STAT 108: Final Project Analysis

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Youtube Analysis

```
library(tidyverse)
library(knitr)
library(patchwork)
library(broom)
library(leaps)
```

In this project, we wish to explore how certain characteristics of a trending youtube videos affects its view count. We plan on checking whether video lengths, times of uploads, length of titles, etc. affect the number of views a video gets. We would suspect that certain titling strategies like putting titles in all caps may have an effect on the video. We also suspect that the length of a video as well as the number of tags will be positively associated with the number of views a video gets. We also would think that the time and weekday of upload will have a large effect on the number of views a trending video might have since there are certain times of the day where there are more youtube users active than usual.

The dataset was obtained through Kaggle. The dataset includes all videos that have been trending starting from August of 2020 and includes data on all trending videos up to the present. We have decided only to include trending videos from the US. For the purpose of this project, the data we will use is a simple random sample from the US trending videos dataset. In addition to the variables from the original dataset, we have added a number of different variables. Using the titles and description we have variables such as title and description length. We also used the Youtube API using the provided video and channel IDs to get the number of subscribers and videos on each channel as well as the length of videos.

The structure of the Dataset is shown below. See the data folder for more information on the dataset.

```
youtube_raw <- read.csv('data/youtube_data.csv') %>%
subset(select = -c(X)) # removed redundant X column
glimpse(youtube_raw)
```

```
## Rows: 982
## Columns: 32
                       <chr> "05HuTGeF5AA", "SXrOuIhoslA", "hzwTq8ZZeyM", "Z6dwgW~
## $ video_id
## $ title
                       <chr> "Khabib Nurmagomedov Announces Retirement | UFC 254"~
                       <chr> "2020-10-24 21:27:37+00:00", "2020-09-26 15:33:12+00~
## $ publishedAt
                       <chr> "UCvgfXK4nTYKudb0rFR6noLA", "UCjwmbv6NE4m0h8Z8VhPUx1~
## $ channelId
                       <chr> "UFC - Ultimate Fighting Championship", "Rosanna Pan~
## $ channelTitle
## $ categoryId
                       <int> 17, 26, 20, 22, 24, 20, 27, 17, 10, 26, 17, 24, 20, ~
                       <chr> "2020-10-27 00:00:00+00:00", "2020-09-30 00:00:00+00~
## $ trending_date
## $ tags
                       <chr> "khabib|retires|nurmagomedov|retirement|annouces|ufc~
                       <int> 17992021, 710333, 1647002, 812308, 3662591, 801205, ~
## $ view count
## $ likes
                       <int> 461029, 36136, 49652, 51599, 248601, 30804, 58505, 1~
                       <int> 10048, 619, 1676, 503, 2797, 618, 203, 456, 1492, 20~
## $ dislikes
```

```
<int> 50333, 4093, 2179, 2235, 10062, 2418, 1717, 1250, 17~
## $ comment count
## $ comments_disabled <chr> "False", "False", "False", "False", "False", "False", "False"
                     <chr> "False", "False", "False", "False", "False"~
## $ ratings disabled
## $ description
                     <chr> "After defeating Justin Gaethje and improving to 29-~
## $ num_tags
                     <int> 252, 468, 7, 85, 93, 432, 59, 172, 406, 7, 44, 281, ~
                     <int> 7, 26, 7, 7, 38, 13, 7, 7, 16, 9, 4, 17, 5, 7, 12, 6~
## $ num caps
## $ num_exc
                     <int> 0, 0, 0, 1, 0, 1, 0, 0, 0, 2, 0, 0, 0, 0, 0, 0, 0~
                     ## $ num qm
## $ num_period
                     <int> 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 3, 0, 0, 0, 1, 3~
## $ num_dollar
                     ## $ title_length
                     <int> 50, 38, 37, 43, 64, 76, 42, 39, 83, 51, 54, 95, 38, ~
                     <dbl> 986, 1131, 113, 1835, 64, 753, 866, 647, 648, 739, 4~
## $ desc_length
## $ weekday_published <int> 5, 5, 6, 1, 1, 1, 0, 1, 3, 0, 4, 6, 3, 1, 0, 2, 1, 0~
                     <int> 24, 26, 4, 19, 3, 8, 30, 18, 17, 3, 12, 3, 6, 2, 2, ~
## $ day_published
## $ hour_published
                     <int> 21, 15, 17, 18, 13, 6, 16, 17, 19, 22, 19, 6, 16, 18~
## $ trending_age
                     <int> 3, 4, 6, 4, 9, 6, 1, 5, 5, 5, 4, 5, 1, 2, 4, 4, 3, 5~
                     <dbl> 331, 1226, 524, 902, 351, 613, 287, 920, 233, 690, 1~
## $ video_length
## $ subscriberCount
                     <int> 13300000, 13200000, 1130000, 7330000, 19300000, 1550~
## $ videoCount
                     <int> 11340, 917, 124, 1548, 27360, 594, 648, 895, 52, 133~
                     <chr> "Movies", "Horror", "Classics", "Documentary", "Fami~
## $ category
## $ channel_length
                     <int> 36, 15, 11, 9, 10, 13, 9, 12, 7, 8, 17, 17, 15, 36, ~
```

We will need to change the types of a few of the variables.

We will now drop some of the columns which we will not use in our analysis. This leaves us with the following dataset.

```
youtube <- subset(youtube, select = -c(video_id, channelId, categoryId, tags, description, title, chann
glimpse(youtube)</pre>
```

```
## Rows: 982
## Columns: 25
## $ publishedAt
                     <dttm> 2020-10-24 21:27:37, 2020-09-26 15:33:12, 2021-04-0~
                     <date> 2020-10-27, 2020-09-30, 2021-04-10, 2021-01-23, 202~
## $ trending_date
                     <int> 17992021, 710333, 1647002, 812308, 3662591, 801205, ~
## $ view_count
## $ likes
                     <int> 461029, 36136, 49652, 51599, 248601, 30804, 58505, 1~
## $ dislikes
                     <int> 10048, 619, 1676, 503, 2797, 618, 203, 456, 1492, 20~
                     <int> 50333, 4093, 2179, 2235, 10062, 2418, 1717, 1250, 17~
## $ comment_count
## $ comments_disabled <chr> "False", "False", "False", "False", "False", "False", "False"
## $ ratings_disabled <chr> "False", "False", "False", "False", "False", "False", "False"
## $ num_tags
                     <int> 252, 468, 7, 85, 93, 432, 59, 172, 406, 7, 44, 281, ~
                     <int> 7, 26, 7, 7, 38, 13, 7, 7, 16, 9, 4, 17, 5, 7, 12, 6~
## $ num caps
## $ num_exc
                     <int> 0, 0, 0, 1, 0, 1, 0, 0, 0, 2, 0, 0, 0, 0, 0, 0, 0~
## $ num qm
                     ## $ num_period
                     <int> 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 3, 0, 0, 0, 1, 3~
## $ num dollar
                     <int> 50, 38, 37, 43, 64, 76, 42, 39, 83, 51, 54, 95, 38, ~
## $ title_length
## $ desc length
                     <dbl> 986, 1131, 113, 1835, 64, 753, 866, 647, 648, 739, 4~
## $ weekday_published <fct> 5, 5, 6, 1, 1, 1, 0, 1, 3, 0, 4, 6, 3, 1, 0, 2, 1, 0~
## $ day_published
                     <int> 24, 26, 4, 19, 3, 8, 30, 18, 17, 3, 12, 3, 6, 2, 2, ~
```

As discussed, we are interested in looking at the relationship between many of these predictors and view count. But as we will discuss in the next section, in order to have our data better reflect the normal distribution, we will instead be using the log of view count as our response variable. For the description of what each variable is measuring, look in the data folder.

Exploratory Data Analysis

Let's start by checking for missing values. When generating some of the features, we automatically dropped videos which no longer exist anymore.

```
colSums(is.na(youtube))
##
         publishedAt
                           trending_date
                                                                           likes
                                                  view_count
##
##
             dislikes
                           comment_count
                                          comments_disabled
                                                               ratings_disabled
##
                    0
                                        0
                                                            0
##
            num_tags
                                num_caps
                                                     num exc
                                                                          num_qm
##
                    0
                                                                               0
##
          num_period
                              num_dollar
                                                title_length
                                                                     desc_length
##
                                        0
                                                                               32
                                             hour_published
##
   weekday_published
                           day_published
                                                                    trending age
##
                                                                               0
##
        video_length
                         subscriberCount
                                                  videoCount
                                                                        category
##
                                                                               0
##
      channel_length
##
```

The only column with missing values is subscriberCount and desc_length. When using the Youtube API to access subscriber counts, for channels with hidden subscriber counts, we decided to input those values of subscriberCount as missing. Seeing as we have so few observations, we will drop these from the dataset. For those with missing description length, this is because those videos have no description. So we will replace those with desc_length of 0.

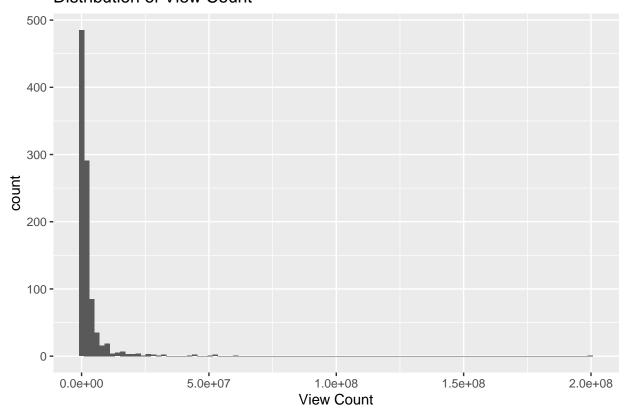
```
youtube$desc_length[is.na(youtube$desc_length)] <- 0
youtube <- youtube %>%
  drop_na()
```

Univariate

We will start by looking at the distributions for the response variable and each of the predictor variables.

```
ggplot(data = youtube, aes(view_count)) +
  geom_histogram(bins = 100) +
  labs(x = 'View Count', title = 'Distribution of View Count')
```

Distribution of View Count



```
summarise(youtube, mean = mean(view_count),
    std_dev = sd(view_count),
    min = min(view_count),
    q1 = quantile(view_count, 0.25),
    median = median(view_count),
    q3 = quantile(view_count, 0.75),
    max = max(view_count),
    IQR = q3-q1)
```

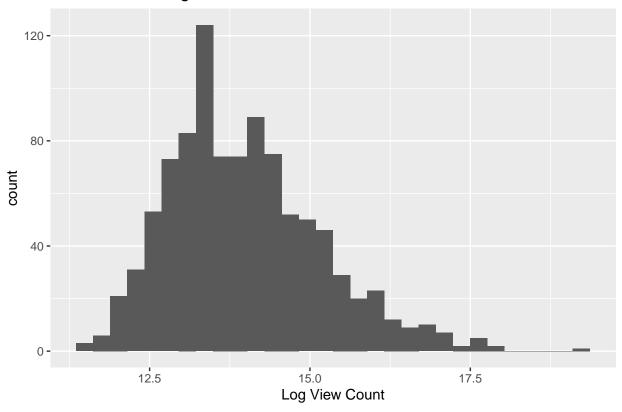
mean std_dev min q1 median q3 max IQR ## 1 2908286 8495062 86407 504949.5 1015847 2377521 199860302 1872572

Looking at the histogram for view count, we see that the distribution is heavily positively skewed. We also have quite a few outliers. Since we wish to conduct inference, we will be looking at the looking at the log view count.

```
youtube <- youtube %%
mutate(log_views = log(view_count))

ggplot(data = youtube, aes(log_views))+
  geom_histogram(bins = 30) +
  labs(x = 'Log View Count', title = 'Distribution of Log View Count')</pre>
```

Distribution of Log View Count



We also will investigate the like to dislike ratio. Note that to avoid division by 0, if we have a video with no dislikes, we will let the like to dislike ratio just be the number of likes.

```
youtube <- youtube %>%
  mutate(like_dislike_ratio = ifelse(dislikes == 0, likes, likes/dislikes)) # avoid division by 0

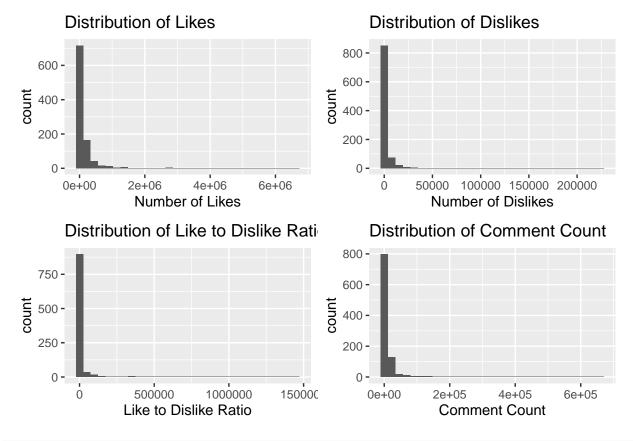
p1 <- ggplot(data = youtube, aes(likes))+
  geom_histogram(bins = 30) +
  labs(x = 'Number of Likes', title = 'Distribution of Likes')

p2 <- ggplot(data = youtube, aes(dislikes))+
  geom_histogram(bins = 30) +
  labs(x = 'Number of Dislikes', title = 'Distribution of Dislikes')

p3 <- ggplot(data = youtube, aes(like_dislike_ratio))+
  geom_histogram(bins = 30) +
  labs(x = 'Like to Dislike Ratio', title = 'Distribution of Like to Dislike Ratio')

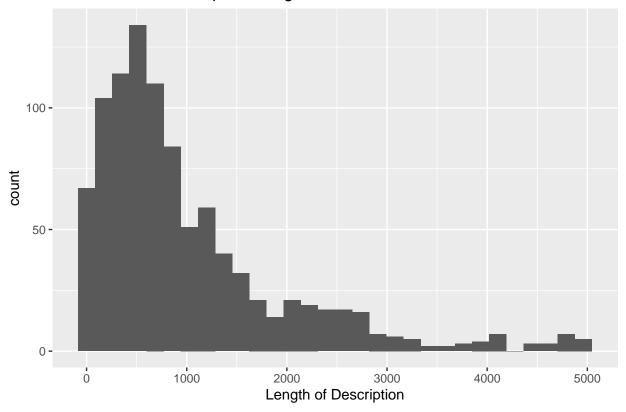
p4 <- ggplot(data = youtube, aes(comment_count)) +
  geom_histogram(bins = 30) +
  labs(x = 'Comment Count', title = 'Distribution of Comment Count')

p1 + p2 + p3 + p4</pre>
```

