# Lazy evaluation in Haskell

exploring some mental models and implementations

Takenobu T.

Lazy,... 1111

..., It's fun.

## NOTE

- Meaning of terms are different by communities.
- There are a lot of good documents. Please see also references.
- This is written for GHC's Haskell.

### Contents

- Introduction
- Evaluation strategies
- Expressions in Haskell
- Constructor
- Thunk
- let, case expression
- WHNF
- Evaluation in Haskell (GHC)
- Control the evaluation in Haskell
- Examples of evaluation steps

- Semantics
- Graph reduction
- Implementation in GHC
- References



# What is an expression?



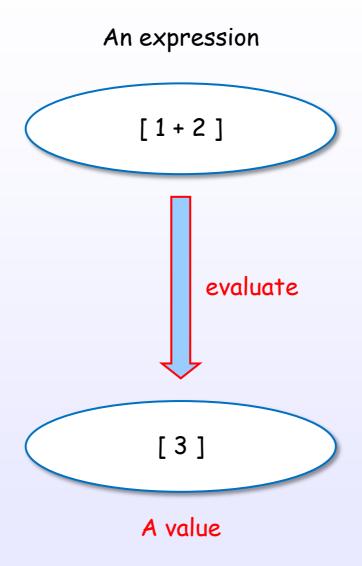


# An expression denotes a value

## An expression

[HR2010] [Bird, Chapter 2]

# An expression evaluates to a value



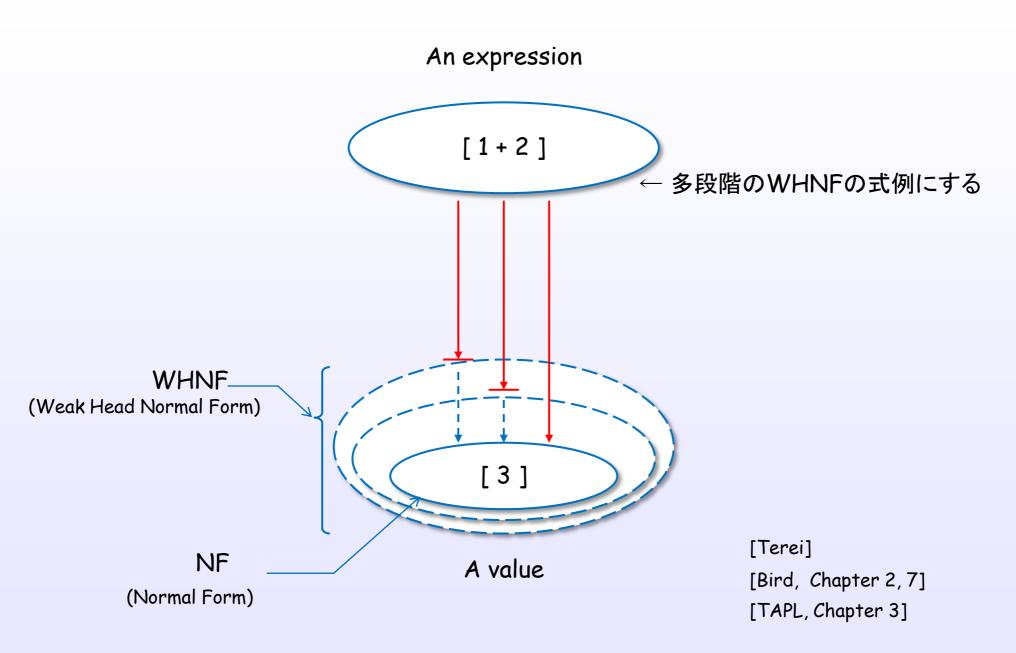
[HR2010] [Bird, Chapter 2]

# There are many evaluation approaches

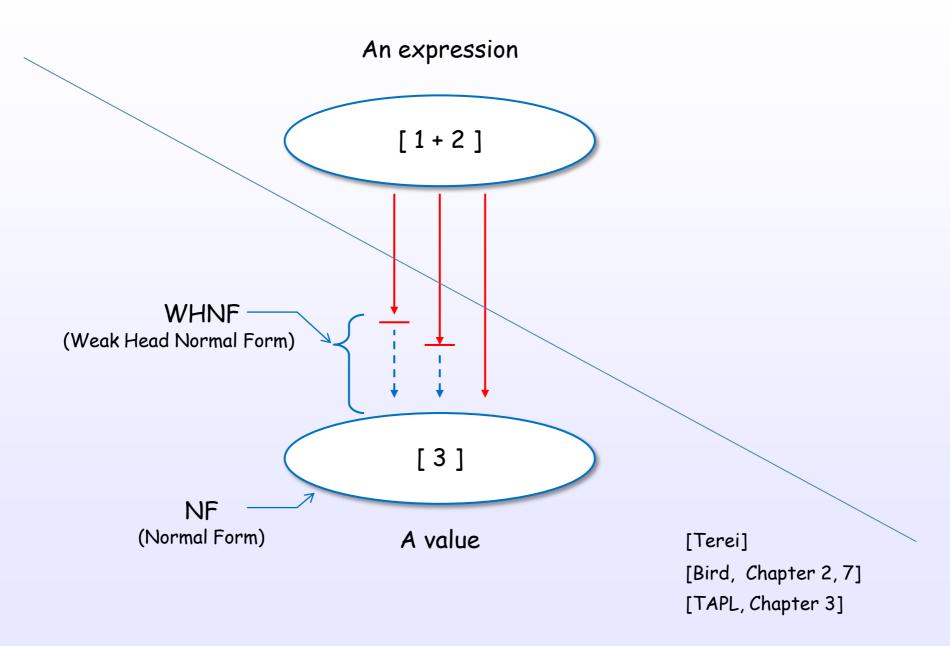


References: [1]

## There are some evaluation levels



## There are some evaluation levels



Evaluation strategies

# There are many evaluation approaches



References: [1]

# Evaluation layers

denotational semantics

evaluation strategies

implementation techniques

```
[Bird, Chapter 7]
[Hutton, Chapter 8]
[TAPL, Chapter 3]
References: [1]
```

# Evaluation layers

denotational semantics

Strict semantics

Non-strict semantics

evaluation strategies Eager evaluation (Strict evaluation)

Nondeterministic evaluation

Lazy evaluation
(Non-strict evaluation)

Call-by-Value

Call-by-Name

Call-by-Need

implementation techniques

Graph reduction

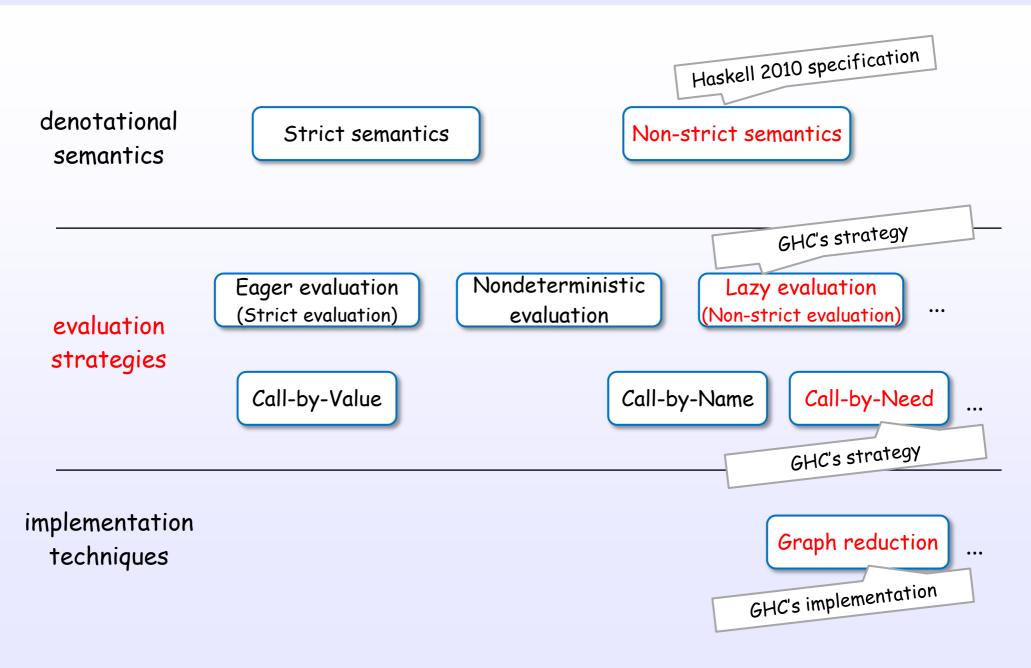
[Bird, Chapter 7]

[Hutton, Chapter 8]

[TAPL, Chapter 3]

References: [1]

