Lazy evaluation in Haskell

exploring some mental models and implementations

Takenobu T.

Lazy,... 1111

..., It's fun.

NOTE

- Meaning of terms are different by communities.
- There are a lot of good documents. Please see also references.
- This is written for GHC's Haskell.

Contents

- Introduction
- Evaluation strategies
- Expressions in Haskell
- Constructor
- Thunk
- let, case expression
- WHNF
- Evaluation in Haskell (GHC)
- Control the evaluation in Haskell
- Examples of evaluation steps

- Semantics
- Graph reduction
- Implementation in GHC
- References



What is an expression?



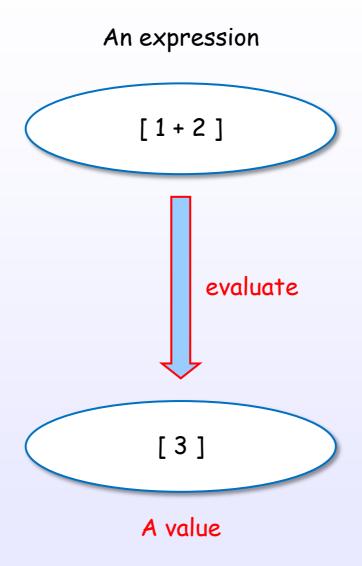


An expression denotes a value

An expression

[HR2010] [Bird, Chapter 2]

An expression evaluates to a value



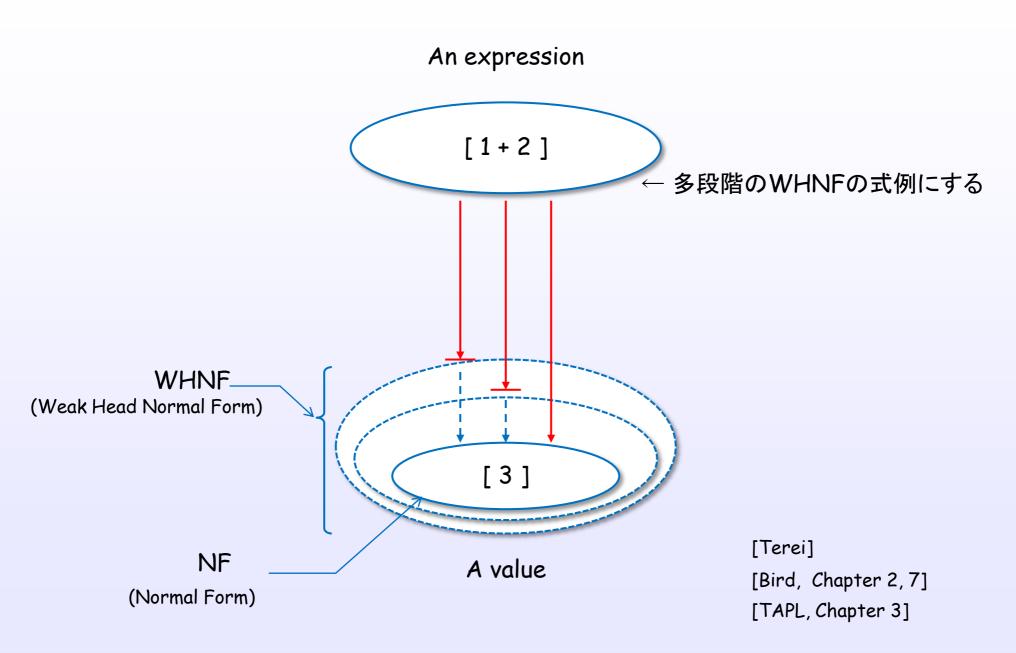
[HR2010] [Bird, Chapter 2]

There are many evaluation approaches

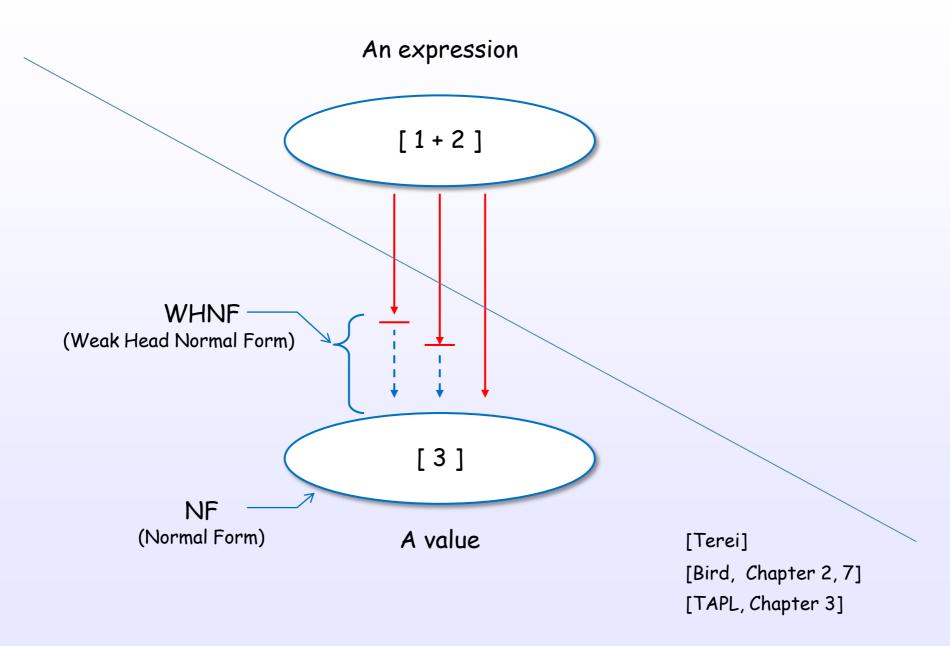


References: [1]

There are some evaluation levels



There are some evaluation levels



Evaluation strategies

There are many evaluation approaches



References: [1]

Evaluation layers

denotational semantics

evaluation strategies

implementation techniques

```
[Bird, Chapter 7]
[Hutton, Chapter 8]
[TAPL, Chapter 3]
References: [1]
```

Evaluation layers

denotational semantics

Strict semantics

Non-strict semantics

evaluation strategies Eager evaluation (Strict evaluation)

Nondeterministic evaluation

Lazy evaluation
(Non-strict evaluation)

Call-by-Value

Call-by-Name

Call-by-Need

implementation techniques

Graph reduction

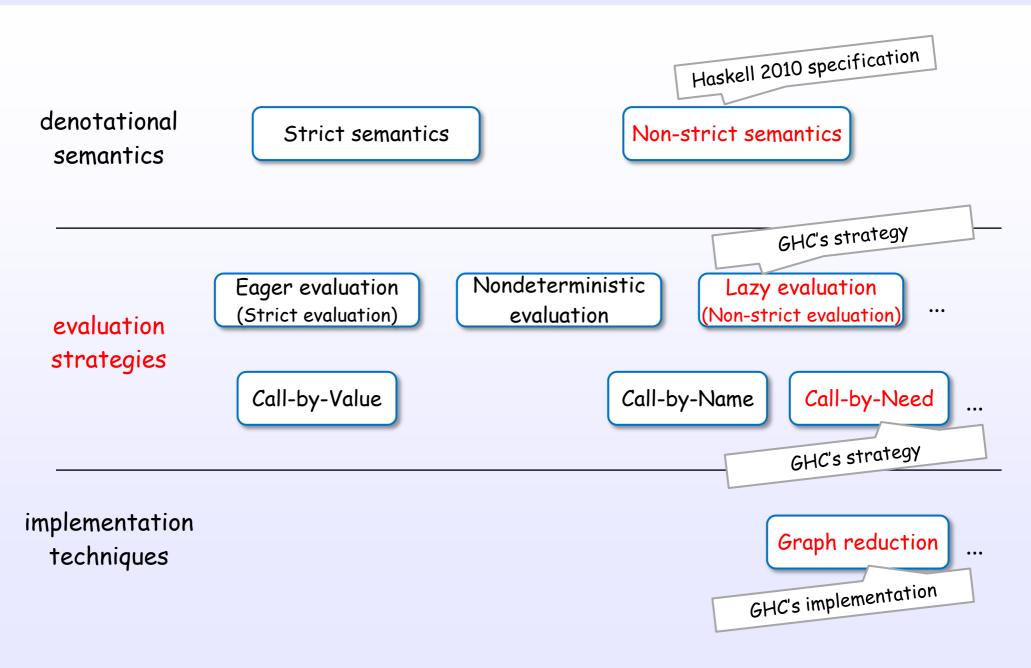
[Bird, Chapter 7]

[Hutton, Chapter 8]

[TAPL, Chapter 3]

References: [1]

