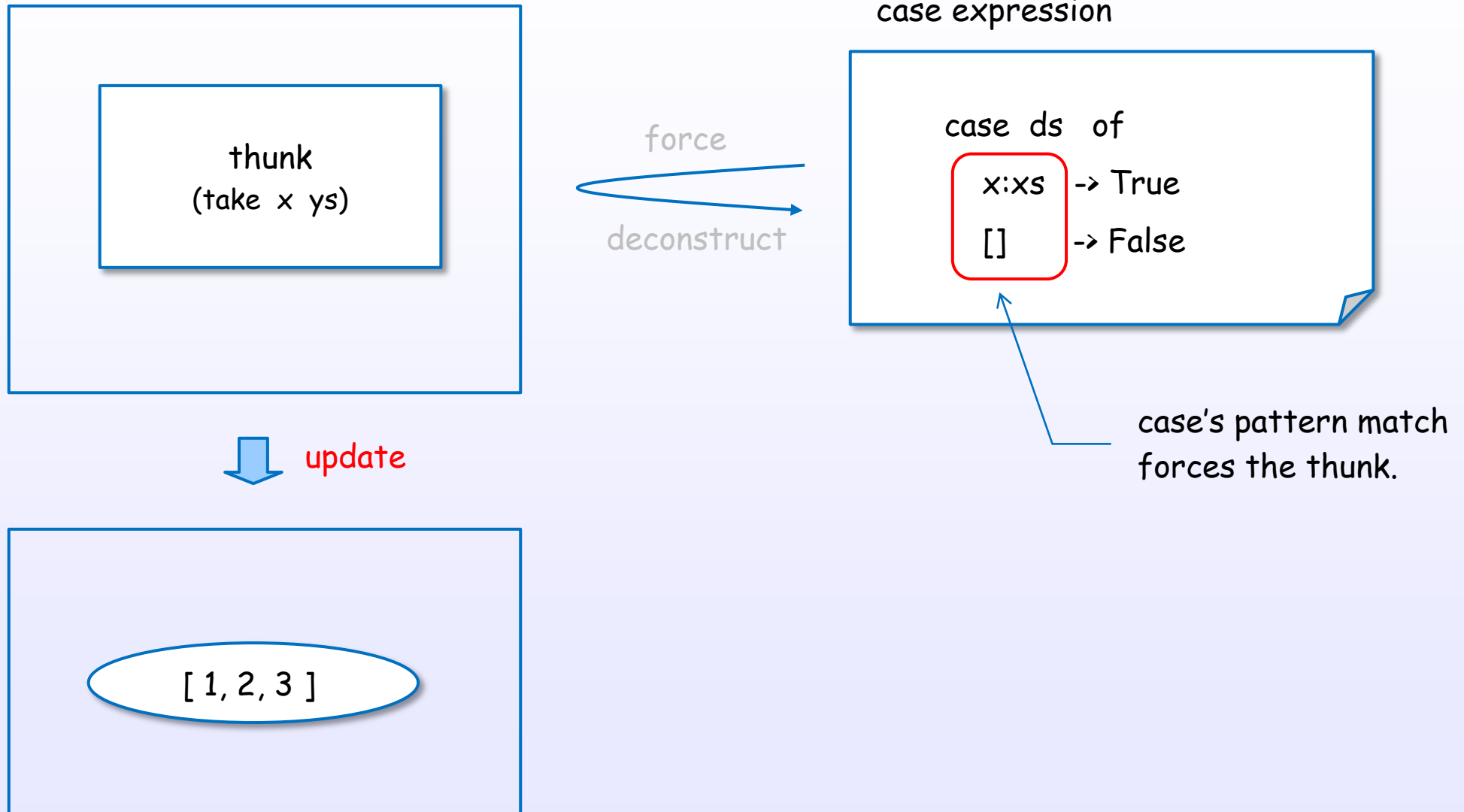
thunk  
(take x ys)