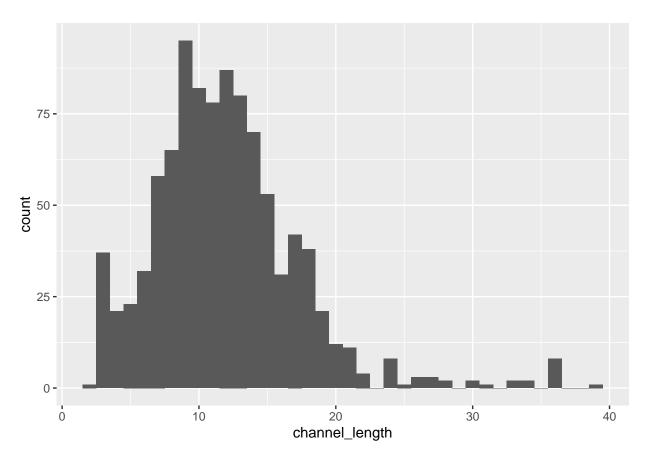


```
ggplot(data = youtube, aes(desc_length)) +
geom_histogram(bins = 30) +
labs(x = 'Length of Description', title = 'Distribution of Description Length')
```

Distribution of Description Length

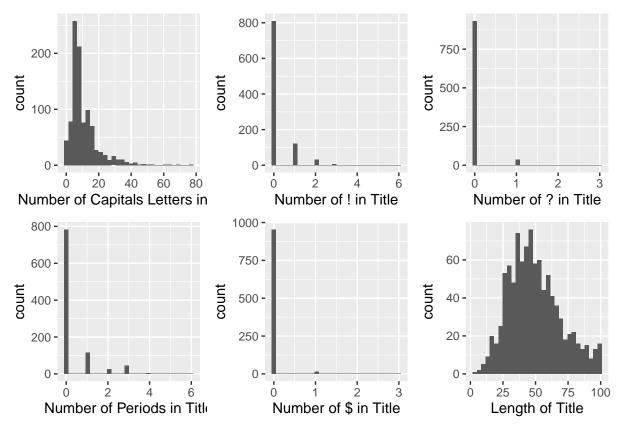


```
ggplot(data = youtube, aes(channel_length)) +
  geom_histogram(binwidth = 1)
```



Considering that view count is positively skewed, it is no surprise that the likes, dislikes, and comment count is also positively skewed. Now we will investigate some of the predictors based on the title.

```
p5 <- ggplot(data = youtube, aes(num_caps))+
  geom_histogram(bins = 30)+
  labs(x = 'Number of Capitals Letters in Title')
p6 <- ggplot(data = youtube, aes(num_exc))+
  geom_histogram(bins = 30) +
  labs(x = 'Number of ! in Title')
p7 <- ggplot(data = youtube, aes(num_qm))+
  geom_histogram(bins = 30) +
  labs(x = 'Number of ? in Title')
p8 <- ggplot(data = youtube, aes(num_period))+
  geom_histogram(bins = 30) +
  labs(x = 'Number of Periods in Title')
p9 <- ggplot(data = youtube, aes(num_dollar))+</pre>
  geom_histogram(bins = 30) +
  labs(x = 'Number of $ in Title')
p10 <- ggplot(data = youtube, aes(title_length))+
  geom_histogram(bins = 30)+
  labs(x = 'Length of Title')
p5+p6+p7+p8+p9+p10
```

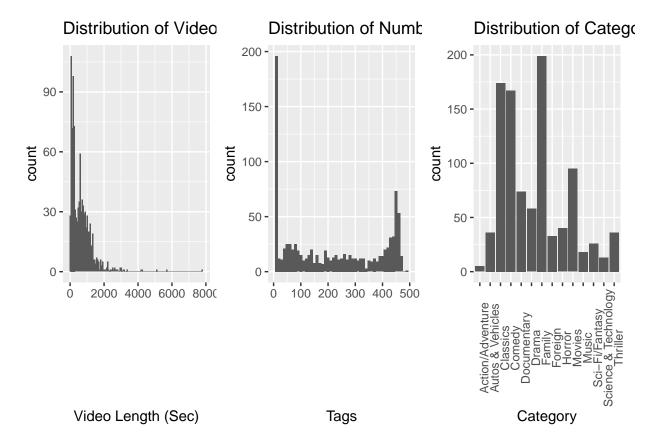


```
p11 <- ggplot(data = youtube, aes(video_length)) +
    geom_histogram(binwidth = 60) +
    labs(x = 'Video Length (Sec)', title = 'Distribution of Video Length')

p12 <- ggplot(data = youtube, aes(num_tags))+
    geom_histogram(binwidth = 10)+
    labs(x = 'Tags', title = 'Distribution of Number of Tags')

p13 <- ggplot(data = youtube, aes(category)) +
    geom_bar() +
    labs(x = 'Category', title = 'Distribution of Category') +
    theme(axis.text.x = element_text(angle = 90))

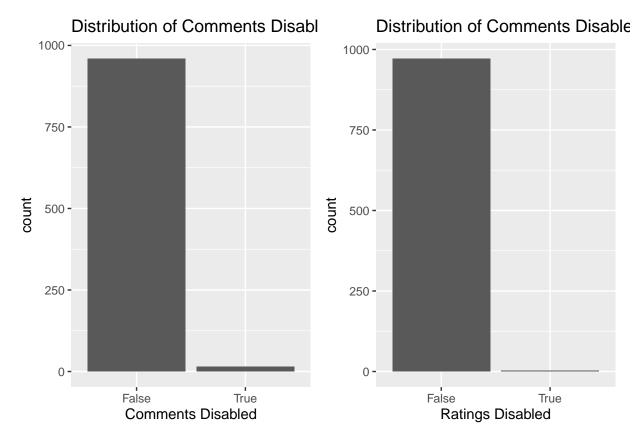
p11 + p12 + p13</pre>
```



```
p14 <- ggplot(data = youtube, aes(comments_disabled))+
   geom_bar()+
   labs(x = 'Comments Disabled', title = 'Distribution of Comments Disabled')

p15 <- ggplot(data = youtube, aes(ratings_disabled))+
   geom_bar()+
   labs(x = 'Ratings Disabled', title = 'Distribution of Comments Disabled')

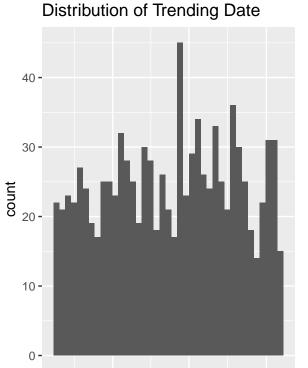
p14 + p15</pre>
```



```
p16 <- ggplot(data = youtube, aes(trending_date))+
    geom_histogram(binwidth = 14) +
    labs(title = 'Distribution of Trending Date', x = 'Trending Date')

p17<- ggplot(data = youtube, aes(publishedAt))+
    geom_histogram(binwidth = 14*60*60*24)+ # 2 week bin width
    labs(x = 'Date Published', title = 'Distribution of Date Published')

p16 + p17</pre>
```

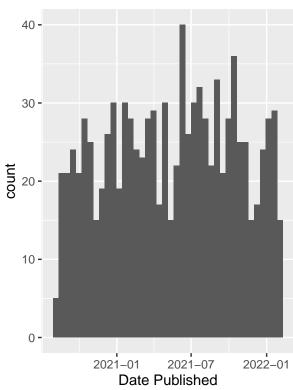


2021-07

Trending Date

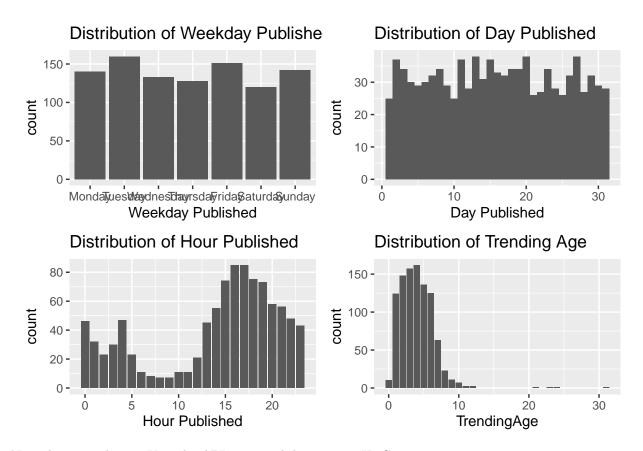
2021-01

Distribution of Date Published



```
levels(youtube$weekday_published) = c('Monday', 'Tuesday', 'Wednesday', 'Thursday', 'Friday', 'Saturday
p18 <- ggplot(data = youtube, aes(weekday_published))+
  geom_bar() +
  labs(x = 'Weekday Published', title = 'Distribution of Weekday Published')
p19 <-ggplot(data = youtube, aes(day_published)) +
  geom_histogram(binwidth = 1) +
  labs(x = 'Day Published', title = 'Distribution of Day Published')
p20 <- ggplot(data = youtube, aes(hour_published))+</pre>
  geom_bar(binwidth = 1) +
  labs(x = 'Hour Published', title = 'Distribution of Hour Published')
## Warning: Ignoring unknown parameters: binwidth
p21 <- ggplot(data = youtube, aes(trending_age))+
  geom_bar(binwidth = 1) +
  labs(x = 'TrendingAge', title = 'Distribution of Trending Age')
## Warning: Ignoring unknown parameters: binwidth
p18 + p19 + p20 + p21
```

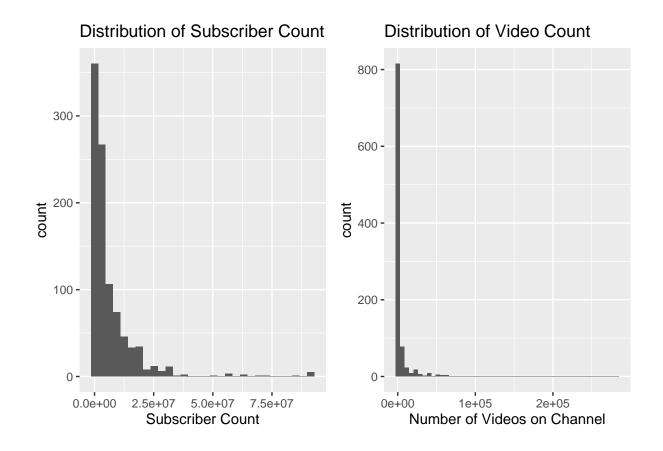
2022-01



Note that according to Youtube API, time and dates are in UTC time zone.

```
p22 <- ggplot(data = youtube, aes(subscriberCount))+
  geom_histogram(bins = 30) +
  labs(x = 'Subscriber Count', title = 'Distribution of Subscriber Count')
p23 <- ggplot(data = youtube, aes(videoCount)) +
  geom_histogram(bins = 50) +
  labs(x = 'Number of Videos on Channel', title = 'Distribution of Video Count')

p22 + p23</pre>
```



Bivariate

Now we will explore the relationship between our predictor variables and our response variable. As we discussed earlier, we will be using log_views instead of view_count as our response since we wish to conduct inference. We will start by observing the correlations for some of the numerical data.

