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# 1 Basic Test Results

```
1  ex2/
2  ex2/README.md
3  ex2/answer_q1.txt
4  ex2/answer_q2.txt
5  ex2/answer_q3.txt
6  ex2/sol2.py
7  Ex2 Presubmission Script
8
9      Disclaimer
10     -----
11     The purpose of this script is to make sure that your code is compliant
12     with the exercise API and some of the requirements
13     The script does not test the quality of your results.
14     Don't assume that passing this script will guarantee that you will get
15     a high grade in the exercise
16
17
18
19  === Check Submission ===
20
21  README file:
22
23  tal.porezky
24  sol2.py
25  answer_q1.txt
26  answer_q2.txt
27  answer_q3.txt
28  Answer to q1:
29  change_rate function changes the rate of the audio file - but keeping the same
30  number of samples. This causes the new audio file, when modified with ratio =
31  2 to have an higher pitch.
32  change_samples changes the new audio file so it will have the same rate, but
33  with smaller amount of samples on the audio. In practice we cut the higher
34  frequencis so we still have the "main" frequencis within the audio file.
35  Answer to q2:
36  Sample created using resize_spectrogram is "gibrish" and it is not possible to
37  recognize any words in the audio file after it is fast forwarded.
38  Sample created using resize_vocoder is much better and words can be recognized
39  in the fast forwarded audio file.
40  The difference between the two file is, of course, due to the phase fixing we
41  implemented in the resize_vocoder function.
42  Since resize_spectrogram does not handle the phases, there is an interference
43  between the waves of the over laping windows and the audio changes.
44
45  Answer to q3:
46  Actually, there should be no difference between the magnitude images.
47  I guess the difference is caused due to using my own a-bit less accurate DFT
48  and IDFT functions (and not numpy's fft and ifft).
49  Or maybe the difference is caused because there is no one definision for
50  derrevitae in the discrete case - we can use [-1, 1] or [-1, 0, 1] and get
51  different results although we try to do the same thing.
52
53  === Load Student Library ===
54
55  Loading...
56  === Section 1.1 ===
57
58  DFT and IDFT
59  === Section 1.2 ===
```

```

60
61 2D DFT and IDFT
62 === Section 2.1 ===
63
64 Fast foward by rate change
65 === Section 2.2 ===
66
67 Fast forward using Fourier
68 === Section 2.3 ===
69
70 Fast forward using Spectrogram
71 === Section 2.4 ===
72
73 Fast forward using Spectrogram and phase vocoder
74 === Section 3.1 ===
75
76 derivative using convolution
77 === Section 3.2 ===
78
79 derivative using fourier
80
81
82 === Presubmission Completed Successfully ===
83
84
85 Please go over the output and verify that there were no failures / warnings.
86 Remember that this script tested only some basic technical aspects of your implementation.
87 It is your responsibility to make sure your results are actually correct and not only
88 technically valid.

```

## 2 ex2/README.md

```
1  tal.porezky
2  sol2.py
3  answer_q1.txt
4  answer_q2.txt
5  answer_q3.txt
```

### 3 ex2/answer q1.txt

```
1  change_rate function changes the rate of the audio file - but keeping the same
2  number of samples. This causes the new audio file, when modified with ratio =
3  2 to have an higher pitch.
4  change_samples changes the new audio file so it will have the same rate, but
5  with smaller amount of samples on the audio. In practice we cut the higher
6  frequencis so we still have the "main" frequncies within the audio file.
```

## 4 ex2/answer q2.txt

```
1 Sample created using resize_spectrogram is "gibrish" and it is not possible to
2 recognize any words in the audio file after it is fast forwarded.
3 Sample created using resize_vocoder is much better and words can be recognized
4 in the fast forwarded audio file.
5 The difference between the two file is, of course, due to the phase fixing we
6 implemented in the resize_vocoder function.
7 Since resize_spectrogram does not handle the phases, there is an interference
8 between the waves of the over laping windows and the audio changes.
```

## 5 ex2/answer q3.txt

```
1  Actually, there should be no difference between the magnitude images.  
2  I guess the difference is caused due to using my own a-bit less accurate DFT  
3  and IDFT functions (and not numpy's fft and ifft).  
4  Or maybe the difference is caused because there is no one definision for  
5  derrevitae in the discrete case - we can use [-1, 1] or [-1, 0, 1] and get  
6  different results although we try to do the same thing.
```