heap memory

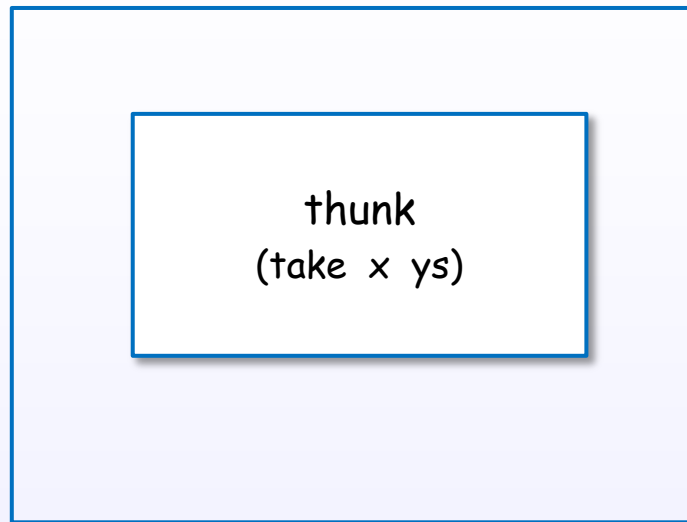
# A case expression forces a thunk



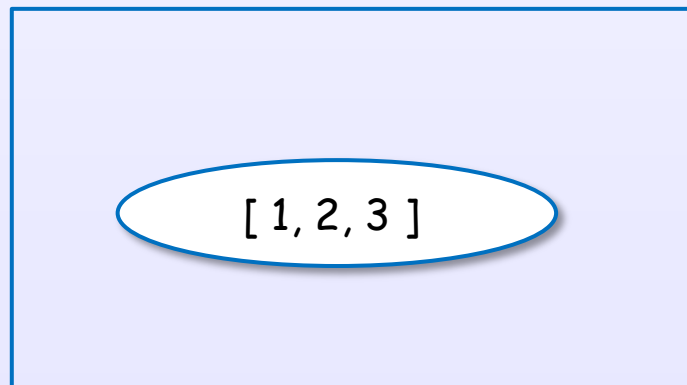
# A case expression forces a thunk



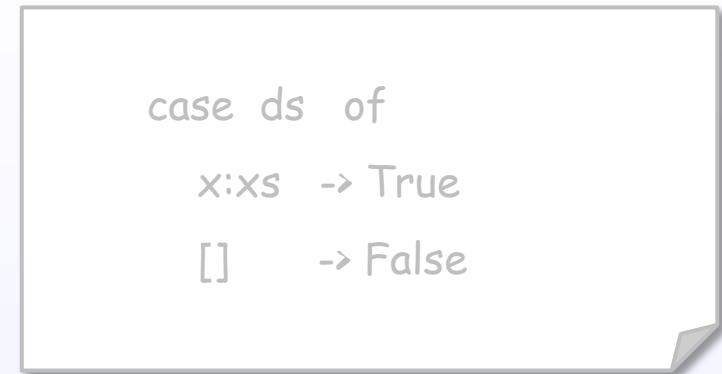
# A case expression forces a thunk



↓ update

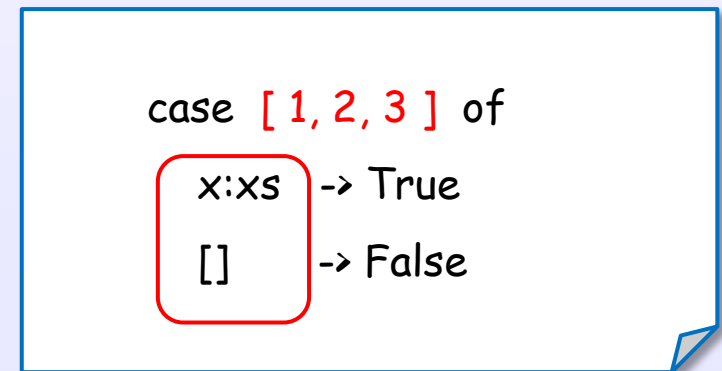


case expression



force  
→  
deconstruct

case expression

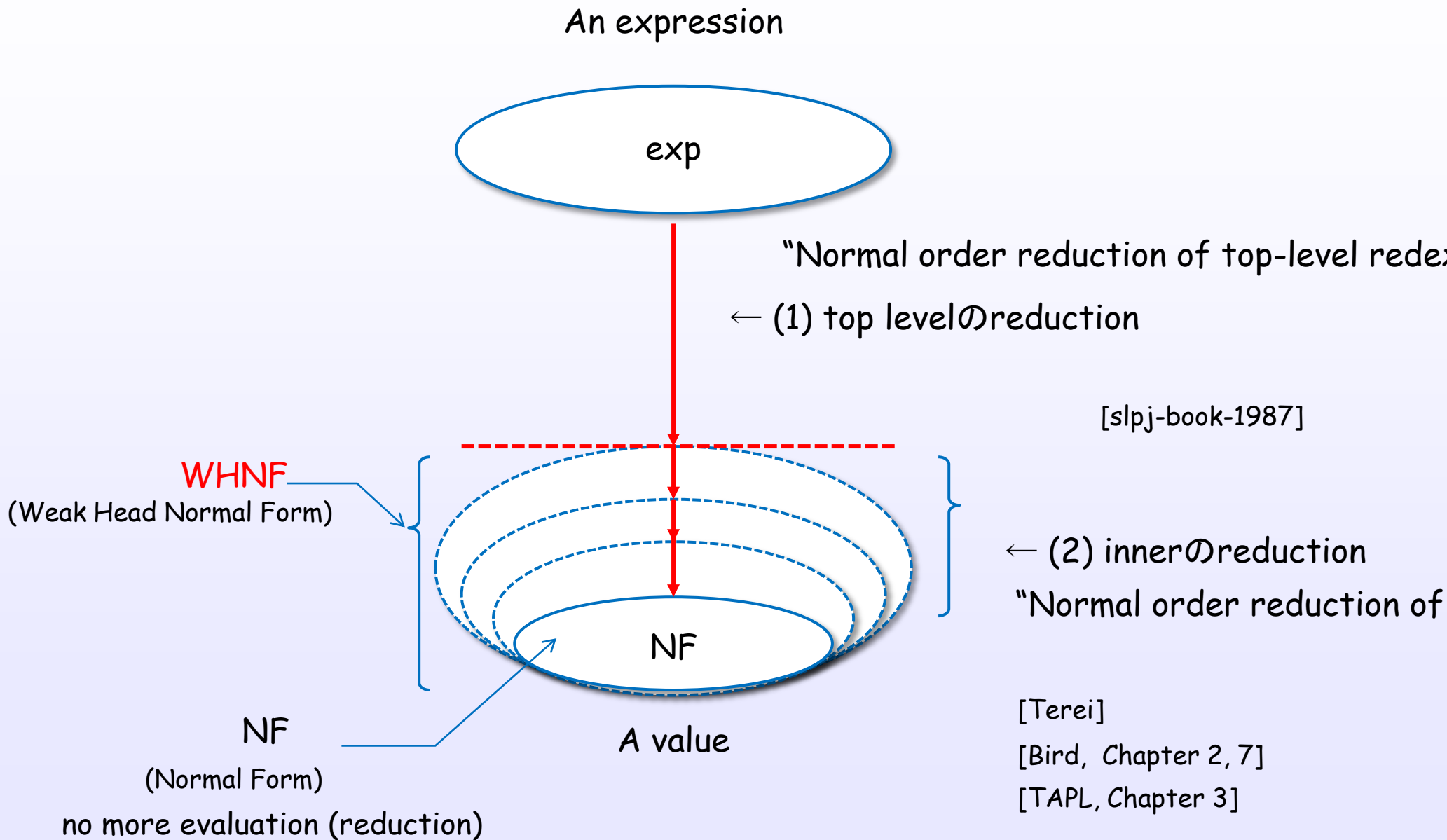


force  
→  
deconstruct



WHNF

# evaluation step (GHC)



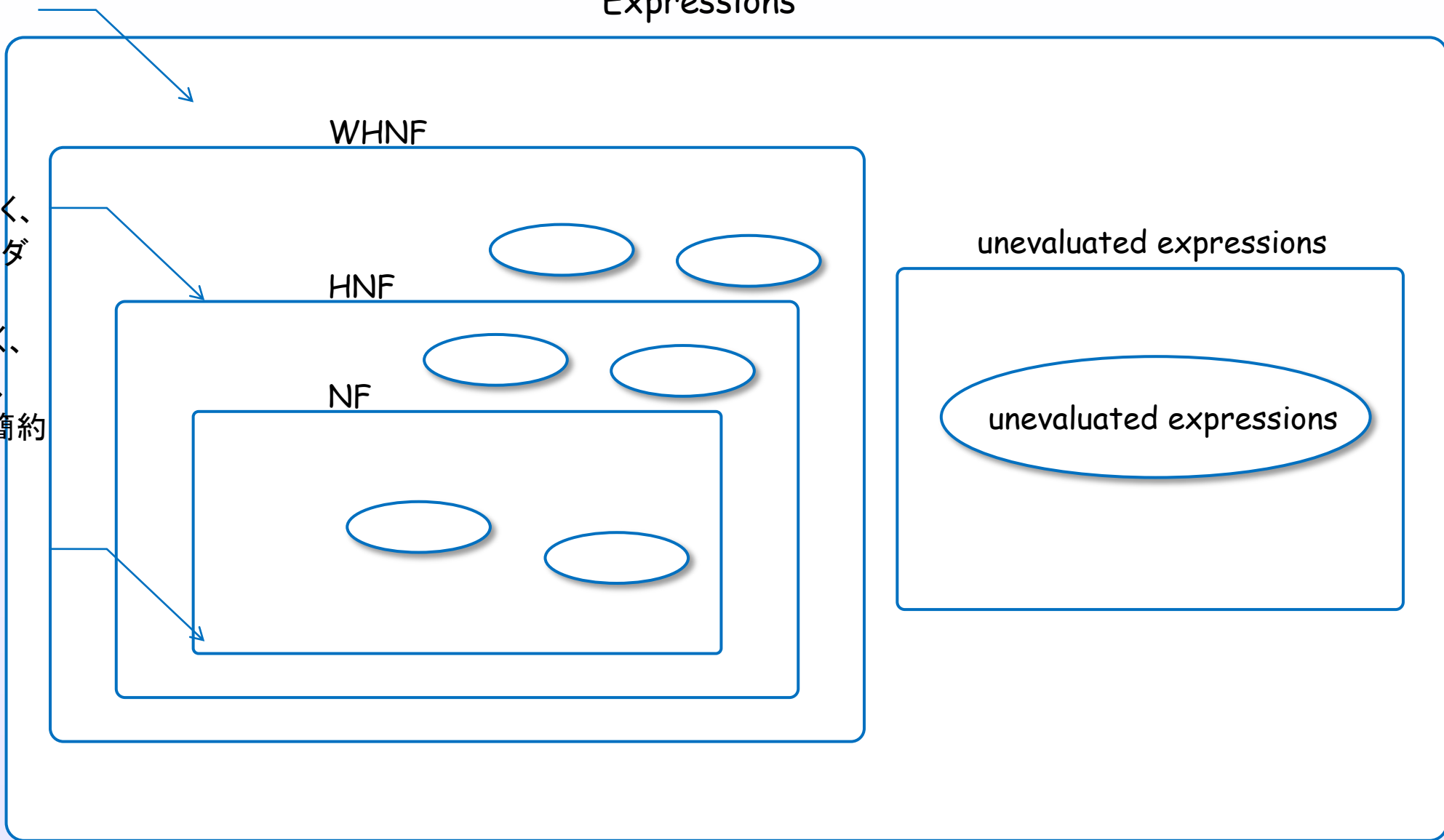
再掲

## evaluation level

Expressions

でなく、  
ラムダ  
でなく、  
は、  
も簡約

い。  
)

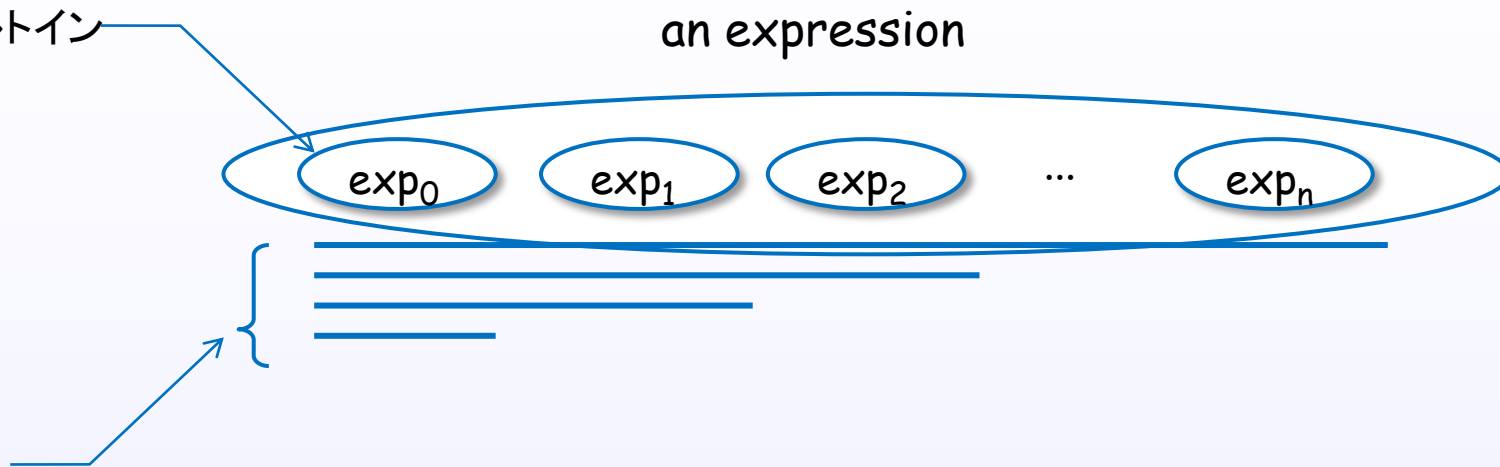


値には、評価レベルがある。

[STG]

# WHNF

データ抽象、ビルトイン



more

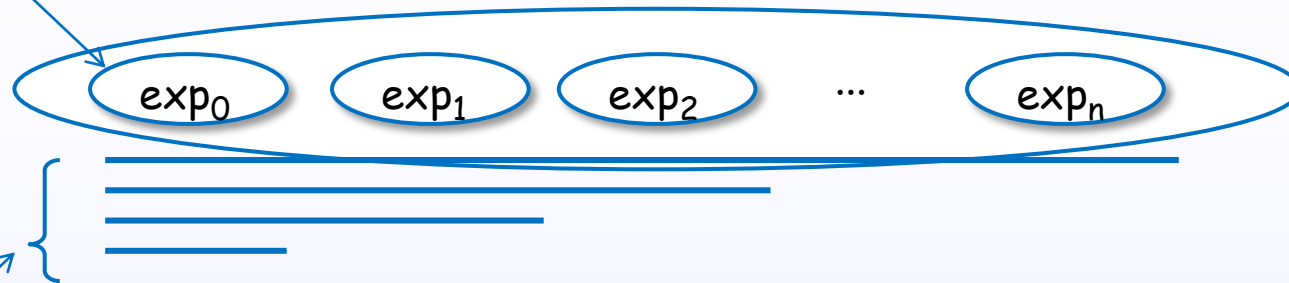
An expression has no top level redex, if it is in WHNF.

[slpj-book-1987]

# Examples of WHNF

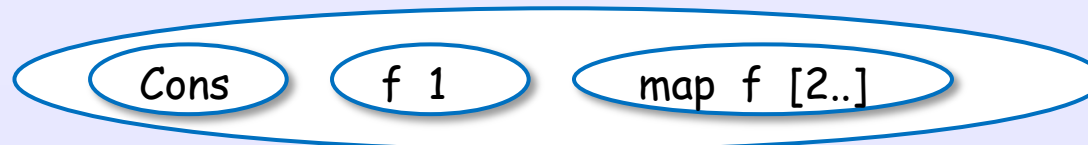
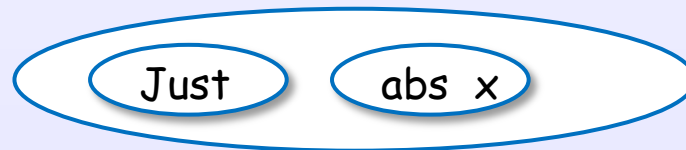
データ抽象、ビルトイン

an expression



Just (abs x)

Cons (f 1) (map f [2..])



[slpj-book-1987]

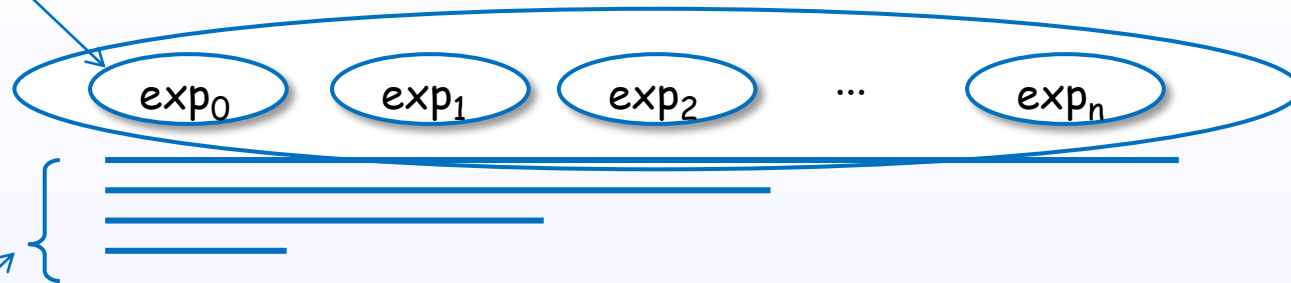
# HNF

データ抽象、ビルトイン

内側(body)が、簡

more

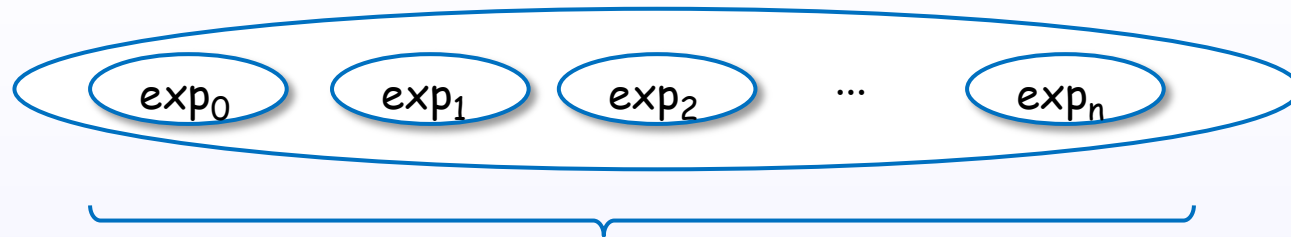
an expression



[slpj-book-1987]