library(Hmisc)

```
## Loading required package: lattice
## Loading required package: survival
## Loading required package: Formula
##
## Attaching package: 'Hmisc'
## The following objects are masked from 'package:dplyr':
##
##
       src, summarize
##
   The following objects are masked from 'package:base':
##
##
       format.pval, units
youtube_num <- youtube %>%
  subset(select = -c(publishedAt, trending_date, comments_disabled, ratings_disabled, weekday_published
cor(youtube_num)
```

```
##
                         view count
                                            likes
                                                       dislikes comment count
## view count
                       1.000000000
                                     0.872865928
                                                   0.8788954385
                                                                  0.307851384
                       0.8728659278
                                      1.00000000
## likes
                                                   0.8338809379
                                                                  0.521898270
## dislikes
                                     0.833880938
                                                   1.000000000
                                                                  0.299306683
                       0.8788954385
  comment count
                       0.3078513845
                                     0.521898270
                                                   0.2993066828
                                                                  1.00000000
## num tags
                      -0.0458425316 -0.069974898 -0.0374015958
                                                                 -0.014041795
## num caps
                      -0.0508995632 -0.059118998 -0.0425567443
                                                                  0.017747779
## num exc
                      -0.0499645567 -0.063765402 -0.0437459943
                                                                 -0.044233308
##
  num_qm
                      -0.0118469424 -0.007696133 -0.0087973666
                                                                 -0.033779080
  num_period
                      -0.0393117102 -0.024384378 -0.0090681248
                                                                 -0.007896145
## num_dollar
                       0.0234788072
                                     0.037913686 0.0002469487
                                                                  0.019937566
## title_length
                      -0.0692386946 -0.111962718 -0.0558722700
                                                                 -0.062303957
## desc_length
                      -0.0005891424
                                     0.011044968
                                                   0.0008517721
                                                                  0.044398062
                      -0.0182071450
                                     0.001700713 0.0020587045
## day_published
                                                                  0.012126508
## hour_published
                      -0.0768285716 -0.062706669 -0.1214434861
                                                                 -0.022231024
## trending_age
                       0.5009803222
                                      0.434955363
                                                   0.4611275000
                                                                  0.131391831
## video_length
                      -0.0817083689 -0.083095989 -0.0506311551
                                                                 -0.013075584
## subscriberCount
                       0.2614496422
                                     0.403858831
                                                  0.1920597452
                                                                  0.446491764
## videoCount
                      -0.0285374923 -0.057484812 -0.0262261289
                                                                 -0.032059520
## channel length
                      -0.0170774584 -0.028720798 -0.0108705645
                                                                 -0.029331897
## log_views
                       0.5833814071
                                     0.617382072  0.4748307703
                                                                  0.398837427
                                     0.159037116 -0.0448482614
## like_dislike_ratio
                       0.0945812291
                                                                 -0.016000982
##
                          num_tags
                                        num_caps
                                                       num_exc
                                                                     num_qm
## view count
                      -0.045842532 -0.050899563 -0.0499645567 -0.011846942
## likes
                      -0.069974898 -0.059118998 -0.0637654020 -0.007696133
## dislikes
                      -0.037401596 -0.042556744 -0.0437459943 -0.008797367
                                    0.017747779 -0.0442333083 -0.033779080
## comment_count
                      -0.014041795
##
  num_tags
                       1.00000000
                                    0.149769522
                                                  0.0020065826
                                                                0.001655671
                                    1.000000000
                                                  0.2508693253
  num_caps
                       0.149769522
                                                                0.043895999
                       0.002006583
                                    0.250869325
                                                  1.000000000
                                                                0.130361826
## num_exc
  num_qm
                       0.001655671
                                    0.043895999
                                                  0.1303618263
                                                                1.000000000
## num_period
                       0.087201705 -0.031230752 -0.0881118263 -0.064900664
  num_dollar
                       0.000443382 -0.051868814
                                                  0.0502914775 -0.025749555
## title_length
                       0.232756665
                                    0.404452660
                                                  0.0620674627
                                                                0.037724679
## desc length
                       0.258649333
                                    0.083722031
                                                  0.0007045872
                                                                0.042820881
## day_published
                       0.026638228 -0.030288479 -0.0186109827 -0.058146980
## hour published
                      -0.014474825 -0.118627435 0.0481512167
                                                                0.044725001
## trending_age
                      -0.016961327 -0.039431297 -0.0126081210
                                                                0.010807121
## video_length
                                    0.111571219
                                                  0.0794666555
                                                                0.048964323
                       0.052218126
## subscriberCount
                      -0.007911243 -0.027756366 -0.0378116840 -0.050221419
## videoCount
                      -0.012278348
                                    0.050452542 -0.0611177922 -0.036238454
## channel length
                                    0.005148084 0.0058393639
                       0.022110372
                                                                0.043868248
## log views
                      -0.004778297 -0.092851993 -0.1388607675 -0.037941641
  like_dislike_ratio -0.057429053 -0.015500992 -0.0136695510 -0.015729864
##
                                       num_dollar title_length
                        num_period
                                                                 desc_length
## view_count
                      -0.039311710
                                    0.0234788072 -0.069238695 -0.0005891424
## likes
                      -0.024384378
                                     0.0379136863 -0.111962718
                                                                0.0110449684
## dislikes
                      -0.009068125
                                     0.0002469487 -0.055872270
                                                                0.0008517721
## comment_count
                      -0.007896145
                                     0.0199375665 -0.062303957
                                                                0.0443980625
## num_tags
                       0.087201705
                                     0.0004433820
                                                   0.232756665
                                                                0.2586493329
## num_caps
                      -0.031230752 -0.0518688139
                                                   0.404452660
                                                                0.0837220306
## num_exc
                      -0.088111826
                                    0.0502914775
                                                   0.062067463
                                                                0.0007045872
## num qm
                      -0.064900664 -0.0257495555
                                                   0.037724679
                                                                0.0428208810
## num period
                       1.000000000 0.0239839759 0.121111215 -0.0097051057
```

```
## num dollar
                       0.023983976 1.0000000000 -0.023348075
                                                                0.0056257035
## title_length
                       0.121111215 -0.0233480752 1.000000000
                                                                0.1759318524
                      -0.009705106
## desc length
                                    0.0056257035 0.175931852
                                                                1.000000000
## day_published
                       0.005129004
                                    0.0224966857 -0.015409999
                                                                0.0430072239
## hour_published
                       0.023669898
                                    0.0033922089 -0.130745538 -0.0346772955
                      -0.011197392
## trending age
                                    ## video length
                       0.103315069
                                    0.0251557982 0.031904721
                                                                0.1331435863
## subscriberCount
                      -0.049774735
                                    0.0918141525 -0.099107456
                                                                0.0458835698
  videoCount
                       0.039557508 -0.0134512393
                                                  0.188035417 -0.0602952626
## channel_length
                      -0.102395591 -0.0159156692 0.017167599
                                                                0.0785635596
  log_views
                      -0.014487082 0.0440810089 -0.089705236
                                                                0.0706481913
                      -0.044342524 -0.0167616767 -0.043822655 -0.0403716055
  like_dislike_ratio
                      day_published hour_published trending_age video_length
## view_count
                       -0.018207145
                                      -0.076828572
                                                    0.500980322
                                                                  -0.08170837
                        0.001700713
## likes
                                      -0.062706669
                                                    0.434955363
                                                                  -0.08309599
## dislikes
                        0.002058705
                                       -0.121443486
                                                    0.461127500
                                                                  -0.05063116
## comment_count
                                      -0.022231024
                                                    0.131391831
                                                                  -0.01307558
                        0.012126508
                        0.026638228
                                      -0.014474825 -0.016961327
                                                                   0.05221813
  num_tags
                       -0.030288479
                                      -0.118627435 -0.039431297
                                                                   0.11157122
## num_caps
## num exc
                       -0.018610983
                                       0.048151217 -0.012608121
                                                                   0.07946666
## num_qm
                       -0.058146980
                                       0.044725001 0.010807121
                                                                   0.04896432
## num_period
                        0.005129004
                                       0.023669898 -0.011197392
                                                                   0.10331507
## num dollar
                        0.022496686
                                       0.003392209
                                                    0.020533218
                                                                   0.02515580
## title length
                       -0.015409999
                                       -0.130745538
                                                    0.006316315
                                                                   0.03190472
## desc length
                        0.043007224
                                       -0.034677295 -0.030284961
                                                                   0.13314359
## day_published
                        1.00000000
                                       0.019038332 -0.027331760
                                                                   0.04250078
## hour_published
                        0.019038332
                                       1.000000000
                                                    0.076503251
                                                                   0.03063420
## trending_age
                       -0.027331760
                                       0.076503251
                                                    1.00000000
                                                                  -0.01538800
## video_length
                        0.042500777
                                       0.030634202 -0.015387996
                                                                   1.00000000
## subscriberCount
                        0.056126296
                                                    0.067077340
                                                                   0.04082792
                                       0.025852179
## videoCount
                        0.031557289
                                      -0.109263272 -0.067552387
                                                                  -0.04122981
## channel_length
                        0.050576343
                                       0.015543291
                                                    0.017929979
                                                                  -0.07240164
  log_views
                        0.048693925
                                      -0.024849701
                                                     0.376875913
                                                                  -0.07385917
                                                                  -0.07390559
                                       0.044948015
                                                    0.027467910
  like_dislike_ratio
                        0.037911636
                                       videoCount channel length
                      subscriberCount
                                                                     log_views
## view_count
                                                                   0.583381407
                          0.261449642 -0.02853749
                                                     -0.017077458
## likes
                          0.403858831 -0.05748481
                                                     -0.028720798
                                                                   0.617382072
## dislikes
                          0.192059745 -0.02622613
                                                     -0.010870564
                                                                   0.474830770
                          0.446491764 -0.03205952
## comment count
                                                     -0.029331897
                                                                   0.398837427
## num_tags
                         -0.007911243 -0.01227835
                                                      0.022110372 -0.004778297
## num caps
                         -0.027756366 0.05045254
                                                      0.005148084 -0.092851993
                         -0.037811684 -0.06111779
                                                      0.005839364 -0.138860768
  num exc
##
  num_qm
                         -0.050221419 -0.03623845
                                                      0.043868248 -0.037941641
                                                     -0.102395591 -0.014487082
  num_period
                         -0.049774735 0.03955751
## num_dollar
                          0.091814152 -0.01345124
                                                     -0.015915669 0.044081009
                                                      0.017167599 -0.089705236
## title_length
                         -0.099107456 0.18803542
## desc_length
                          0.045883570 -0.06029526
                                                      0.078563560 0.070648191
## day_published
                          0.056126296 0.03155729
                                                      0.050576343
                                                                   0.048693925
                                                      0.015543291 -0.024849701
## hour_published
                          0.025852179 -0.10926327
## trending_age
                          0.067077340 -0.06755239
                                                      0.017929979
                                                                  0.376875913
## video_length
                          0.040827919 -0.04122981
                                                     -0.072401637 -0.073859175
## subscriberCount
                          1.00000000 0.07090522
                                                     -0.066478908 0.462068940
                                                     -0.138082167 -0.029270485
## videoCount
                          0.070905224 1.00000000
## channel length
                         -0.066478908 -0.13808217
                                                      1.000000000 -0.012408926
```

```
## log_views
                          0.462068940 -0.02927049
                                                     -0.012408926 1.000000000
## like_dislike_ratio
                          0.006709642 -0.03389018
                                                      0.010800693 0.180504961
##
                      like dislike ratio
                             0.094581229
## view_count
## likes
                             0.159037116
## dislikes
                            -0.044848261
## comment_count
                            -0.016000982
## num tags
                            -0.057429053
## num_caps
                            -0.015500992
## num_exc
                            -0.013669551
## num_qm
                            -0.015729864
## num_period
                            -0.044342524
## num_dollar
                            -0.016761677
## title_length
                            -0.043822655
## desc_length
                            -0.040371606
## day_published
                             0.037911636
## hour_published
                             0.044948015
## trending_age
                             0.027467910
## video_length
                            -0.073905586
## subscriberCount
                             0.006709642
## videoCount
                            -0.033890177
## channel length
                             0.010800693
## log_views
                             0.180504961
## like dislike ratio
                             1.000000000
```

Looking at the correlations, we unsurprisingly see some moderate correlation between log_views and likes, dislikes, and comment_count. This is unsurprising as naturally videos which have more viewers will have more people rating and commenting on the video. But much like with view count, the likes, dislikes, and comment count on a video will not be observed until after it has been uploading. Since we want to focus on predictor variables that are known at or before the video is uploaded, we will not use these.

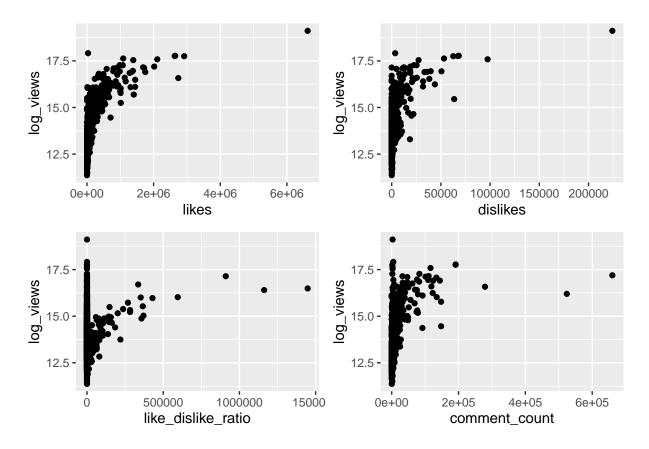
Of the variables which are useful in this sense, we see the channel's subscriber count has a moderate postive correlation of 0.484 with log_views. We also see that the number of exclamation points has a weak negative correlation as well as the length of the description.

```
b1 <- ggplot(data = youtube, aes(x = likes, y = log_views)) +
    geom_point()

b2 <- ggplot(data = youtube, aes(x = dislikes, y = log_views)) +
    geom_point()

b3 <- ggplot(data = youtube, aes(x = like_dislike_ratio, y = log_views)) +
    geom_point()

b4 <- ggplot(data = youtube, aes(x = comment_count, y = log_views)) +
    geom_point()</pre>
```

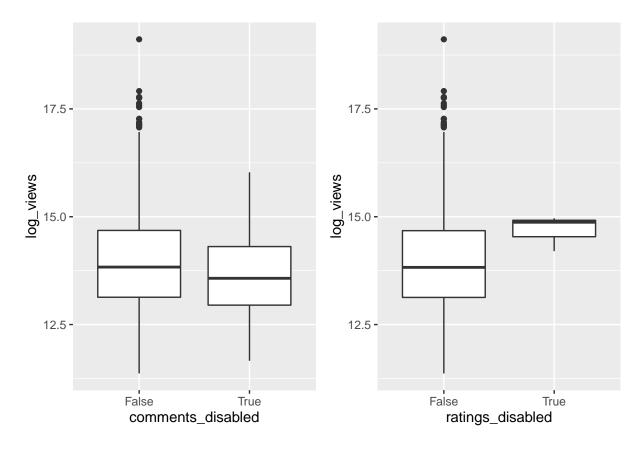


We might expect a linear relationship between likes/dislikes and the number of views. Since we took the log of views, then if we were to include likes and dislikes in our model, we might want to also take the log of likes and dislikes so we can preserved this relationship. This will likely be true for other variables as well such as subscriber count.

```
b5 <- ggplot(data = youtube, aes(x = comments_disabled, y = log_views)) +
   geom_boxplot()

b6 <- ggplot(data = youtube, aes(x = ratings_disabled, y = log_views)) +
   geom_boxplot()

b5 + b6</pre>
```



It looks like disabling ratings might have an effect on <code>log_views</code> shown by the different means across videos with disabled and enabled ratings. There is also a small difference in means for videos with comments disabled.