Evaluation layers for GHC's Haskell



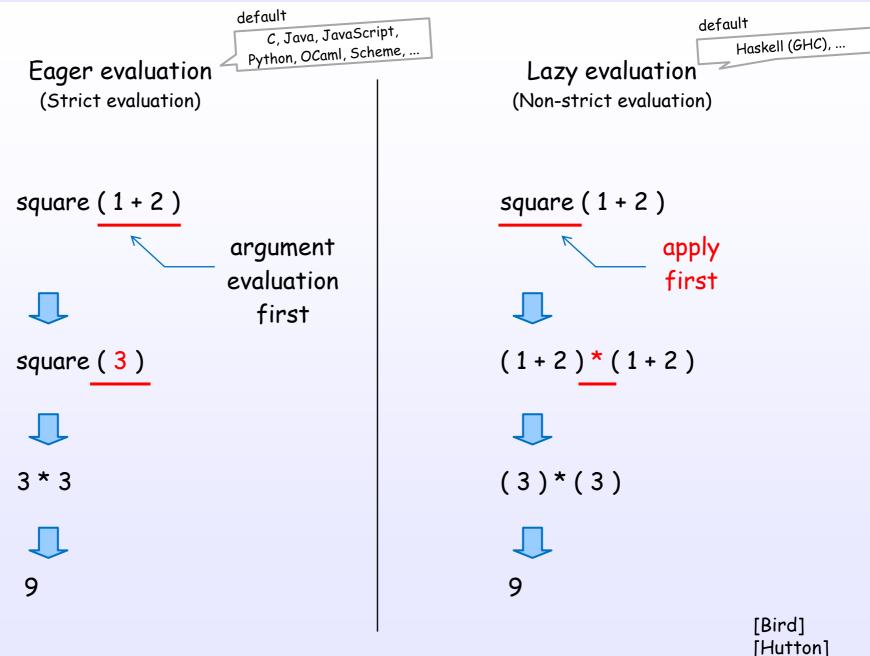
Evariation strategies and order

$$a(bc) + d(e(fg))$$

order

[Bird] [Hutton]

Simple example of both evaluations



Simple example of both evaluations

Eager evaluation (Strict evaluation)

square (1+2)



square (3)



argument evaluated

3 * 3



9

Lazy evaluation (Non-strict evaluation)

square (1 + 2)



(1+2)*(1+2)



(3)*(3)



9

argument evaluation delayed!

[Bird] [Hutton]

References: [1]

Expressions in Haskell

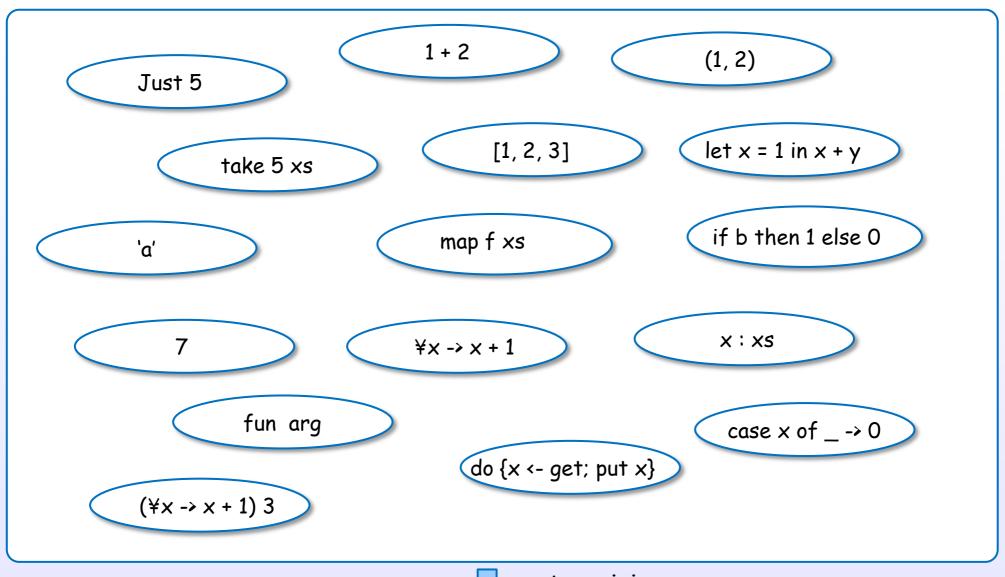
An expression denotes a value

An expression

[HR2010] [Bird, Chapter 2]

There are many expressions in Haskell

Expressions



categorizing

[HR2010]

[Bird, Chapter 2] References: [1]

Expression categories in Haskell

lambda abstraction

let expression

$$\forall x \rightarrow x + 1$$

let x = 1 in x + y

conditional

case expression

do expression

if b then 1 else 0

case x of $_ \rightarrow 0$

do {x <- get; put x}

general constructor, literal and some forms

7

[1, 2, 3]

(1, 2)

'α'

x : xs

Just 5

function application

take 5 xs

1 + 2

map f xs

fun arg

[HR2010] [Bird, Chapter 2

Specification is defined in Haskell 2010 Language Report

Haskell 2010 Language Report, Chapter 3 Expressions [1]

```
\rightarrow infixexp :: [context =>] type
                                                                          (expression type signature)
exp
                   infixexp
infixexp
             \rightarrow lexp qop infixexp
                                                                          (infix operator application)

    infixexp

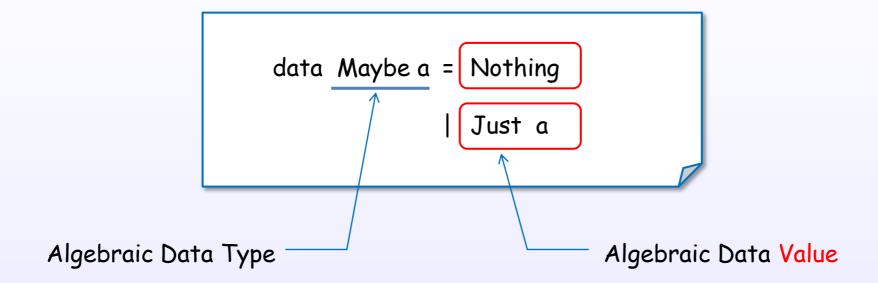
                                                                          (prefix negation)
                   lexp
             (lambda abstraction, n > 1)
lexp
                  let decls in exp
                                                                          (let expression)
                   if exp [;] then exp [;] else exp
                                                                          (conditional)
                   case exp of { alts }
                                                                          (case expression)
                   do { stmts }
                                                                          (do expression)
                   fexp
                                                                          (function application)
fexp
                   [fexp] aexp
                                                                          (variable)
                   qvar
aexp
                                                                          (general constructor)
                   qcon
                   literal
                                                                          (parenthesized expression)
                   (exp)
                   (exp_1, \ldots, exp_k)
                                                                          (tuple, k \geq 2)
                   [exp_1, \ldots, exp_k]
                                                                          (list, k > 1)
                   [exp_1 [, exp_2] .. [exp_3]]
                                                                          (arithmetic sequence)
                   [exp \mid qual_1, \ldots, qual_n]
                                                                          (list comprehension, n \ge 1)
                   ( infixexp qop )
                                                                          (left section)
                   ( qop_{\langle - \rangle} infixexp )
                                                                          (right section)
                   qcon \{ fbind_1, \dots, fbind_n \}
                                                                          (labeled construction, n > 0)
                   aexp_{(acon)} \{ fbind_1, \dots, fbind_n \}
                                                                         (labeled update, n \geq 1)
```



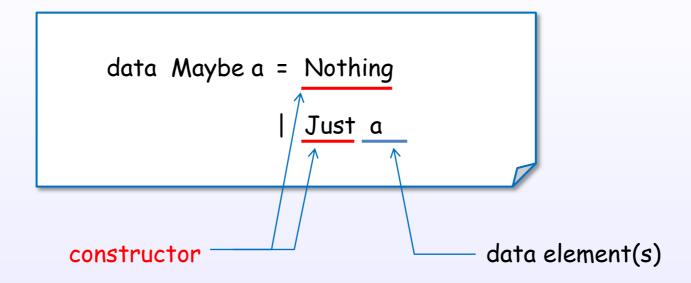
Constructor

Constructor is one of the key elements to understand WHNF and lazy evaluation.