# NF

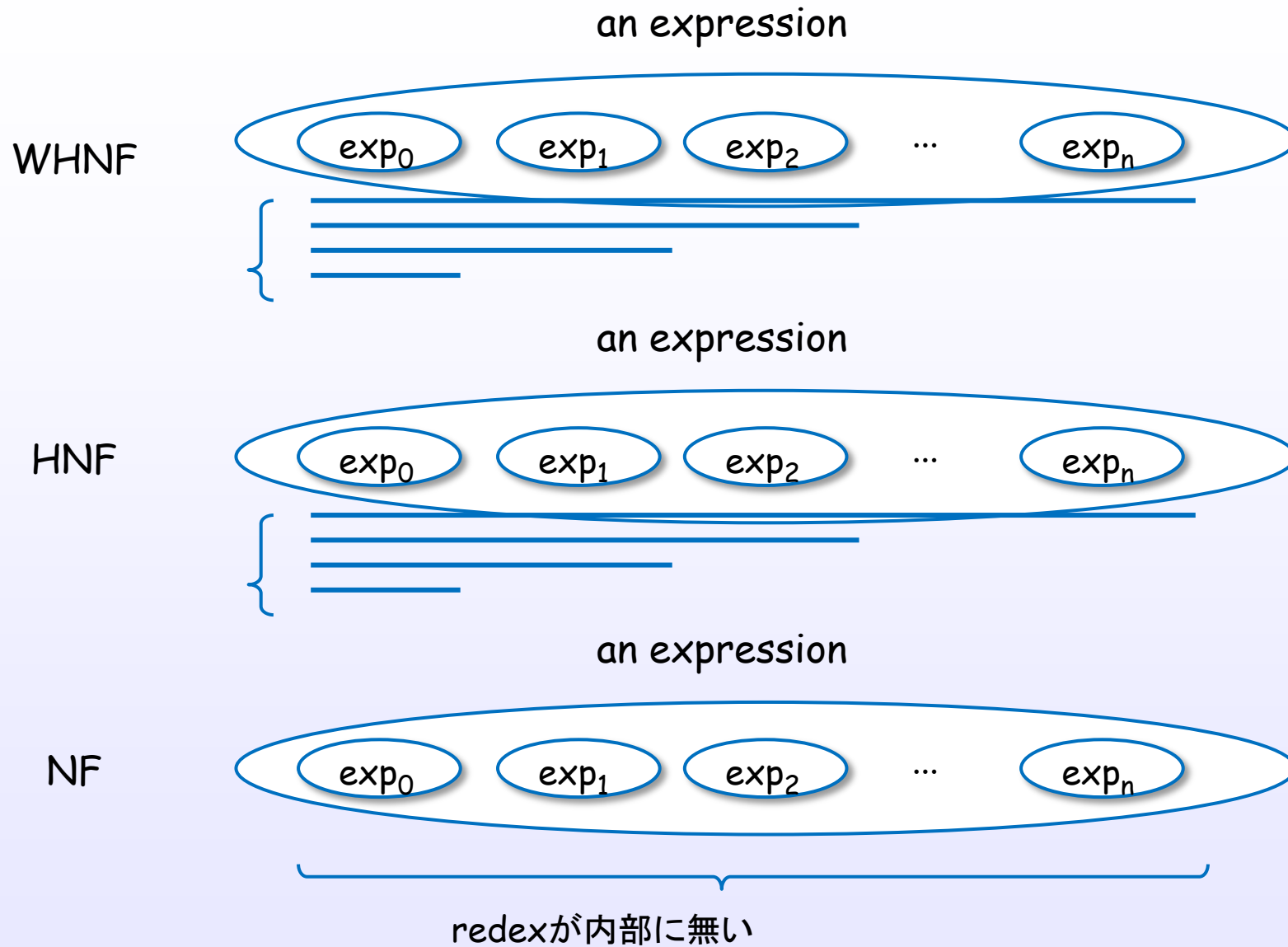
an expression



redexが内部に無い

[slpj-book-1987]

# WHNF, HNF, NF



[slpj-book-1987]

References : [1]



## definition of WHNF and HNF

## The implementation of functional programming languages [19]

### 11.3.1 Weak Head Normal Form

To express this idea precisely we need to introduce a new definition:

### DEFINITION

A lambda expression is in *weak head normal form* (WHNF) if and only if it is of the form

$$F \ E_1 \ E_2 \ \dots \ E_n$$

where  $n \geq 0$ ;

and either  $F$  is a variable or data object

or  $F$  is a lambda abstraction or built-in function

and  $(F \ E_1 \ E_2 \ \dots \ E_m)$  is not a redex for any  $m \leq n$ .

An expression has no *top-level redex* if and only if it is in weak head normal form.

### 11.3.3 Head Normal Form

Head normal form is often confusing and requires some discussion. The content of the `head` field is since for most purposes head normal form is the same as normal form. Nevertheless, we will stick to

### DEFINITION

A lambda expression is in *head normal form* (HNF) if and only if it is of the form

$$\lambda x_1. \lambda x_2. \dots \lambda x_n. (v \ M_1 \ M_2 \ \dots \ M_m)$$

where  $n, m \geq 0$ ;

**v** is a variable ( $x_i$ ), a data object, or a built-in function;

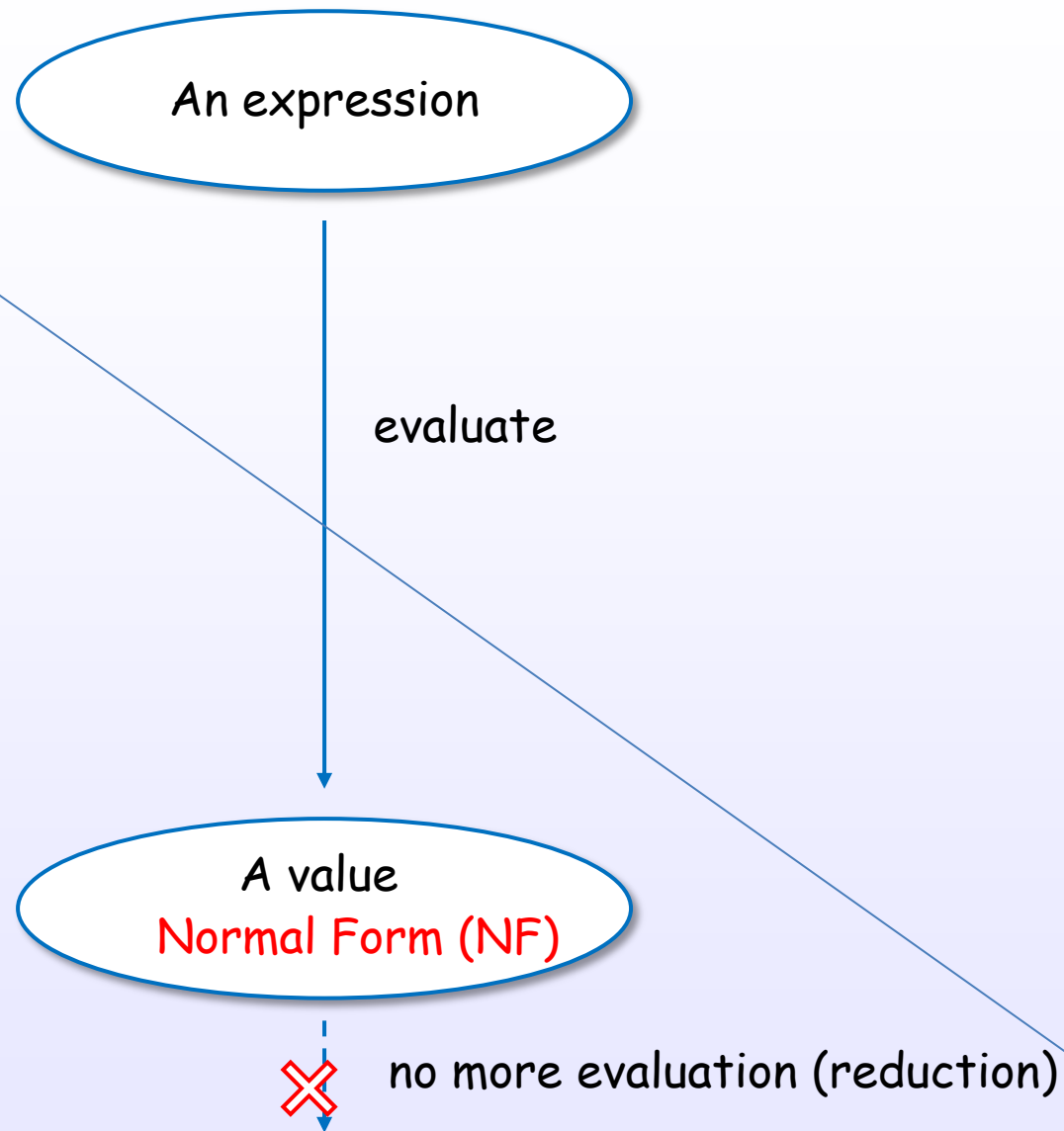
and  $(v \ M_1 \ M_2 \ \dots \ M_p)$  is not a redex for any  $p \leq m$ .

[slpj-book-1987]

# internal representation of WHNF

heap objectイメージ

# Normal form は、これ以上評価できない値



[Terei]

