

1. Implement a sequence recognizer using T or J-K flip-flops that can detect the "1010" subsequences, while overlap will be supported between detected subsequences.

For this design:

- Draw the state diagram by using gray code for assigning state.
- Draw the state table with output and Flip Flop inputs.
- Minimize the functions of output and Flip Flop inputs.
- Draw the circuit diagram using the block diagram of Flip Flops and basic gates.
- For an input bit sequence of $x = \text{"101010001101001010"}$, what will be the output bit sequence?

[1.5]

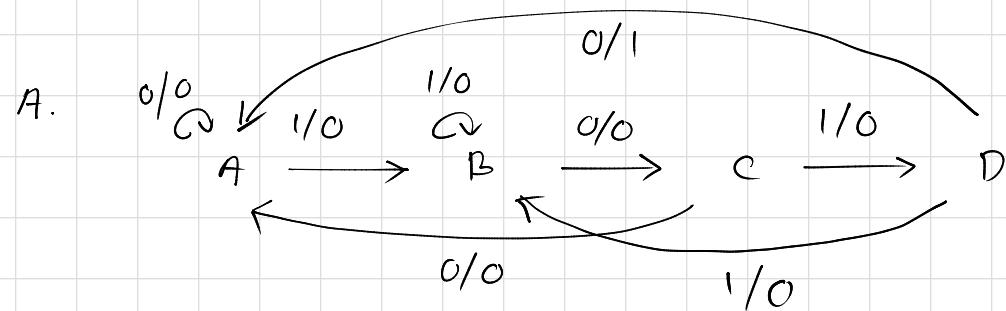
[2]

[2]

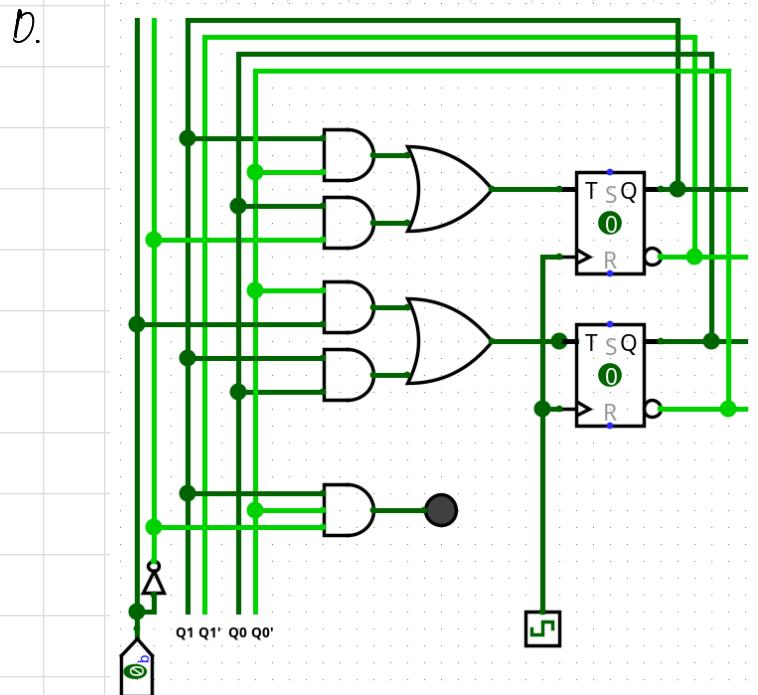
[1.5]

[1]

Disclaimer: Benzin's brain can only consider overlap of a single bit. Therefore no overlap in 1010.



	next state $x=0$	output $x=0$	next state $x=1$	output $x=1$
A (00)	A	0	B	0
B (01)	C	0	B	0
C (11)	A	0	D	0
D (10)	A	1	B	0



B.

$Q_1 Q_0 x$	$Q_1 Q_0 y$	$T_1 T_0$
0 0 0	0 0 0	0 0
0 0 1	0 1 0	0 1
0 1 0	1 1 0	1 0
0 1 1	0 1 0	0 0
1 0 0	0 0 1	1 1 0
1 0 1	0 1 0	1 1 1
1 1 0	0 0 0	1 1 1
1 1 1	1 0 0	0 1 1