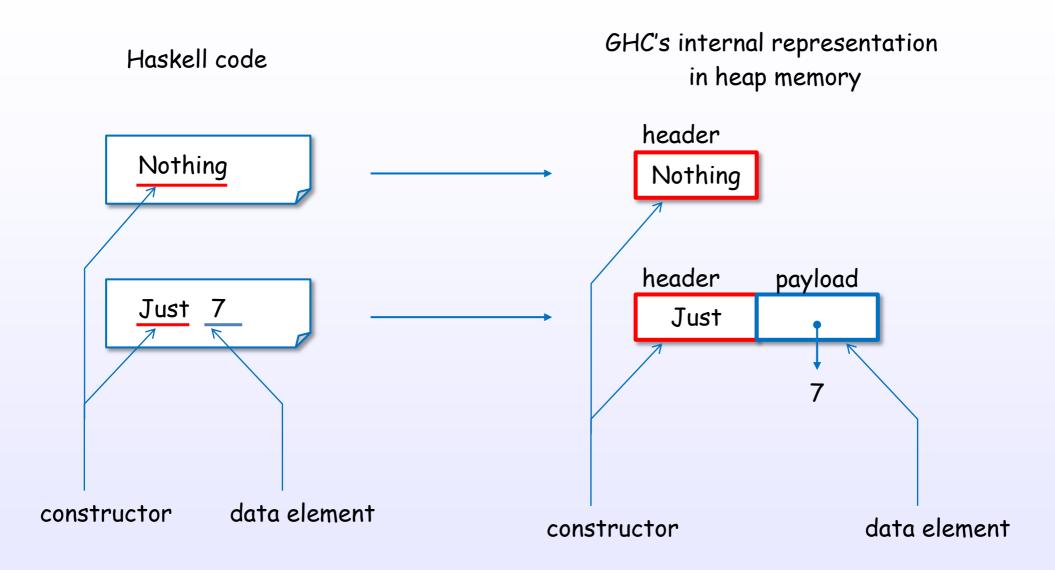
data文で宣言する代数的データ型とその値



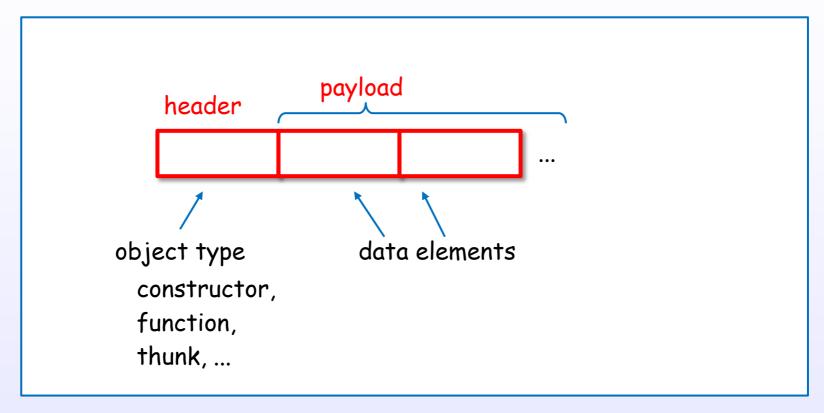
Constructorはdata文で宣言する代数的データ値



Constructorの内部表現

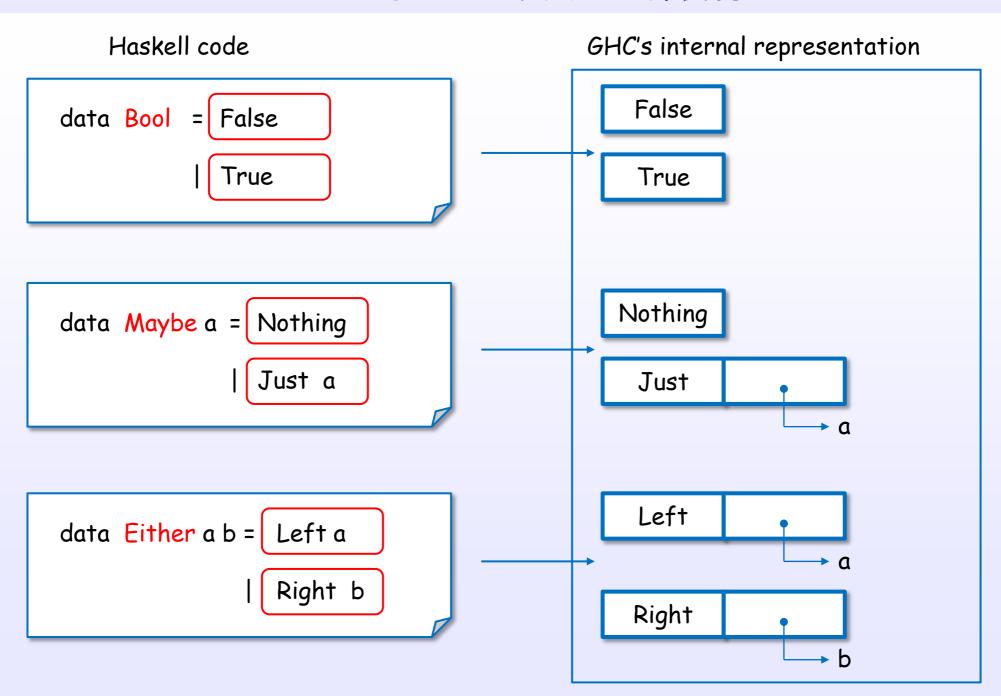


Constructorは統一内部表現で表現される



in heap memory, stack, registers or static memory

いろいろなコンストラクタと内部表現



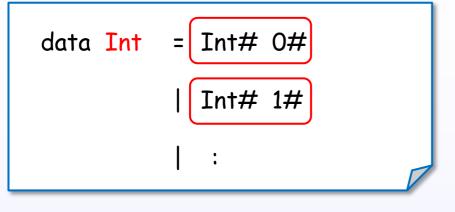
基本データ型も実はコンストラクタで構成されている

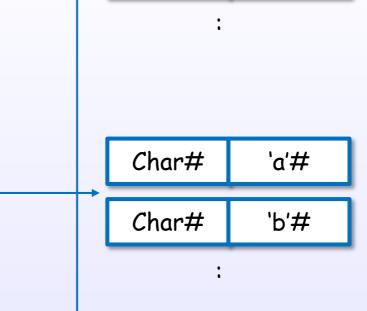
Haskell code

GHC's internal representation

0#

1#





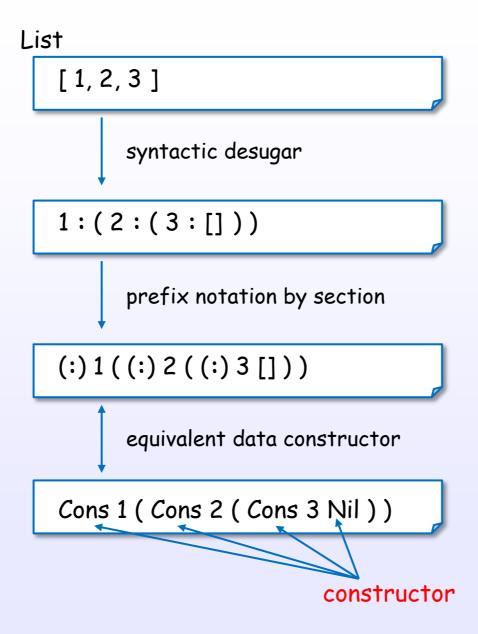
Int#

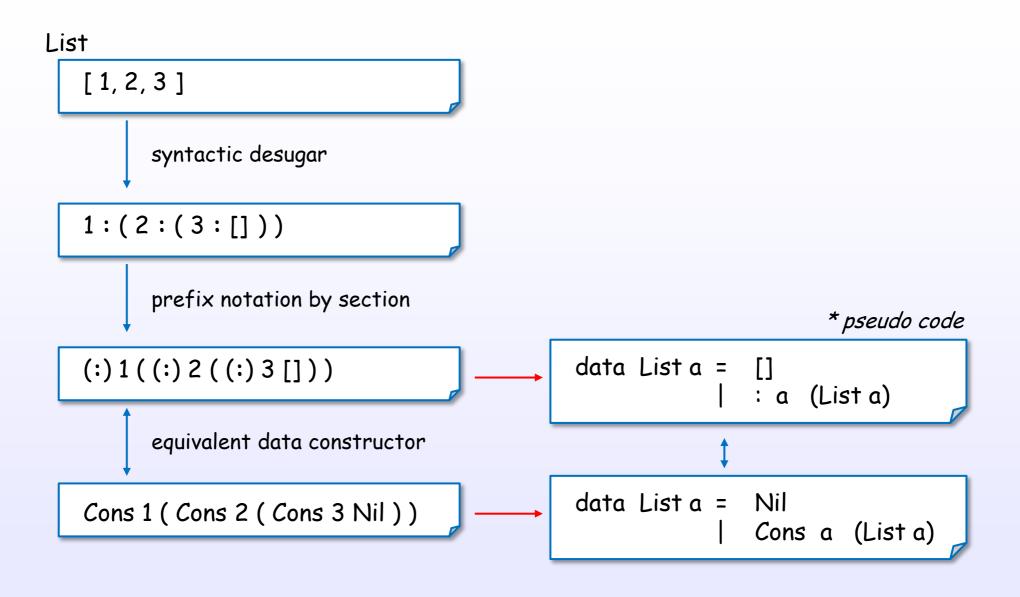
Int#

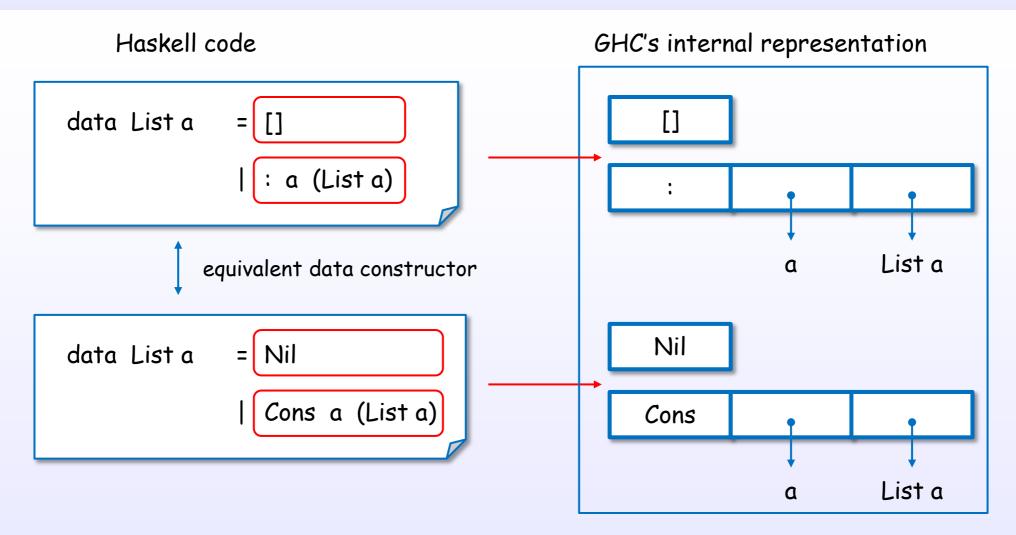
data Char = Char# 'a'#