# Evaluation layers for GHC's Haskell



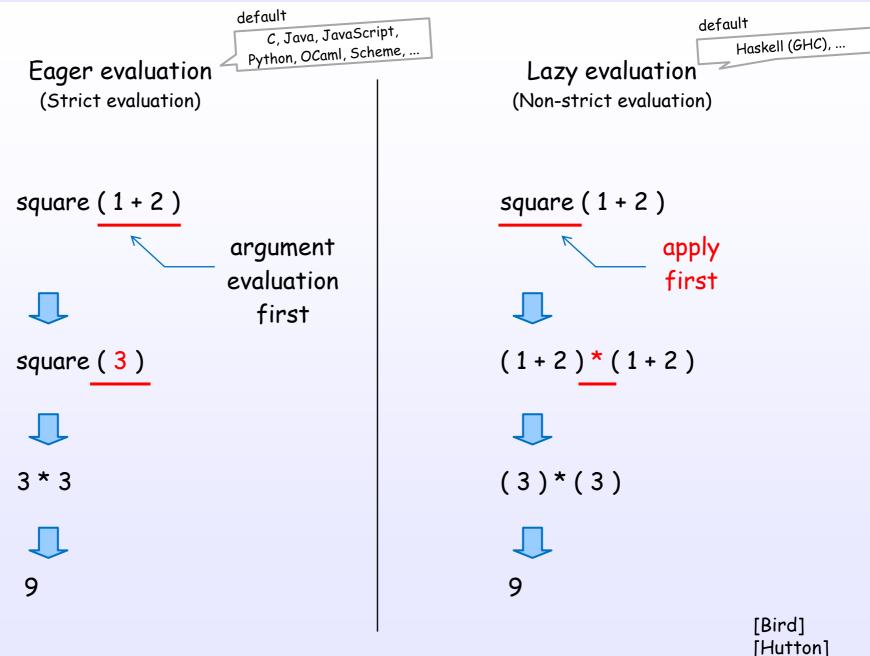
# Evariation strategies and order

$$a(bc) + d(e(fg))$$

order

[Bird] [Hutton]

# Simple example of both evaluations



# Simple example of both evaluations

Eager evaluation (Strict evaluation)

square (1+2)



square (3)



argument evaluated

3 \* 3



9

Lazy evaluation (Non-strict evaluation)

square (1 + 2)



(1+2)\*(1+2)



(3)\*(3)



9

argument evaluation delayed!

[Bird] [Hutton]

References: [1]

Expressions in Haskell

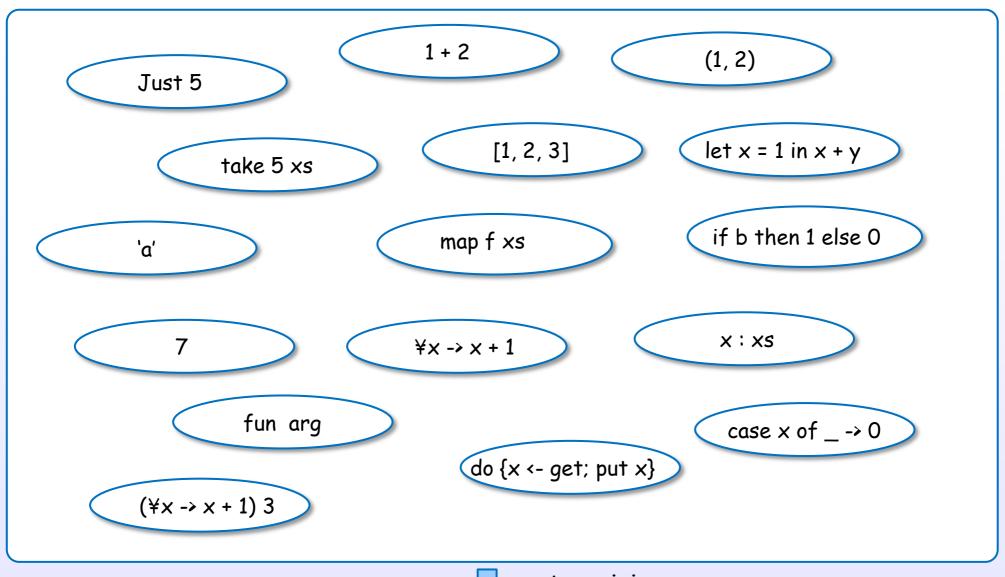
# An expression denotes a value

## An expression

[HR2010] [Bird, Chapter 2]

# There are many expressions in Haskell

## Expressions



categorizing

[HR2010]

[Bird, Chapter 2] References: [1]

# Expression categories in Haskell

#### lambda abstraction

let expression

$$\forall x \rightarrow x + 1$$

let x = 1 in x + y

#### conditional

case expression

do expression

if b then 1 else 0

case x of  $\_ \rightarrow 0$ 

do {x <- get; put x}

#### general constructor, literal and some forms

7

[1, 2, 3]

(1, 2)

**'**α'

x : xs

Just 5

## function application

take 5 xs

1 + 2

map f xs

fun arg

[HR2010] [Bird, Chapter 2

# Specification is defined in Haskell 2010 Language Report

#### Haskell 2010 Language Report, Chapter 3 Expressions [1]

```
\rightarrow infixexp :: [context =>] type
                                                                          (expression type signature)
exp
                   infixexp
infixexp
             \rightarrow lexp qop infixexp
                                                                          (infix operator application)

    infixexp

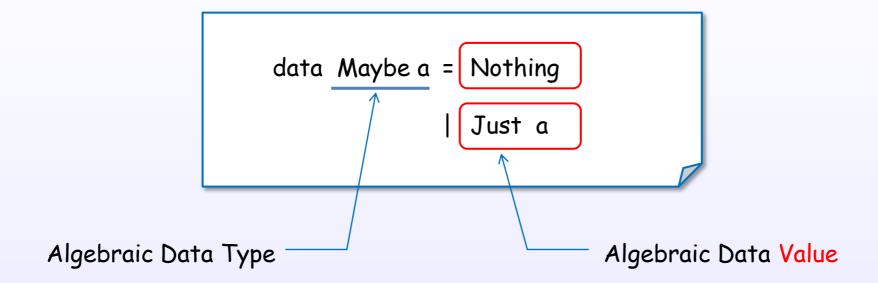
                                                                          (prefix negation)
                   lexp
             (lambda abstraction, n > 1)
lexp
                  let decls in exp
                                                                          (let expression)
                   if exp [;] then exp [;] else exp
                                                                          (conditional)
                   case exp of { alts }
                                                                          (case expression)
                   do { stmts }
                                                                          (do expression)
                   fexp
                                                                          (function application)
fexp
                   [fexp] aexp
                                                                          (variable)
                   qvar
aexp
                                                                          (general constructor)
                   qcon
                   literal
                                                                          (parenthesized expression)
                   (exp)
                   (exp_1, \ldots, exp_k)
                                                                          (tuple, k \geq 2)
                   [exp_1, \ldots, exp_k]
                                                                          (list, k > 1)
                   [exp_1 [, exp_2] .. [exp_3]]
                                                                          (arithmetic sequence)
                   [exp \mid qual_1, \ldots, qual_n]
                                                                          (list comprehension, n \ge 1)
                   ( infixexp qop )
                                                                          (left section)
                   ( qop_{\langle - \rangle} infixexp )
                                                                          (right section)
                   qcon \{ fbind_1, \dots, fbind_n \}
                                                                          (labeled construction, n > 0)
                   aexp_{(acon)} \{ fbind_1, \dots, fbind_n \}
                                                                         (labeled update, n \geq 1)
```



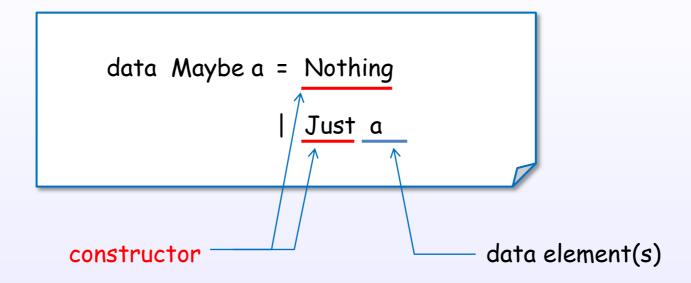
## Constructor

Constructor is one of the key elements to understand WHNF and lazy evaluation.