c. $T_1 = Q_1 \bar{Q}_0 + Q_0 \bar{x}$

$Q_1 x$	00	01	11	10
Q_0	0	1	1	0
\bar{x}	0	0	1	1

$T_0 = \bar{Q}_0 x + Q_1 Q_0$

$Q_1 x$	00	01	11	10
Q_0	0	1	1	0
\bar{x}	0	0	1	1

$y = Q_1 \bar{Q}_0 \bar{x}$

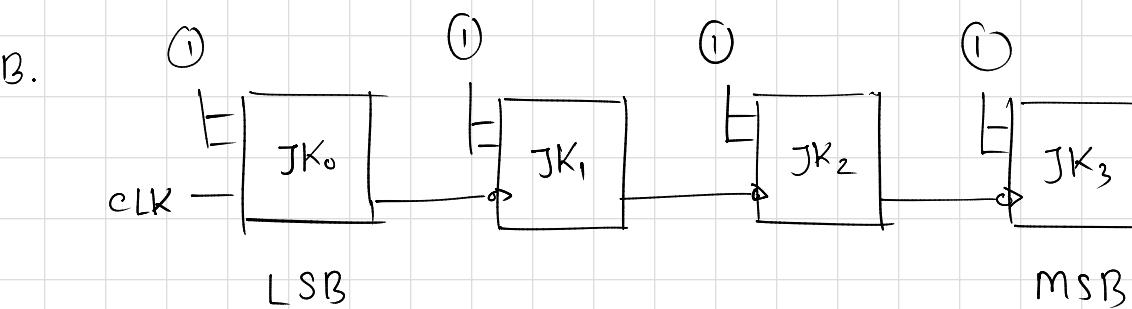
$Q_1 x$	00	01	11	10
Q_0	0	1	1	0
\bar{x}	0	0	1	1

E. input: 1 0 1 0 1 0 0 0 1 1 0 1 0 0 1 0 1 0
output: 0 0 0 1 0 0 0 0 0 0 0 0 1 0 0 0 0 0 1

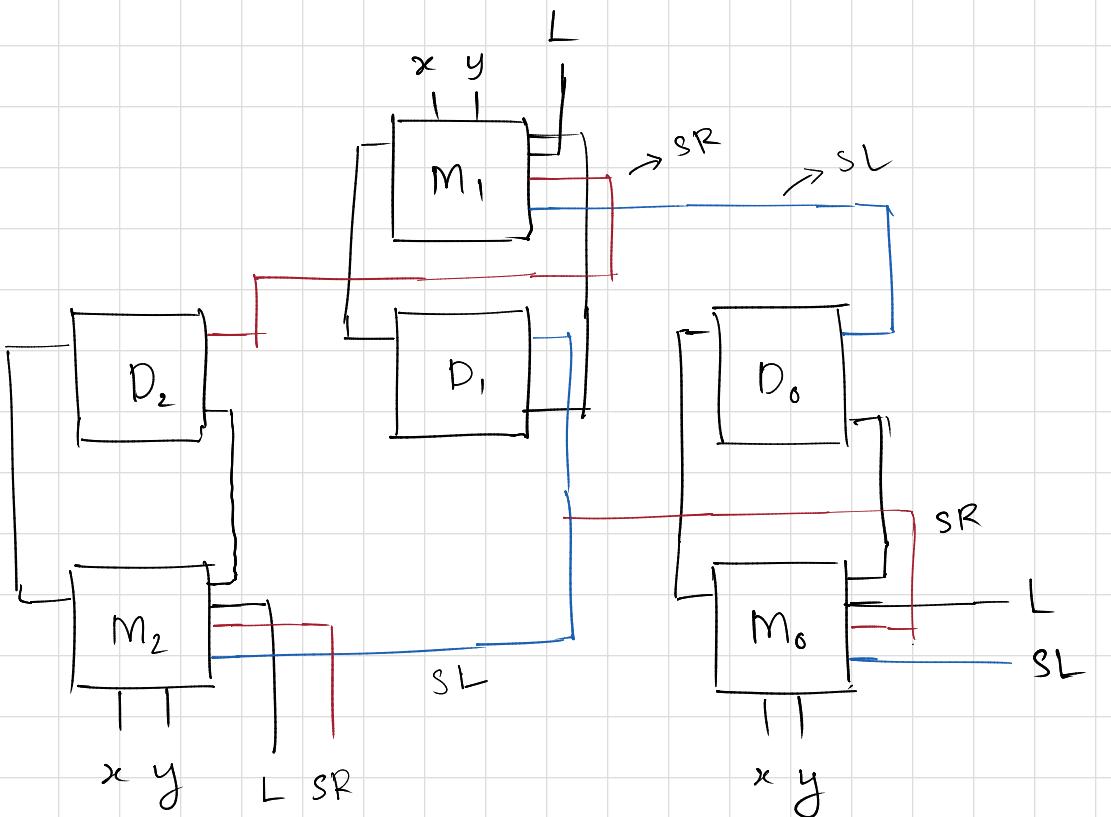
2. A. Design a 3-bit universal shift register with the functions given in the function table below. Here two control bits X and Y determine the mode of operation. Use D Flip Flops for your design [6]

X	Y	Operation
0	0	Toggle
0	1	Parallel Load
1	0	Shift Right
1	1	Shift Left

- B. Design a 4-bit asynchronous Downward Ripple Counter using negative edge J-K Flip Flops. [2]



A.