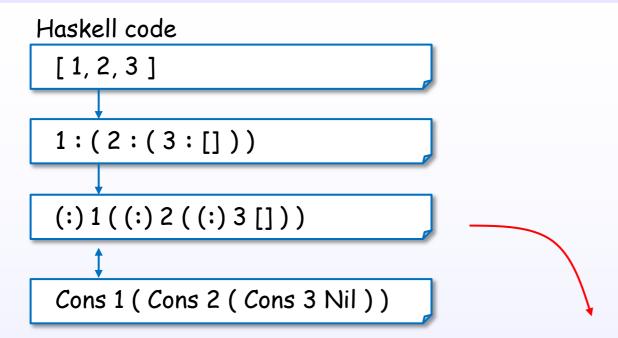
| Char# 'b'#

| :

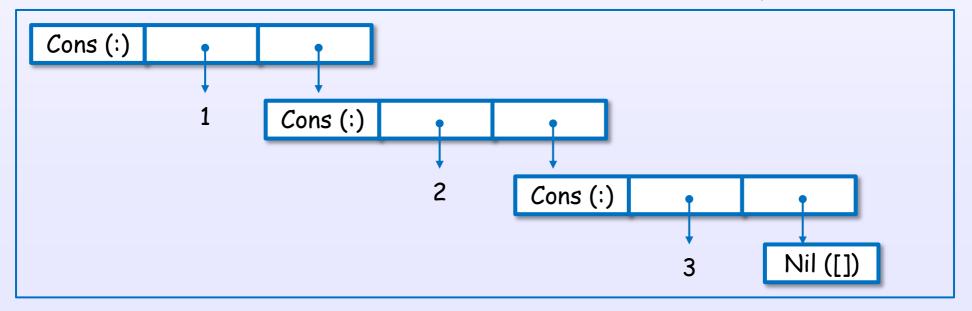




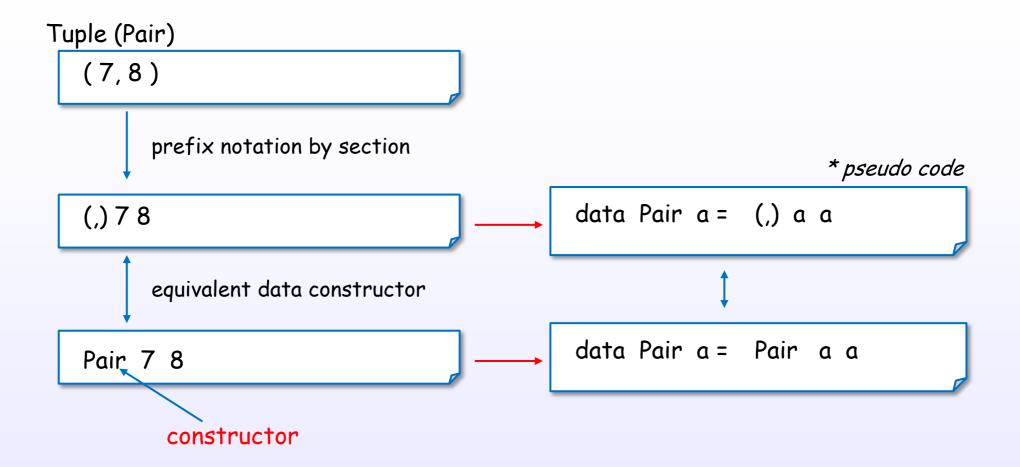




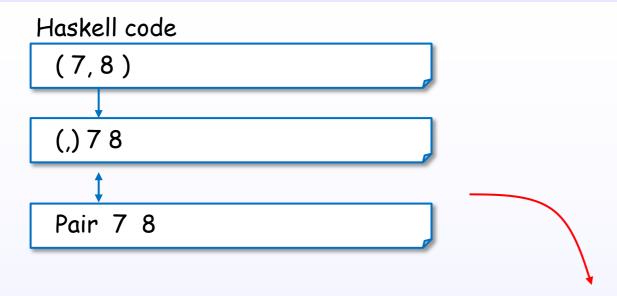
GHC's internal representation



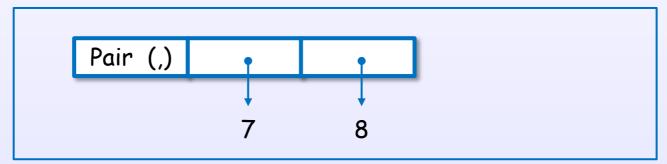
タプルも実はコンストラクタで構成されている



タプルも実はコンストラクタで構成されている



GHC's internal representation



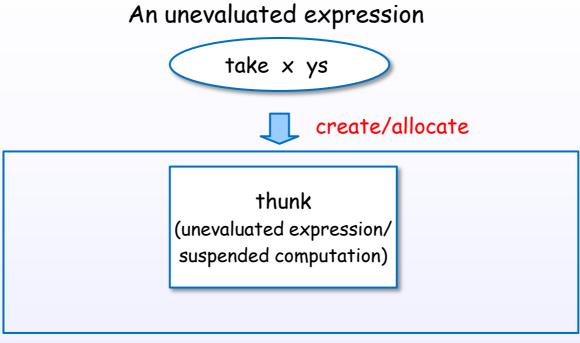


Thunk

thunk
(unevaluated expression/
suspended computation)

A thunk is an unevaluated expression in heap memory.

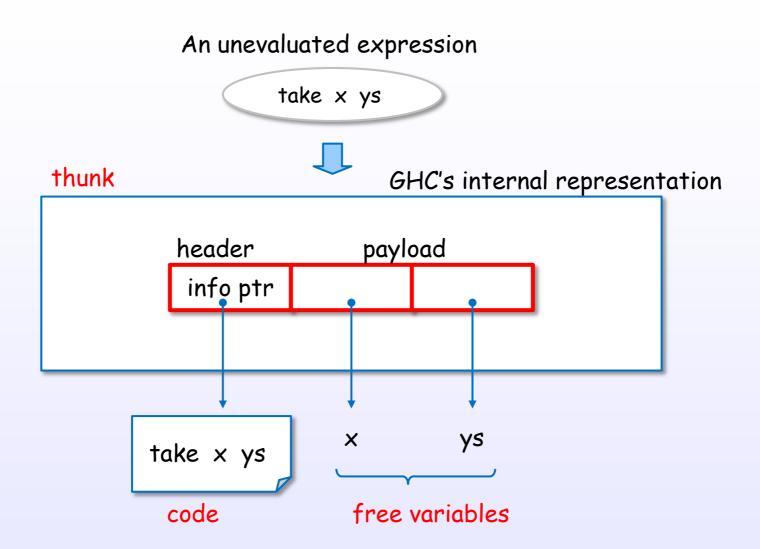
Thunk



in heap memory

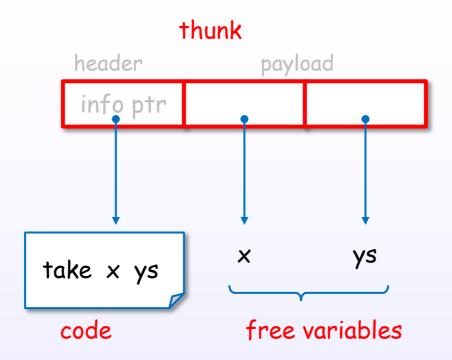
A thunk is created for an unevaluated expression.

