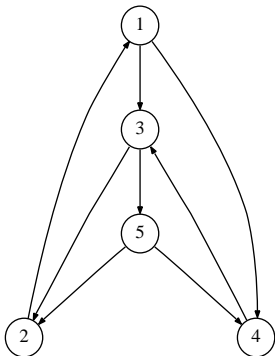


Description of the problem (noname)



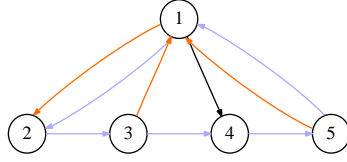
arc	c_{ij}	u_{ij}
(1, 3)	8	∞
(1, 4)	-2	5
(2, 1)	3	∞
(3, 2)	1	1
(3, 5)	1	4
(4, 3)	-11	∞
(5, 2)	2	5
(5, 4)	9	∞

node	b_i
1	2
2	-4
3	2
4	-3
5	3

Legend	
Arc color	Description
—	Natural arc
—	Artificial arc
—	Swapping arc
—	Natural arc in \mathcal{L} set
—	Natural arc in \mathcal{U} set
—	Thread array
Dashed arcs enter the Tree	
Dotted arcs leave the Tree	

***1

Description of the initial iteration (M-noname)



$M = 55, z = 489$			
arc	x_{ij}^k	\mathbb{E}	c_{ij}
$(1, 2)_M$	4	\mathcal{T}	55
$(1, 3)$	0	\mathcal{L}	8
$(1, 4)$	3	\mathcal{T}	-2
$(2, 1)$	0	\mathcal{L}	3
$(3, 1)_M$	2	\mathcal{T}	55
$(3, 2)$	0	\mathcal{L}	1
$(3, 5)$	0	\mathcal{L}	1
$(4, 3)$	0	\mathcal{L}	-11
$(5, 1)_M$	3	\mathcal{T}	55
$(5, 2)$	0	\mathcal{L}	2
$(5, 4)$	0	\mathcal{L}	9

node	thread	pred	depth	π
1	2	0	0	0
2	3	1	1	-55
3	4	1	1	55
4	5	1	1	2
5	1	1	1	55

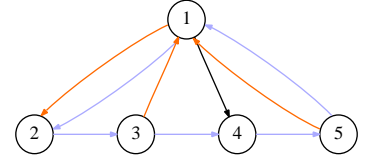
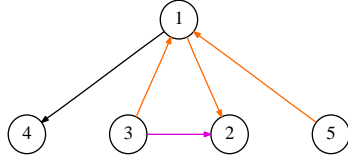
Iteration 0: ***2

Iteration 1 (M-noname)

Reduced Costs Table

Set \mathcal{L} ($c_{ij}^\pi \geq 0$)												
π_3	-	π_1	+	c_{13}	=	(55)	-	(0)	+	(8)	=	63
π_1	-	π_2	+	c_{21}	=	(0)	-	(-55)	+	(3)	=	58
π_2	-	π_3	+	c_{32}	=	(-55)	-	(55)	+	(1)	=	-109 *
π_5	-	π_3	+	c_{35}	=	(55)	-	(55)	+	(1)	=	1
π_3	-	π_4	+	c_{43}	=	(55)	-	(2)	+	(-11)	=	42
π_2	-	π_5	+	c_{52}	=	(-55)	-	(55)	+	(2)	=	-108 *
π_4	-	π_5	+	c_{54}	=	(2)	-	(55)	+	(9)	=	-44 *

The arc (3, 2) enters the tree.



The arc (3, 2) reaches its upper bound and is moved to the \mathcal{U} set, the tree does not change.