3. A sequential circuit has two D flip flops, one input X, and one output y is specified by the following input equations:

$$\begin{aligned}A(t+1) &= Ax \oplus B'x' \\B(t+1) &= (A' + B)x \\y(t+1) &= Ax' + (B' \oplus x)\end{aligned}$$

- A. Draw the logic diagram of the circuit.
B. Derive the state table.
C. Derive the state diagram.

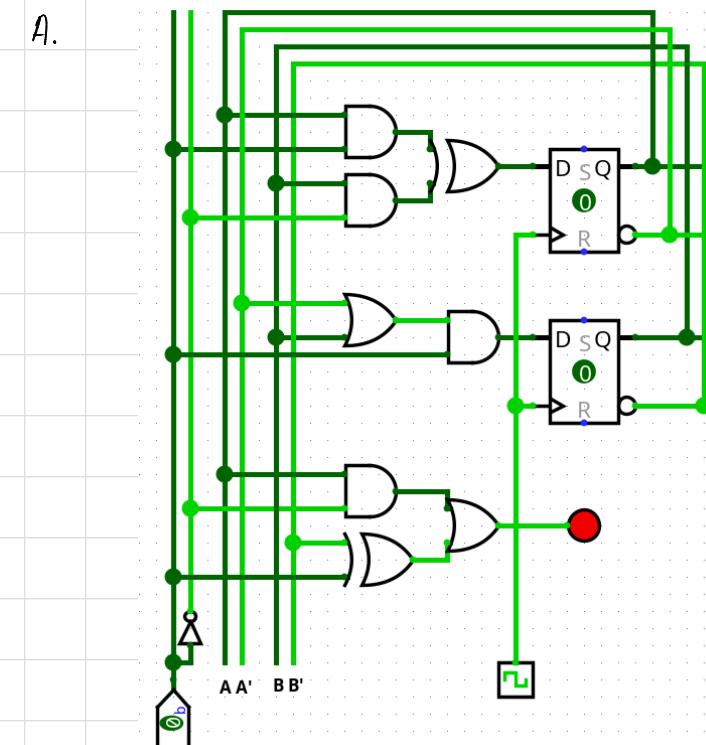
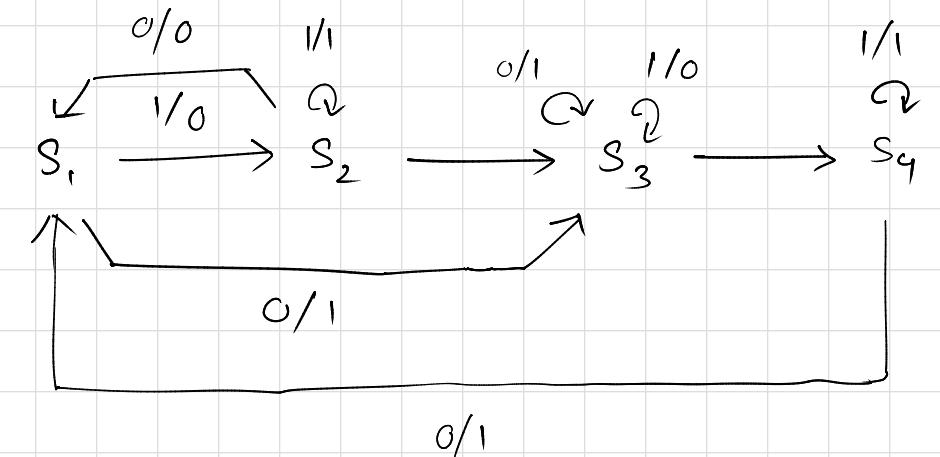
[2.5]
[3]
[2.5]

$$\begin{aligned}B. \quad A &= Ax \oplus \bar{B}\bar{x} \\&= \bar{A}x\bar{B}\bar{x} + Ax\bar{B}\bar{x} \\&= (\bar{A} + \bar{x})\bar{B}\bar{x} + Ax(B+x) \\&= \bar{A}\bar{B}\bar{x} + \bar{B}\bar{x} + ABx + Ax \\&= \bar{A}\bar{B}\bar{x} + A\bar{B}\bar{x} + \bar{A}\bar{B}\bar{x} + ABx + ABx + A\bar{B}x \\&= \bar{A}\bar{B}\bar{x} + A\bar{B}\bar{x} + ABx + A\bar{B}x \\&= \sum m(0, 4, 5, 7)\end{aligned}$$