Thunkの内部表現



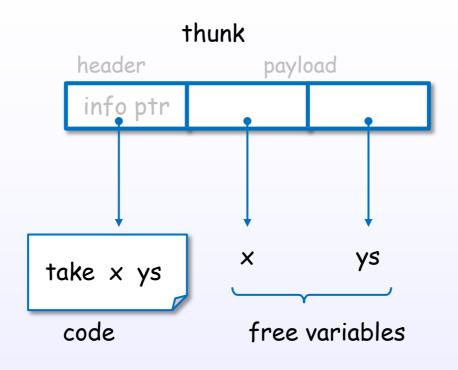
A thunk is represented with header(code) + payload(free variables).

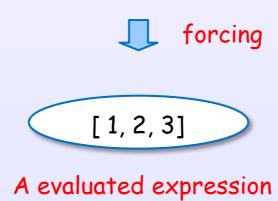
Thunkは、codeとfree variablesをパッケージ化したもの



A thunk is a package of code + free variables.

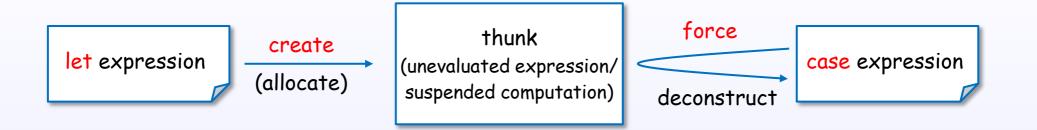
Thunkは、forcing要求により評価される





let, case expression

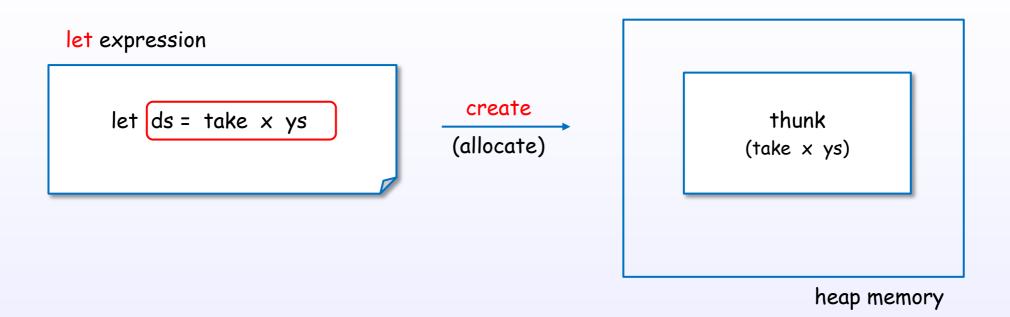
let/case expressions and thunk



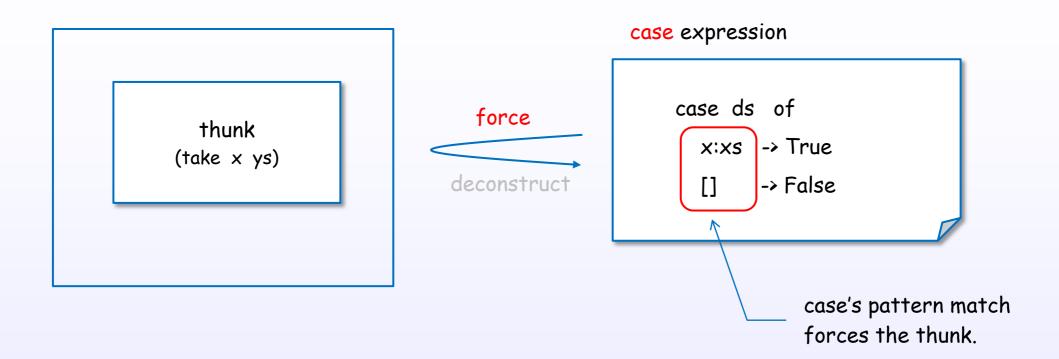
A let expression may create a thunk.

A case expression forces and deconstructs the thunk.

