

## Assignment 4

3 a)  $O(n^2)$  b) same for all cases  $O(n^2)$

c) No, because we don't have break points  
we need to compare all values in the array

5.

Let  $C(n)$  be the number of comparisons we need to sort an integer array using sortR.

placeLargest and placeSmallest have the same complexity for the same size of  $n$  (end-start+1)

Let  $D(n)$  be the number of comparisons to place the smallest/largest value at the left/right position

$$D(n) = n - 1$$

$$C(0) = 0$$

$$C(1) = 0$$

$$C(2) = D(2) + D(1) + C(0) = 1 + 0 + 0 = 1$$

$$C(3) = D(3) + D(2) + C(1) = 2 + 1 + 0 = 3 \quad 2(n-4)-3$$

$$C(4) = D(4) + D(3) + C(2) = 3 + 2 + 1 = 6. \quad 2n-11$$

$$C(5) = D(5) + D(4) + C(3) = 4 + 3 + 3 = 10$$

$$C(6) = D(6) + D(5) + C(4) = 5 + 4 + 6 = 15$$

$$C(n) = C(n-1) + (n-1)$$

$$= (n-1) + (n-2) + C(n-2)$$

$$= (n-1) + (n-2) + (n-3) + (n-4) + \dots + 3 + 2 + 1$$

$$= \sum_{i=1}^{n-1} i = \frac{(n-1)(n-2)}{2} = \frac{1}{2}n^2 - \frac{3}{2}n + 1 \Rightarrow O(n)$$

6. a) there is no worst/best/average case because we don't exit the program until all values are sorted

b) No, same reason as above.