## 05124265: Reinforcement Learning Exercise 3

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# 1 Theory

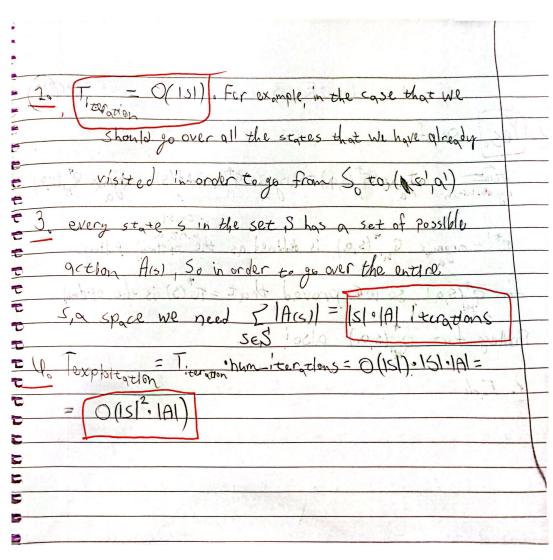
for theory sections please see handwritten solution.

01 - 5 2	
QL-Ex 3.	程年/克
Q1. les. Proof:	
trist argmax of (s,a) = argmax of (s,a) + f(s) = argmax of h	(5,0)
The argmax Q *(S,a) is defined as the optimal policy	
for Q*(S,a), so we proved that = T*(S) is the opting	
Policy for Q' (s,a) also!	
(03) 1. Each Iteration we run to the opt, policy for iter t	

```
Q 1 8
              Bellman eg for mo
                               Q* = \[ \rangle (s' | s, a) \[ \rangle (s, a, s') + r may \rangle m (s', a') \]
        - Bellman eg sor m's
                         Q = = [ (5' | 5, a) [ R'(5, a, 5') + > max Q'm(5', a')]
                               = \( \rangle (\s, \a) \( \rangle (\s, \a), \s') + \phi(\s) - \rangle (\s') + \rangle \max \Q^*_m(\s', \a') \)
  Plugin
      R' as
                          = \( \rightarrow (\s\a, \a, \s') \rightarrow \( \rightarrow (\s') \s' \rightarrow \rightarrow (\s') \)
\( \rightarrow \rightarrow (\s') \rightarrow \rightarrow \rightarrow (\s') \rightarrow \rightar
                                                     + F 5 P(5'15, a) max ( 1, (51, a))
                         = EP(SIS,a) R(S,a,5') + O(S) EP(S'IS,a) - 1 EP(S'IS,a) O(S')
 (s)
                                                      + F = P(5'15,0) max ( "1 (5', a')
  independent
       05 5'
\sum_{s'} P(s'|s,a) = \sum_{s'} P(s|s,a) R(s,a,s') + O(s) - 1 - 1 - \sum_{s'} P(s'|s,a) O(s')
                                                            + F = P(5'15,0) max (1,1(5',a')
                        (5,a) = (5,a) + ((s) - + EP(5'15,a) ((s')
                                                        singce this term is a state dependent and
                                                          independent of a , it does not assect
                                                           on the slection of the uptimal policy
                                   The optimal Policity for m and m'
                                                                      identical /
                                     0-10
```

(02) 151	iteration we run to the OPT. policy for iter t
	new state-action is found. Let's assume by.
	iction that exists a parr(s,a) such that
R'(s, a) = 1	we dight discover at iteration to In other words, the
	icy $\pi_{\xi}$ Stuck on $(s,a)$ : $h_{\xi}^{\dagger}(s,a) = 0$ , So $V_{\xi}^{\pi} = 0$ .
	rongly connected DOP, We know (stal) can be visited
	The that does so will got a reward of 1 at (5', a'),
	not optimal, in contradiction!
	Each izeration must end!