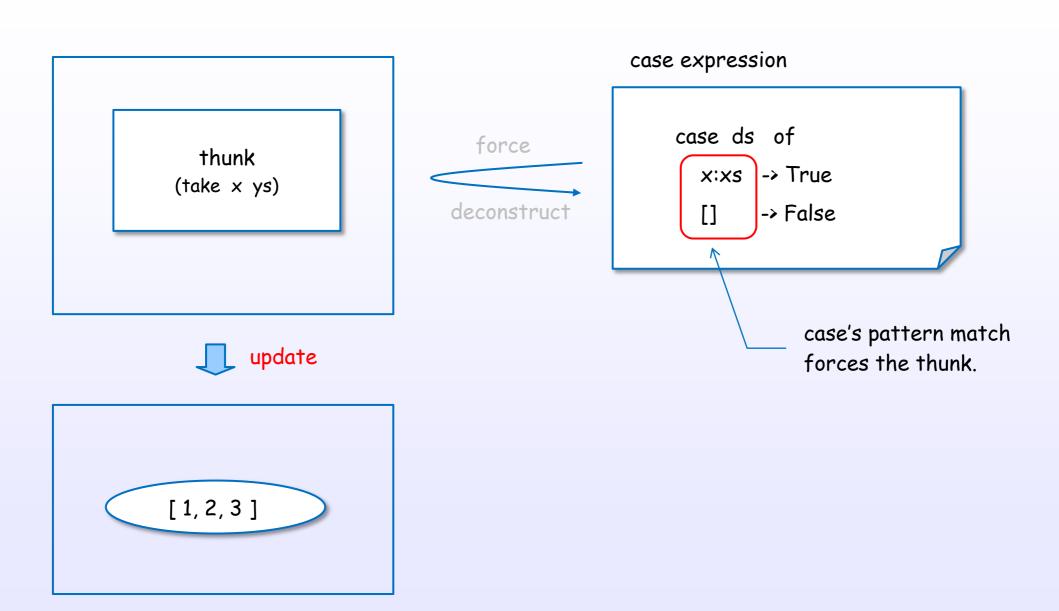
A let expression creates a thunk



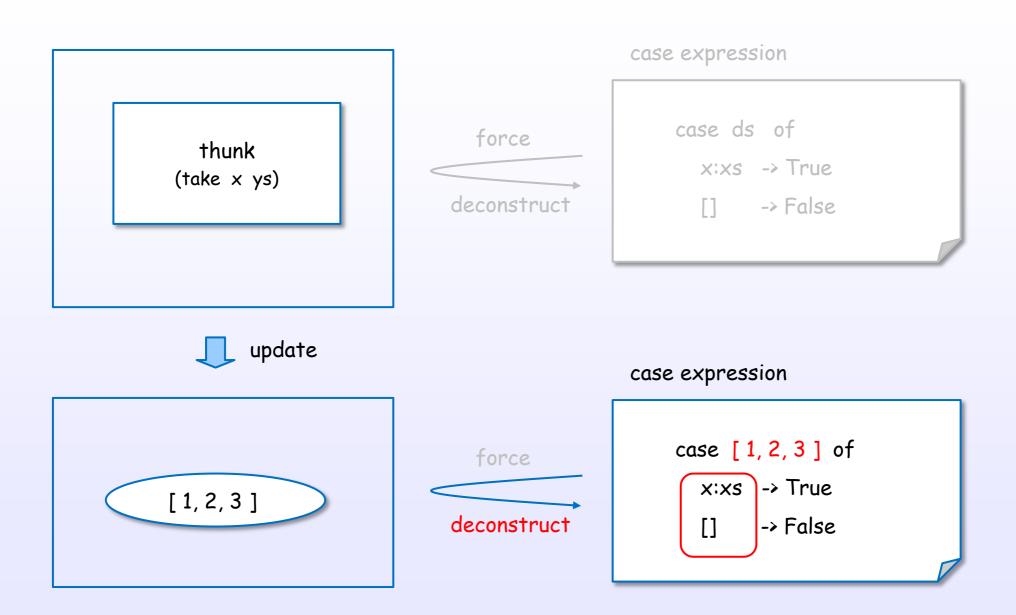
A case expression forces a thunk



A case expression forces a thunk

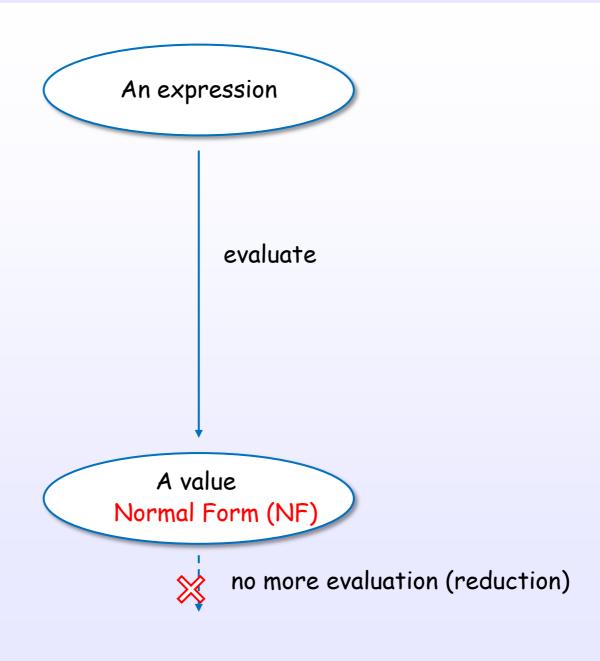


A case expression forces a thunk



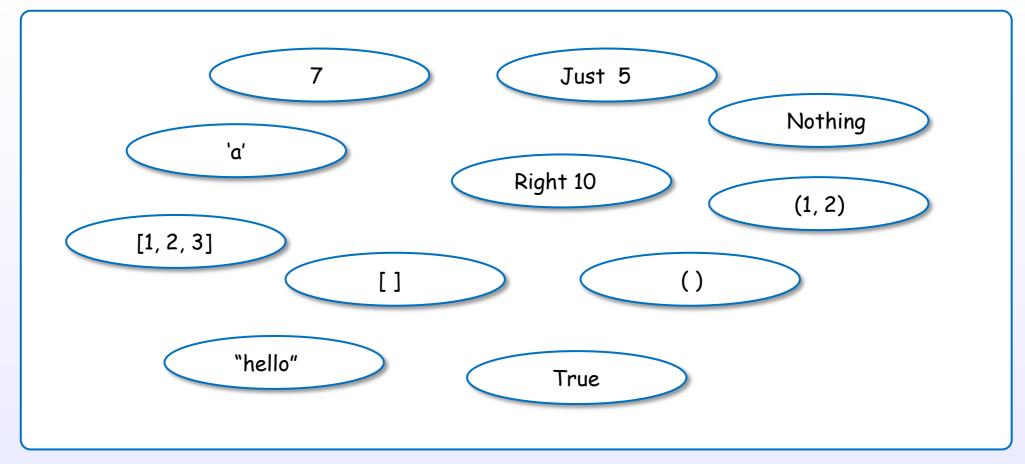


Normal form は、これ以上評価できない値

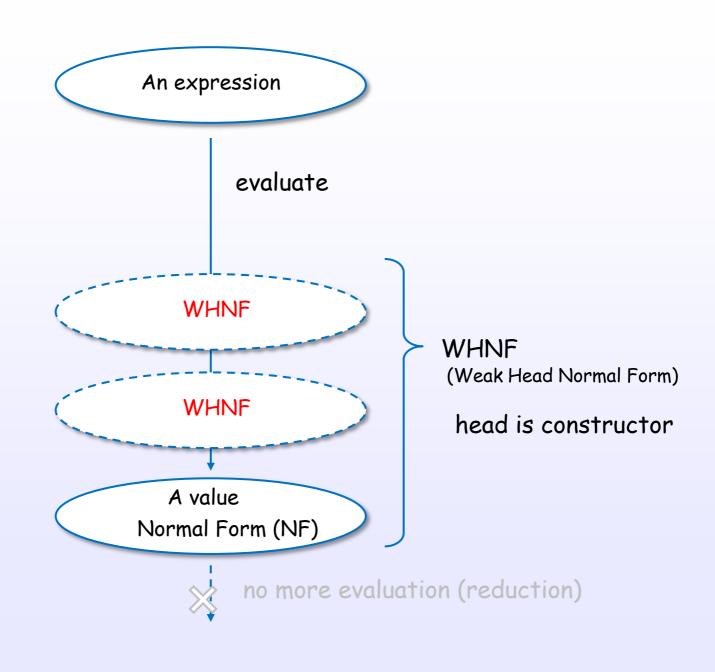


Examples of normal form (NF)

Normal Forma (NF)

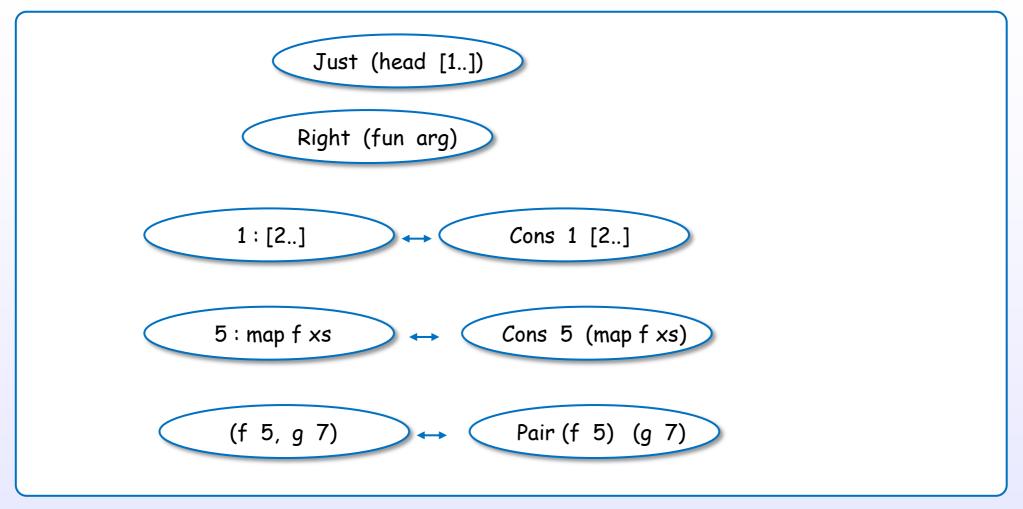


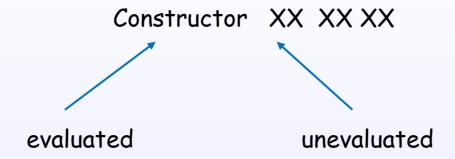
Weak Head Normal form は、少なくとも先頭が評価された式

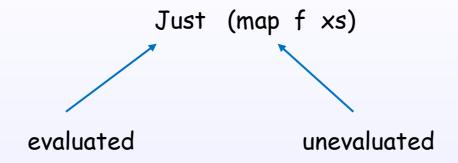


Examples of weak head normal form (WHNF)

Weak Head Normal Forma (WHNF)







前頁の、heap objectイメージ

[4]

normal form: an expression without an redexes

head normal form:

an expression where the top level (head) is neither a redex NOR a lambda abstraction with a reducible body

weak head normal form: an expression where the top level (head) isn't a redex

[Terei]

[4]

evaluation strategies:
call-by-value: arguments evaluated before function entered (copied)
call-by-name: arguments passed unevaluated
call-by-need: arguments passed unevaluated but an expression is only
evaluated once (sharing)

no-strict evaluation Vs. lazy evaluation:

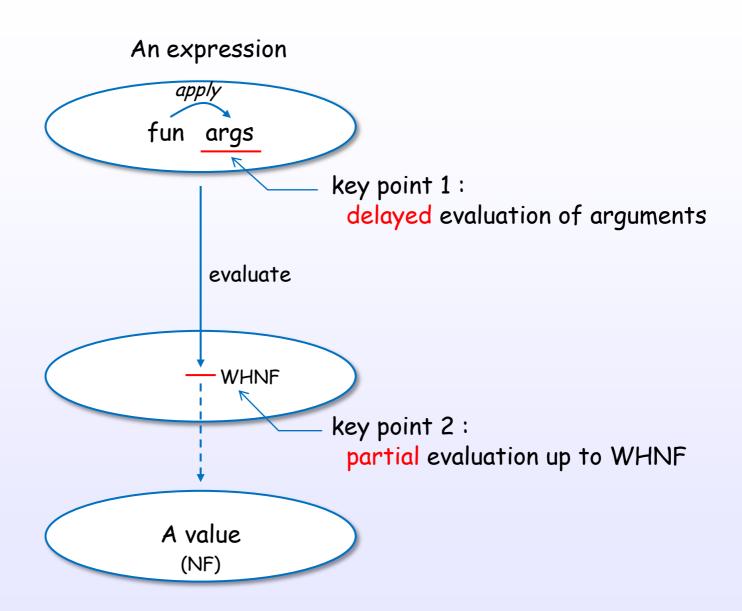
non-strict: Includes both call-by-name and call-by-need, general term for evaluation strategies that don't evaluate arguments before entering a function

lazy evaluation: Specific type of non-strict evaluation. Uses call-by-need (for sharing).