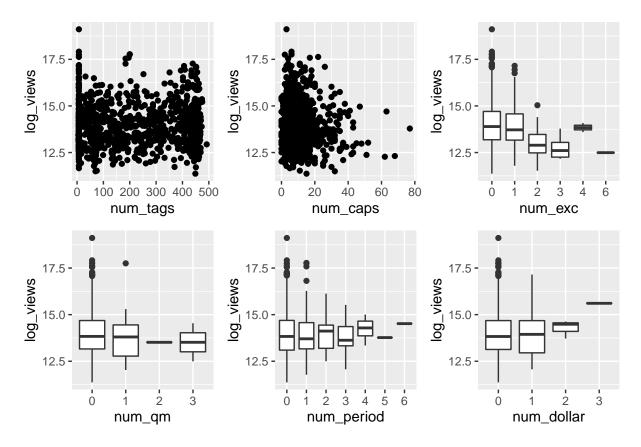
For the sake of plotting some of these variables, we will convert the following variables to factors.

```
youtube <- youtube %>%
  mutate(num_exc = as.factor(num_exc),
         num_qm = as.factor(num_qm),
         num_period = as.factor(num_period),
         num_dollar = as.factor(num_dollar),
         hour_published = as.factor(hour_published), # convert back after eda
         trending_age = as.factor(trending_age),
         day_published = as.factor(day_published))
b7 \leftarrow ggplot(data = youtube, aes(x = num_tags, y = log_views)) +
  geom_point()
b8 <- ggplot(data = youtube, aes(x = num_caps, y = log_views)) +
  geom_point()
b9 <- ggplot(\frac{data}{data} = youtube, aes(x = num_exc, y = log_views)) +
  geom boxplot()
b10 <- ggplot(\frac{data}{data} = youtube, aes(x = num_qm, y = log_views)) +
  geom_boxplot()
```

```
b11 <- ggplot(data = youtube, aes(x = num_period, y = log_views)) +
    geom_boxplot()

b12 <- ggplot(data = youtube, aes(x = num_dollar, y = log_views)) +
    geom_boxplot()

b7+b8+b9+b10+b11+b12</pre>
```



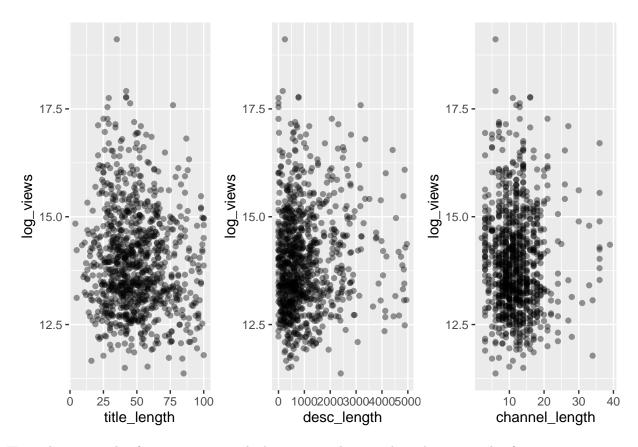
Here it looks like the num_qm has little to no predictive power. But we do see there is quite a bit of variability for log_views across the groups for num_dollar, num_period, and num_exc. Also there might be a weak downward trend for num_caps as well. Meanwhile num_tags looks completely random. So the number of tags doesn't appear to help us.

```
b13 <- ggplot(data = youtube, aes(x = title_length, y = log_views)) +
  geom_point(alpha = 0.4)

b14 <- ggplot(data = youtube, aes(x = desc_length, y = log_views)) +
  geom_point(alpha = 0.4)

b15 <- ggplot(data = youtube, aes(x = channel_length, y = log_views)) +
  geom_point(alpha = 0.4)

b13+b14+b15</pre>
```



Here, the scatterplot for title_length looks quite random, as does the scatterplot for channel_length. Meanwhile there looks like there might be a weak positive trend for desc_length.

```
b15 <- ggplot(data = youtube, aes(x = weekday_published, y = log_views)) +
    geom_boxplot() +
    theme(axis.text.x = element_text(angle = 90))

b16 <- ggplot(data = youtube, aes(x = day_published, y = log_views)) +
    geom_boxplot()

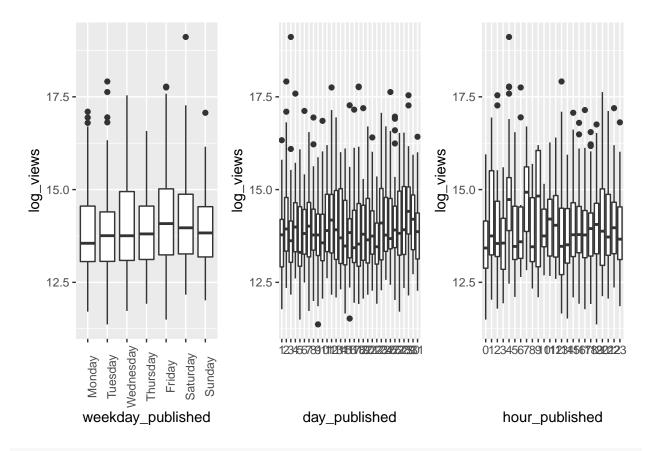
b17 <- ggplot(data = youtube, aes(x = hour_published, y = log_views)) +
    geom_boxplot()

b18 <- ggplot(data = youtube, aes(x = video_length, y = log_views)) +
    geom_point(alpha = 0.2)

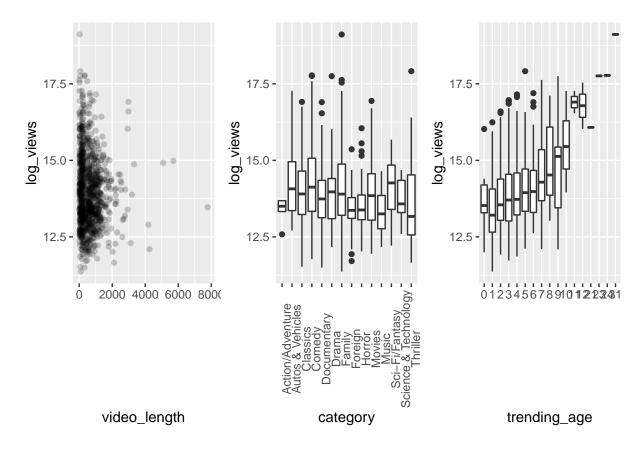
b19 <- ggplot(data = youtube, aes(x = category, y = log_views)) +
    geom_boxplot() +
    theme(axis.text.x = element_text(angle = 90))

b20 <- ggplot(data = youtube, aes(x = trending_age, y = log_views)) +
    geom_boxplot()

b15+b16+b17</pre>
```



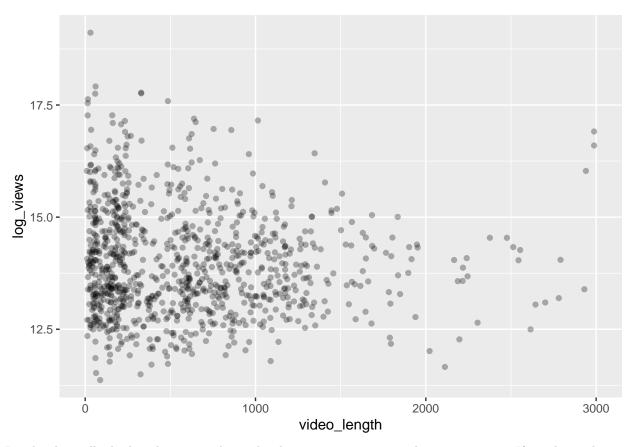
b18+b19+b20



It looks like trending_age and log_views have an association. This is expected since older videos will have had more time to get more views. That being said, the uploader will not know whether a video will trend or how long it takes to get to trending so it would not make sense to include it in our model. As for the category it looks like log_views varies quite a bit between different categories. Hence it might be useful to consider it in our model. For video_length it is hard to tell whether there is a relationship. We will construct another plot with adjusted limits

```
ggplot(data = youtube, aes(x = video_length, y = log_views)) +
geom_point(alpha = 0.3) +
xlim(0,3000)
```

Warning: Removed 8 rows containing missing values (geom_point).

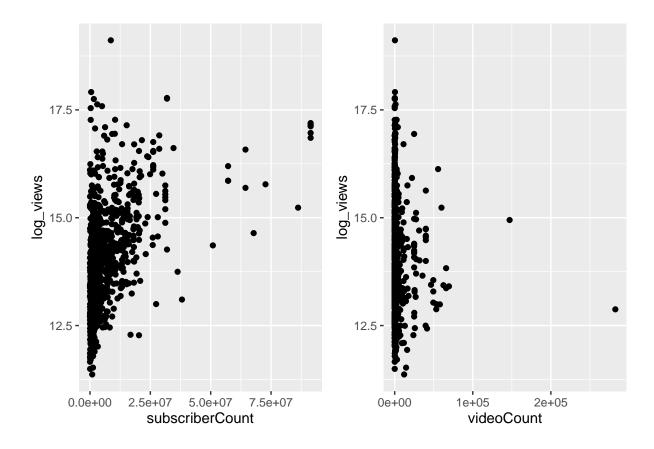


It is hard to tell whether there is a relationship between log_views and video_length. If anything, there is a very weak negative relationship between video_length and log_views, but it is hard to tell due to the difference in variability between short and long videos.

```
b21 <- ggplot(data = youtube, aes(x = subscriberCount, y = log_views)) +
  geom_point()

b22 <- ggplot(data = youtube, aes(x = videoCount, y = log_views)) +
  geom_point()

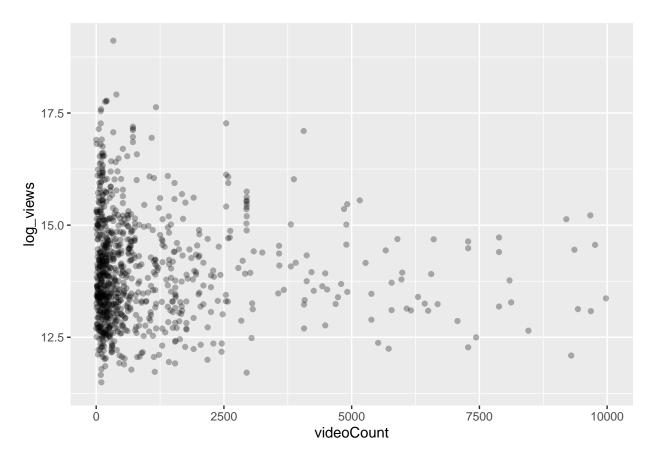
b21+b22</pre>
```



As we noted earlier, it looks like there may be a postive relationship between subscriberCount and log_views. Meanwhile videoCount doesn't seem to be all that useful. Just to check, we will adjust the limits of our plot to get a clearer picture.

```
ggplot(data = youtube, aes(x = videoCount, y = log_views)) +
geom_point(alpha = 0.3)+
xlim(0,10000)
```

Warning: Removed 73 rows containing missing values (geom_point).



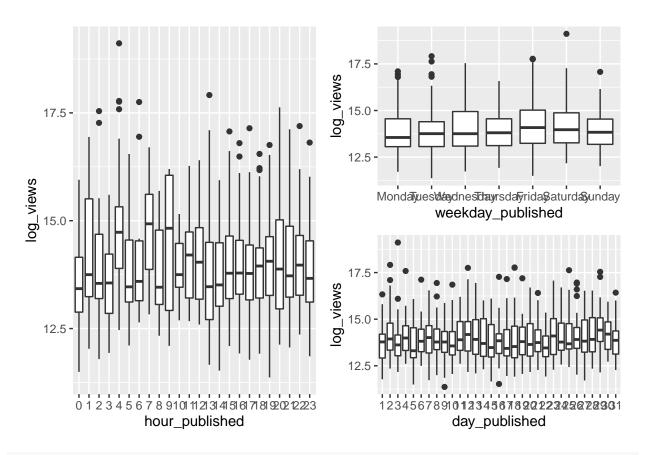
Based off of this second plot, videoCount still does not appear to be all that useful. It doesn't look like the number of video's a channel has affects the number of views a trending video might have.

```
b23 <- ggplot(data = youtube, aes(x = weekday_published, y =log_views)) +
  geom_boxplot()

b24 <- ggplot(data = youtube, aes(x = hour_published, y =log_views)) +
  geom_boxplot()

b25 <- ggplot(data = youtube, aes(x = day_published, y =log_views)) +
  geom_boxplot()

b24+b23/b25</pre>
```



youtube %>% group_by(weekday_published) %>%
summarise(across(log_views, mean))

```
##
  # A tibble: 7 x 2
##
     weekday_published log_views
##
     <fct>
                             <dbl>
## 1 Monday
                              13.9
##
  2 Tuesday
                              13.8
   3 Wednesday
                              14.0
  4 Thursday
                              13.9
  5 Friday
                              14.2
  6 Saturday
                              14.2
## 7 Sunday
                              13.9
```

Here it looks like the day of the week might be useful in predicting log_views . While the boxplot doesn't look all that helpful, looking at the means across the weekdays, log_views for Friday and Saturday are closer to around 14.2 while that mean is closer to 13.8 for Mondays and Tuesdays. While this seems like a very small difference, this is in fact a $e^{14.2} - e^{13.8} = 484255$ view difference which is quite substantial. Looking at the box plots, there is quite a bit of variability in log_views across hour_published. So hour_published might be useful in our model. The same could be said about day_published as well.