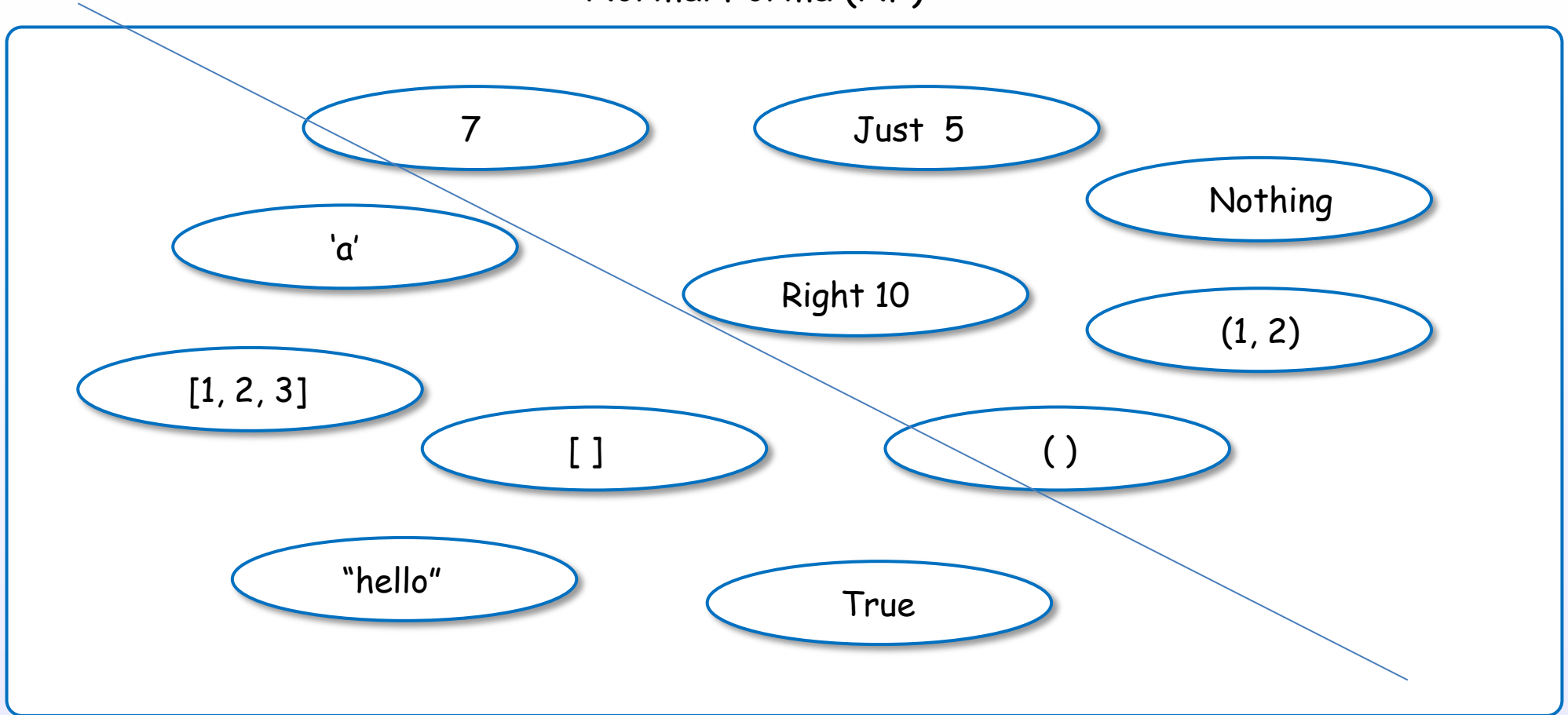
[Bird, Chapter 2, 7]

[TAPL, Chapter 3]

References : [1]

# Examples of normal form (NF)

## Normal Forma (NF)

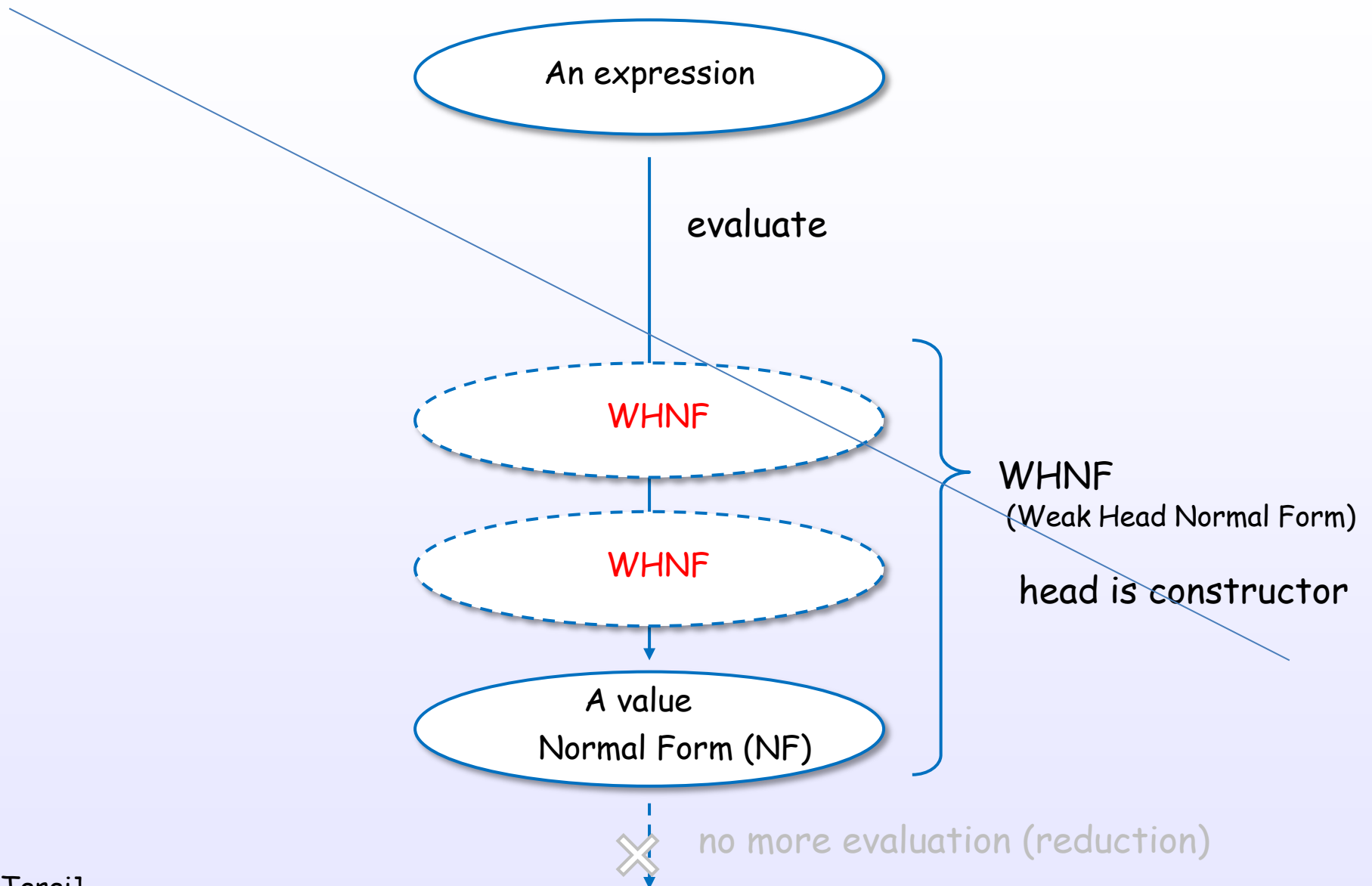


[Terei]

[Bird, Chapter 2, 7]

[TAPL, Chapter 3]

# Weak Head Normal form は、少なくとも先頭が評価された式



[Terei]

[Bird, Chapter 2, 7]

[TAPL, Chapter 3]

References : [1]

# Examples of weak head normal form (WHNF)

## Weak Head Normal Form (WHNF)

Just (head [1..])

Right (fun arg)

$1 : [2..]$

Cons 1 [2..]

$5 : \text{map } f \text{ } xs$

Cons 5 (map f xs)

$(f \ 5, \ g \ 7)$

Pair (f 5) (g 7)

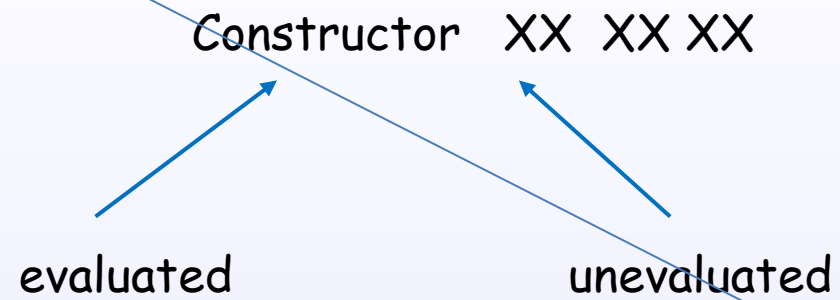
[Terei]

[Bird, Chapter 2, 7]

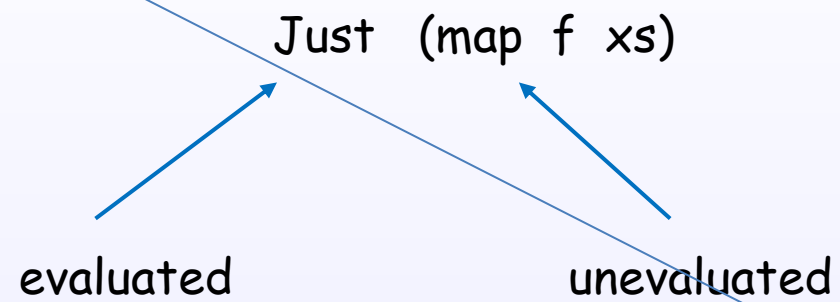
[TAPL, Chapter 3]

References : [1]

# WHNF



# WHNF





前頁の、heap objectイメージ

[4]

normal form:

an expression without an redexes

head normal form:

an expression where the top level (head) is neither a redex NOR  
a lambda abstraction with a reducible body

weak head normal form:

an expression where the top level (head) isn't a redex

[Terei]

[4]

evaluation strategies:

call-by-value: arguments evaluated before function entered (copied)

call-by-name: arguments passed unevaluated

call-by-need: arguments passed unevaluated but an expression is only evaluated once (sharing)

no-strict evaluation Vs. lazy evaluation:

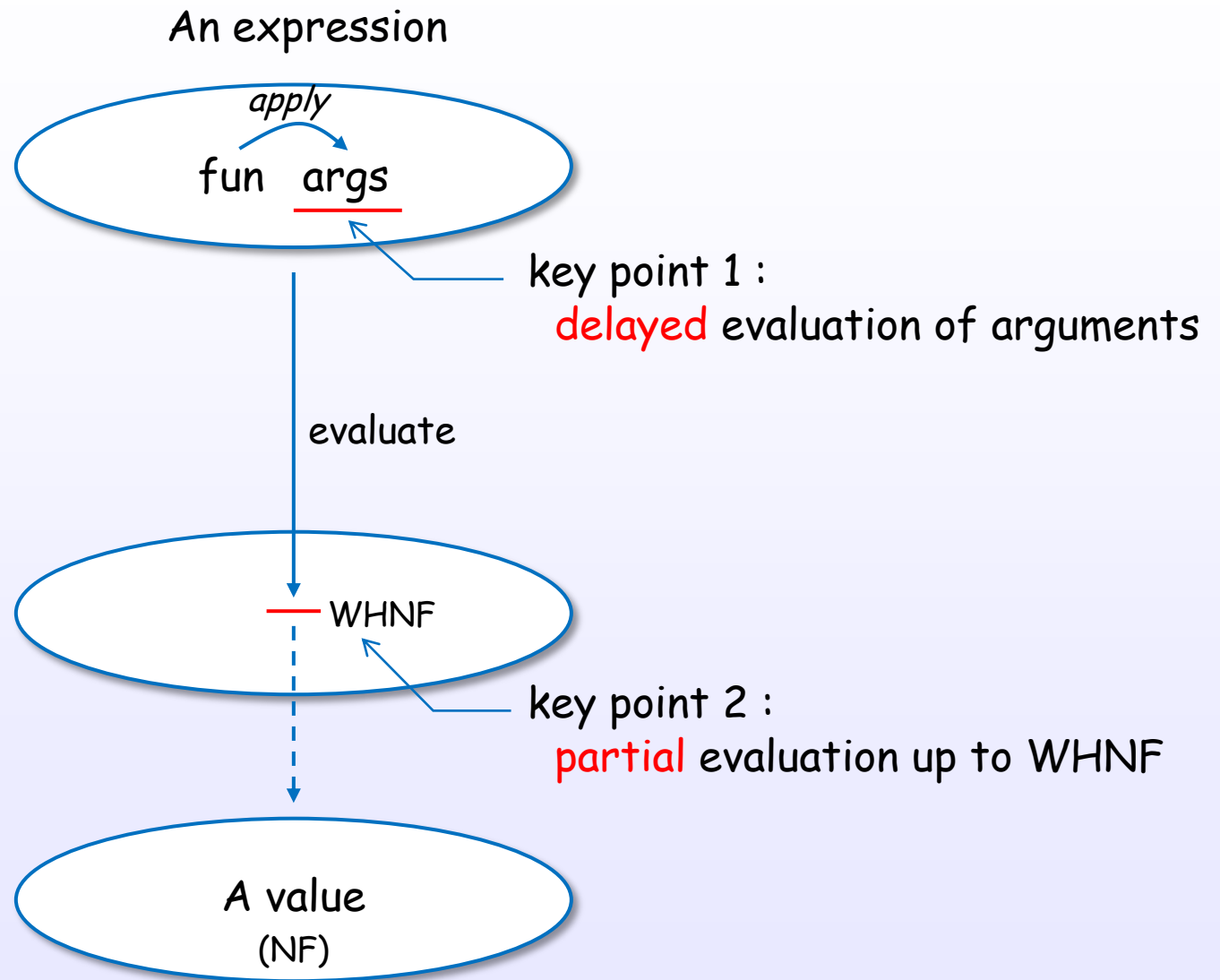
non-strict: Includes both call-by-name and call-by-need, general term for evaluation strategies that don't evaluate arguments before entering a function

lazy evaluation: Specific type of non-strict evaluation. Uses call-by-need (for sharing).