$z = 380, \delta = 1$			
arc	x_{ij}^{k-1}	x_{ij}^k	\mathbb{E}
(1, 2) _M	4	3	\mathcal{T}
(1, 3)	0	0	\mathcal{L}
(1, 4)	3	3	\mathcal{T}
(2, 1)	0	0	\mathcal{L}
(3, 1) _M	2	1	\mathcal{T}
(3, 2)	0	1	\mathcal{U}
(3, 5)	0	0	\mathcal{L}
(4, 3)	0	0	\mathcal{L}
(5, 1) _M	3	3	\mathcal{T}
(5, 2)	0	0	\mathcal{L}
(5, 4)	0	0	\mathcal{L}

node	thread	pred	depth	π
1	2	0	0	0
2	3	1	1	-55
3	4	1	1	55
4	5	1	1	2
5	1	1	1	55

Iteration 1: ***3

Iteration 2 (M-noname)

Reduced Costs Table

Set \mathcal{L} ($c_{ij}^\pi \geq 0$)												
π_3	-	π_1	+	c_{13}	=	(55)	-	(0)	+	(8)	=	63
π_1	-	π_2	+	c_{21}	=	(0)	-	(-55)	+	(3)	=	58
π_5	-	π_3	+	c_{35}	=	(55)	-	(55)	+	(1)	=	1
π_3	-	π_4	+	c_{43}	=	(55)	-	(2)	+	(-11)	=	42
π_2	-	π_5	+	c_{52}	=	(-55)	-	(55)	+	(2)	=	-108 *
π_4	-	π_5	+	c_{54}	=	(2)	-	(55)	+	(9)	=	-44 *
Set \mathcal{U} ($c_{ij}^\pi \leq 0$)												
π_2	-	π_3	+	c_{32}	=	(-55)	-	(55)	+	(1)	=	-109

The arc (5, 2) enters the tree.



The artificial arc (1, 2) reaches its lower bound and is removed from the problem.

$z = 56, \delta = 3$			
arc	x_{ij}^{k-1}	x_{ij}^k	\mathbb{E}
(1, 2) _M	3	0	
(1, 3)	0	0	\mathcal{L}
(1, 4)	3	3	\mathcal{T}
(2, 1)	0	0	\mathcal{L}
(3, 1) _M	1	1	\mathcal{T}
(3, 2)	1	1	\mathcal{U}
(3, 5)	0	0	\mathcal{L}
(4, 3)	0	0	\mathcal{L}
(5, 1) _M	3	0	\mathcal{T}
(5, 2)	0	3	\mathcal{T}
(5, 4)	0	0	\mathcal{L}

node	thread	pred	depth	π
1	3	0	0	0
2	1	5	2	53
3	4	1	1	55
4	5	1	1	2
5	2	1	1	55

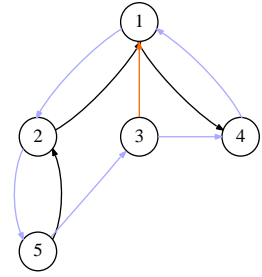
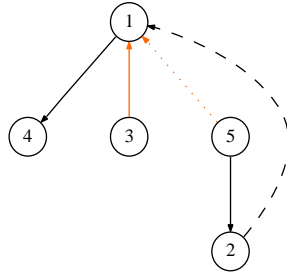
Iteration 2: ***3

Iteration 3 (M-noname)

Reduced Costs Table

Set \mathcal{L} ($c_{ij}^\pi \geq 0$)												
π_3	-	π_1	+	c_{13}	=	(55)	-	(0)	+	(8)	=	63
π_1	-	π_2	+	c_{21}	=	(0)	-	(53)	+	(3)	=	-50 *
π_5	-	π_3	+	c_{35}	=	(55)	-	(55)	+	(1)	=	1
π_3	-	π_4	+	c_{43}	=	(55)	-	(2)	+	(-11)	=	42
π_4	-	π_5	+	c_{54}	=	(2)	-	(55)	+	(9)	=	-44 *
Set \mathcal{U} ($c_{ij}^\pi \leq 0$)												
π_2	-	π_3	+	c_{32}	=	(53)	-	(55)	+	(1)	=	-1

The arc (2, 1) enters the tree.