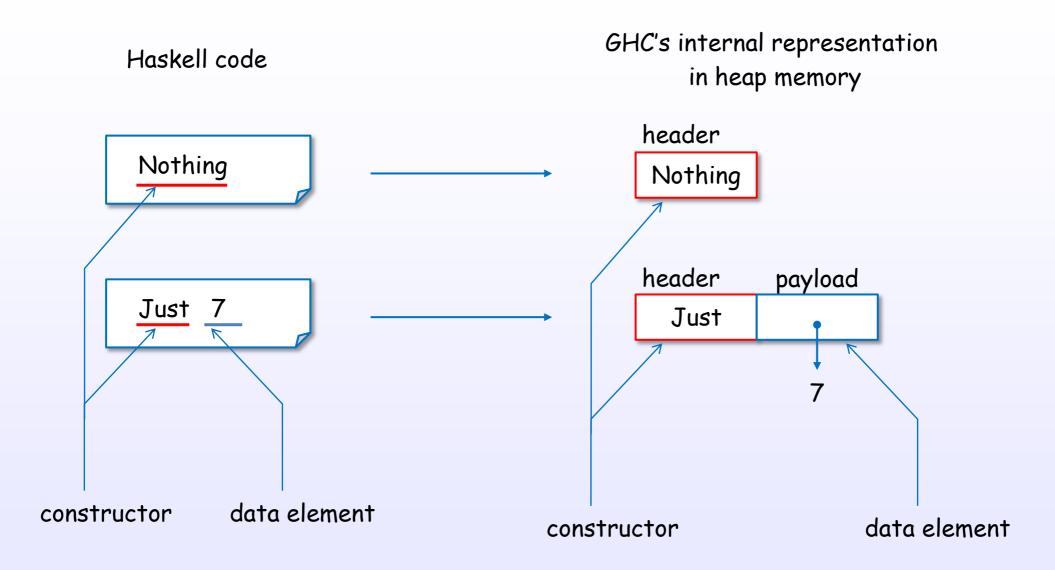
## data文で宣言する代数的データ型とその値



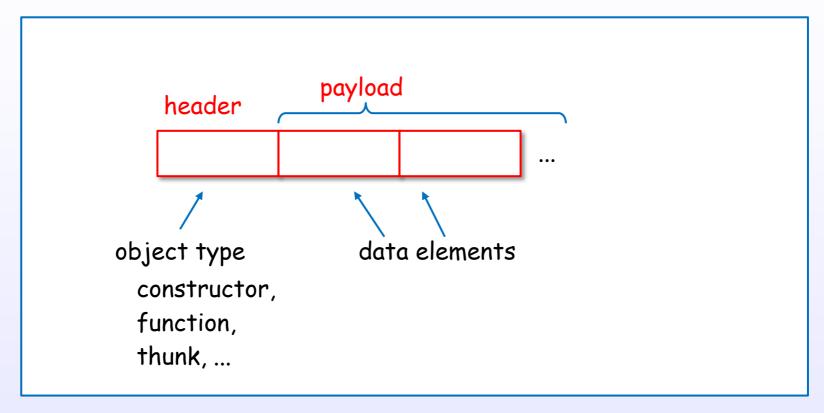
## Constructorはdata文で宣言する代数的データ値



## Constructorの内部表現

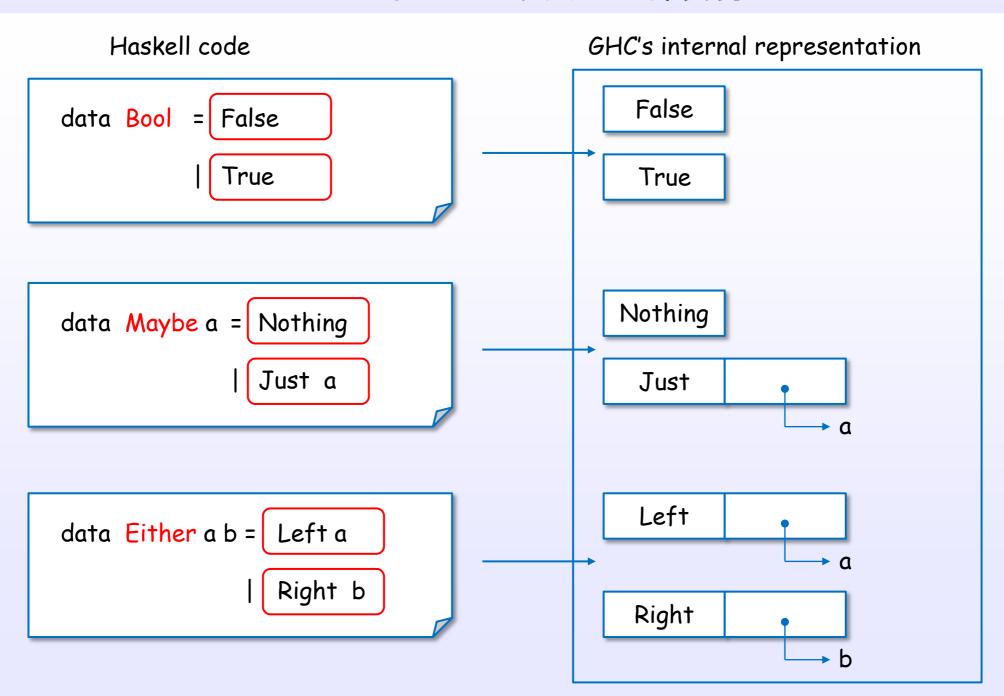


## Constructorは統一内部表現で表現される



in heap memory, stack, registers or static memory

## いろいろなコンストラクタと内部表現



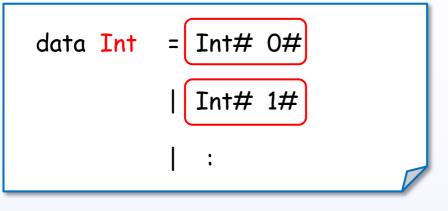
## 基本データ型も実はコンストラクタで構成されている

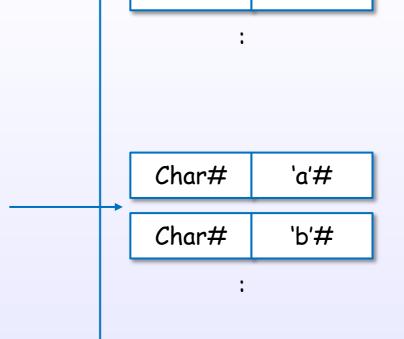
#### Haskell code

## GHC's internal representation

0#

1#





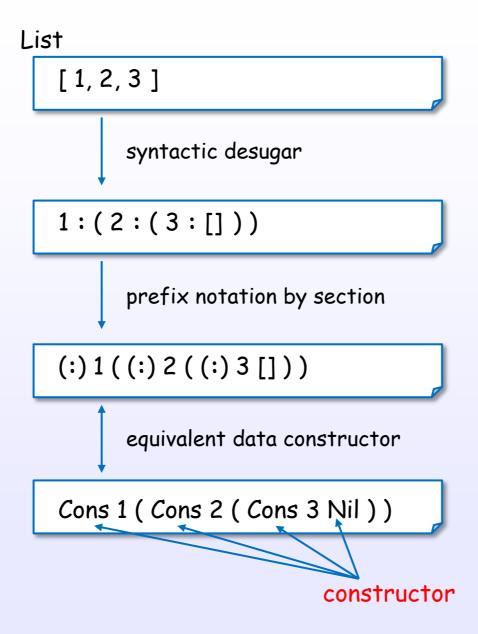
Int#

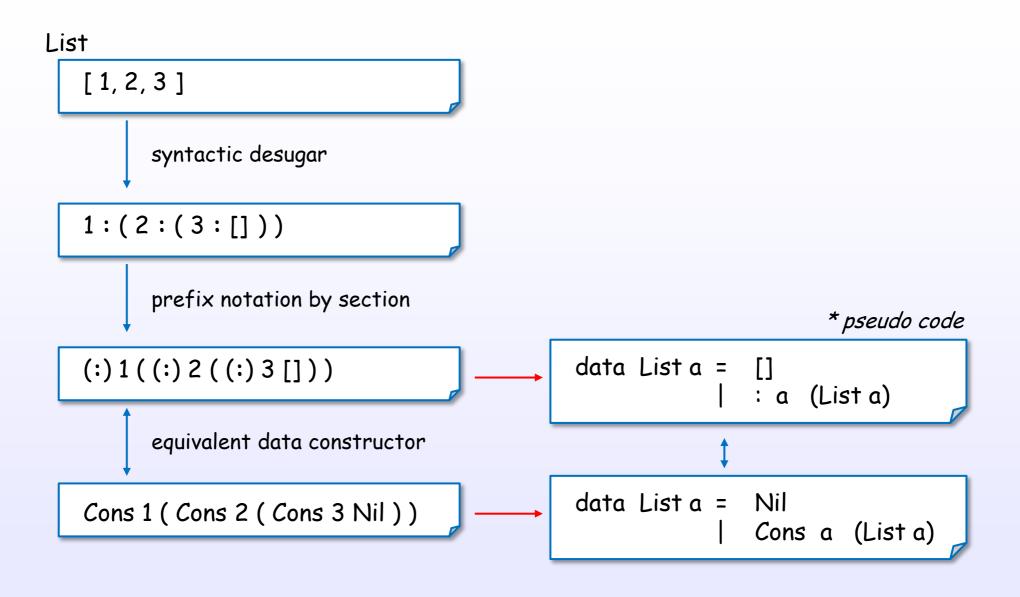
Int#

