

**1**

- a) It will be a weakly connected directed graph.

The direction is implied by one-way/two-way roads and it's weakly connected because there cannot be a vertex without an edge as vertices are intersections.

- b) Suppose, there are  $o$  odd-degree vertices and  $e$  even-degree vertices.

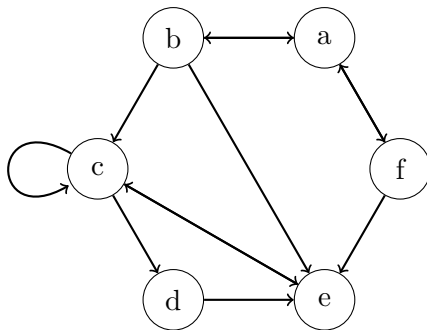
Therefore we have the following equations.

$$\begin{cases} 3o + 4e = 19 \times 2 \\ o + e = 11 \end{cases}$$

By solving them we find  $o = 6$  and  $e = 5$ .

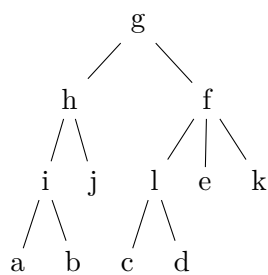
**2**

- c) Graph from the given adjacency matrix:



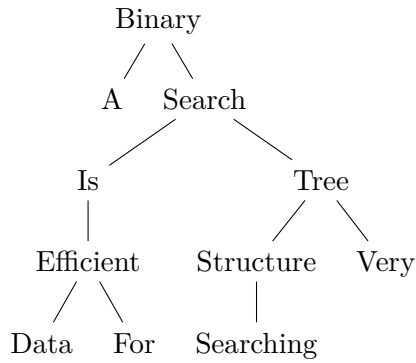
**3**

- a) Tree following the given info:



**4**

- a) Binary search tree:



- b) A, Data, For, Efficient, Is, Searching, Structure, Very, Tree, Search, Binary
- c) Nope; A is leaf at height 2 when the height of the tree is 4.

## 5

- b) Possible combinations of outcome are (1 heads, 5 tails) or (3 heads, 3 tails) or (5 heads, 1 tails). So the number of possible outcomes is 3
- c) First we take the possible combinations of courses that a student has to finish, the number of possible combinations of such courses is  $C(n_1, r_1) \times C(n_2, r_2)$ .

For every such combination there can be different order of completion. The number of ways  $r_1 + r_2$  courses can be finished  $= (r_1 + r_2)!$ .

Therefore the total number of ways a student can complete the courses  $= C(n_1, r_1) \times C(n_2, r_2) \times (r_1 + r_2)!$