Multivariate

Now that we have identified some potentially useful predictor variables that may be useful, we will explore some of the relationships between them. As we noted in the previous section of our EDA, subscriberCount, category, weekday_published, hour_published and a few other variables. We will explore the relationships between some of these variables here.

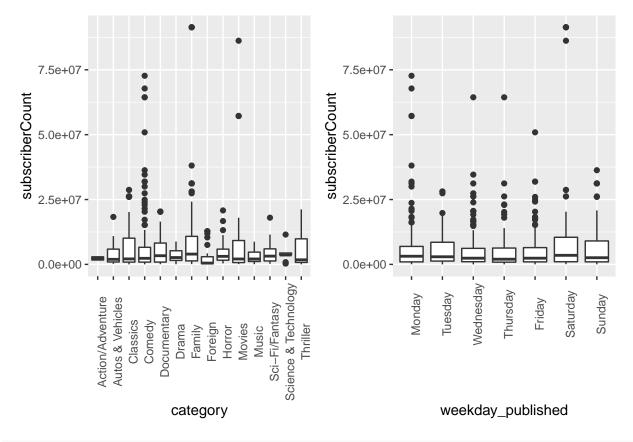
We will start with subscriber count. It is possible that more popular channels tend to have videos of a certain length or tend to upload at specific times or days. It is also possible that subscriber counts vary across video categories.

```
m1 <- ggplot(data = youtube, aes(x = category, y = subscriberCount)) +
    geom_boxplot() +
    theme(axis.text.x = element_text(angle = 90))

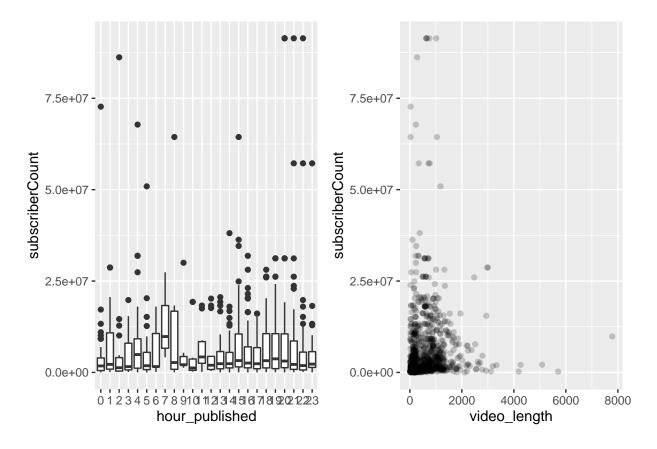
m2 <- ggplot(data = youtube, aes(x = weekday_published, y = subscriberCount)) +
    geom_boxplot() +
    theme(axis.text.x = element_text(angle = 90))

m3 <- ggplot(data = youtube, aes(x = hour_published, y = subscriberCount)) +
    geom_boxplot()

m4 <- ggplot(data = youtube, aes(x = video_length, y = subscriberCount)) +
    geom_point(alpha = 0.2)</pre>
```



m3+m4



Looking at the above plots, it looks like the hour_published and weekday_published are potential covariates. Meanwhile video_length doesn't appear to be associated with subscriberCount. This isn't super surprising as the in the correlation matrix, we found the correlation between subscriberCount and video_length to be quite small.

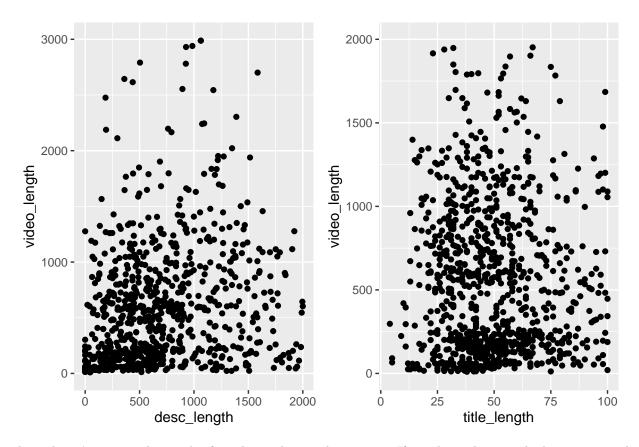
Now we will look at video_length. A few possible relationships may be with respect to desc_length and title_length. Potentially longer videos might have more characters in the description or title since there might be more content to summarize in these videos.

```
m5 <- ggplot(data = youtube, aes(x = desc_length, y = video_length)) +
   geom_point() + xlim(0,2000) + ylim(0, 3000)# note: limits adjusted to zoom in

m6 <- ggplot(data = youtube, aes(x = title_length, y = video_length)) +
   geom_point() + ylim(0,2000)</pre>
m5+m6
```

Warning: Removed 148 rows containing missing values (geom_point).

Warning: Removed 32 rows containing missing values (geom_point).



There doesn't seem to be much of a relationship in these cases. If anything there might be a very weak positive relationship between title_length and video_length.

One thing we would expect is that there is a relationship between many of the variables related to title. We would expect variables like title_length, num_exc, num_qm and so on to be related.

```
m7 <- ggplot(data = youtube, aes(fill = num_exc, y = num_qm))+
    geom_bar(position = 'fill')

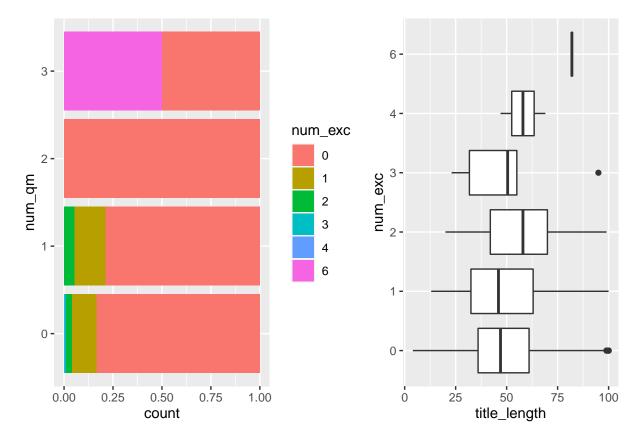
m8 <- ggplot(data = youtube, aes(x = title_length, y = num_exc))+
    geom_boxplot()

m9 <- ggplot(data = youtube, aes(x = title_length, y = num_qm))+
    geom_boxplot()

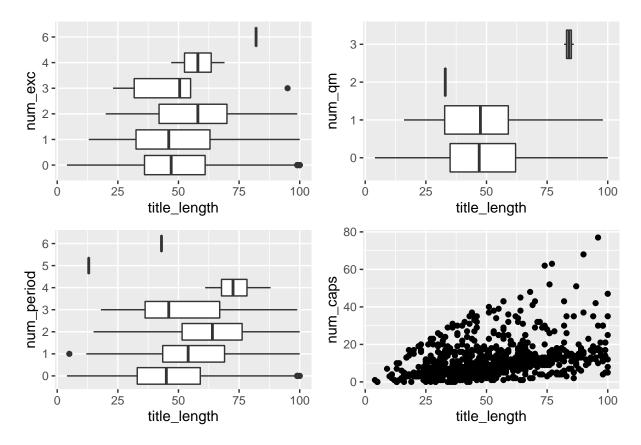
m10 <- ggplot(data = youtube, aes(x = title_length, y = num_period))+
    geom_boxplot()

m11 <- ggplot(data = youtube, aes(x = title_length, y = num_caps))+
    geom_point()

m7 +m8</pre>
```



m8+m9+m10+m11



As we can see, many of these variables having to do with the title are associated. title_length and num_caps seem most obvious with a fairly clear positive linear association.

Once we decide on what variables to use in our model, we can further investigate whether any other predictors are associated with one another.

Modeling

As discussed earlier, the distribution for view_count is heavily skewed. Since the purpose of our analysis is to conduct inference on our model, we would like our response variable to be approximately normally distributed. Hence we will be using log_views instead of view_count for our predictions. As for the predictor variables, we only want to include predictor variables that the uploader might have knowledge of before uploading. So we will not be using variables such as likes, dislikes, and trending_age since the uploader will not know the values of these variables until the video is uploaded. This narrows down the variables we can use considerably. Following from the EDA we will build a model using the following predictor variables:

subscriberCount, category, comments_disabled, ratings_disabled, num_caps, num_exc, num_period, num_dollar, desc_length, hour_published, weekday_published, video_length

We can quickly build a model to predict log_views with these predictor variables with no interaction terms. But as we noted in the Exploratory data analysis, there seems to be a weak linear relationship between num_exc, num_period, num_dollar and log_views. So we will consider 2 separate models: one with those variables as factors, the other with those variables as integers. For the model with those variables treated as integers, we will use the data youtube_int.

Now we will create 2 models both using all of the variables we mentioned above. In full_model_factor, we will treat num_exc, num_period, and num_dollar as factors. In full_model_int they will be treated as integers.

```
full_model_factor <- lm(log_views ~ subscriberCount + category + comments_disabled + ratings_disabled +
full_model_int <- lm(log_views ~ subscriberCount + category + comments_disabled + ratings_disabled + nu
glance(full model factor)
## # A tibble: 1 x 12
##
    r.squared adj.r.squared sigma statistic p.value
                                                          df logLik
                                                                      AIC
                                                                            BIC
         <dbl>
                       <dbl> <dbl>
                                       <dbl>
                                                             <dbl> <dbl> <dbl>
##
                                                 <dbl> <dbl>
                       0.266 1.01
## 1
         0.335
                                        4.83 3.46e-36
                                                          92 -1344. 2876. 3335.
## # ... with 3 more variables: deviance <dbl>, df.residual <int>, nobs <int>
glance(full_model_int)
## # A tibble: 1 x 12
    r.squared adj.r.squared sigma statistic p.value
                                                                      AIC
                                                          df logLik
##
         <dbl>
                       <dbl> <dbl>
                                       <dbl>
                                                 <dbl> <dbl>
                                                             <dbl> <dbl> <dbl>
## 1
         0.322
                                        5.24 3.92e-37
                                                          81 -1353. 2872. 3278.
                       0.261 1.01
## # ... with 3 more variables: deviance <dbl>, df.residual <int>, nobs <int>
```