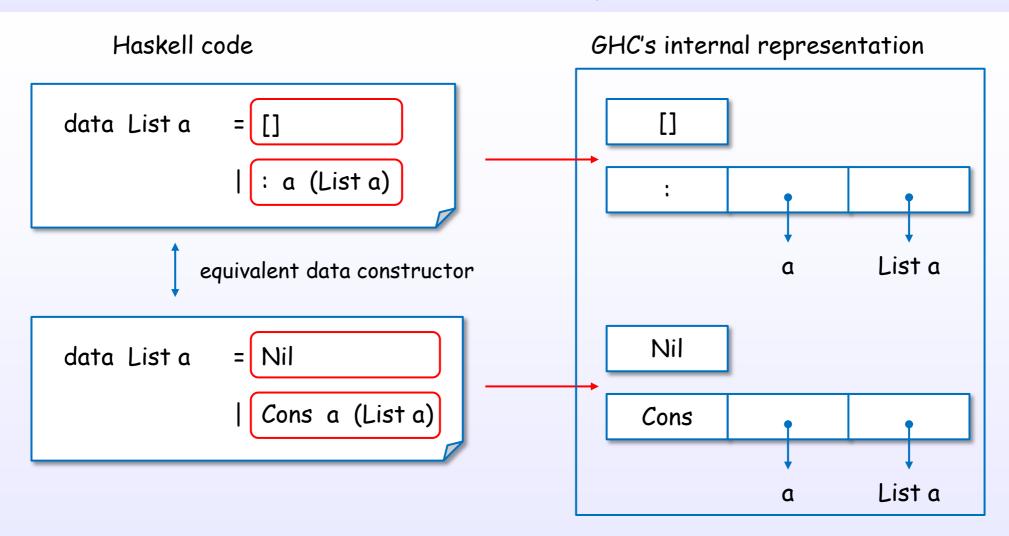
data Char = Char# 'a'#

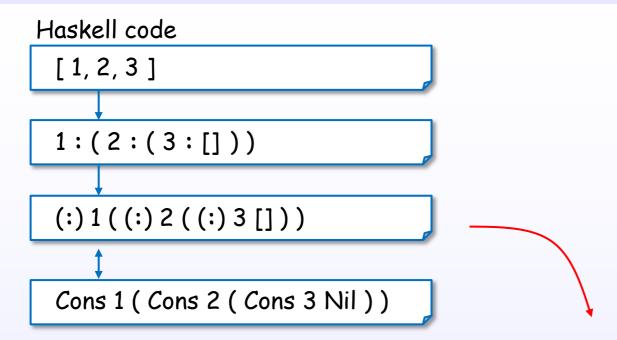
| Char# 'b'#

| :

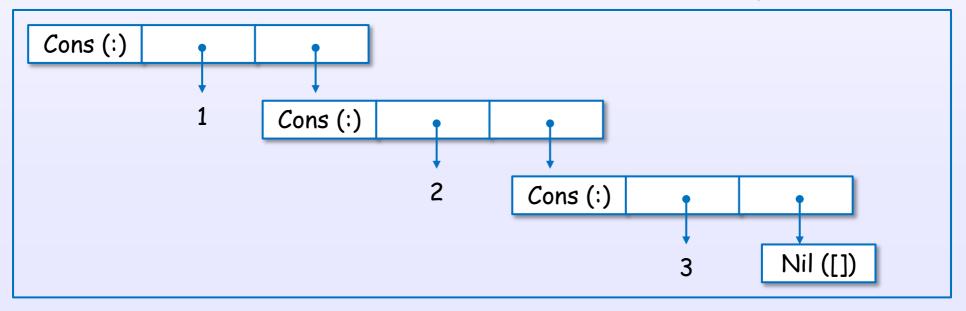




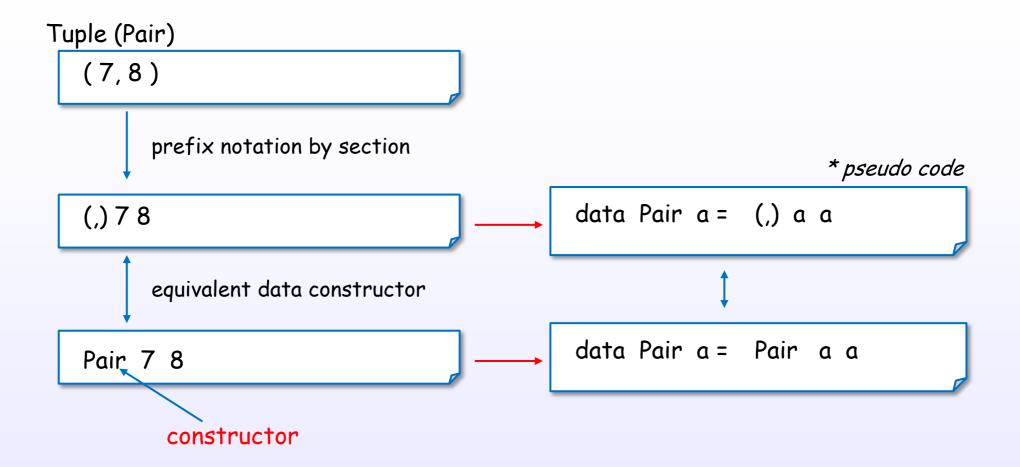




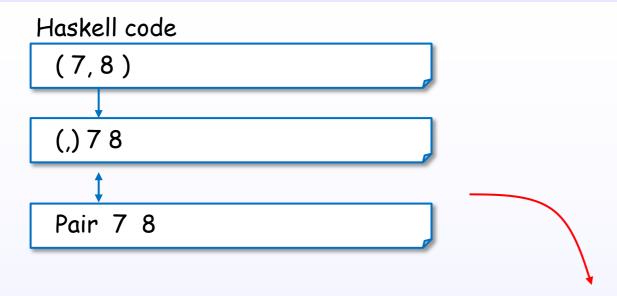
GHC's internal representation



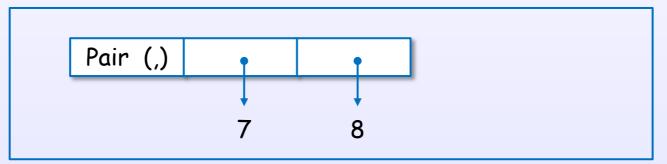
## タプルも実はコンストラクタで構成されている



## タプルも実はコンストラクタで構成されている



#### GHC's internal representation



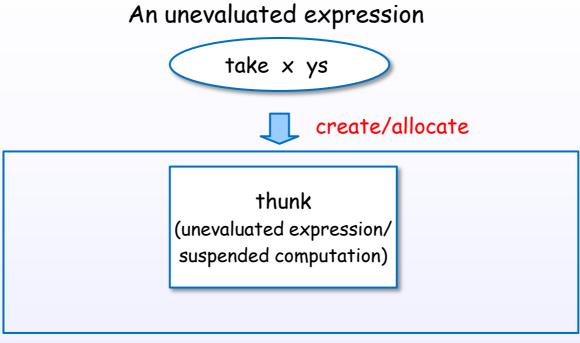


#### Thunk

thunk
(unevaluated expression/
suspended computation)

A thunk is an unevaluated expression in heap memory.