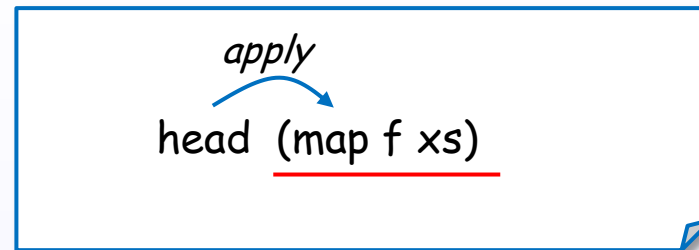
[Terei]

# Evaluation in Haskell (GHC)

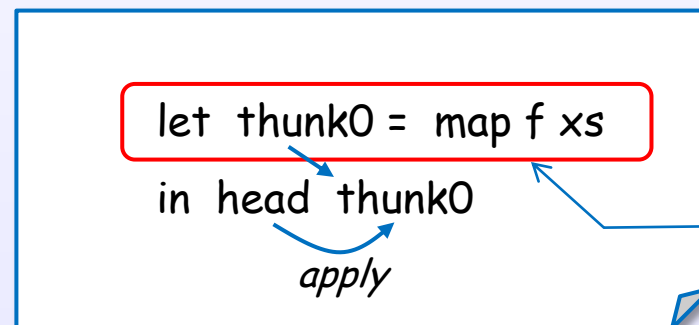
# Key concept of Haskell's lazy evaluation



# key point 1 : delayed evaluation of arguments



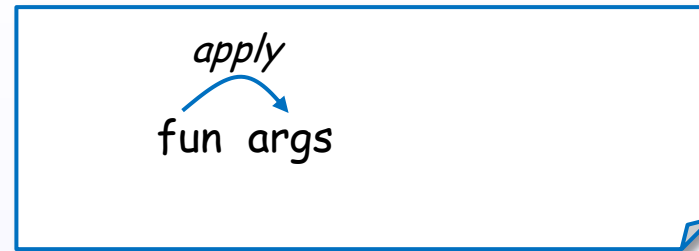
↓ internal transformation by GHC



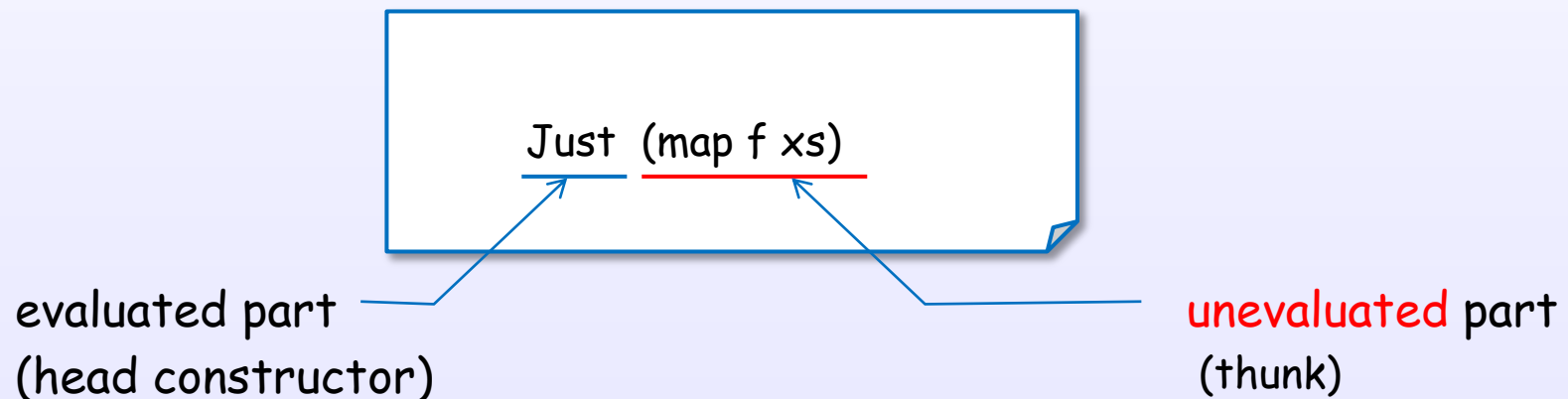
create a thunk  
in heap memory

GHC implements lazy evaluation using the thunk.  
Evaluation of arguments is delayed with the thunk.

## key point 2 : partial evaluation up to WHNF



↓ evaluation up to WHNF



GHC can partially evaluate a expression.  
Constructor can hold an unevaluated expression (a thunk).

# Pattern match

[CIS194]



## Examples of evaluation steps

# Example of repeat

repeat 1



1 : repeat 1



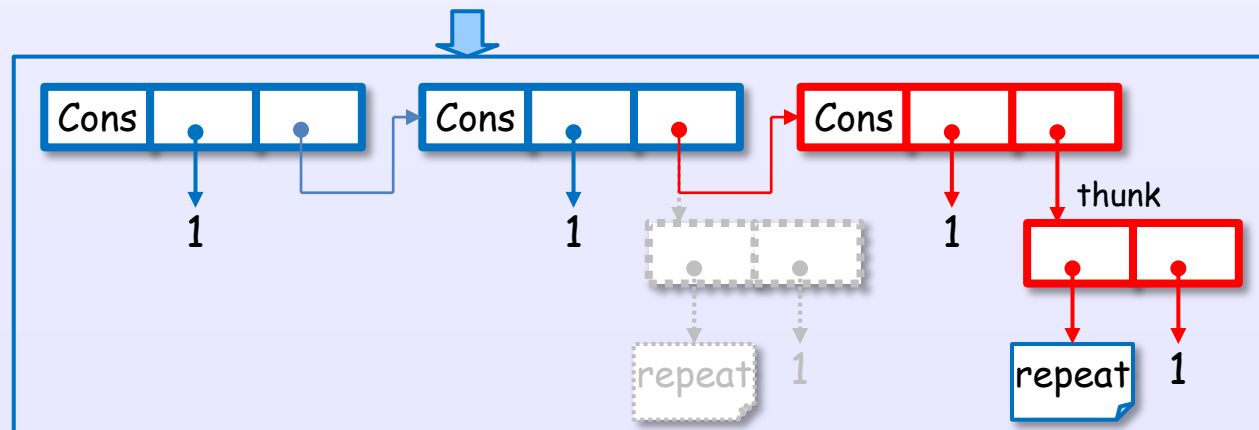
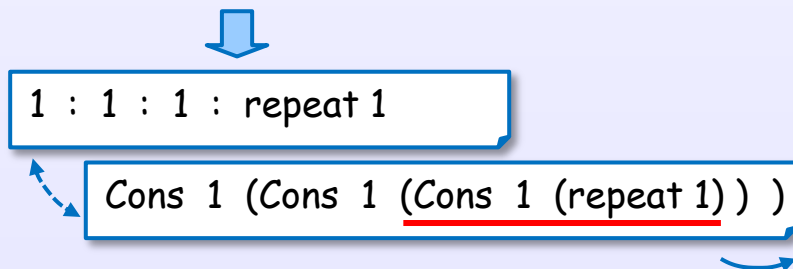
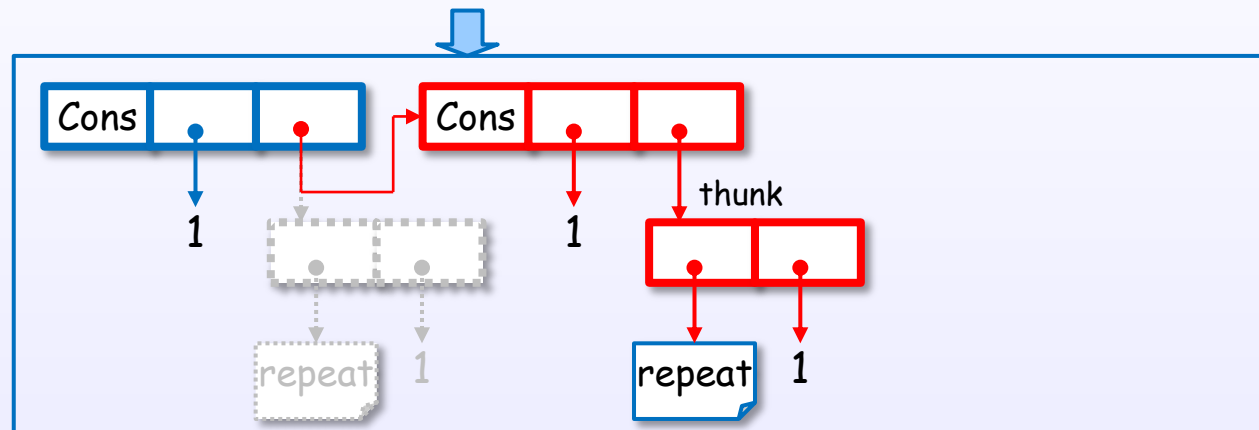
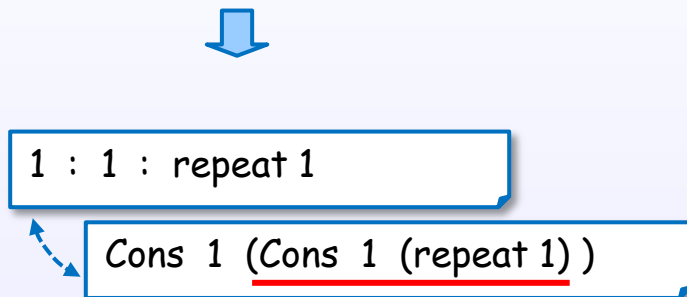
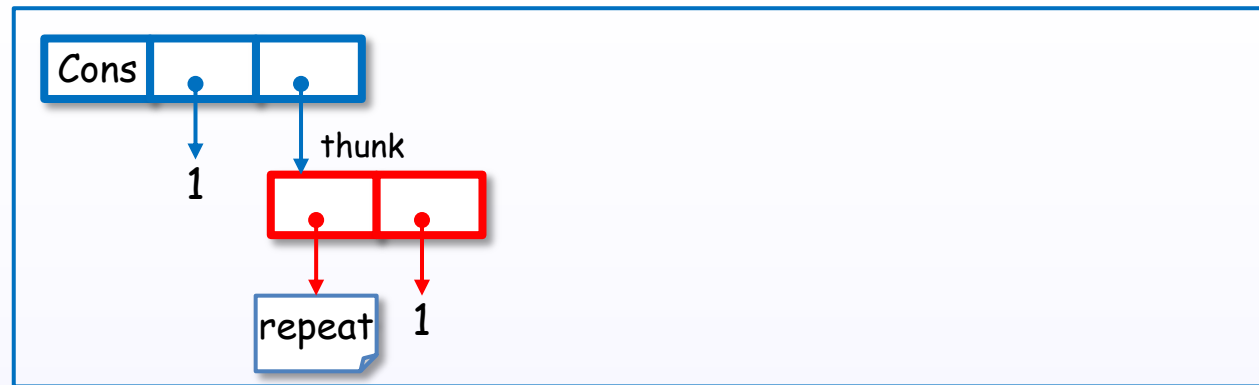
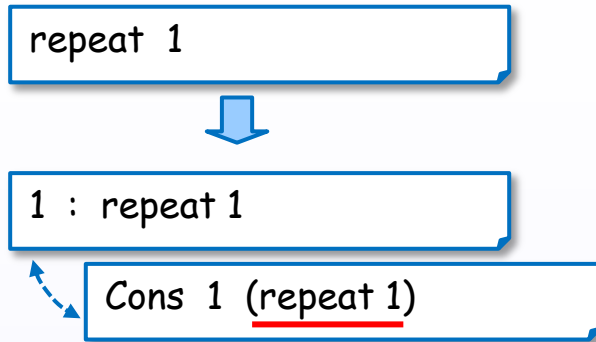
1 : 1 : repeat 1