## 6 ex2/sol2.py

```
1  import numpy as np
2  import scipy.io.wavfile as wavfile
3  from scipy import signal
4  from scipy.ndimage.interpolation import map_coordinates
5  import scipy.signal
6  from imageio import imread
7  from skimage.color import rgb2gray
8  import matplotlib.pyplot as plt
9
10
11  # ----- helper functions -----
12
13
14  def stft(y, win_length=640, hop_length=160):
15      fft_window = signal.windows.hann(win_length, False)
16
17      # Window the time series.
18      n_frames = 1 + (len(y) - win_length) // hop_length
19      frames = [y[s:s + win_length] for s in np.arange(n_frames) * hop_length]
20
21      stft_matrix = np.fft.fft(fft_window * frames, axis=1)
22      return stft_matrix.T
23
24
25  def istft(stft_matrix, win_length=640, hop_length=160):
26      n_frames = stft_matrix.shape[1]
27      y_rec = np.zeros(win_length + hop_length * (n_frames - 1), dtype=np.float)
28      ifft_window_sum = np.zeros_like(y_rec)
29
30      ifft_window = signal.windows.hann(win_length, False)[: , np.newaxis]
31      win_sq = ifft_window.squeeze() ** 2
32
33      # invert the block and apply the window function
34      ytmp = ifft_window * np.fft.ifft(stft_matrix, axis=0).real
35
36      for frame in range(n_frames):
37          frame_start = frame * hop_length
38          frame_end = frame_start + win_length
39          y_rec[frame_start: frame_end] += ytmp[:, frame]
40          ifft_window_sum[frame_start: frame_end] += win_sq
41
42      # Normalize by sum of squared window
43      y_rec[ifft_window_sum > 0] /= ifft_window_sum[ifft_window_sum > 0]
44      return y_rec
45
46
47  def phase_vocoder(spec, ratio):
48      time_steps = np.arange(spec.shape[1]) * ratio
49      time_steps = time_steps[time_steps < spec.shape[1]]
50
51      # interpolate magnitude
52      yy = np.meshgrid(np.arange(time_steps.size), np.arange(spec.shape[0]))[1]
53      xx = np.zeros_like(yy)
54      coordiantes = [yy, time_steps + xx]
55      warped_spec = map_coordinates(np.abs(spec), coordiantes, mode='reflect', order=1).astype(np.complex)
56
57      # phase vocoder
58      # Phase accumulator; initialize to the first sample
59      spec_angle = np.pad(np.angle(spec), [(0, 0), (0, 1)], mode='constant')
```



```

60     phase_acc = spec_angle[:, 0]
61
62     for (t, step) in enumerate(np.floor(time_steps).astype(np.int)):
63         # Store to output array
64         warped_spec[:, t] *= np.exp(1j * phase_acc)
65
66         # Compute phase advance
67         dphase = (spec_angle[:, step + 1] - spec_angle[:, step])
68
69         # Wrap to -pi:pi range
70         dphase = np.mod(dphase - np.pi, 2 * np.pi) - np.pi
71
72         # Accumulate phase
73         phase_acc += dphase
74
75     return warped_spec
76
77
78 def read_image(file_name, representation):
79     """
80     this function read an image from a given path and represent it in rgb
81     or grayscale, according to the user request
82     :param file_name: the path of the image
83     :param representation: 1 - grayscale 2 - rgb
84     :return: an rgb or grayscale image
85     """
86     image = imread(file_name)
87     if representation == 1:
88         new_image = rgb2gray(image)
89     else:
90         new_image = image.astype(np.float64)
91         new_image = new_image / 255
92     return new_image
93
94
95 # ----- part 1 -----
96
97
98 def DFT(signal):
99     """
100     Transforms 1D discrete signal to fourier representation.
101     :param signal: is an array of dtype float64 with shape (N, 1)
102     :return: fourier representation
103     """
104     N = signal.shape[0]
105     assert(N > 0)
106     u = np.arange(N)
107     x = u[:, np.newaxis]
108     exp = complex(np.cos(2 * np.pi / N), - np.sin(2 * np.pi / N))
109     new_basis = np.power(exp, x * u)
110     dft = new_basis @ signal
111     return dft
112
113
114 def IDFT(fourier_signal):
115     """
116     Transforms inverse 1D discrete signal to fourier representation.
117     :param fourier_signal: is an array of dtype complex128 with shape (N, 1)
118     :return: signal representation.
119     """
120     N = fourier_signal.shape[0]
121     assert(N > 0)
122     x = np.arange(N)
123     u = x[:, np.newaxis]
124     exp = complex(np.cos(2 * np.pi / N), np.sin(2 * np.pi / N))
125     new_basis = np.power(exp, u * x)
126     idft = (new_basis @ fourier_signal) / N
127     return idft