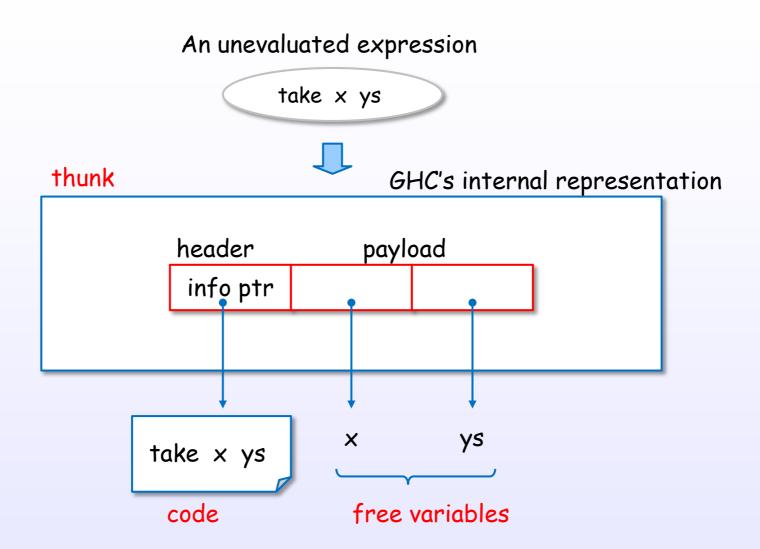
#### Thunk



in heap memory

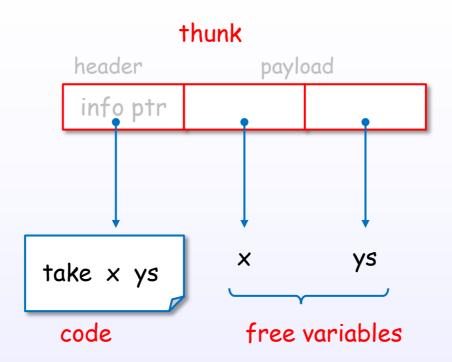
A thunk is created for an unevaluated expression.

#### Thunkの内部表現



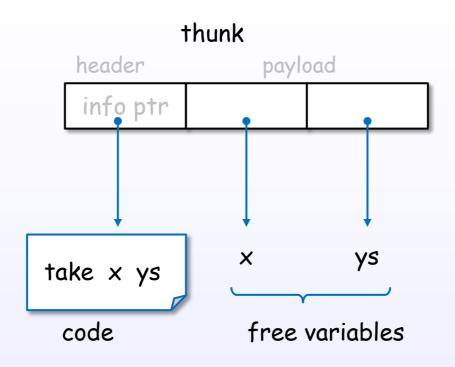
A thunk is represented with header(code) + payload(free variables).

## Thunkは、codeとfree variablesをパッケージ化したもの



A thunk is a package of code + free variables.

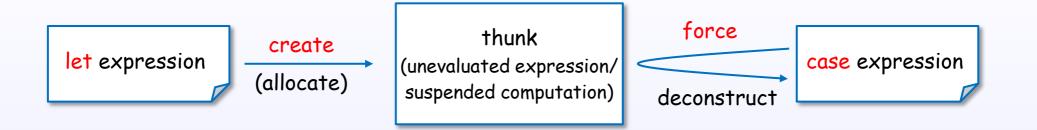
# Thunkは、forcing要求により評価される





let, case expression

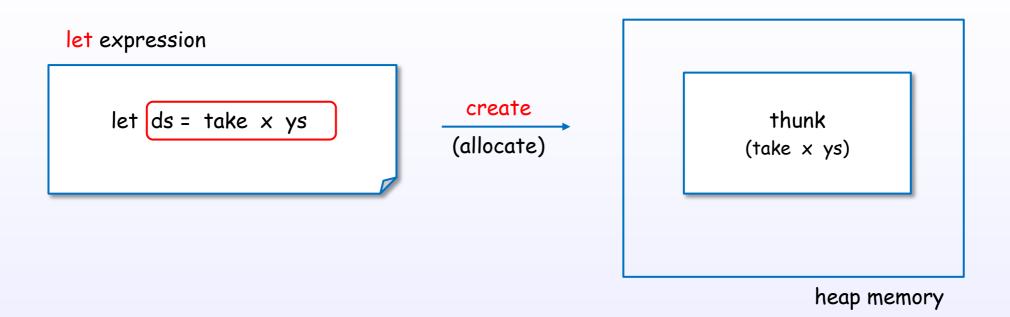
# let/case expressions and thunk



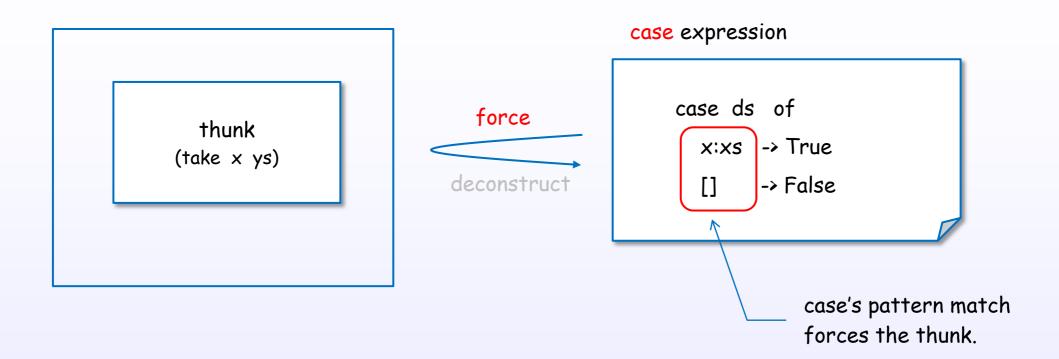
A let expression may create a thunk.

A case expression forces and deconstructs the thunk.