Looking at the AIC and BIC of our 2 models, it looks like our model with full_model_int is considered better. This isn't super surprising as they have fairly close values of R^2 but full_model_factor has 92 degrees of freedom compared to full_model_int with only 81. Seeing as AIC and BIC penalizes more complex models, this is expected. Since the difference in R^2 is still fairly small, we will be building off of full_model_int Now we will try running backwards selection on our model using AIC.

```
model_back_selection <- step(full_model_int, direction = 'backward')</pre>
```

```
## Start: AIC=106.28
## log_views ~ subscriberCount + category + comments_disabled +
##
       ratings_disabled + num_caps + num_exc + num_period + num_dollar +
       desc_length + hour_published + weekday_published + day_published +
##
##
       video_length
##
##
                       Df Sum of Sq
                                        RSS
                                               AIC
                                    946.36 75.96
## - day_published
                       30
                             28.405
## - hour_published
                       23
                             38.623 956.58 100.42
## - weekday_published 6
                              7.671
                                    925.63 102.38
## - num_period
                        1
                              0.047
                                     918.00 104.33
## - num_dollar
                              0.109 918.07 104.39
                        1
## - comments_disabled 1
                              0.204 918.16 104.49
## - ratings_disabled
                              0.404 918.36 104.71
                        1
                                     917.96 106.28
## <none>
## - desc_length
                              3.159 921.11 107.62
                        1
## - num_caps
                        1
                              3.312 921.27 107.79
                              3.772 921.73 108.27
## - video_length
                        1
## - category
                       13
                             29.119
                                    947.08 110.70
## - num exc
                              6.812 924.77 111.48
                        1
## - subscriberCount
                            237.735 1155.69 328.60
                        1
##
## Step: AIC=75.96
## log_views ~ subscriberCount + category + comments_disabled +
      ratings_disabled + num_caps + num_exc + num_period + num_dollar +
##
```

```
##
       desc_length + hour_published + weekday_published + video_length
##
##
                       Df Sum of Sq
                                        RSS
                                                AIC
## - hour_published
                       23
                            40.388
                                    986.75
                                            70.666
## - weekday_published 6
                              9.631
                                    955.99
                                            73.823
## - num period
                              0.019 946.38 73.980
                        1
## - num dollar
                              0.033 946.39 73.995
                        1
## - comments_disabled
                             0.175 946.54
                       1
                                            74.141
## - ratings_disabled
                       1
                             0.620 946.98
                                            74.599
                       13
## - category
                             25.533 971.89 75.891
## <none>
                                     946.36 75.961
## - desc_length
                        1
                              3.437 949.80 77.491
## - video_length
                              4.246 950.61 78.321
                        1
## - num_caps
                             4.542 950.90 78.624
                        1
## - num_exc
                              8.328 954.69 82.494
                        1
## - subscriberCount
                        1
                           239.872 1186.23 294.001
##
## Step: AIC=70.67
## log_views ~ subscriberCount + category + comments_disabled +
      ratings disabled + num caps + num exc + num period + num dollar +
##
       desc_length + weekday_published + video_length
##
                       Df Sum of Sq
##
                                       RSS
                                                AIC
                              0.030 986.78
                                             68.696
## - num period
                        1
## - comments_disabled 1
                              0.076 986.82
                                             68.741
## - num dollar
                        1
                              0.093 986.84
                                            68.758
## - weekday_published
                             10.685 997.43
                                            69.156
                       6
## - ratings_disabled
                       1
                             1.734 988.48
                                            70.376
                       13
                             26.450 1013.20 70.431
## - category
                                     986.75 70.666
## <none>
## - num_caps
                        1
                              3.908 990.66 72.516
## - desc_length
                        1
                              4.141 990.89 72.746
## - video_length
                              4.809 991.56 73.401
                        1
                              9.926 996.68 78.415
## - num_exc
                        1
## - subscriberCount
                            251.002 1237.75 289.409
##
## Step: AIC=68.7
## log_views ~ subscriberCount + category + comments_disabled +
##
       ratings_disabled + num_caps + num_exc + num_dollar + desc_length +
       weekday_published + video_length
##
##
##
                       Df Sum of Sq
                                       RSS
                                                AIC
                                    986.85
## - comments_disabled
                       1
                              0.073
                                            66.768
## - num_dollar
                              0.098 986.88
                                            66.792
                        1
## - weekday_published
                                    997.45
                       6
                            10.669
                                            67.170
## - ratings_disabled
                             1.741 988.52
                                            68.413
                        1
## - category
                       13
                             26.486 1013.26
                                            68.494
## <none>
                                     986.78 68.696
## - num_caps
                        1
                              3.933 990.71 70.570
## - desc_length
                        1
                              4.138 990.92
                                            70.771
                             4.787 991.57
## - video_length
                                            71.409
                        1
## - num exc
                        1
                            10.118 996.90 76.632
## - subscriberCount
                        1
                            252.004 1238.78 288.221
##
```

```
## Step: AIC=66.77
## log_views ~ subscriberCount + category + ratings_disabled + num_caps +
       num_exc + num_dollar + desc_length + weekday_published +
##
       video_length
##
##
                      Df Sum of Sq
                                       RSS
                                               AIC
                             0.094 986.95 64.861
## - num dollar
                       1
## - weekday_published 6
                            10.781 997.63
                                            65.352
## - ratings_disabled
                      1
                             1.724 988.58
                                            66.468
## - category
                      13
                            26.548 1013.40 66.625
## <none>
                                    986.85 66.768
## - num_caps
                       1
                             3.892 990.74 68.602
## - desc_length
                             4.082 990.93 68.788
                       1
                             4.748 991.60 69.443
## - video_length
                       1
## - num_exc
                            10.128 996.98 74.713
                        1
## - subscriberCount
                        1
                           252.010 1238.86 286.283
##
## Step: AIC=64.86
## log_views ~ subscriberCount + category + ratings_disabled + num_caps +
      num_exc + desc_length + weekday_published + video_length
##
##
                      Df Sum of Sq
                                       RSS
                            10.856 997.80 63.516
## - weekday_published 6
                             1.719 988.67
                                            64.556
## - ratings disabled
                      1
## - category
                      13
                            26.483 1013.43 64.652
## <none>
                                    986.95 64.861
## - num_caps
                       1
                             3.987 990.93 66.787
                             4.075 991.02 66.874
## - desc_length
                       1
## - video_length
                             4.736 991.68 67.524
                       1
## - num exc
                            10.042 996.99 72.721
                       1
## - subscriberCount
                       1
                           254.579 1241.53 286.375
##
## Step: AIC=63.52
## log_views ~ subscriberCount + category + ratings_disabled + num_caps +
##
      num_exc + desc_length + video_length
##
                     Df Sum of Sq
                                      RSS
                                              AIC
## - ratings_disabled 1
                            1.645 999.45 63.121
## <none>
                                   997.80 63.516
                           28.080 1025.88 64.548
## - category
                     13
## - num caps
                            4.275 1002.08 65.680
                      1
## - desc length
                            4.292 1002.09 65.697
                      1
                            4.918 1002.72 66.305
## - video_length
                      1
## - num_exc
                           10.557 1008.36 71.767
                      1
## - subscriberCount
                          257.889 1255.69 285.425
                      1
##
## Step: AIC=63.12
## log_views ~ subscriberCount + category + num_caps + num_exc +
##
       desc_length + video_length
##
##
                                     RSS
                                             AIC
                    Df Sum of Sq
## <none>
                                   999.45 63.121
## - category
                    13
                          28.227 1027.67
                                          64.247
## - num caps
                     1
                           3.819 1003.27 64.835
```

```
## - desc_length
                                                   4.055 1003.50 65.065
                                        1
## - video_length
                                         1
                                                    4.507 1003.95 65.503
## - num exc
                                        1
                                                  11.044 1010.49 71.824
## - subscriberCount 1
                                                258.300 1257.75 285.019
glance(model_back_selection)
## # A tibble: 1 x 12
         r.squared adj.r.squared sigma statistic p.value
                                                                                                          df logLik
                                                                                                                                 AIC
                                                                                                                                            BTC
##
                                          <dbl> <dbl>
                                                                         <dbl>
                                                                                         <dbl> <dbl>
                                                                                                               <dbl> <dbl> <dbl>
## 1
                0.262
                                           0.248 1.02
                                                                          18.9 1.49e-51
                                                                                                          18 -1395. 2829. 2927.
## # ... with 3 more variables: deviance <dbl>, df.residual <int>, nobs <int>
Thus, according to the backwards selection our best model has the predictors subscriberCount, num_exc,
video_length, desc_length, num_caps, category. But while we have a small AIC, our R^2 has dropped
significantly from its level of about 0.32. So we are going to consider adding back some of our variables which
had quite a bit of predictive power.
aic model weekday <- lm(log views ~ subscriberCount + category + num caps + num exc + desc length + vid
aic_model_hr <- lm(log_views ~ subscriberCount + category + num_caps + num_exc + desc_length + video_length + v
aic_model_day <- lm(log_views ~ subscriberCount + category + num_caps + num_exc + desc_length + video_l
aic_model_weekday_hr <- lm(log_views ~ subscriberCount + category + num_caps + num_exc + desc_length +
glance(aic_model_weekday)
## # A tibble: 1 x 12
         {\tt r.squared\ adj.r.squared\ sigma\ statistic\ p.value}
                                                                                                          df logLik
                                                                                                                                 AIC
##
                                          <dbl> <dbl>
                                                                         <dbl>
                                                                                         <dbl> <dbl> <dbl> <dbl> <dbl> <
                0.270
                                          0.252 1.02
                                                                          14.6 6.01e-50
                                                                                                          24 -1389. 2831. 2958.
## # ... with 3 more variables: deviance <dbl>, df.residual <int>, nobs <int>
glance(aic_model_hr)
## # A tibble: 1 x 12
        r.squared adj.r.squared sigma statistic p.value
                                                                                                          df logLik
                                                                                                                                 AIC
                                          <dbl> <dbl>
                                                                         <dbl>
                                                                                         <dbl> <dbl> <dbl> <dbl> <dbl> <
##
                <dbl>
                0.294
                                          0.263 1.01
                                                                          9.45 6.35e-47
                                                                                                          41 -1373. 2833. 3043.
## # ... with 3 more variables: deviance <dbl>, df.residual <int>, nobs <int>
glance(aic_model_day)
## # A tibble: 1 x 12
        r.squared adj.r.squared sigma statistic p.value
                                                                                                          df logLik
                <dbl>
                                          <dbl> <dbl>
                                                                         <dbl>
                                                                                         <dbl> <dbl> <dbl> <dbl> <dbl> <
##
## 1
                0.286
                                           0.249 1.02
                                                                          7.73 8.98e-42
                                                                                                          48 -1378. 2857. 3101.
## # ... with 3 more variables: deviance <dbl>, df.residual <int>, nobs <int>
glance(aic_model_weekday_hr)
## # A tibble: 1 x 12
         r.squared adj.r.squared sigma statistic p.value
                                                                                                          df logLik
##
                <dbl>
                                           <dbl> <dbl>
                                                                         <dbl>
                                                                                         <dbl> <dbl> <dbl> <dbl> <dbl> <
## 1
                0.301
                                          0.265 1.01
                                                                          8.47 7.28e-46
                                                                                                          47 -1368. 2835. 3074.
\#\# # ... with 3 more variables: deviance <dbl>, df.residual <int>, nobs <int>
```

As shown above, it looks like adding back weekday_published and hour_published has increased our R^2 close to 0.3 shown in our model aic_model_weekday_hr. While our AIC has increased, R^2 has increased a fairly significant amount. Now we will consider adding in some interaction terms. So in our model we

have subscriberCount,category,num_caps,num_exc,desc_length,video_length,weekday_published, and hour_published. As we noted in the EDA, the variables relating to the title seem to be associated. So we might want to include the interaction between num_caps and num_exc in our model. Also from the EDA, we might want to include the interaction between subscriberCount and hour_published. Additionally, we will include the interaction between category and subscriberCount.

term	estimate	std.error	statistic	p.value	conf.low	conf.high
(Intercept)	12.286	1.947	6.311	0.000	8.465	16.106
subscriberCount	0.000	0.000	0.712	0.476	0.000	0.000
hour_published1	0.060	0.284	0.211	0.833	-0.498	0.618
hour_published2	0.503	0.281	1.793	0.073	-0.048	1.054
hour_published3	-0.462	0.287	-1.609	0.108	-1.026	0.102
hour_published4	0.959	0.244	3.927	0.000	0.480	1.438
hour_published5	-0.006	0.291	-0.019	0.985	-0.577	0.566
hour_published6	0.329	0.441	0.747	0.455	-0.536	1.195
hour_published7	-0.178	0.705	-0.252	0.801	-1.562	1.206
hour_published8	-0.292	0.484	-0.603	0.547	-1.241	0.658
hour_published9	0.408	0.485	0.842	0.400	-0.543	1.360
hour_published10	0.497	0.401	1.239	0.216	-0.290	1.285
hour_published11	0.391	0.492	0.795	0.427	-0.574	1.357
hour_published12	0.459	0.322	1.423	0.155	-0.174	1.091
hour_published13	-0.193	0.263	-0.733	0.464	-0.708	0.323
hour_published14	0.129	0.243	0.530	0.596	-0.347	0.605
hour_published15	0.036	0.220	0.163	0.870	-0.396	0.468
hour_published16	0.062	0.215	0.286	0.775	-0.361	0.484
hour_published17	0.140	0.225	0.620	0.536	-0.302	0.581
hour_published18	0.062	0.226	0.275	0.784	-0.382	0.506
hour_published19	-0.112	0.229	-0.489	0.625	-0.562	0.338
hour_published20	0.120	0.225	0.532	0.595	-0.323	0.562
hour_published21	0.078	0.227	0.345	0.730	-0.368	0.524
hour_published22	0.278	0.230	1.209	0.227	-0.173	0.729
hour_published23	0.122	0.245	0.499	0.618	-0.358	0.602
categoryAutos & Vehicles	1.600	1.953	0.819	0.413	-2.233	5.433
categoryClassics	1.156	1.942	0.595	0.552	-2.656	4.968
categoryComedy	1.489	1.943	0.766	0.444	-2.325	5.303
categoryDocumentary	1.283	1.944	0.660	0.509	-2.532	5.097
categoryDrama	1.259	1.953	0.645	0.519	-2.573	5.091
categoryFamily	1.580	1.940	0.814	0.416	-2.228	5.388
categoryForeign	0.780	1.949	0.400	0.689	-3.044	4.605
categoryHorror	1.164	1.953	0.596	0.551	-2.668	4.997
categoryMovies	1.326	1.941	0.683	0.495	-2.484	5.136
categoryMusic	0.542	1.976	0.274	0.784	-3.336	4.421
categorySci-Fi/Fantasy	1.537	1.965	0.782	0.434	-2.320	5.394
categoryScience & Technology	1.013	1.996	0.507	0.612	-2.904	4.930
categoryThriller	1.024	1.951	0.525	0.600	-2.806	4.854
num_caps	-0.004	0.008	-0.496	0.620	-0.019	0.011
num_exc	-0.160	0.101	-1.583	0.114	-0.359	0.038
desc_length	0.000	0.000	1.430	0.153	0.000	0.000
video_length	0.000	0.000	-2.800	0.005	0.000	0.000