```

```

128
129
130 def DFT2(image):
131     """
132     Transforms 2D image to its fourier representation.
133     :param image: grayscale of dtype float64
134     :return: fourier representation.
135     """
136     return DFT(DFT(image).T).T
137
138
139 def IDFT2(fourier_image):
140     """
141     Transforms inverse fourier representation to its 2D image
142     :param fourier_image: 2D array of dtype complex128 with shape
143     :return: image representation
144     """
145     return IDFT(IDFT(fourier_image).T).T
146
147
148 # ----- part 2 -----
149
150
151 def change_rate(filename, ratio):
152     """
153     changes the duration of an audio file by keeping the same samples, but
154     changing the sample rate written in the file header.
155     :param filename: is a string representing the path to a WAV file
156     :param ratio: positive float64 representing the duration change s.t
157     0.25 < ratio < 4.
158     :return: nothing.
159     """
160     original_sample_rate, original_data = wavfile.read(filename)
161     new_sample_rate = int(original_sample_rate * ratio)
162     wavfile.write('change_rate.wav', new_sample_rate, original_data)
163     return
164
165
166 def change_samples(filename, ratio):
167     """
168     changes the duration of an audio file by reducing the number of samples
169     using Fourier
170     :param filename: string representing the path to a WAV file.
171     :param ratio: positive float64
172     :return: a 1D ndarray of dtype float64 representing the new sample points
173     """
174     original_sample_rate, original_data = wavfile.read(filename)
175     new_signal = resize(original_data, ratio)
176     wavfile.write('change_samples.wav', original_sample_rate,
177                  np.real(new_signal) / np.max(np.real(new_signal)))
178     return
179
180
181 def resize(data, ratio):
182     """
183     change the number of samples by the given ratio.
184     :param data: 1D ndarray of dtype float64 representing the original
185     sample points.
186     :param ratio: positive float64
187     :return: 1D ndarray of dtype of float64 representing the new sample
188     points.
189     """
190     assert(ratio > 0)
191     assert(data.shape[0] > 0)
192     fft_data = DFT(data)
193     if ratio < 1: # I should pad it
194         new_num_of_samples = int(data.shape[0] / ratio)
195         total_num_of_pads = new_num_of_samples - data.shape[0]

```

```

196         return IDFT(np.fft.ifftshift(np.pad(np.fft.fftshift(fft_data),
197             (int(np.floor(total_num_of_pads /
198                 2)),
199                 int(np.ceil(total_num_of_pads /
200                     2))),
201                 'constant',
202                 constant_values=0)))
203     elif ratio > 1: # I should clip it
204         return IDFT(clip_data(fft_data, ratio))
205     else: # ratio = 1, do nothing
206         assert(ratio == 1)
207         return data
208
209
210 def clip_data(data, ratio):
211     """
212     clip the data with the new ratio
213     :param data: 1D ndarray of dtype float64 representing the original
214     sample points.
215     :param ratio: positive float64
216     :return: clipped data
217     """
218     new_num_of_samples = int(data.shape[0] / ratio)
219     cut_index = int((data.shape[0] - new_num_of_samples) / 2)
220     shift_data = np.fft.fftshift(data)
221     cut_fft = shift_data[cut_index : cut_index + new_num_of_samples]
222     return np.fft.ifftshift(cut_fft)
223
224
225 def resize_spectrogram(data, ratio):
226     """
227     change the number of samples by the given ratio.
228     :param data: 1D ndarray of dtype float64 representing the original
229     sample points.
230     :param ratio: positive float64
231     :return: 1D ndarray of dtype of float64 representing the new sample
232     points.
233     """
234     stft_matrix = stft(data)
235     new_stft_matrix = list()
236     for index, stft_vec in enumerate(stft_matrix):
237         new_stft_matrix.append(resize(stft_vec, ratio))
238     new_stft_matrix = np.array(new_stft_matrix)
239     new_data = istft(new_stft_matrix)
240     return np.real(new_data)
241
242
243 def resize_vocoder(data, ratio):
244     """
245     change the number of samples by the given ratio.
246     :param data: 1D ndarray of dtype float64 representing the original
247     sample points.
248     :param ratio: positive float64
249     :return: 1D ndarray of dtype of float64 representing the new sample
250     points.
251     """
252     spec = stft(data)
253     resized_spec = phase_vocoder(spec, ratio)
254     resized_data = istft(resized_spec)
255     return np.real(resized_data)
256
257
258 # ----- part 3 -----
259
260
261 def conv_der(im):
262     """
263     computes the magnitude of image derivatives.

```

```

264     :param im: grayscale image of type float64
265     :return: magnitude of the derivative, with the same dtype and shape.
266     """
267     dx = np.array([0.5, 0, -0.5]).reshape(1, 3)
268     dy = dx.T
269     im_by_dx = scipy.signal.convolve2d(im, dx, mode='same')
270     im_by_dy = scipy.signal.convolve2d(im, dy, mode='same')
271     magnitude = np.sqrt(np.abs(im_by_dx) ** 2 +
272                        np.abs(im_by_dy) ** 2)
273     return magnitude
274
275
276 def fourier_der(im):
277     """
278     computes the magnitude of image derivatives using Fourier transform.
279     :param im: float64 grayscale image.
280     :return: magnitude of the derivative calculated using fourier.
281     """
282     dft = np.fft.fftshift(DFT2(im))
283     u = np.arange(-im.shape[1] / 2, im.shape[1] / 2)[np.newaxis, :]
284     v = np.arange(-im.shape[0] / 2, im.shape[0] / 2)[:, np.newaxis]
285     derivative_x_factor = complex(0, 2 * np.pi / im.shape[1]) * u
286     derivative_y_factor = complex(0, 2 * np.pi / im.shape[0]) * v
287     dft_x_derivative = derivative_x_factor * dft
288     dft_y_derivative = derivative_y_factor * dft
289     idft_x_derivative = IDFT2(np.fft.ifftshift(dft_x_derivative))
290     idft_y_derivative = IDFT2(np.fft.ifftshift(dft_y_derivative))
291     magnitude = np.sqrt(np.abs(idft_x_derivative) ** 2 +
292                        np.abs(idft_y_derivative) ** 2)
293     return magnitude

```