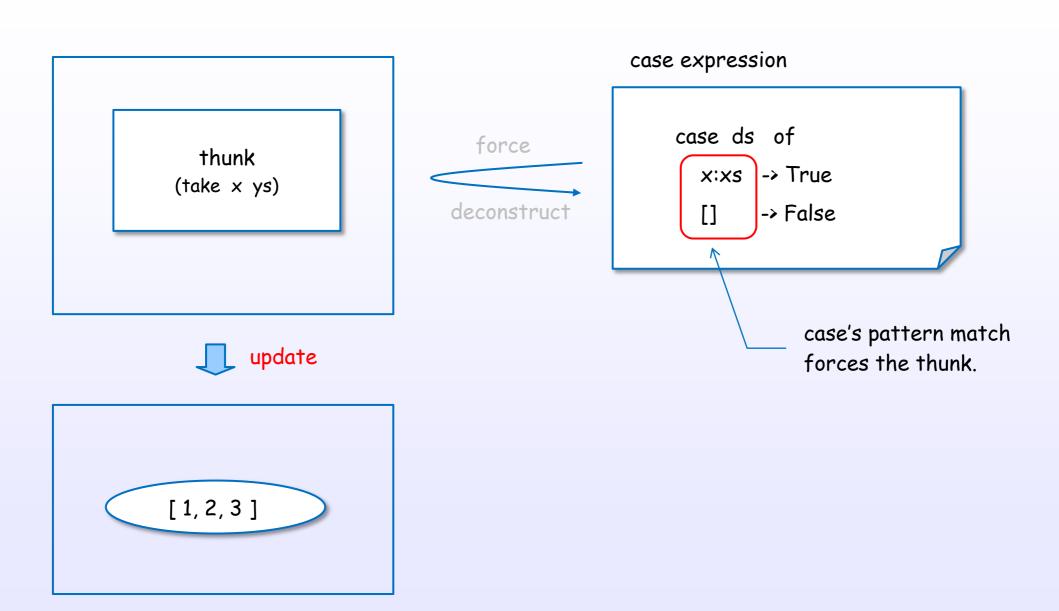
# A let expression creates a thunk



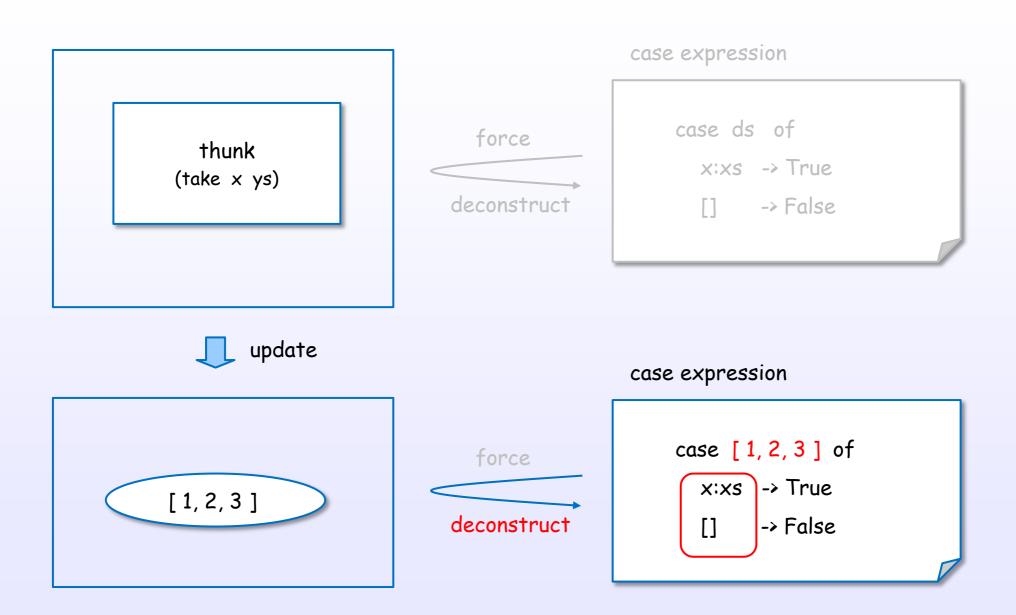
# A case expression forces a thunk



# A case expression forces a thunk

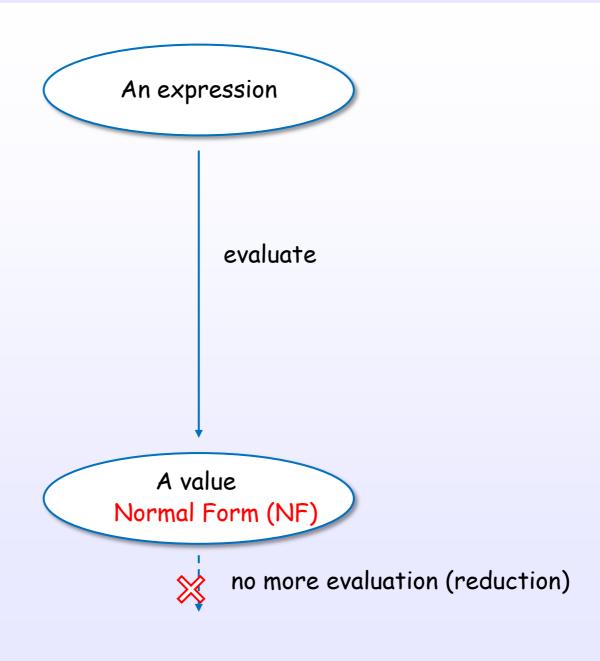


# A case expression forces a thunk



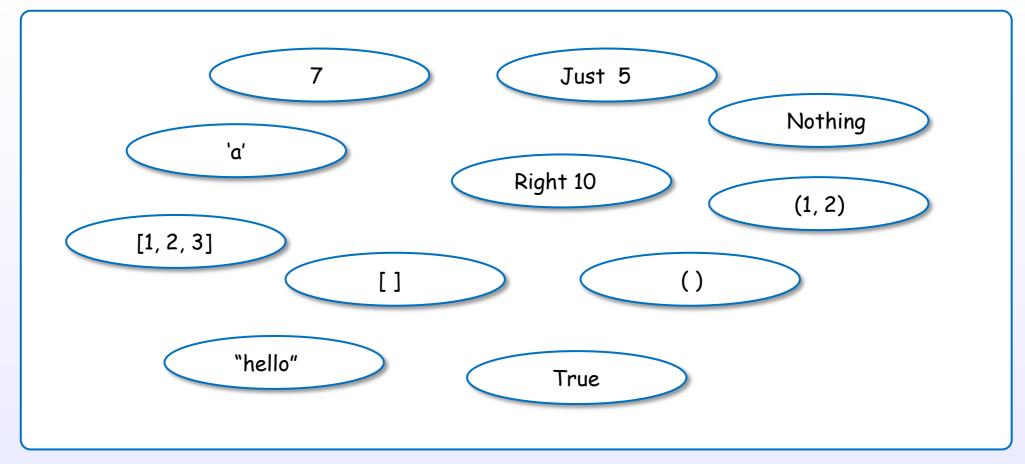


#### Normal form は、これ以上評価できない値

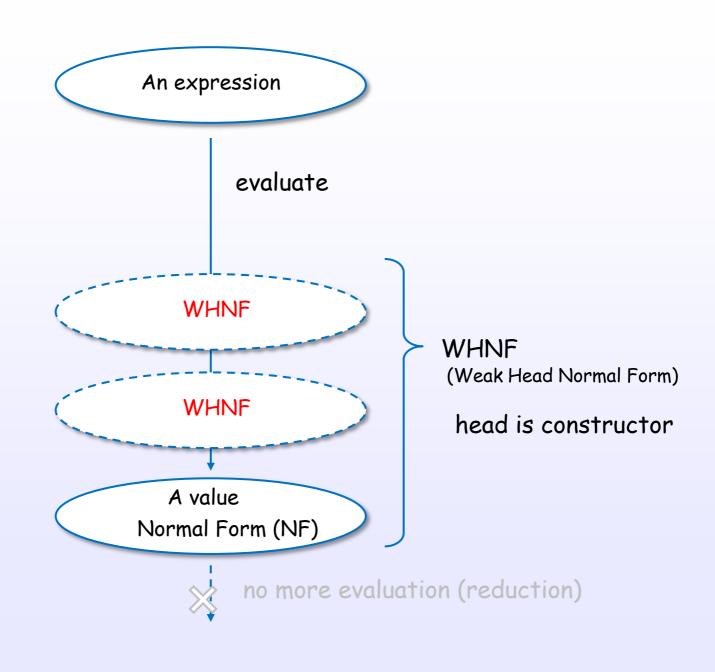


# Examples of normal form (NF)

#### Normal Forma (NF)

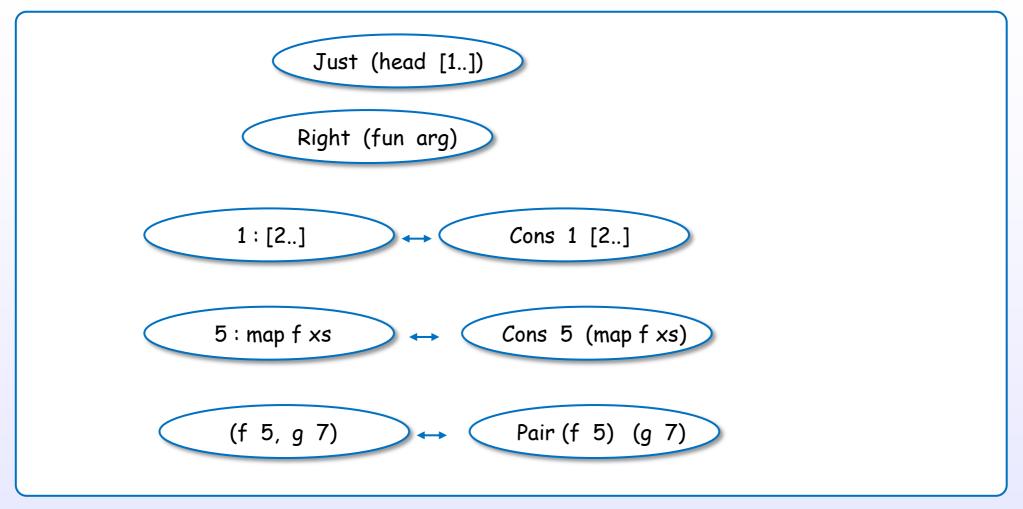


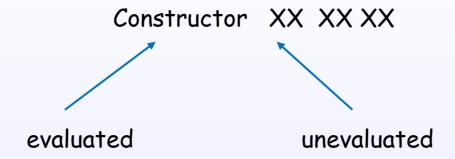
#### Weak Head Normal form は、少なくとも先頭が評価された式

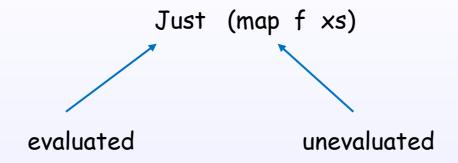


## Examples of weak head normal form (WHNF)

#### Weak Head Normal Forma (WHNF)







前頁の、heap objectイメージ

[4]

normal form: an expression without an redexes

head normal form:

an expression where the top level (head) is neither a redex NOR a lambda abstraction with a reducible body

weak head normal form: an expression where the top level (head) isn't a redex

[Terei]

#### [4]

evaluation strategies:
call-by-value: arguments evaluated before function entered (copied)
call-by-name: arguments passed unevaluated
call-by-need: arguments passed unevaluated but an expression is only
evaluated once (sharing)

no-strict evaluation Vs. lazy evaluation:

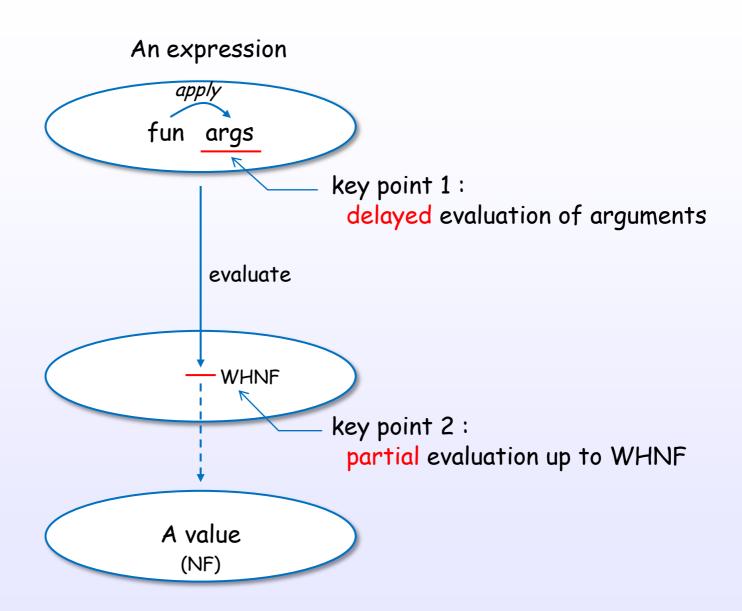
non-strict: Includes both call-by-name and call-by-need, general term for evaluation strategies that don't evaluate arguments before entering a function

lazy evaluation: Specific type of non-strict evaluation. Uses call-by-need (for sharing).

