

SC U1

1.2. SC VS HC

Feature	Soft Computing	Hard Computing
Definition	A computational approach that mimics human reasoning and handles imprecision, uncertainty, and approximation.	A traditional computing approach based on precise and deterministic solutions.
Basis	Works on approximate reasoning and probability.	Works on binary logic and exact algorithms.
Flexibility	More flexible, adapts to changing environments.	Rigid, follows strict rules and predefined logic.
Tolerance to Uncertainty	Can handle uncertainty, partial truth, and approximations.	Requires complete and precise data for processing.
Computation Speed	Often faster for complex, real-world problems.	May take longer to process complex problems.
Key Techniques	Neural networks, Fuzzy logic, Genetic algorithms, Evolutionary computing.	Boolean logic, Crisp mathematical models, Algorithmic problem-solving.
Application Areas	Pattern recognition, Robotics, Image processing, Artificial intelligence, Speech recognition.	Arithmetic calculations, Database management, Cryptography, Scientific computing.
Examples	Google Search, Handwriting Recognition, AI Chatbots, Self-driving cars.	Arithmetic operations, Traditional programming languages (C, Java), ATM transactions.

3. Artificial neurons are inspired by **biological neurons**, which are the basic units of the brain and nervous system. Here's a detailed explanation of the inspiration and the functioning of artificial neurons:

1. Inspiration from Biological Neurons

Biological Neuron:

- A biological neuron has:
 - **Dendrites:** Receive input signals from other neurons.
 - **Cell Body (Soma):** Processes the signals.
 - **Axon:** Sends output signals to other neurons.
 - **Synapse:** The connection between two neurons where signals are transmitted.

Artificial Neuron:

- Mimics the working of a biological neuron by:
 - Taking multiple inputs (like dendrites),
 - Applying processing (similar to the soma),
 - Generating an output (like the axon output through synapses).
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2. Key Components of an Artificial Neuron

Component	Description
Inputs (x_1, x_2, \dots, x_n)	These are numerical values (features of data) fed into the neuron.
Weights (w_1, w_2, \dots, w_n)	Each input has an associated weight that represents its importance.
Bias (b)	A constant added to the weighted sum to adjust the output.
Weighted Sum	The neuron computes: $\sum w_i \cdot x_i + b$
Activation Function	Applies a non-linear function (e.g., sigmoid, ReLU, tanh) to the weighted sum to produce the final output.

3. Function in an Artificial Neural Network

- Each **artificial neuron** processes input data using weights and bias, producing an **output**.
 - Neurons are arranged in **layers**:
 - **Input layer**: Receives raw data.
 - **Hidden layers**: Perform intermediate processing.
 - **Output layer**: Gives the final prediction or classification.
 - The network **learns** by adjusting weights using algorithms like **backpropagation** during training, minimizing the error between predicted and actual output.
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Summary Diagram (Textual):

Let me know if you'd like a diagram, code example, or a deeper breakdown of activation functions and training.

4. Feedforward Neural Networks (FNN) and Recurrent Neural Networks (RNN):

Feature	Feedforward Neural Network (FNN)	Recurrent Neural Network (RNN)
Definition	A neural network where information flows in one direction, from input to output.	A neural network with loops where past outputs influence future computations.
Architecture	Has layers (input, hidden, output) with no cycles or feedback connections.	Has recurrent connections, allowing information to persist across time steps.
Data Processing	Processes static data where each input is independent.	Processes sequential data where current output depends on previous inputs.
Memory	Does not retain memory of past inputs.	Maintains internal memory, making it suitable for time-series tasks.
Complexity	Simpler and easier to train due to the absence of recurrent loops.	More complex and harder to train due to vanishing/exploding gradient issues.
Training Time	Faster training as there are no dependencies between inputs.	Slower training because of sequential dependencies.
Applications	Image classification, Object detection, Speech recognition (static data).	Speech recognition, Language modeling, Time-series forecasting.
Example Models	Multi-Layer Perceptron (MLP), Convolutional Neural Networks (CNN).	Long Short-Term Memory (LSTM), Gated Recurrent Unit (GRU).

5. Artificial Neural Network (ANN):

An **Artificial Neural Network (ANN)** is a computational model inspired by the structure and functioning of the human brain.

It consists of interconnected processing units called **neurons**, which work together to recognize patterns, learn from data, and make decisions.

ANNs are widely used in tasks such as image recognition, speech processing, and predictive analytics.