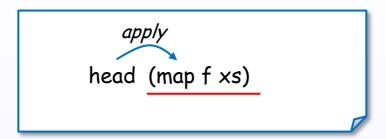
[Terei]

Evaluation in Haskell (GHC)

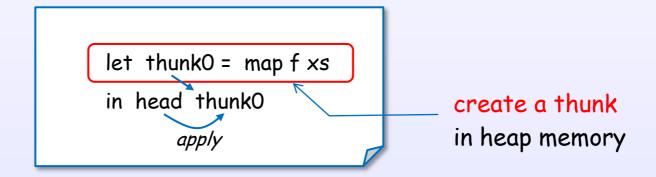
Key concept of Haskell's lazy evaluation



key point 1: delayed evaluation of arguments

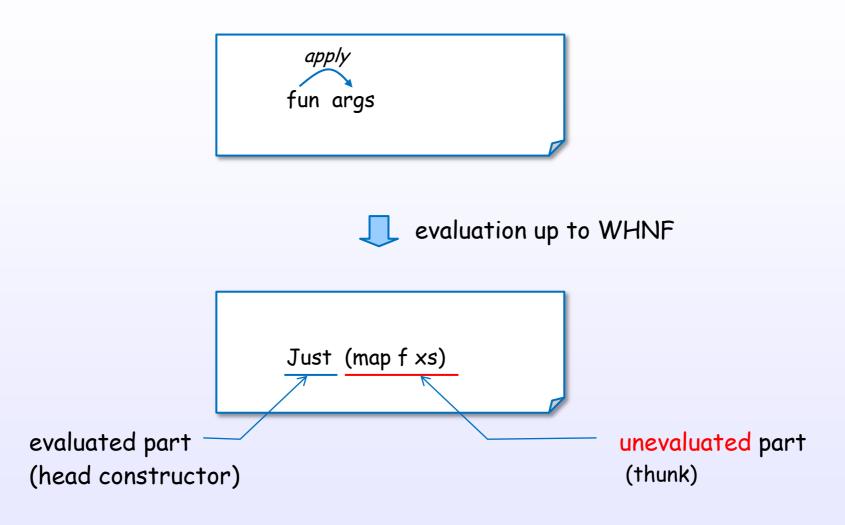


internal transformation by GHC



GHC implements lazy evaluation using the thunk. Evaluation of arguments is delayed with the thunk.

key point 2: partial evaluation up to WHNF



GHC can partially evaluate a expression.

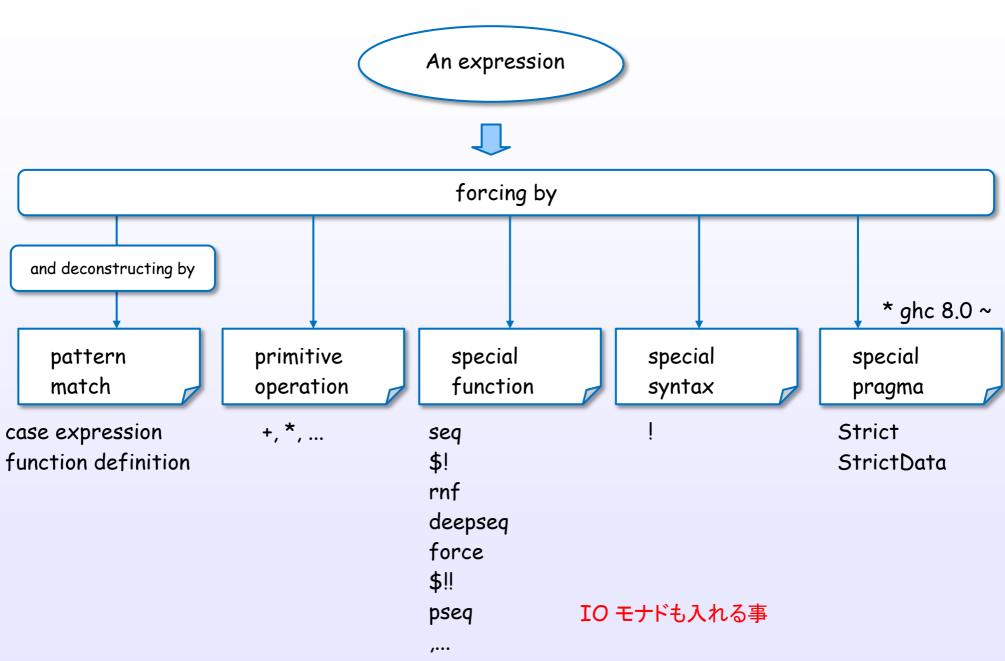
Constructor can hold an unevaluated expression (a thunk).

Pattern match

[CIS194]

Control the evaluation in Haskell

How to drive evaluation



References: [1]

Examples of evaluation steps

Example of foldl (non-strict)

foldl (+) 0 [1 .. 100]



foldl (+) (0 + 1) [2 .. 100]

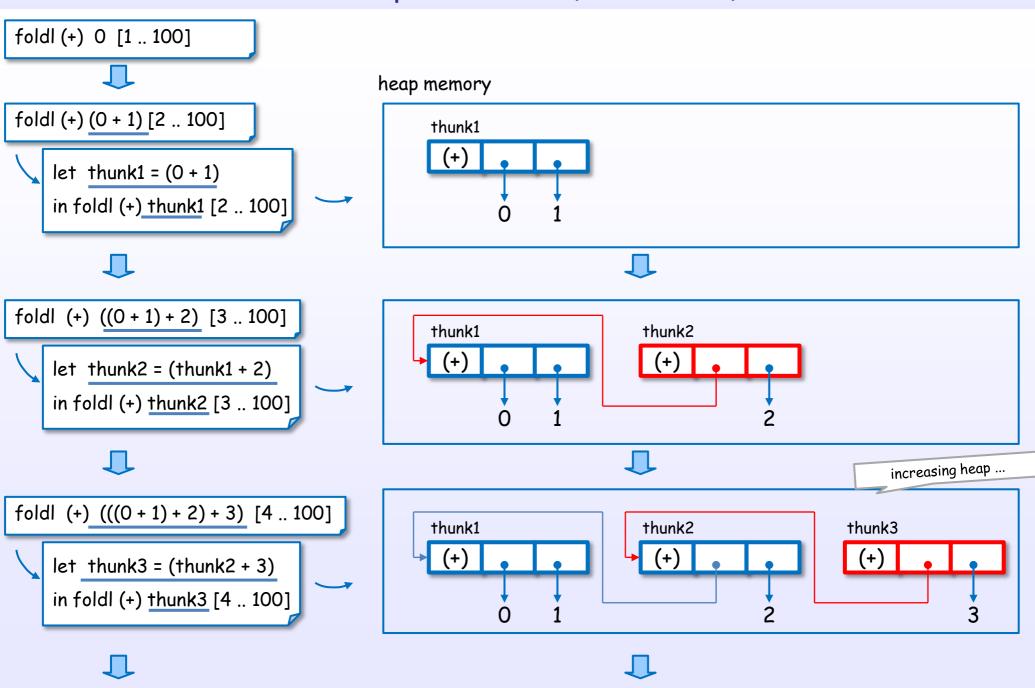


foldl (+) ((0+1)+2) [3 .. 100]



foldl (+) (((0+1)+2)+3) [4 .. 100]

Example of foldl (non-strict)



References: [1]

Example of foldl' (strict)

foldl'(+) 0 [1..100]



foldl' (+) (0 + 1) [2 .. 100]