$$\begin{aligned}B &= (\bar{A} + B)x \\&= \bar{A}x + Bx \\&= \bar{A}Bx + \bar{A}\bar{B}x + ABx + \bar{A}Bx \\&= \bar{A}\bar{B}x + \bar{A}Bx + ABx \\&= \sum m(1, 3, 7)\end{aligned}$$

$$\begin{aligned}Y &= A\bar{x} + (\bar{B} \oplus x) \\&= AB\bar{x} + A\bar{B}\bar{x} + Bx + \bar{B}\bar{x} \\&= AB\bar{x} + A\bar{B}\bar{x} + ABx + \bar{A}Bx + A\bar{B}\bar{x} + \bar{A}\bar{B}\bar{x} \\&= AB\bar{x} + A\bar{B}\bar{x} + ABx + \bar{A}Bx + \bar{A}\bar{B}\bar{x} \\&= \sum m(6, 4, 7, 3, 0) \\&= \sum m(0, 3, 4, 6, 7)\end{aligned}$$

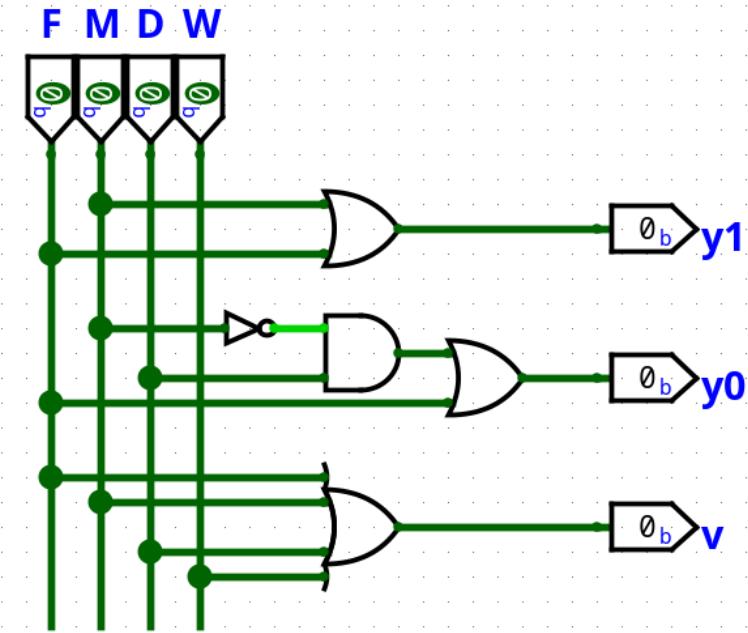
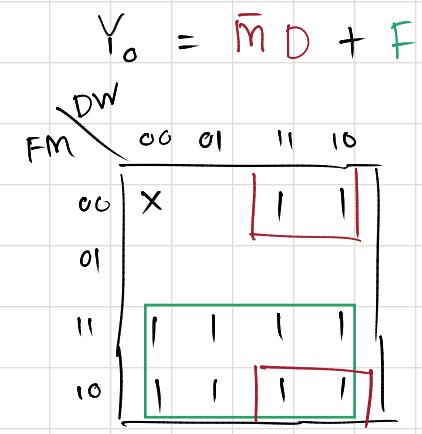
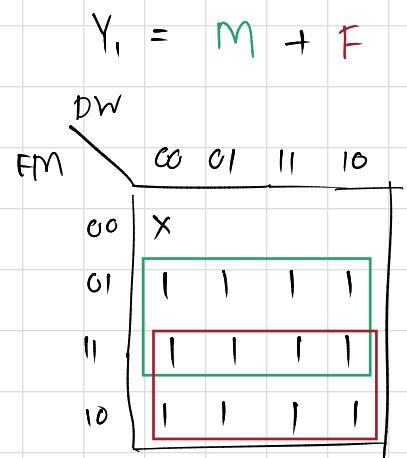
	next state	output
	$x = 0$	$x = 1$
$s_1 (00)$	s_3	s_2
$s_2 (01)$	s_1	s_2
$s_3 (10)$	s_3	s_3
$s_4 (11)$	s_1	s_4



4. You are tasked with designing an alarm system for a security application. The system has multiple sensors: Door Sensor, Window Sensor, Motion Sensor, and Fire Sensor. Design a priority encoder circuit that detects the highest priority event among these sensors. Assume that Fire Sensor has the highest priority, followed by Motion Sensor, Door Sensor, and Window Sensor.