Basic Models of Artificial Neural Networks:

There are three primary types of ANN models:

1. Single-Layer Perceptron (SLP):

- It consists of one input layer and one output layer without hidden layers.
- Uses a weighted sum of inputs followed by an activation function.
- Suitable for solving **linearly separable** problems.
- Example: **Binary classification using a threshold function.**

2. Multi-Layer Perceptron (MLP):

- Has one or more hidden layers between the input and output layers.
- Uses non-linear activation functions like **ReLU, Sigmoid, or Tanh** for complex decision-making.
- Can solve **non-linearly separable problems** effectively.
- Example: **Handwritten digit recognition (MNIST dataset)**.

3. Recurrent Neural Network (RNN):

- Contains loops to retain memory of previous inputs.
- Suitable for sequential data such as **speech recognition and time-series forecasting**.
- Variants include **Long Short-Term Memory (LSTM)** and **Gated Recurrent Unit (GRU)**.
- Example: **Language modeling in chatbots**.

6. activation function - book

9. binary sigmoidal and bipolar

Calculation of Net Input & Activation Output

Given Inputs and Weights:

- Inputs: $x_1 = 0.5, x_2 = 0.9, x_3 = 0.2$
- Weights: $w_1 = 0.2, w_2 = 0.3, w_3 = -0.6$

Step 1: Compute Net Input (Weighted Sum)

The net input is given by:

$$Z = (x_1 \cdot w_1) + (x_2 \cdot w_2) + (x_3 \cdot w_3)$$

Substituting values:

$$Z = (0.5 \times 0.2) + (0.9 \times 0.3) + (0.2 \times -0.6)$$

$$Z = 0.1 + 0.27 - 0.12$$

$$Z = 0.25$$

Step 2: Apply Activation Functions

i) Binary Sigmoidal Function

The binary sigmoidal activation function is:

$$f(Z) = \frac{1}{1 + e^{-Z}}$$

Substituting $Z = 0.25$:

$$f(0.25) = \frac{1}{1 + e^{-0.25}}$$

Approximating $e^{-0.25} \approx 0.7788$:

$$f(0.25) = \frac{1}{1 + 0.7788} = \frac{1}{1.7788} \approx 0.5622$$

✅ Binary Sigmoidal Output: 0.5622

ii) Bipolar Sigmoidal Function

The bipolar sigmoidal activation function is:

$$f(Z) = \frac{2}{1 + e^{-Z}} - 1$$

Substituting $Z = 0.25$:

$$f(0.25) = \frac{2}{1 + e^{-0.25}} - 1$$

Using $e^{-0.25} \approx 0.7788$:

$$\begin{aligned} f(0.25) &= \frac{2}{1.7788} - 1 \\ &= 1.1244 - 1 = 0.1244 \end{aligned}$$

✅ Bipolar Sigmoidal Output: 0.1244

11. Types of Learning in Soft Computing

Soft computing includes various learning techniques that help models adapt and improve their performance over time. The three main types of learning are:

1. Supervised Learning

- In **supervised learning**, the model is trained on labeled data, meaning each input has a corresponding correct output.
- The system learns by minimizing the error between predicted and actual values using algorithms like **Neural Networks, Decision Trees, and Support Vector Machines (SVM)**.
- **Example:** Email spam classification (Spam or Not Spam).

Diagram:

Input Data → Model → Output (Labeled Training Data) → (Learning Algorithm) → (Predicted Labels)

2. Unsupervised Learning

- In **unsupervised learning**, the model is trained on **unlabeled data**, meaning there is no predefined output.
- The system discovers patterns, structures, or clusters in the data without human intervention.
- Common algorithms include **K-Means Clustering, Principal Component Analysis (PCA), and Autoencoders**.
- **Example:** Customer segmentation in marketing.

Diagram:

Input Data → Model → Patterns/Clusters (Unlabeled Data) → (Learning Algorithm) → (Grouped Data)

3. Reinforcement Learning (RL)

- In **reinforcement learning**, an agent learns by interacting with an environment and receiving feedback in the form of **rewards or penalties**.
- The goal is to maximize cumulative rewards over time.

- Used in **robotics, game playing (e.g., AlphaGo), and autonomous vehicles.**
- **Example:** Training an AI to play chess by rewarding winning moves.

Diagram:

Agent → Action → Environment → Reward/Feedback → Agent

12. design a Hebb Network for the AND function using the given inputs and target values

we'll follow the Hebbian learning rule. The Hebbian learning rule updates the weights based on the correlation between the input and the output.