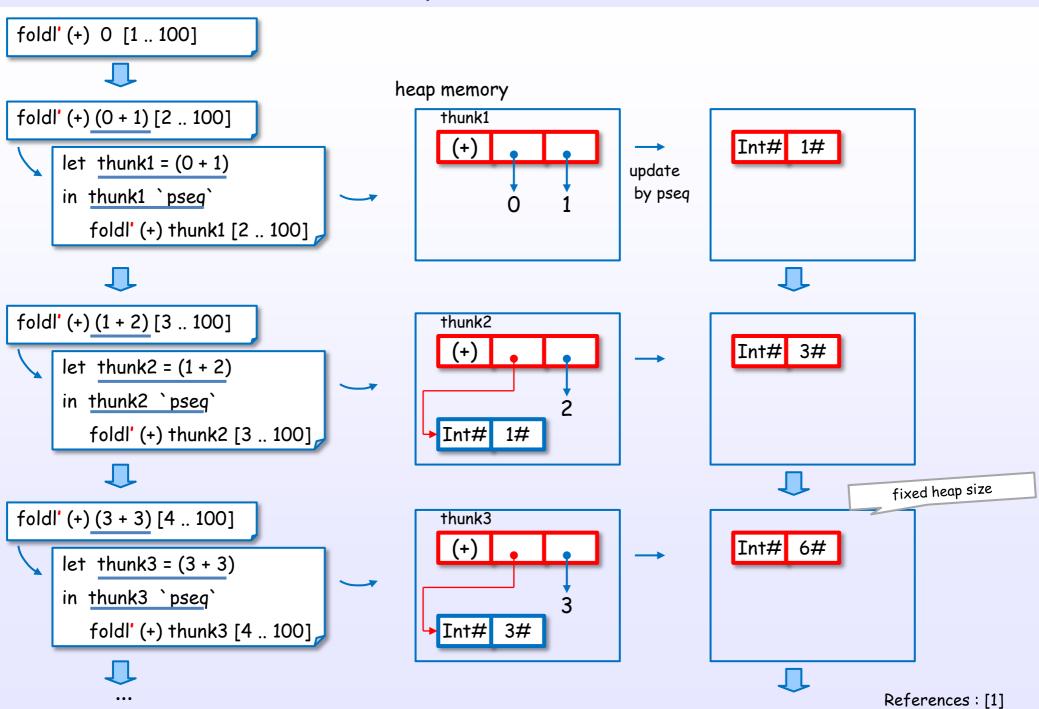
foldl' (+) (1 + 2) [3 .. 100]



foldl' (+) (3 + 3) [4 .. 100]



Example of foldl' (strict)

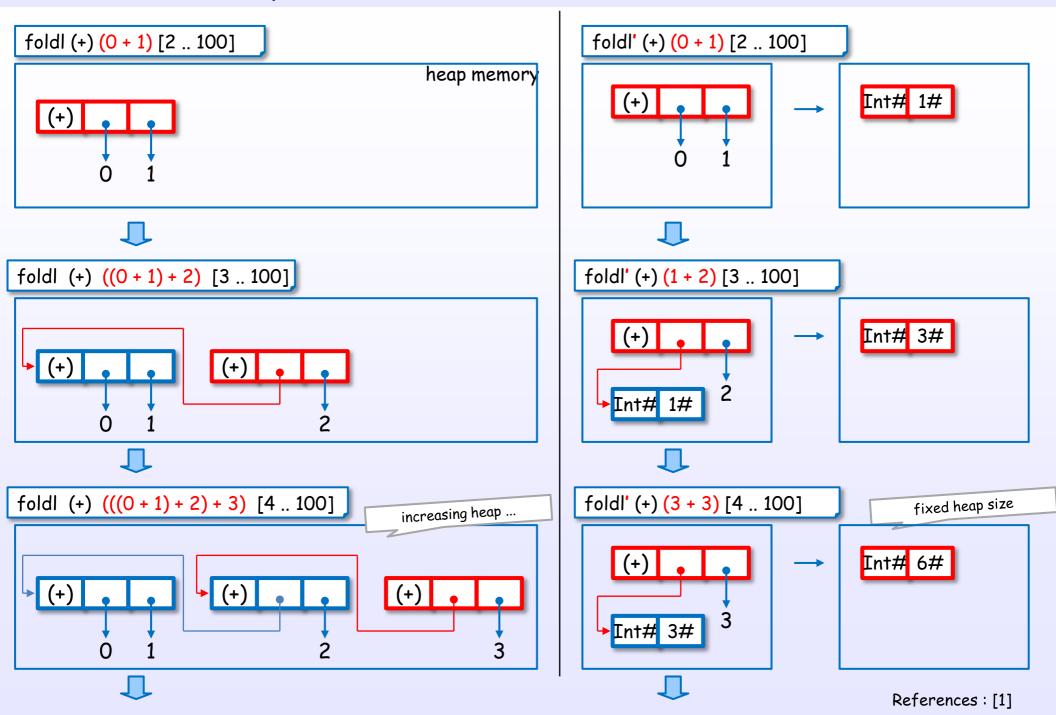


Example of foldl (non-strict) and foldl' (strict)

foldl' (+) (0 + 1) [2 .. 100] foldl (+) (0 + 1) [2 .. 100] foldl (+) ((0 + 1) + 2) [3 .. 100] foldl' (+) (1 + 2) [3 .. 100] foldl (+) (((0 + 1) + 2) + 3) [4 .. 100] foldl' (+) (3 + 3) [4 .. 100]



Example of foldl (non-strict) and foldl' (strict)



Implementation in GHC

Tree, Graph

a expression

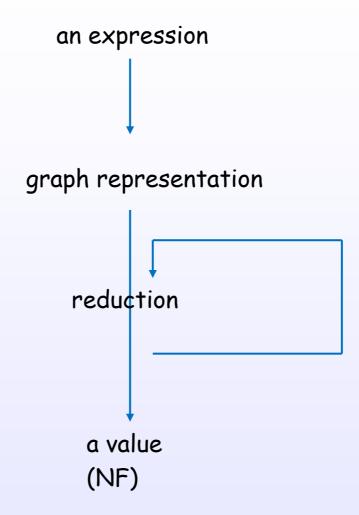
AST

Tree Graph

Shared Term

Lazy

evaluation, reduction



Expressions examples

STG heap objects

language Just 5

implementation heap object

Layer

Non-strictness

$$f \perp = \perp$$

Lazy evaluation

Graph reduction

STG machine

Layer

Haskell semantics take 5 [1..10]

internal representation graph

STG semantics heap object

STG machine



Bottom

domain

co-domain

defined

undefined

f \perp = \perp

[Bird, Chapter 2]

Strictness, Bottom

[Bird, Chapter 2]

- [1] Haskell 2010 Language Report https://www.haskell.org/definition/haskell2010.pdf
- [2] The Glorious Glasgow Haskell Compilation System (GHC user's guide) https://downloads.haskell.org/~ghc/latest/docs/users_guide.pdf
- [3] Thinking Functionally with Haskell (IFPH 3rd edition) http://www.cs.ox.ac.uk/publications/books/functional/
- [4] Types and Programming Languages https://mitpress.mit.edu/books/types-and-programming-languages
- [5] A Haskell Compiler http://www.scs.stanford.edu/11au-cs240h/notes/ghc-slides.html http://www.scs.stanford.edu/11au-cs240h/notes/ghc-slides.html#(11)
- [6] Being Lazy with Class http://www.seas.upenn.edu/~cis194/lectures/06-laziness.html
- [7] The Incomplete Guide to Lazy Evaluation (in Haskell) https://hackhands.com/guide-lazy-evaluation-haskell/
- [8] Programming in Haskell https://www.cs.nott.ac.uk/~gmh/book.html
- [9] Parallel and Concurrent Programming in Haskell http://chimera.labs.oreilly.com/books/123000000929/ch02.html
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https://en.wikibooks.org/wiki/Haskell/Graph_reduction

[18] Haskell/Graph reduction

- [19] Implementing lazy functional languages on stock hardware: the Spineless Tagless G-machine Version 2.5 http://research.microsoft.com/en-us/um/people/simonpj/Papers/spineless-tagless-gmachine.ps.gz
- [20] Making a Fast Curry Push/Enter vs Eval/Apply for Higher-order Languages http://research.microsoft.com/en-us/um/people/simonpj/papers/eval-apply/
- [21] I know kung fu: learning STG by example https://ghc.haskell.org/trac/ghc/wiki/Commentary/Compiler/GeneratedCode
- [22] GHC Commentary: The Layout of Heap Objects https://ghc.haskell.org/trac/ghc/wiki/Commentary/Rts/Storage/HeapObjects
- [23] GHC Commentary: Strict & StrictData https://ghc.haskell.org/trac/ghc/wiki/StrictPragma
- [24] GHC illustrated http://takenobu-hs.github.io/downloads/haskell_ghc_illustrated.pdf

Lazy,... 1212