1 : 1 : 1 : repeat 1



# Example of repeat



# Example of map

```
map f [1, 2, 3]
```



```
f 1 : map f [2, 3]
```



```
f 1 : f 2 : map f [3]
```



```
f 1 : f 2 : f 3
```



...

# Example of map

map f [1, 2, 3]



f 1 : map f [2, 3]

Cons (f 1) (map f [2, 3])



f 1 : f 2 : map f [3]

Cons (f 1) (Cons (f 2) (map f [3]))

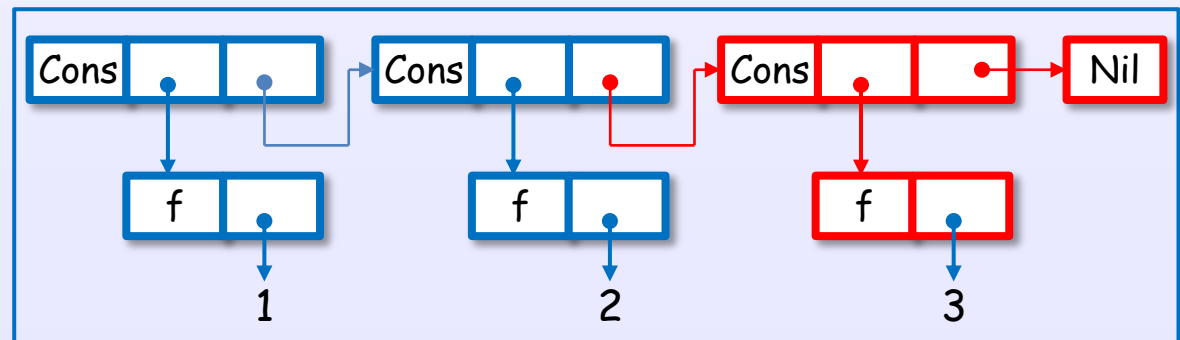
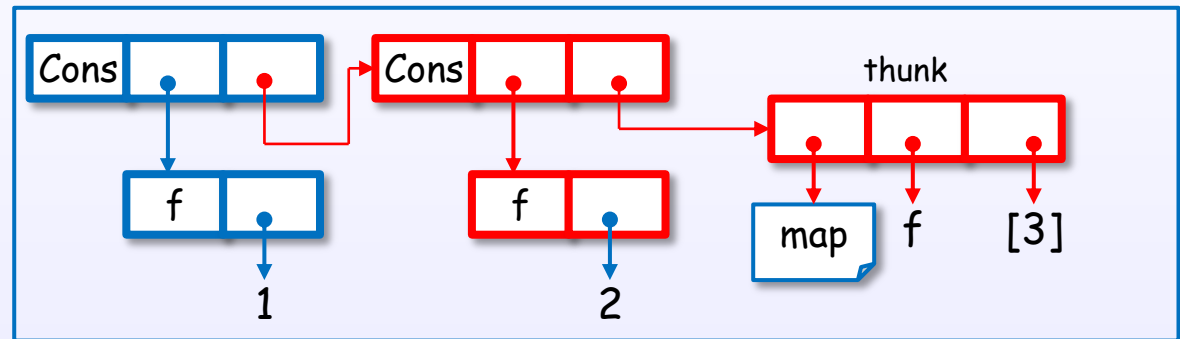
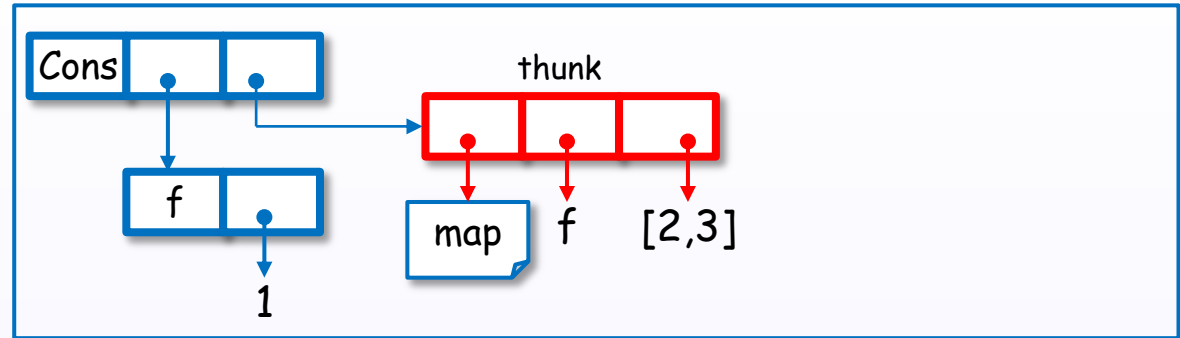


f 1 : f 2 : f 3

Cons (f 1) (Cons (f 2) (Cons (f 3) Nil))



...



...

# Example of foldl (non-strict)

`foldl (+) 0 [1 .. 100]`



`foldl (+) (0 + 1) [2 .. 100]`



`foldl (+) ((0 + 1) + 2) [3 .. 100]`



`foldl (+) ((((0 + 1) + 2) + 3) [4 .. 100]`



...

# Example of foldl (non-strict)

```
foldl (+) 0 [1 .. 100]
```



```
foldl (+) (0 + 1) [2 .. 100]
```

```
let thunk1 = (0 + 1)  
in foldl (+) thunk1 [2 .. 100]
```



```
foldl (+) ((0 + 1) + 2) [3 .. 100]
```

```
let thunk2 = (thunk1 + 2)  
in foldl (+) thunk2 [3 .. 100]
```



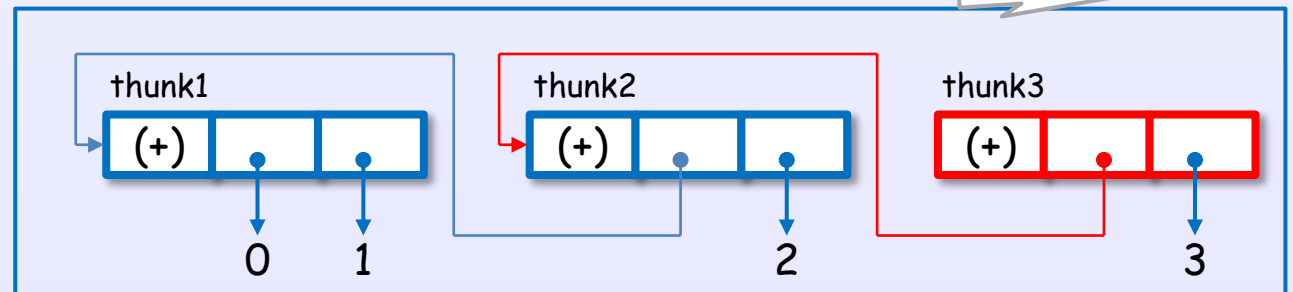
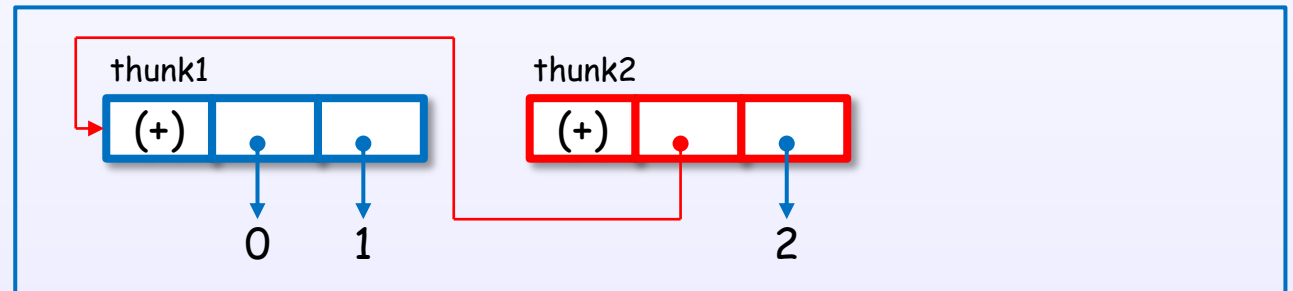
```
foldl (+) (((0 + 1) + 2) + 3) [4 .. 100]
```

```
let thunk3 = (thunk2 + 3)  
in foldl (+) thunk3 [4 .. 100]
```



...

heap memory



## Example of foldl' (strict)

foldl' (+) 0 [1 .. 100]



foldl' (+) (0 + 1) [2 .. 100]



foldl' (+) (1 + 2) [3 .. 100]



foldl' (+) (3 + 3) [4 .. 100]



...