term	estimate	std.error	statistic	p.value	conf.low	conf.high
weekday_publishedTuesday	0.035	0.120	0.293	0.770	-0.201	0.271
weekday_publishedWednesday	0.201	0.125	1.610	0.108	-0.044	0.446
weekday_publishedThursday	0.133	0.126	1.051	0.293	-0.115	0.381
weekday_publishedFriday	0.264	0.126	2.091	0.037	0.016	0.511
weekday_publishedSaturday	0.188	0.132	1.433	0.152	-0.070	0.447
weekday_publishedSunday	0.154	0.124	1.238	0.216	-0.090	0.397
subscriberCount:hour published1	0.000	0.000	1.836	0.067	0.000	0.000
subscriberCount:hour_published2	0.000	0.000	-1.058	0.290	0.000	0.000
subscriberCount:hour_published3	0.000	0.000	1.684	0.092	0.000	0.000
subscriberCount:hour_published4	0.000	0.000	-0.762	0.446	0.000	0.000
subscriberCount:hour_published5	0.000	0.000	-0.364	0.716	0.000	0.000
subscriberCount:hour_published6	0.000	0.000	0.752	0.452	0.000	0.000
subscriberCount:hour_published7	0.000	0.000	1.020	0.308	0.000	0.000
subscriberCount:hour_published8	0.000	0.000	-0.120	0.905	0.000	0.000
subscriberCount:hour_published9	0.000	0.000	0.803	0.422	0.000	0.000
subscriberCount:hour_published10	0.000	0.000	-0.474	0.636	0.000	0.000
subscriberCount:hour_published11	0.000	0.000	-0.243	0.808	0.000	0.000
subscriberCount:hour_published12	0.000	0.000	-0.197	0.844	0.000	0.000
subscriberCount:hour_published13	0.000	0.000	1.754	0.080	0.000	0.000
subscriberCount:hour_published14	0.000	0.000	-1.429	0.153	0.000	0.000
subscriberCount:hour published15	0.000	0.000	0.225	0.822	0.000	0.000
subscriberCount:hour_published16	0.000	0.000	0.802	0.423	0.000	0.000
subscriberCount:hour_published17	0.000	0.000	0.383	0.702	0.000	0.000
subscriberCount:hour_published18	0.000	0.000	-0.066	0.948	0.000	0.000
subscriberCount:hour_published19	0.000	0.000	1.761	0.079	0.000	0.000
subscriberCount:hour_published20	0.000	0.000	0.519	0.604	0.000	0.000
subscriberCount:hour_published21	0.000	0.000	0.660	0.509	0.000	0.000
subscriberCount:hour_published22	0.000	0.000	0.257	0.797	0.000	0.000
subscriberCount:hour_published23	0.000	0.000	0.330	0.742	0.000	0.000
num_caps:num_exc	-0.003	0.004	-0.603	0.742 0.547	-0.011	0.006
subscriberCount:categoryAutos &	0.000	0.000	-0.596	0.547 0.551	0.000	0.000
Vehicles	0.000	0.000	-0.030	0.551	0.000	0.000
subscriberCount:categoryClassics	0.000	0.000	-0.601	0.548	0.000	0.000
subscriberCount:categoryComedy	0.000	0.000	-0.662	0.508	0.000	0.000
subscriberCount:categoryDocumentary	0.000	0.000	-0.642	0.521	0.000	0.000
subscriberCount:categoryDrama	0.000	0.000	-0.576	0.564	0.000	0.000
subscriberCount:categoryFamily	0.000	0.000	-0.676	0.499	0.000	0.000
subscriberCount:categoryForeign	0.000	0.000	-0.586	0.558	0.000	0.000
subscriberCount:categoryHorror	0.000	0.000	-0.655	0.513	0.000	0.000
subscriberCount:categoryMovies	0.000	0.000	-0.669	0.504	0.000	0.000
subscriberCount:categoryMusic	0.000	0.000	-0.494	0.622	0.000	0.000
subscriberCount:categorySci-Fi/Fantasy	0.000	0.000	-0.592	0.554	0.000	0.000
subscriberCount:categoryScience &	0.000	0.000	-0.612	0.541	0.000	0.000
Technology	3.000	2.000	0.012	0.011	0.000	3.000
subscriberCount:categoryThriller	0.000	0.000	-0.600	0.548	0.000	0.000

Looking at the model output, we see that the interactions between subscriberCount and hour_published mostly seem to have fairly large p-values. While there are a few with small p-values, such as subscriberCount:hour_published1 with a p-value of 0.008, looking at the confidence interval, it is extremely close to 0. So while the p-value suggests we include the interaction in our model, since the confidence interval is so close to 0, we will not include it. Also, the interaction between num_caps and num_exc has a large p-value of 0.404 and the confidence interval captures 0. So that interaction will

not be included in the final model as well. We reach the same conclusions for the interactions between subscriberCount and category. So our model will not include any interaction terms. But looking at the coefficient for subscriberCount, it is essentially 0. Looking at the confidence interval, it is also extremely close to 0. So while the p-value suggests that subscriberCount is important, we will remove it from our model.

```
model <- lm(log_views ~ category + num_caps + num_exc + desc_length + video_length + weekday_published</pre>
```

But one thing we have not addressed is outliers. Just looking at the EDA, we have quite a few outliers in both the response variable and many of the predictors. Since this is the case it is quite likely there are a few leverage points.

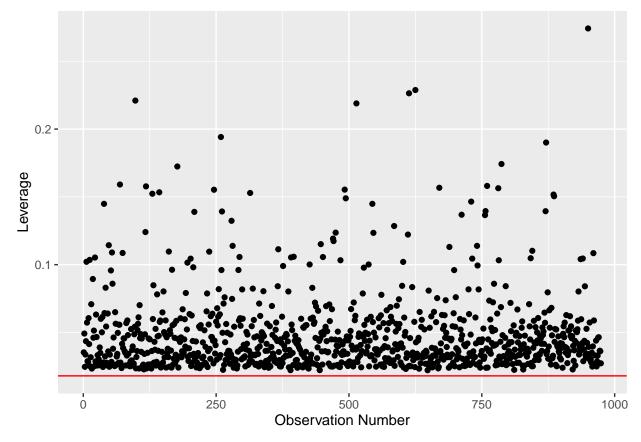
```
model_aug <- augment(model) %>%
  mutate(obs_num = 1:n())
```

Now we will investigate the leverage for each of the observations in our dataset. We will set the threshold for leverage at

$$\frac{2(p+1)}{n} = \frac{2(8+1)}{974} = 0.018$$

We can plot the leverage for each observation.

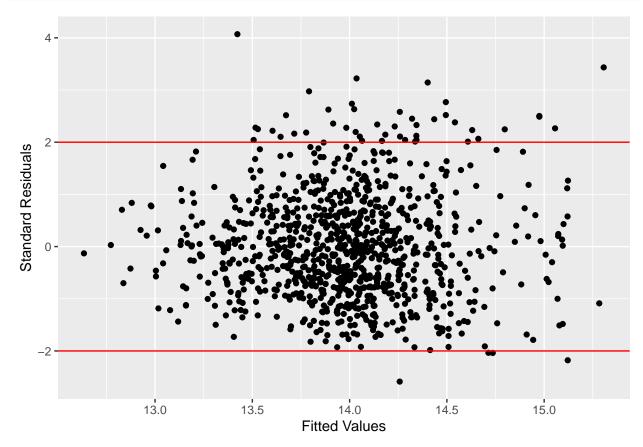
```
ggplot(data = model_aug, aes(x = obs_num, y = .hat))+
geom_point() +
geom_hline(yintercept = 0.018, color = 'red') +
labs(x = 'Observation Number', y = 'Leverage')
```



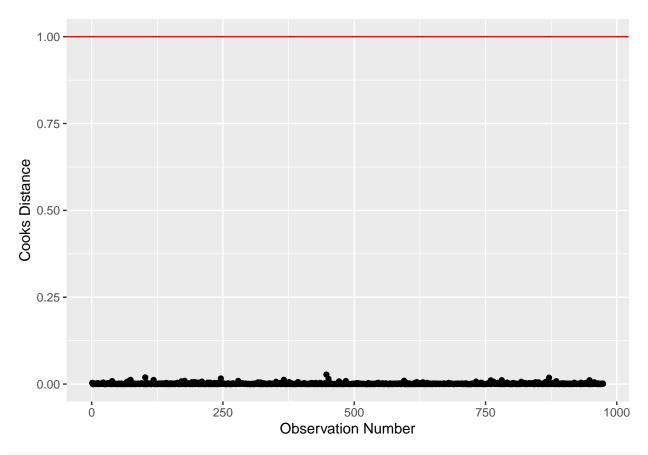
Weirdly it looks like all observations lie above our threshold for

Now we will look at the standardized residuals as well as the cooks distance.

```
ggplot(data = model_aug, aes(x = .fitted, y = .std.resid))+
  geom_point() +
  geom_hline(yintercept = -2, color = 'red')+
  geom_hline(yintercept = 2, color = 'red') +
  labs(x = 'Fitted Values', y='Standard Residuals')
```



```
ggplot(data = model_aug, aes(x = obs_num, y = .cooksd))+
geom_point() +
geom_hline(yintercept = 1, color = 'red')+
labs(x = 'Observation Number', y='Cooks Distance')
```



model_aug[which(abs(model_aug\$.cooksd)>1),]

```
## # A tibble: 0 x 15
## # ... with 15 variables: log_views <dbl>, category <chr>, num_caps <int>,
## # num_exc <int>, desc_length <dbl>, video_length <dbl>,
## # weekday_published <fct>, hour_published <fct>, .fitted <dbl>, .resid <dbl>,
## # .hat <dbl>, .sigma <dbl>, .cooksd <dbl>, .std.resid <dbl>, obs_num <int>
model_aug[which(abs(model_aug$.std.resid)>2),]
```

```
## # A tibble: 48 x 15
      log_views category num_caps num_exc desc_length video_length weekday_publish~
##
##
          <dbl> <chr>
                              <int>
                                      <int>
                                                   <dbl>
                                                                 <dbl> <fct>
##
    1
           16.7 Movies
                                  7
                                           1
                                                     986
                                                                   331 Saturday
    2
                                  7
##
           12.7 Comedy
                                           1
                                                    2319
                                                                   143 Friday
           17.3 Autos &~
                                                    2060
                                                                   159 Saturday
##
    3
                                 11
                                           1
           16.0 Family
                                 30
                                                                    10 Monday
##
                                                      45
##
    5
           16.6 Comedy
                                  9
                                           1
                                                    2495
                                                                   243 Wednesday
##
    6
           17.9 Thriller
                                  6
                                                     164
                                                                    61 Tuesday
##
    7
           17.3 Family
                                  4
                                                                    15 Wednesday
                                           1
                                                       0
           16.5 Comedy
                                  7
                                                                   192 Friday
##
    8
                                           1
                                                    4413
##
    9
           11.4 Family
                                 15
                                           1
                                                    2407
                                                                    88 Tuesday
                                 22
                                           1
## 10
            17.6 Family
                                                       0
                                                                    16 Tuesday
     ... with 38 more rows, and 8 more variables: hour_published <fct>,
        .fitted <dbl>, .resid <dbl>, .hat <dbl>, .sigma <dbl>, .cooksd <dbl>,
       .std.resid <dbl>, obs_num <int>
## #
```

It looks like we have 48 observations which lie outside our standard residual threshold. Meanwhile we have a

no observations lying above the threshold for Cooks Distance. Since this is the case and these observations are perfectly valid videos, we will not remove them from the dataset.

Hence we can get our final model

```
final_model <- lm(log_views ~ category + num_caps + num_exc + desc_length + video_length + weekday_pub
tidy(final_model, conf.int = TRUE) %>%
   kable(digits = 3)
```

term	estimate	std.error	statistic	p.value	conf.low	conf.high
(Intercept)	13.639	0.572	23.846	0.000	12.516	14.761
categoryAutos & Vehicles	0.532	0.563	0.945	0.345	-0.573	1.636
categoryClassics	0.314	0.534	0.587	0.557	-0.734	1.361
categoryComedy	0.373	0.540	0.692	0.489	-0.686	1.432
categoryDocumentary	0.190	0.545	0.348	0.728	-0.881	1.260
categoryDrama	0.148	0.549	0.269	0.788	-0.931	1.226
categoryFamily	0.500	0.531	0.942	0.347	-0.542	1.543
categoryForeign	-0.350	0.566	-0.619	0.536	-1.461	0.760
categoryHorror	-0.016	0.554	-0.029	0.977	-1.104	1.071
categoryMovies	0.214	0.538	0.398	0.690	-0.842	1.271
categoryMusic	-0.314	0.587	-0.535	0.593	-1.466	0.838
categorySci-Fi/Fantasy	0.533	0.568	0.937	0.349	-0.583	1.648
categoryScience & Technology	-0.024	0.621	-0.038	0.969	-1.242	1.194
categoryThriller	0.007	0.561	0.012	0.990	-1.095	1.109
num_caps	-0.012	0.004	-2.769	0.006	-0.021	-0.004
num_exc	-0.224	0.070	-3.196	0.001	-0.361	-0.086
$\operatorname{desc_length}$	0.000	0.000	2.372	0.018	0.000	0.000
video_length	0.000	0.000	-1.094	0.274	0.000	0.000
weekday_publishedTuesday	-0.032	0.134	-0.236	0.814	-0.295	0.232
weekday_publishedWednesday	0.157	0.141	1.112	0.267	-0.120	0.433
weekday_publishedThursday	0.048	0.142	0.339	0.734	-0.231	0.327
weekday_publishedFriday	0.181	0.142	1.278	0.201	-0.097	0.459
weekday_publishedSaturday	0.378	0.145	2.607	0.009	0.093	0.662
weekday_publishedSunday	0.136	0.139	0.982	0.326	-0.136	0.408
hour_published1	0.558	0.266	2.093	0.037	0.035	1.080
hour_published2	0.473	0.292	1.619	0.106	-0.100	1.047
hour_published3	-0.083	0.269	-0.308	0.758	-0.611	0.446
hour_published4	1.029	0.244	4.219	0.000	0.550	1.507
hour_published5	0.050	0.295	0.168	0.867	-0.529	0.628
hour_published6	0.687	0.386	1.781	0.075	-0.070	1.443
hour_published7	0.990	0.438	2.261	0.024	0.131	1.849
hour_published8	0.071	0.465	0.152	0.879	-0.841	0.983
hour_published9	0.699	0.466	1.502	0.133	-0.214	1.613
hour_published10	0.289	0.386	0.748	0.454	-0.468	1.046
hour_published11	0.391	0.392	0.998	0.319	-0.378	1.160
hour_published12	0.413	0.309	1.338	0.181	-0.193	1.019
hour_published13	0.096	0.244	0.391	0.696	-0.384	0.575
hour_published14	-0.038	0.236	-0.160	0.873	-0.500	0.425
hour_published15	0.206	0.219	0.942	0.347	-0.223	0.635
hour_published16	0.217	0.212	1.024	0.306	-0.199	0.634
hour_published17	0.184	0.212	0.871	0.384	-0.231	0.599
hour_published18	0.265	0.216	1.225	0.221	-0.160	0.690
hour published19	0.338	0.219	1.541	0.124	-0.092	0.767

term	estimate	std.error	statistic	p.value	conf.low	conf.high
hour_published20	0.425	0.229	1.857	0.064	-0.024	0.874
hour_published21	0.351	0.230	1.530	0.126	-0.099	0.802
$hour_published22$	0.366	0.237	1.543	0.123	-0.099	0.831
$hour_published23$	0.249	0.244	1.017	0.309	-0.231	0.728

Since we took the log of view count, all of our interpretations for the coefficients need to be adjusted. We will not interprate all of the coefficients, but we will interpret a few. For num_exc, we have a coefficient of -0.224. Interpreting this coefficient, this means that holding all else constant, if we were to increase the number of exclamation points in the title by 1, we would expect the number of views to be multiplied by a factor of $e^{-0.224} = 0.799$. Interpreting weekday_publishedSaturday with a coefficient of 0.378, this means that holding all else constant, if we were to change the publish date of the same video to Saturday from Monday, we would expect the number of views to be multiplied by a factor of $e^{0.378} = 1.459$.