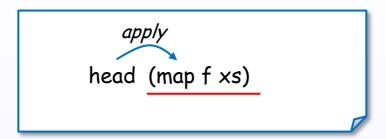
[Terei]

# Evaluation in Haskell (GHC)

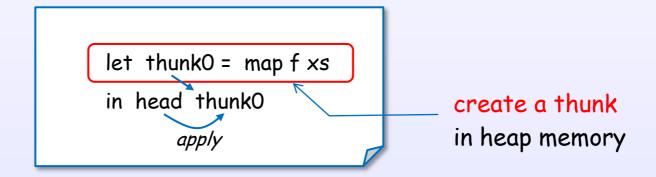
# Key concept of Haskell's lazy evaluation



# key point 1: delayed evaluation of arguments

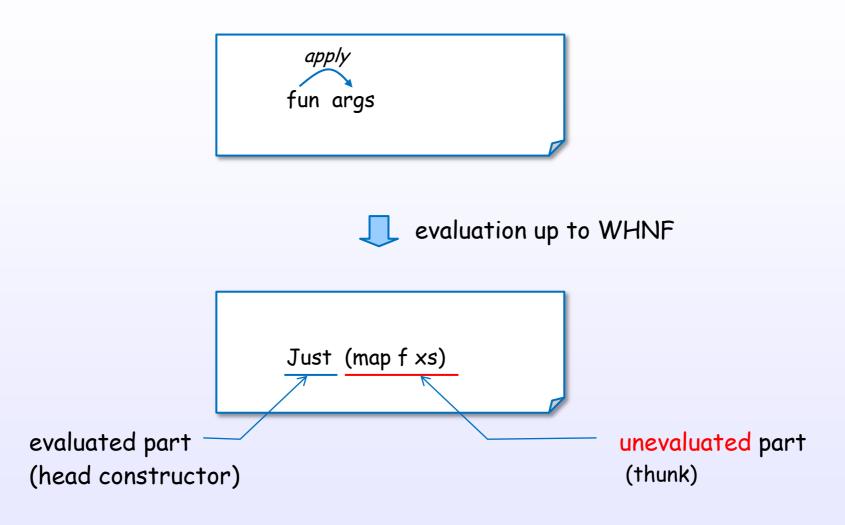


internal transformation by GHC



GHC implements lazy evaluation using the thunk. Evaluation of arguments is delayed with the thunk.

# key point 2: partial evaluation up to WHNF



GHC can partially evaluate a expression.

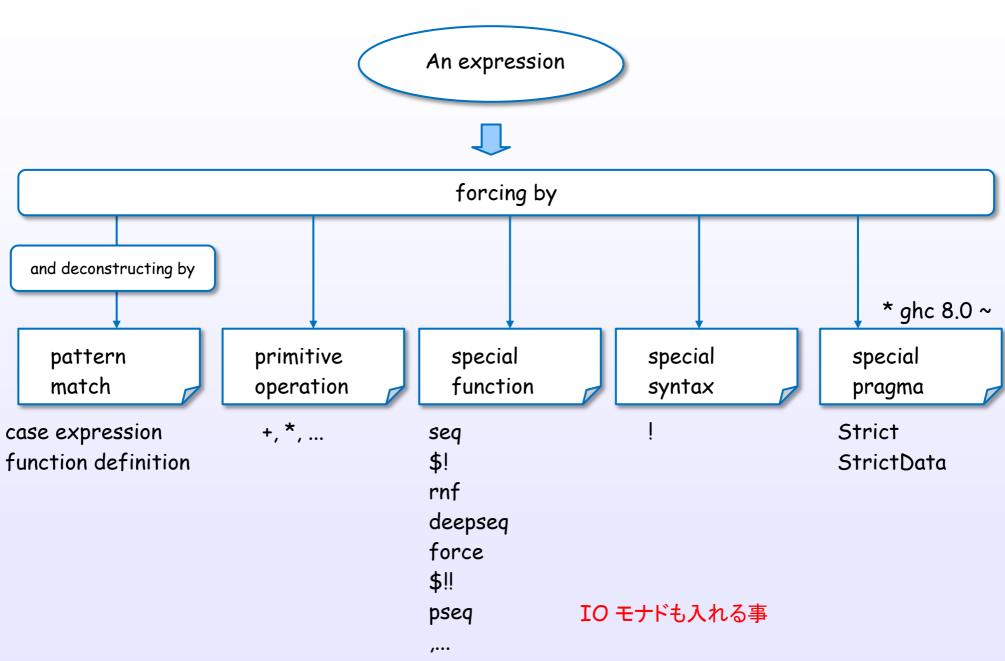
Constructor can hold an unevaluated expression (a thunk).

## Pattern match

[CIS194]

# Control the evaluation in Haskell

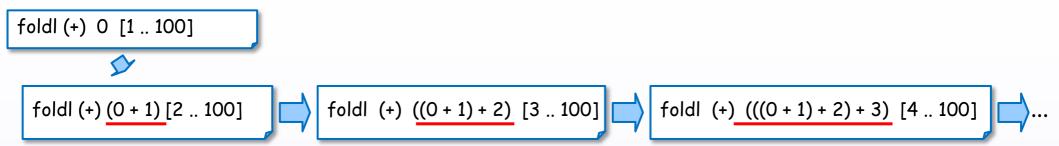
#### How to drive evaluation



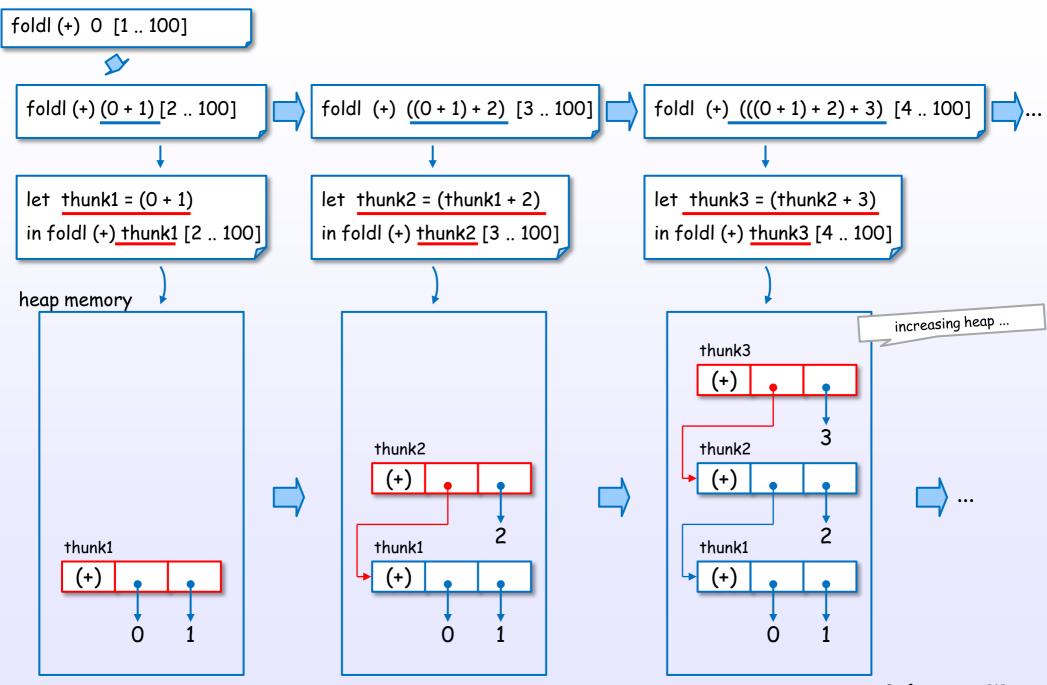
References: [1]