# Example of foldl' (strict)

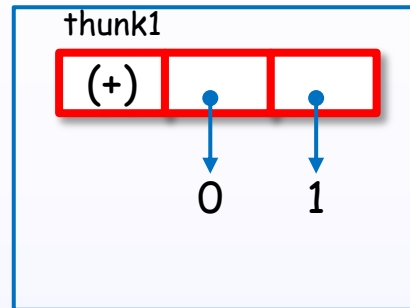
foldl' (+) 0 [1 .. 100]



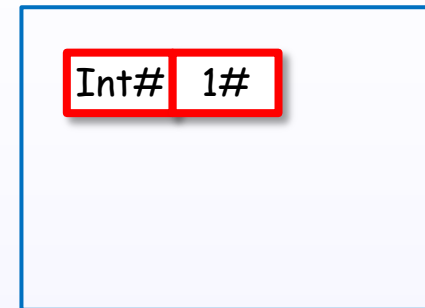
foldl' (+) (0 + 1) [2 .. 100]

let thunk1 = (0 + 1)  
in thunk1 `pseq`  
foldl' (+) thunk1 [2 .. 100]

heap memory

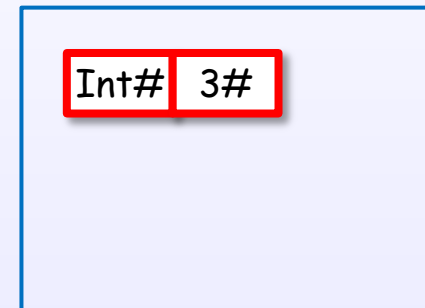
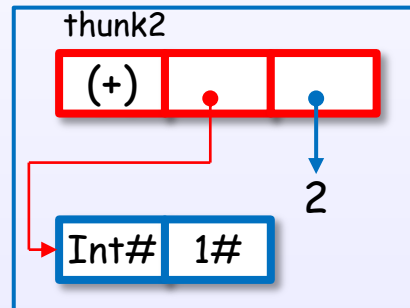


update  
by pseq



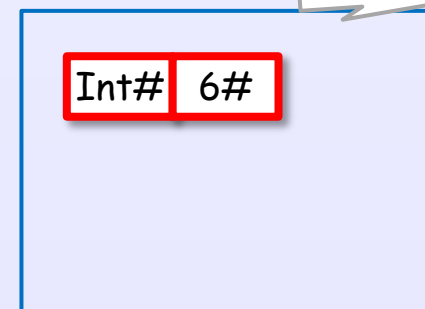
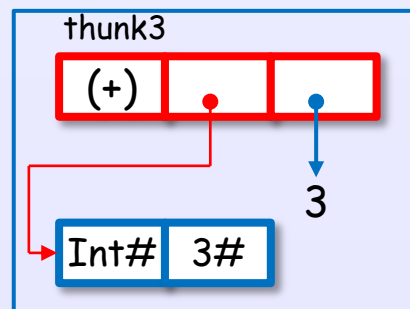
foldl' (+) (1 + 2) [3 .. 100]

let thunk2 = (1 + 2)  
in thunk2 `pseq`  
foldl' (+) thunk2 [3 .. 100]



foldl' (+) (3 + 3) [4 .. 100]

let thunk3 = (3 + 3)  
in thunk3 `pseq`  
foldl' (+) thunk3 [4 .. 100]



fixed heap size



...

References : [1]

# Example of foldl (non-strict) and foldl' (strict)

foldl (+) (0 + 1) [2 .. 100]



foldl (+) ((0 + 1) + 2) [3 .. 100]



foldl (+) (((0 + 1) + 2) + 3) [4 .. 100]



foldl' (+) (0 + 1) [2 .. 100]



foldl' (+) (1 + 2) [3 .. 100]



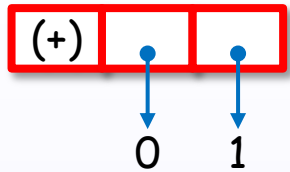
foldl' (+) (3 + 3) [4 .. 100]



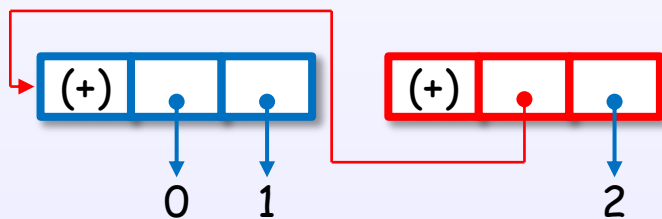
# Example of foldl (non-strict) and foldl' (strict)

foldl (+) (0 + 1) [2 .. 100]

heap memory

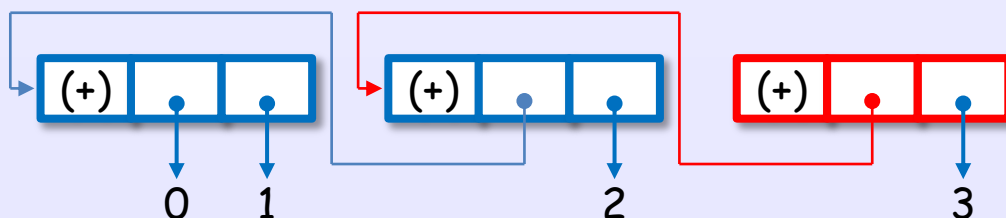


foldl (+) ((0 + 1) + 2) [3 .. 100]

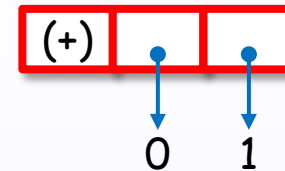


foldl (+) (((0 + 1) + 2) + 3) [4 .. 100]

increasing heap ...



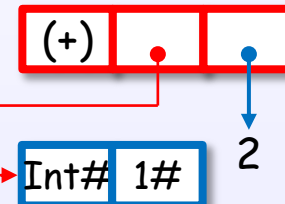
foldl' (+) (0 + 1) [2 .. 100]



Int# 1#



foldl' (+) (1 + 2) [3 .. 100]

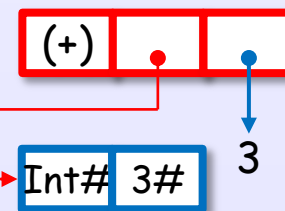


Int# 3#



foldl' (+) (3 + 3) [4 .. 100]

fixed heap size



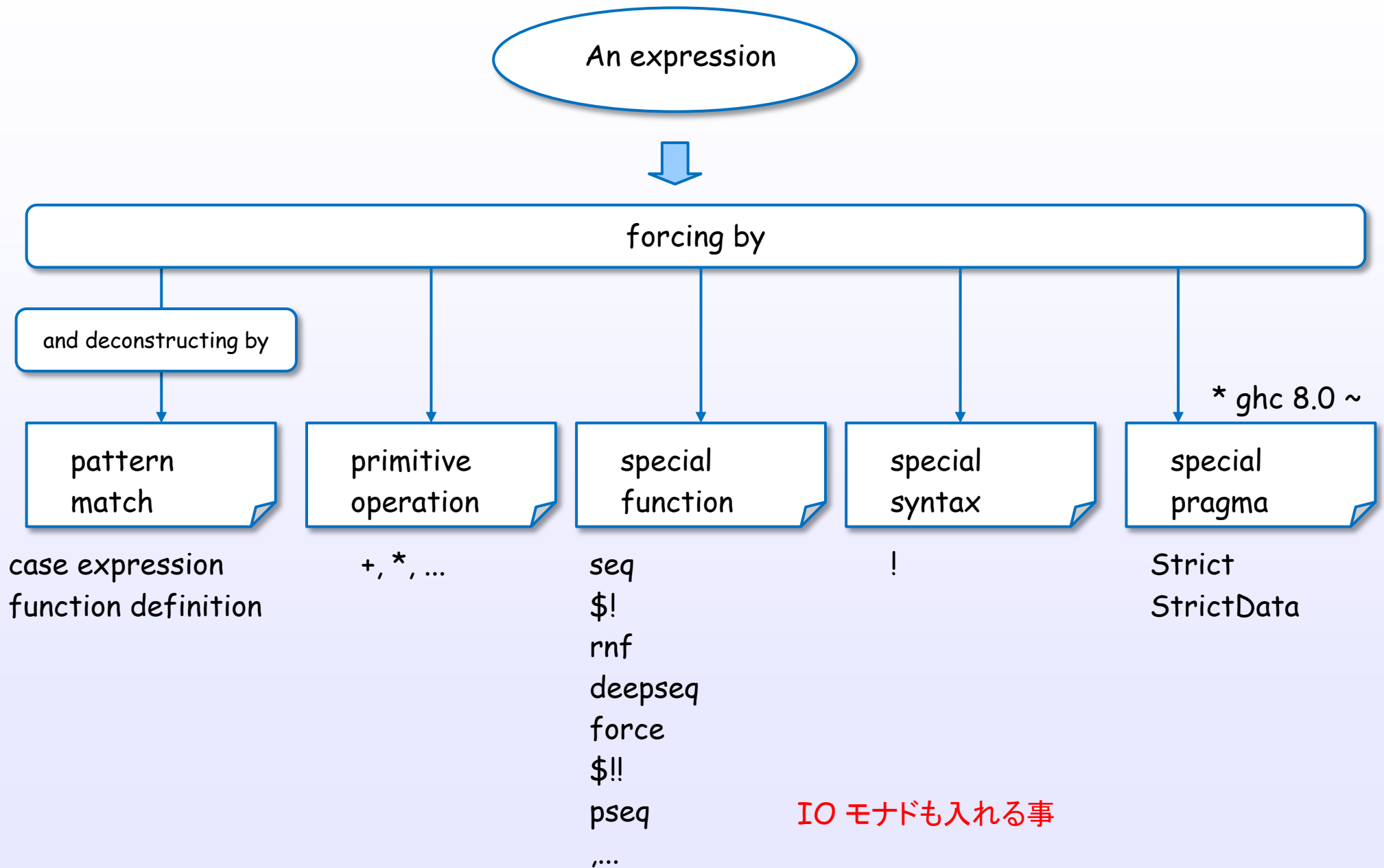
Int# 6#



References : [1]