The coefficients for the different categories of weekday_published are quite interesting. It seems that holding all else constant, changing the day published from Monday to any other day except Tuesday is associated with an increase in viewership. Looking at hour_published4, it looks like 4 and 7 am UTC lead to the largest increases in viewership from midnight UTC holding all else constant. These times correspond to 8 and 11 pm PST. Since we are looking at videos in the US, this might suggest that youtube users are most active during those times.

Checking Assumptions

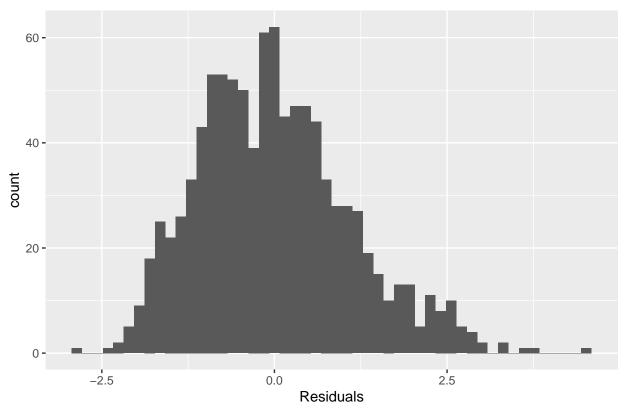
Using our full model, we will check the assumptions for our model.

```
final_model_aug <- augment(final_model) %>%
  mutate(obs_num = 1:n())
```

We will start by looking at Normality.

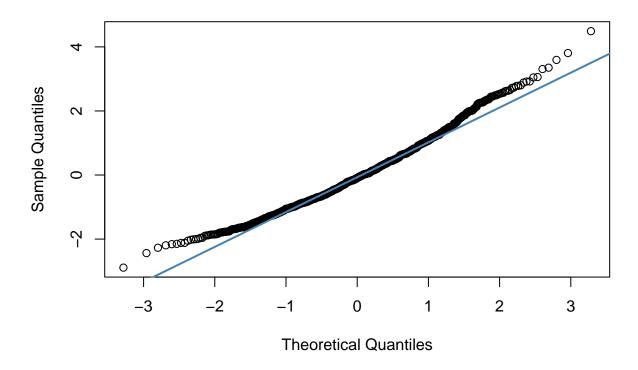
```
ggplot(data = final_model_aug, aes(x =.resid)) +
  geom_histogram(bins = 50)+
  labs(x = 'Residuals', title = 'Distribution of Residuals')
```

Distribution of Residuals



```
qqnorm(final_model_aug$.resid)
qqline(final_model_aug$.resid, col = "steelblue", lwd = 2)
```

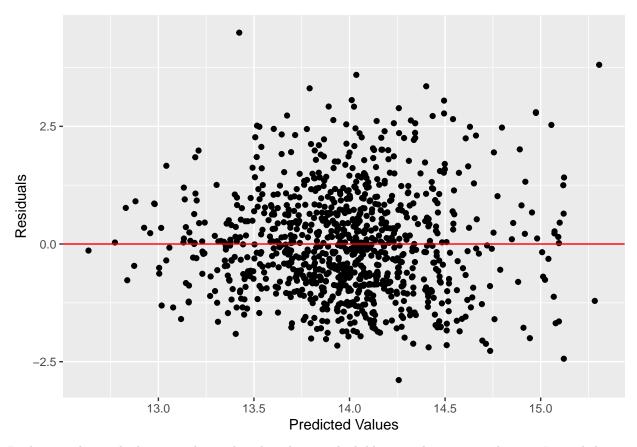
Normal Q-Q Plot



Looking at the histogram, it looks like the residuals follow a fairly normal shape. There is symmetry but it appears to be somewhat bimodal. Also the tails look heavier. Looking at the QQ Plot, it looks like our sample quantiles match the theoretical quantiles around near the center of the data. But at the tails the quantiles do not match. Due to the bimodality and the lack of normality in the tails, we would claim that the normality condition has not been satisfied.

Next we will investigate the constant variance assumption.

```
ggplot(data = final_model_aug, aes(x =.fitted, y=.resid)) +
geom_point()+
geom_hline(yintercept = 0, color = 'red') +
labs(x = 'Predicted Values', y = 'Residuals')
```



Looking at the residuals versus the predicted, it does not look like a random scatter about 0. Instead there is very little variability for low predicted values. Meanwhile the variability with our middle to high predicted values is quite high. Hence the constant variance assumption is not satisfied.

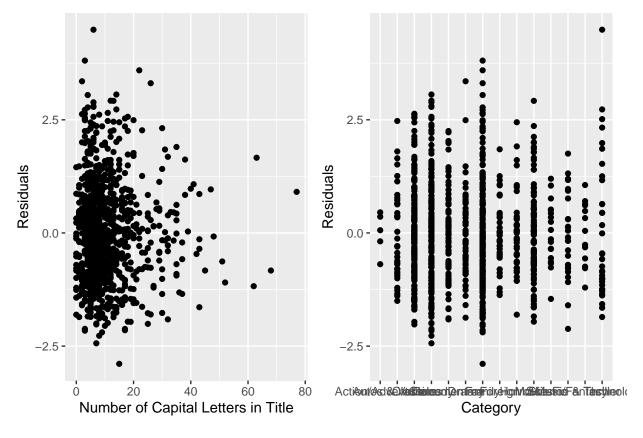
Next we will investigate linearity. We can look at same plot as above to see that there isn't much of a pattern (besides lack of constant variance).

```
a1 <- ggplot(data = final_model_aug, aes(x = num_caps, y=.resid)) +
  geom_point()+
  labs(x = 'Number of Capital Letters in Title', y = 'Residuals')
a2 <- ggplot(data = final_model_aug, aes(x = category, y=.resid)) +
  geom_point()+
  labs(x = 'Category', y = 'Residuals')
a3 <- ggplot(data = final_model_aug, aes(x = num_exc, y=.resid)) +
  geom_point()+
  labs(x = 'Number of Exclamation Points in Title', y = 'Residuals')
a4 <- ggplot(data = final_model_aug, aes(x = desc_length, y=.resid)) +
  geom_point()+
  labs(x = 'Length of Description', y = 'Residuals')
a5 <- ggplot(data = final_model_aug, aes(x = video_length, y=.resid)) +
  geom_point()+
  labs(x = 'Video Length', y = 'Residuals')
a6 <- ggplot(data = final_model_aug, aes(x = weekday_published, y=.resid)) +
```

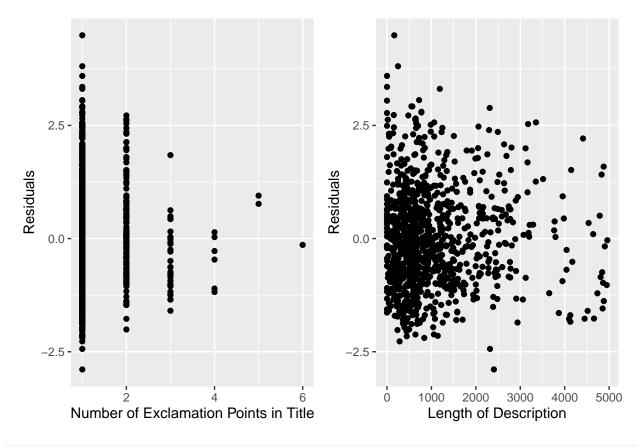
```
geom_boxplot()+
labs(x = 'Weekday Published', y = 'Residuals')

a7 <- ggplot(data = final_model_aug, aes(x = hour_published, y=.resid)) +
  geom_boxplot()+
labs(x = 'Hour Published', y = 'Residuals')

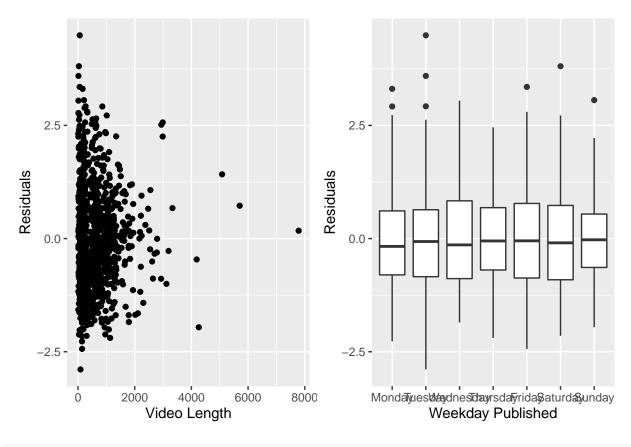
a1+a2</pre>
```



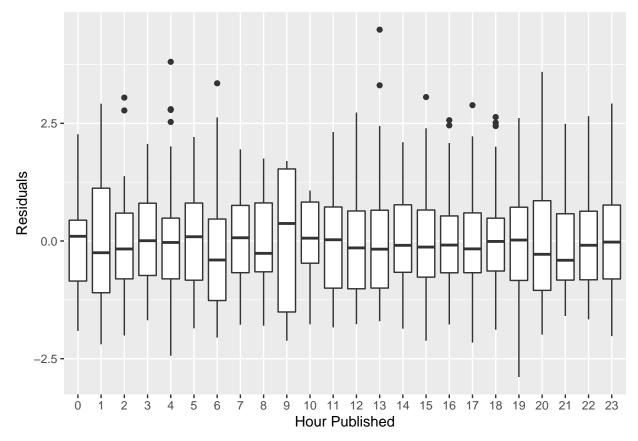
a3+a4



a5+a6



a7



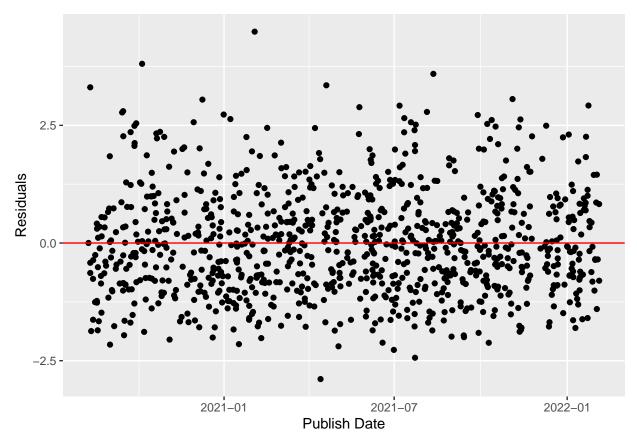
Looking at the residuals versus our predictor variables, there doesn't appear to be a discernible linear relationship between our predictor variables and the residuals. But there is a fan-like shape across many of these plots. The only concerning predictor is hour_published as mean residuals between groups varies somewhat. But overall they seem to stay within the same range. So it doesn't look like the linearity condition has been violated.

Now we will check independence. Since we have taken a random sample from the population dataset of Trending Youtube Videos from August 2020 to February of 2022, we would assume that the independence condition has been satisfied. To check, we will plot the residuals over time.

```
youtube_raw <- read.csv('data/youtube_data.csv') %>%
  subset(select = publishedAt) %>%
  mutate(publishedAt = as.POSIXct(publishedAt), obs_num = 1:n())

final_model_aug_ind <- merge(final_model_aug, youtube_raw, by = 'obs_num')

ggplot(data = final_model_aug_ind, aes(x = publishedAt, y = .resid))+
  geom_point() +
  geom_hline(yintercept = 0, color = 'red') +
  labs(x = 'Publish Date', y = 'Residuals')</pre>
```



Seeing as the the residuals are a random scatter about 0, then it looks like our observations are independent of one another. With this in addition to knowing the methods for gaining the data, it is enough to say that the independence assumption has been satisfied.