Examples of evaluation steps

# Example of foldl (non-strict)

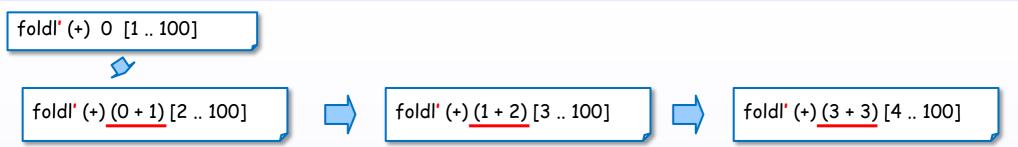


# Example of foldl (non-strict)

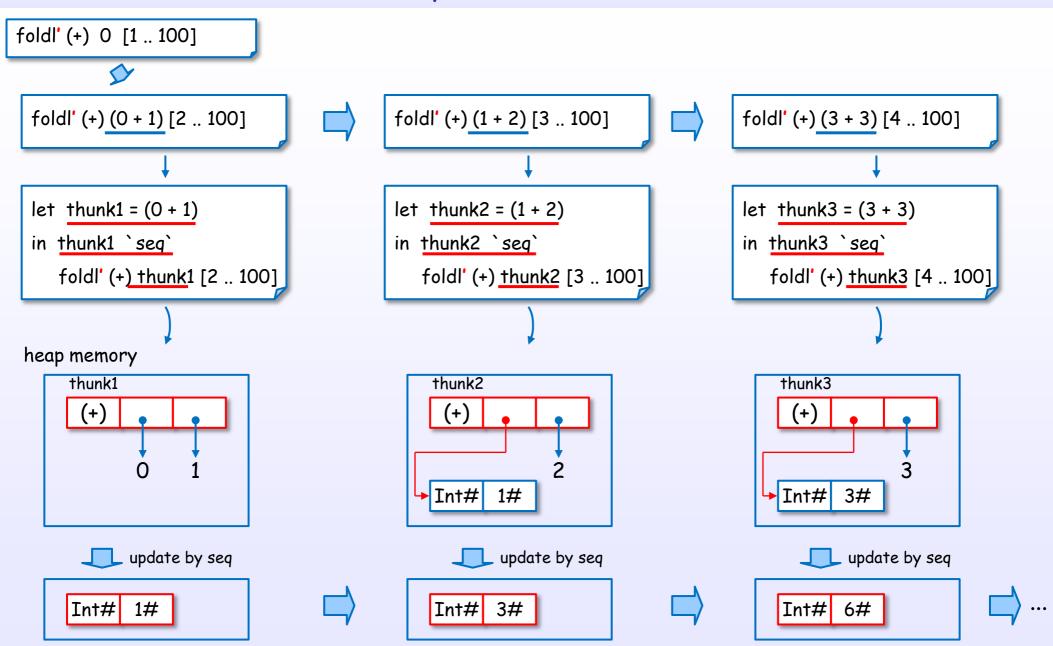


References: [1]

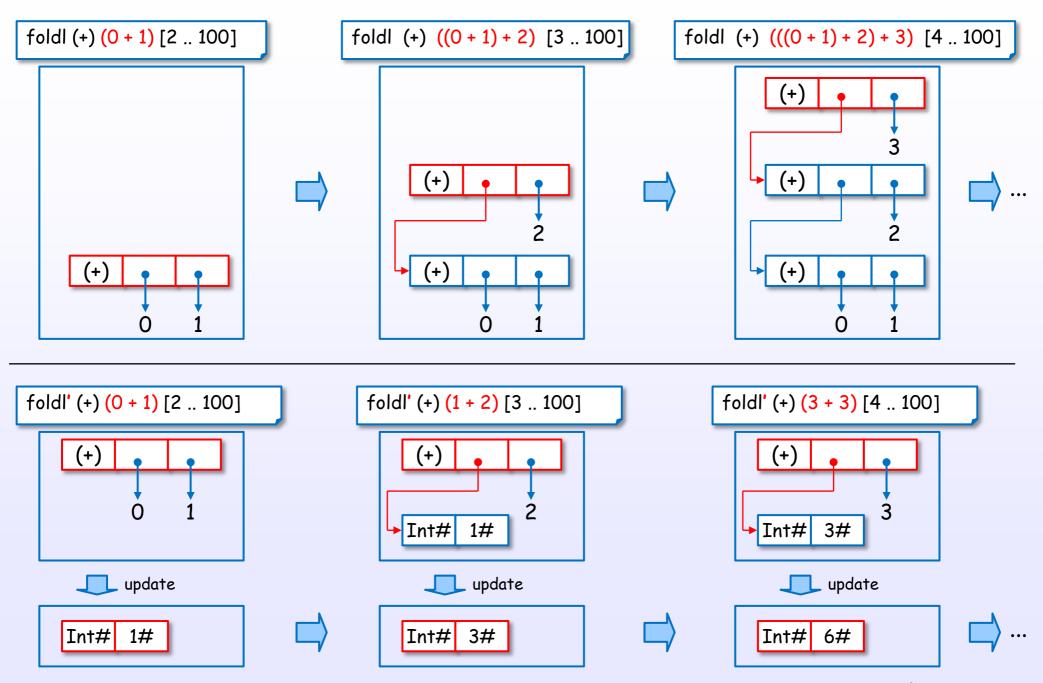
# Example of foldl' (strict)



# Example of foldl' (strict)



## Example of foldl (non-strict) and foldl' (strict)



References: [1]

Implementation in GHC

## Tree, Graph

a expression

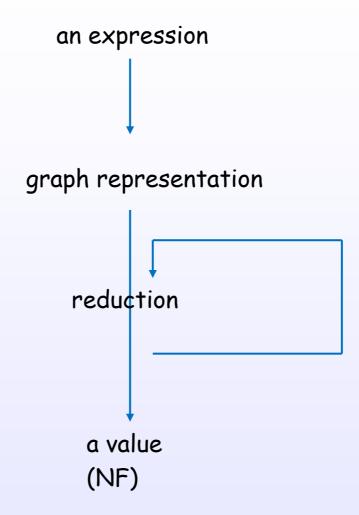
**AST** 

Tree Graph

Shared Term

Lazy

## evaluation, reduction



# Expressions examples

# STG heap objects

language Just 5

implementation heap object

## Layer

Non-strictness

$$f \perp = \perp$$

Lazy evaluation

Graph reduction

STG machine

## Layer

Haskell semantics take 5 [1..10]

internal representation graph

STG semantics heap object

STG machine



## Bottom

domain

co-domain

defined

undefined

f  $\perp$  =  $\perp$ 

[Bird, Chapter 2]

## Strictness, Bottom

[Bird, Chapter 2]

- [1] Haskell 2010 Language Report https://www.haskell.org/definition/haskell2010.pdf
- [2] The Glorious Glasgow Haskell Compilation System (GHC user's guide) https://downloads.haskell.org/~ghc/latest/docs/users\_guide.pdf
- [3] Thinking Functionally with Haskell (IFPH 3rd edition) http://www.cs.ox.ac.uk/publications/books/functional/
- [4] Types and Programming Languages https://mitpress.mit.edu/books/types-and-programming-languages
- [5] A Haskell Compiler http://www.scs.stanford.edu/11au-cs240h/notes/ghc-slides.html http://www.scs.stanford.edu/11au-cs240h/notes/ghc-slides.html#(11)
- [6] Being Lazy with Class http://www.seas.upenn.edu/~cis194/lectures/06-laziness.html
- [7] The Incomplete Guide to Lazy Evaluation (in Haskell) https://hackhands.com/guide-lazy-evaluation-haskell/
- [8] Programming in Haskell https://www.cs.nott.ac.uk/~gmh/book.html
- [9] Parallel and Concurrent Programming in Haskell http://chimera.labs.oreilly.com/books/123000000929/ch02.html
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https://en.wikibooks.org/wiki/Haskell/Graph\_reduction

[18] Haskell/Graph reduction

- [19] Implementing lazy functional languages on stock hardware: the Spineless Tagless G-machine Version 2.5 http://research.microsoft.com/en-us/um/people/simonpj/Papers/spineless-tagless-gmachine.ps.gz
- [20] Making a Fast Curry Push/Enter vs Eval/Apply for Higher-order Languages http://research.microsoft.com/en-us/um/people/simonpj/papers/eval-apply/
- [21] I know kung fu: learning STG by example https://ghc.haskell.org/trac/ghc/wiki/Commentary/Compiler/GeneratedCode
- [22] GHC Commentary: The Layout of Heap Objects https://ghc.haskell.org/trac/ghc/wiki/Commentary/Rts/Storage/HeapObjects
- [23] GHC Commentary: Strict & StrictData https://ghc.haskell.org/trac/ghc/wiki/StrictPragma
- [24] GHC illustrated http://takenobu-hs.github.io/downloads/haskell\_ghc\_illustrated.pdf

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