The artificial arc (5, 1) reaches its lower bound and is removed from the problem.

$z = 56, \delta = 0$				
arc	x_{ij}^{k-1}	x_{ij}^k	\mathbb{E}	
(1, 3)	0	0	\mathcal{L}	
(1, 4)	3	3	\mathcal{T}	
(2, 1)	0	0	\mathcal{T}	
(3, 1) _M	1	1	\mathcal{T}	
(3, 2)	1	1	\mathcal{U}	
(3, 5)	0	0	\mathcal{L}	
(4, 3)	0	0	\mathcal{L}	
(5, 1) _M	0	0		
(5, 2)	3	3	\mathcal{T}	
(5, 4)	0	0	\mathcal{L}	

node	thread	pred	depth	π
1	2	0	0	0
2	5	1	1	3
3	4	1	1	55
4	1	1	1	2
5	3	2	2	5

Iteration 3: ***3

Iteration 4 (M-noname)

Reduced Costs Table

Set \mathcal{L} ($c_{ij}^\pi \geq 0$)												
π_3	-	π_1	+	c_{13}	=	(55)	-	(0)	+	(8)	=	63
π_5	-	π_3	+	c_{35}	=	(5)	-	(55)	+	(1)	=	-49 *
π_3	-	π_4	+	c_{43}	=	(55)	-	(2)	+	(-11)	=	42
π_4	-	π_5	+	c_{54}	=	(2)	-	(5)	+	(9)	=	6
Set \mathcal{U} ($c_{ij}^\pi \leq 0$)												
π_2	-	π_3	+	c_{32}	=	(3)	-	(55)	+	(1)	=	-51

The arc (3, 5) enters the tree.



The artificial arc (3, 1) reaches its lower bound and is removed from the problem.

$z = 7, \delta = 1$			
arc	x_{ij}^{k-1}	x_{ij}^k	\mathbb{E}
(1, 3)	0	0	\mathcal{L}
(1, 4)	3	3	\mathcal{T}
(2, 1)	0	1	\mathcal{T}
(3, 1) _M	1	0	
(3, 2)	1	1	\mathcal{U}
(3, 5)	0	1	\mathcal{T}
(4, 3)	0	0	\mathcal{L}
(5, 2)	3	4	\mathcal{T}
(5, 4)	0	0	\mathcal{L}

node	thread	pred	depth	π
1	2	0	0	0
2	5	1	1	3
3	4	5	3	6
4	1	1	1	2
5	3	2	2	5

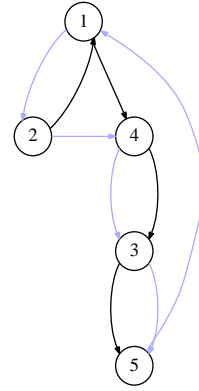
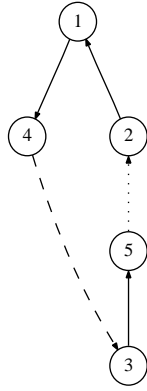
Iteration 4: ***3

Iteration 5 (M-noname)

Reduced Costs Table

Set \mathcal{L} ($c_{ij}^\pi \geq 0$)												
π_3	-	π_1	+	c_{13}	=	(6)	-	(0)	+	(8)	=	14
π_3	-	π_4	+	c_{43}	=	(6)	-	(2)	+	(-11)	=	-7 *
π_4	-	π_5	+	c_{54}	=	(2)	-	(5)	+	(9)	=	6
Set \mathcal{U} ($c_{ij}^\pi \leq 0$)												
π_2	-	π_3	+	c_{32}	=	(3)	-	(6)	+	(1)	=	-2

The arc (4, 3) enters the tree.



The arc (5, 2) reaches its upper bound and is moved to the \mathcal{U} set.