[4]

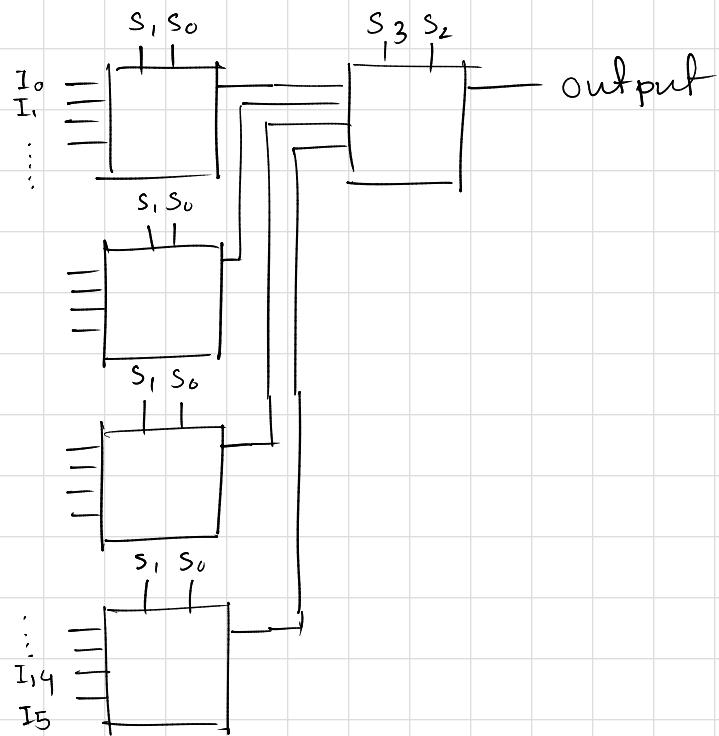
F	M	D	W	Y_1	Y_0	V
0	0	0	0	X	X	0
0	0	0	1	0	0	1
0	0	1	X	0	1	1
0	1	X	X	1	0	1
1	X	X	X	1	1	1



5. Design a 16:1 MUX using 4:1 MUX (as many as you require) only.

[4]

inputs: $I_0 - I_{15}$ selects: $S_0 - S_3$



6. Design an Octal to Binary Encoder.

- A. Draw the function table
B. Write the equations for the output of your encoder.
C. Draw the logic diagram of the encoder.

A.

I_7	I_6	I_5	I_4	I_3	I_2	I_1	I_0	Y_2	Y_1	Y_0
0	0	0	0	0	0	0	1	0	0	0
0	0	0	0	0	0	1	0	0	0	1
0	0	0	0	0	1	0	0	0	1	0
0	0	0	0	1	0	0	0	0	1	1
0	0	0	1	0	0	0	0	1	0	0
0	0	1	0	0	0	0	0	1	0	1
0	1	0	0	0	0	0	0	1	1	0
1	0	0	0	0	0	0	0	1	1	1

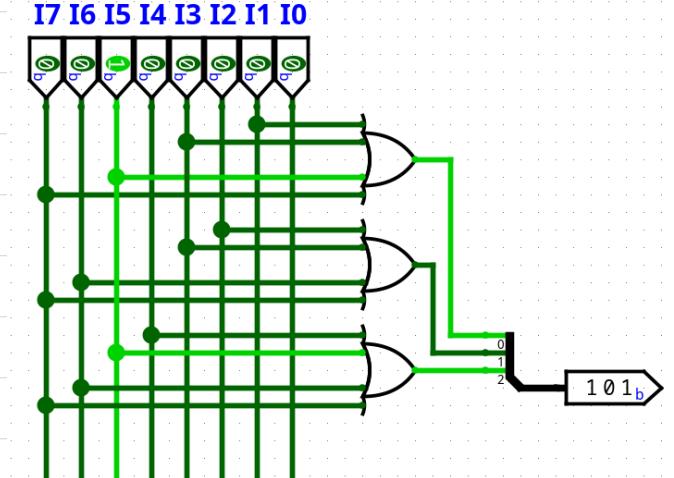
B.

$$Y_0 = I_1 + I_3 + I_5 + I_7$$

$$Y_1 = I_2 + I_3 + I_6 + I_7$$

$$Y_2 = I_4 + I_5 + I_6 + I_7$$

C.



7. Implement the following functions using a decoder and OR gates only.

$$F(X, Y, Z) = \prod M(0, 3, 5, 6)$$

[4]

$$F(x, y, z) = \prod M(0, 3, 5, 6) = \sum m(1, 2, 4, 7)$$