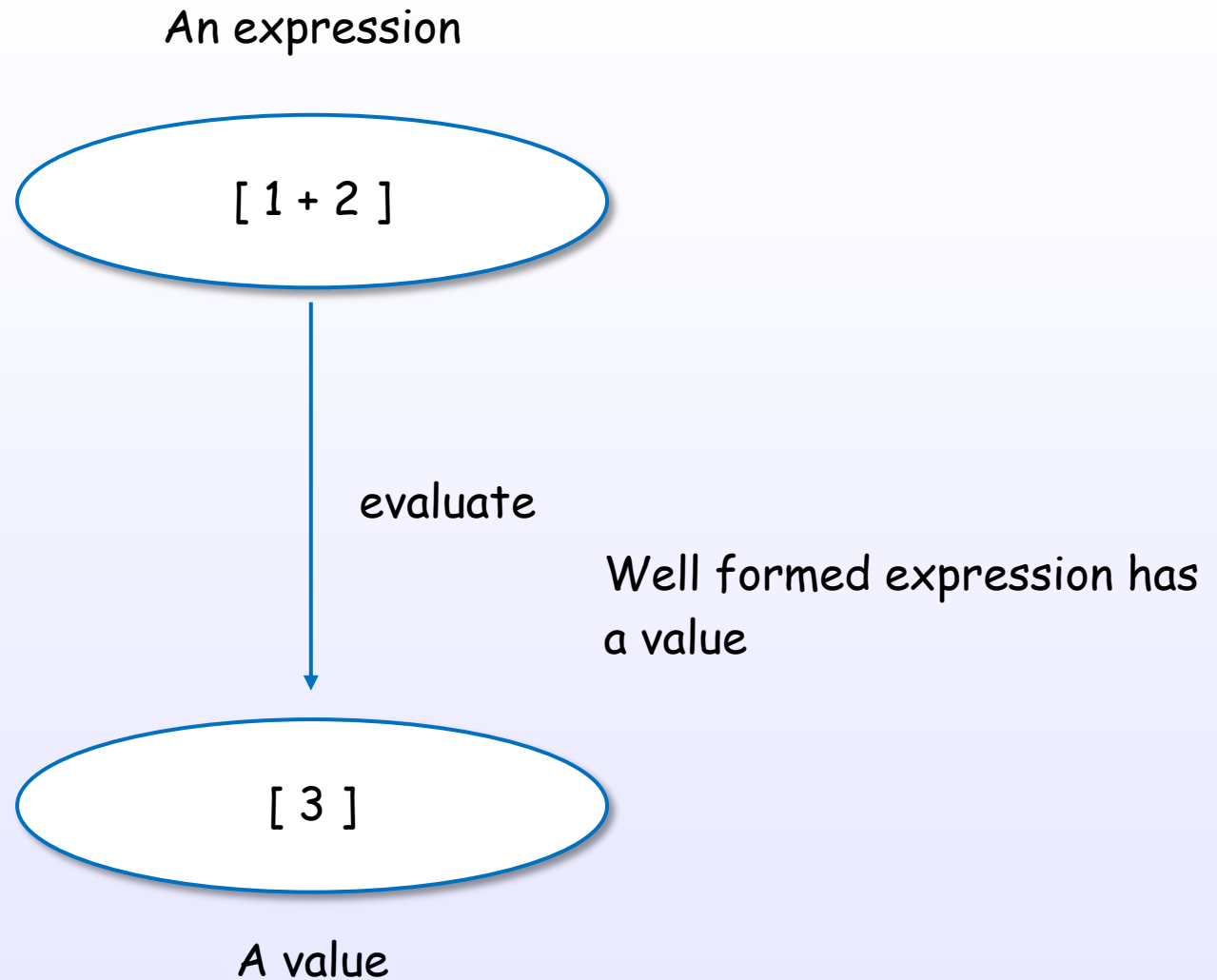
Control the evaluation in Haskell

# How to drive evaluation



Bottom

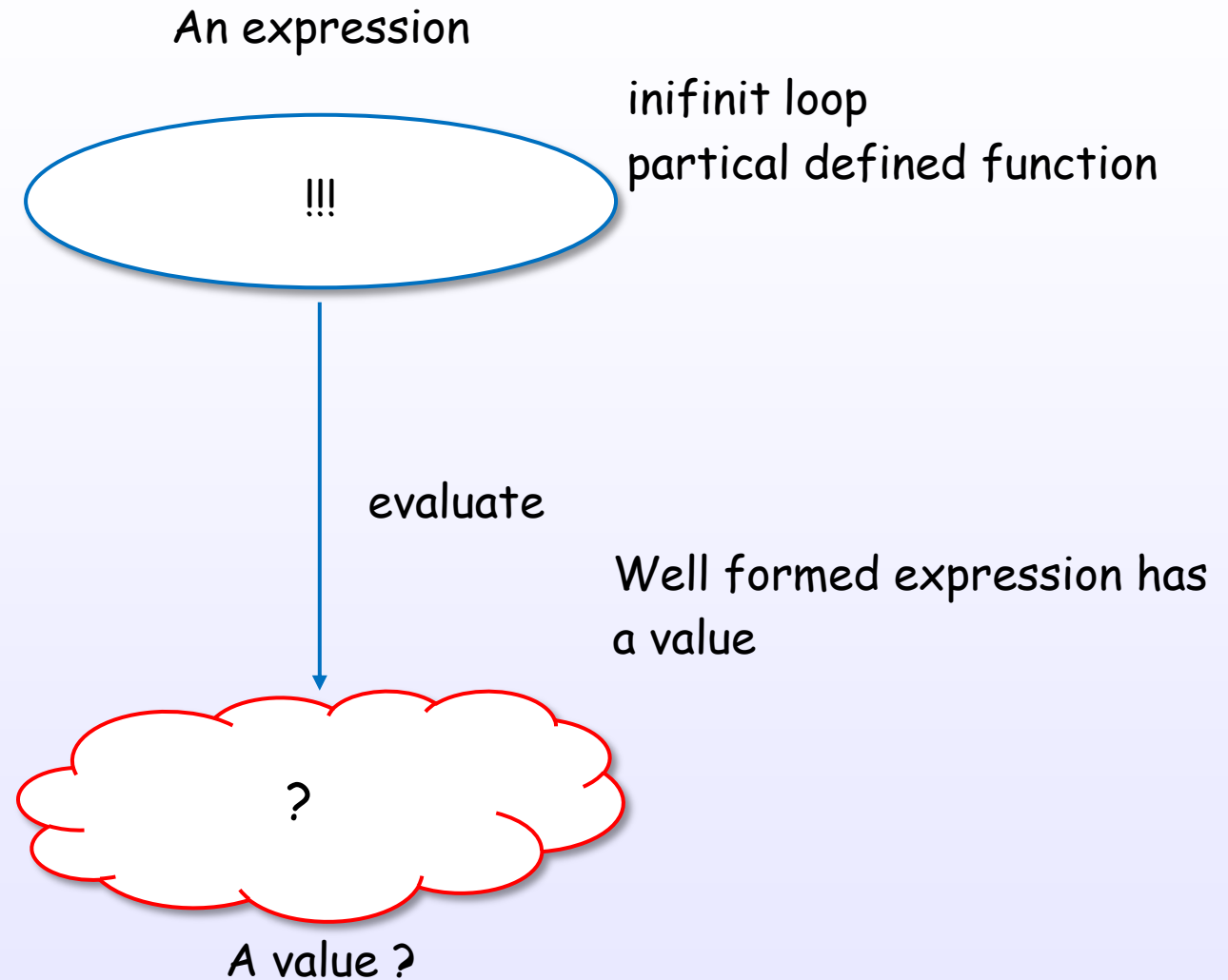
# Well formed expression has a value



[Bird, Chapter 2]

References : [1]

# Well formed expression has a value

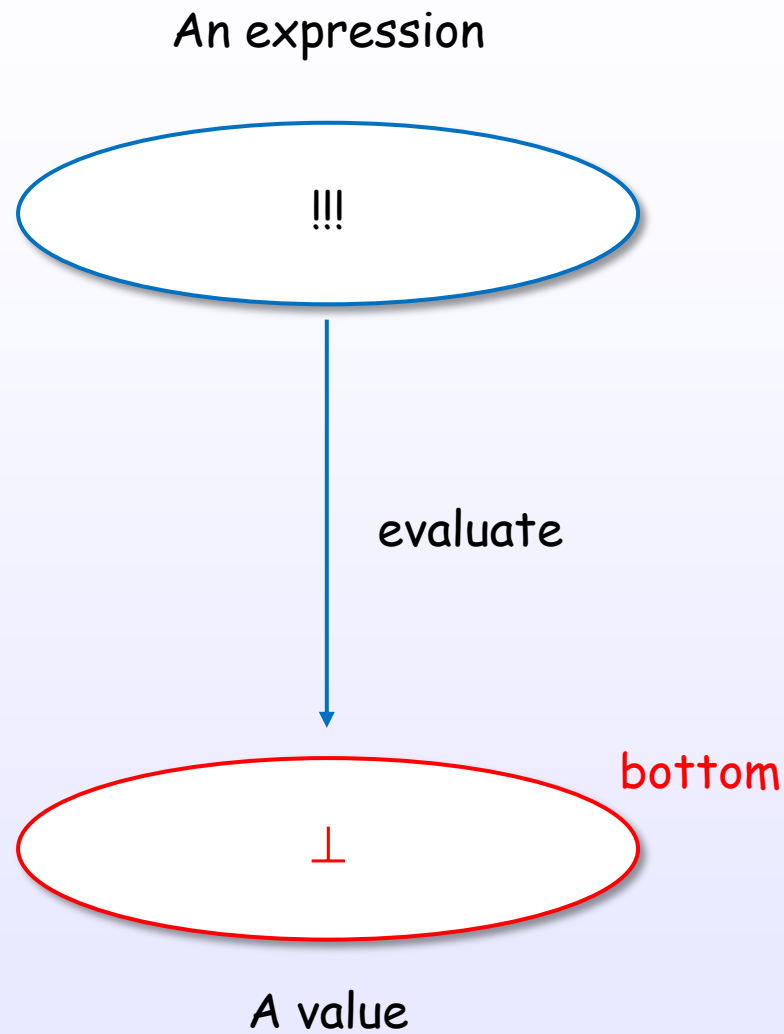


[Bird, Chapter 2]

References : [1]



# Well formed expression has a value



[Bird, Chapter 2]

References : [1]

# Bottom

domain

co-domain

defined

undefined

$$f \perp = \perp$$

[Bird, Chapter 2]

# Non-strict Semantics

# Strictness

$$f \perp = \perp$$

[Bird, Chapter 2]

# Layer

Non-strictness

$$f \perp = \perp$$

Lazy evaluation

Graph reduction

STG machine

# Graph reduction

# Tree, Graph

a expression

AST

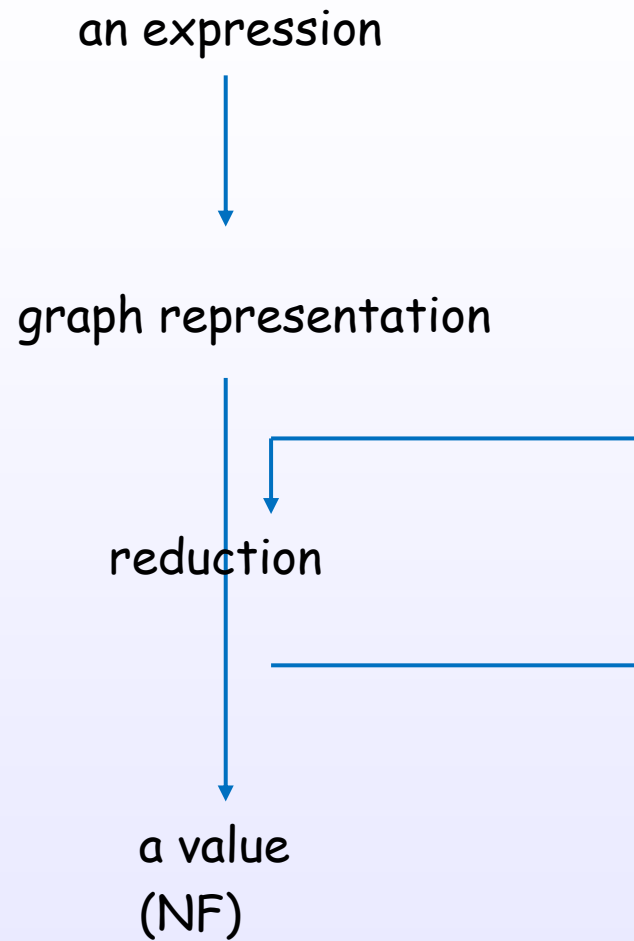
Tree

Graph

Shared Term

Lazy

# evaluation, reduction





Implementation in GHC

# STG heap objects

language

Just 5

implementation

heap object

# Layer

Non-strictness

$$f \perp = \perp$$

Lazy evaluation

Graph reduction

STG machine

# Layer

Haskell semantics

take 5 [1..10]

internal representation

graph

STG semantics

heap object

STG machine

## References

# References

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<http://research.microsoft.com/en-us/um/people/simonpj/Papers/spineless-tagless-gmachine.ps.gz>
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Lazy,... <sup>111</sup>