$z = 0, \delta = 1$			
arc	x_{ij}^{k-1}	x_{ij}^k	\mathbb{E}
(1, 3)	0	0	\mathcal{L}
(1, 4)	3	4	\mathcal{T}
(2, 1)	1	2	\mathcal{T}
(3, 2)	1	1	\mathcal{U}
(3, 5)	1	2	\mathcal{T}
(4, 3)	0	1	\mathcal{T}
(5, 2)	4	5	\mathcal{U}
(5, 4)	0	0	\mathcal{L}

node	thread	pred	depth	π
1	2	0	0	0
2	4	1	1	3
3	5	4	2	13
4	3	1	1	2
5	1	3	3	12

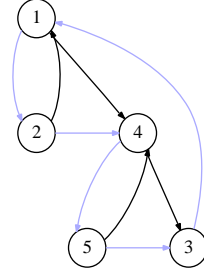
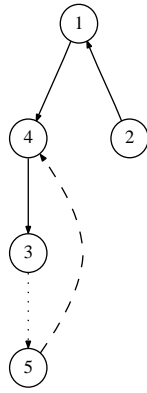
Iteration 5: ***3

Iteration 6 (M-noname)

Reduced Costs Table

Set \mathcal{L} ($c_{ij}^\pi \geq 0$)						
π_3	-	π_1	+	c_{13}	=	$(13) - (0) + (8) = 21$
π_4	-	π_5	+	c_{54}	=	$(2) - (12) + (9) = -1$ *
Set \mathcal{U} ($c_{ij}^\pi \leq 0$)						
π_2	-	π_3	+	c_{32}	=	$(3) - (13) + (1) = -9$
π_2	-	π_5	+	c_{52}	=	$(3) - (12) + (2) = -7$

The arc (5, 4) enters the tree.



The arc (3, 5) reaches its upper bound and is moved to the \mathcal{U} set.

$z = -2, \delta = 2$			
arc	x_{ij}^{k-1}	x_{ij}^k	\mathbb{E}
(1, 3)	0	0	\mathcal{L}
(1, 4)	4	4	\mathcal{T}
(2, 1)	2	2	\mathcal{T}
(3, 2)	1	1	\mathcal{U}
(3, 5)	2	4	\mathcal{U}
(4, 3)	1	3	\mathcal{T}
(5, 2)	5	5	\mathcal{U}
(5, 4)	0	2	\mathcal{T}

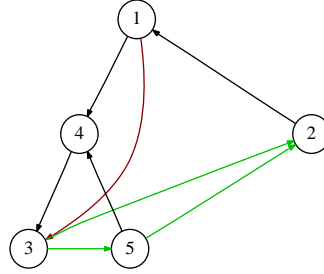
node	thread	pred	depth	π
1	2	0	0	0
2	4	1	1	3
3	1	4	2	13
4	5	1	1	2
5	3	4	2	11

Iteration 6: ***3

Solution of the problem (M-noname)

Reduced Costs Table

Set \mathcal{L} ($c_{ij}^\pi \geq 0$)							
π_3	-	π_1	+	c_{13}	=	(13)	- (0) + (8) = 21
Set \mathcal{U} ($c_{ij}^\pi \leq 0$)							
π_2	-	π_3	+	c_{32}	=	(3)	- (13) + (1) = -9
π_5	-	π_3	+	c_{35}	=	(11)	- (13) + (1) = -1
π_2	-	π_5	+	c_{52}	=	(3)	- (11) + (2) = -6



$z = -2$		
arc	x_{ij}^k	\mathbb{E}
(1, 3)	0	\mathcal{L}
(1, 4)	4	\mathcal{T}
(2, 1)	2	\mathcal{T}
(3, 2)	1	\mathcal{U}
(3, 5)	4	\mathcal{U}
(4, 3)	3	\mathcal{T}
(5, 2)	5	\mathcal{U}
(5, 4)	2	\mathcal{T}

Iteration 7: ***4