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4 % - 5 rom the Starting Position (5,1) the legal Morres are: (b, 1) -3 (a, 3) ( c , 5) (6,2) - to return to (5,1) as ter 2 speps the knigt mot more to position which he can vetrurn to (6,+), bussiste moves are: (a,5) -5 (5,1) (C,s) -5 (617) (6,2) -5 (6,1) - So, initially the knight Las 3 legal moves - 500 m each it can votorn to (500) = 1/3 ° \frac{1}{8} ° 3 = 4/8/1 2) - the markov chain is irreducible Since its Possible to get from any state to any other, sor the knigt it can evetually get to any squere from any starting Position.

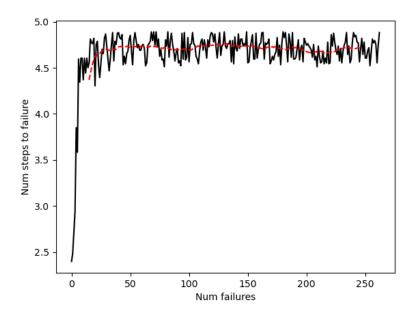
- the markor chain is periodic since the knist can neturn to any stable every "Pair" steps ( & ils 220m), Exos the sissest divitor is 2, 18 thus Periodic With 7=2 3) the moon recurrence time T: to a state i is the reciprocal of the stationar distribution IT; son that stake -let si be the degree of vertex i - since the kinght mous randomly P:= /a: P. Es transition Prosasility in irreducable markor chasn 1 11, = 13 m: = 1/11: - For a corner lorner=d, Ed. = 336 => TCOINEN= 160 => 100 = -108/

## 2 Programming

#### 2.1 Question 1: Off-Policy Model-Based

completed in python in the attached file control.py

In that specific run, it took 263 iterations to converge. The plot of the failure rate is as follows:



#### 2.2 Question 2: Q-Learning

### 2.2.1 Item 1 - tabular\_Q.py

The percentage of successful episodes is roughly 56.6%. The Q-table is as follows:

```
[[1.21427361e-01 1.83254485e-02 1.48874363e-02 1.92531811e-02]
[1.82363151e-03 1.64267572e-03 5.90394023e-04 1.63101858e-01]
 [0.00000000e+00 3.74026090e-03 2.63652325e-03 2.57552930e-01]
 [5.99671903e-04 2.84269525e-04 2.21128911e-04 1.03078260e-01]
 [2.72628630e-01 2.31807525e-03 6.13800917e-04 1.96965210e-03]
 [0.00000000e+00 0.00000000e+00 0.0000000e+00 0.00000000e+00]
 [1.72937261e-04 8.75123858e-08 1.84143980e-01 3.24574625e-05]
 [0.00000000e+00 0.00000000e+00 0.0000000e+00 0.00000000e+00]
 [2.86188773e-03 4.22361064e-04 5.35911767e-04 3.60103396e-01]
 [0.00000000e+00 3.54639242e-01 0.00000000e+00 2.76921632e-03]
 [1.05852451e-01 1.79812038e-03 2.10456247e-04 0.00000000e+00]
 [0.0000000e+00 0.0000000e+00 0.0000000e+00 0.0000000e+00]
 [0.00000000e+00 0.00000000e+00 0.00000000e+00 0.00000000e+00]
 [0.00000000e+00 0.00000000e+00 2.85918529e-01 0.00000000e+00]
 [0.00000000e+00 0.00000000e+00 8.55830849e-01 0.00000000e+00]
 [0.00000000e+00 0.0000000e+00 0.0000000e+00 0.0000000e+00]]
```

#### 2.2.2 Item 2 - network\_Q.py

The percentage of successful episodes is roughly 34.5%. This result is worse than what we achieved with tabular Q-learning, probably due to the fact that the network is not deep and complicated enough to capture the complexity of the environment. We believe that with a deeper network with some activation functions, we could achieve better results.

Score over time: 0.345