Given Data:

We have two input patterns with a bias term (b) and the corresponding target output (y):

1. **Pattern 1:** $X_1=1, X_2=1, b=1 \rightarrow y=1$
2. **Pattern 2:** $X_1=1, X_2=-1, b=1 \rightarrow y=-1$

Hebbian Learning Rule:

The weight update rule is:

$$\Delta w_i = \alpha \cdot x_i \cdot y$$

where:

- α is the learning rate (we can assume $\alpha=1$ for simplicity),
- x_i is the input,
- y is the target output.

The weights are updated as:

$$w_i^{new} = w_i^{old} + \Delta w_i$$

Initial Weights:

Assume initial weights are zero:

$$w_1=0, w_2=0, w_b=0$$

Weight Updates:

Weight Updates:

Pattern 1: $X_1 = 1, X_2 = 1, b = 1, y = 1$

$$\Delta w_1 = 1 \cdot 1 \cdot 1 = 1$$

$$\Delta w_2 = 1 \cdot 1 \cdot 1 = 1$$

$$\Delta w_b = 1 \cdot 1 \cdot 1 = 1$$

New weights:

$$w_1 = 0 + 1 = 1$$

$$w_2 = 0 + 1 = 1$$

$$w_b = 0 + 1 = 1$$

Pattern 2: $X_1 = 1, X_2 = -1, b = 1, y = -1$

$$\Delta w_1 = 1 \cdot 1 \cdot (-1) = -1$$

$$\Delta w_2 = 1 \cdot (-1) \cdot (-1) = 1$$

$$\Delta w_b = 1 \cdot 1 \cdot (-1) = -1$$

New weights:

$$w_1 = 1 + (-1) = 0$$

$$w_2 = 1 + 1 = 2$$

$$w_b = 1 + (-1) = 0$$

Final Weights:

After processing both patterns, the final weights are:

$$w_1=0, w_2=2, w_b=0$$

The network computes the output as:

$$y = \text{sgn}(w_1 \cdot X_1 + w_2 \cdot X_2 + w_b \cdot b)$$

10. Hebbian Network & Learning Rule

A **Hebbian Network** is a type of neural network that follows **Hebb's Learning Rule**, proposed by **Donald Hebb (1949)**. It is based on the principle:

"Neurons that fire together, wire together."

This means if two neurons activate together frequently, the connection (synapse) between them strengthens.

Step-by-Step Process of Hebbian Learning

1. Initialize Weights

- Assign **small random values** to weights (W_{ij}).
- Bias is usually **not** considered in Hebbian learning.

2. Compute Net Input

For a given input vector $X=(x_1,x_2,...,x_n)$

$$Z_j = \sum W_{ij}x_i$$

where:

- Z_j is the net input for neuron j .
- W_{ij} is the weight between neurons i and j .

3. Apply Activation Function

- A threshold or **step function** is used to determine the output Y_j :

$$Y_j = \begin{cases} 1, & \text{if } Z_j \geq 0 \\ 0, & \text{otherwise} \end{cases}$$

4. Update Weights Using Hebbian Learning Rule

- The weight update formula is:

$$W_{ij} = W_{ij} + \eta \times x_i \times Y_j$$

where:

- η is the **learning rate**.
- x_i is the **input**.
- Y_j is the **output**.

5. Repeat Until Convergence

- Keep repeating steps 2-4 for all training samples.
- The weights will stabilize over time as similar patterns strengthen connections.

Example of Hebbian Learning

Given:

- Learning rate $\eta = 0.1$
- Initial weights: $W_1 = 0.2, W_2 = -0.3$
- Input: $X = (1, 1)$
- Desired Output: $Y = 1$

Step 1: Compute Net Input

$$Z = (0.2 \times 1) + (-0.3 \times 1) = -0.1$$

Since $Z < 0$, apply activation:

$Y = 0$ (incorrect prediction).

Step 2: Update Weights

$$W_1 = 0.2 + (0.1 \times 1 \times 1) = 0.3$$

$$W_2 = -0.3 + (0.1 \times 1 \times 1) = -0.2$$

👉 Repeat this process until weights converge!

Key Features of Hebbian Network

- ✅ **Biologically Inspired** – Mimics brain learning.
- ✅ **Unsupervised Learning** – No labeled outputs required.
- ❌ **Unstable Growth** – Weights can grow indefinitely without normalization.

Would you like a Python implementation of Hebbian Learning? 😊

15. Bias:

Bias in a neural network is a constant value added to the weighted sum of inputs before passing through an activation function. It helps shift the activation boundary, allowing the model to learn more complex patterns.

- **Formula:**

$$Y=f(WX+B)$$

where **W** = weights, **X** = inputs, **B** = bias, and **f** = activation function.

- **Example:** In a perceptron, bias ensures the decision boundary is not always forced to pass through the origin.
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Threshold:

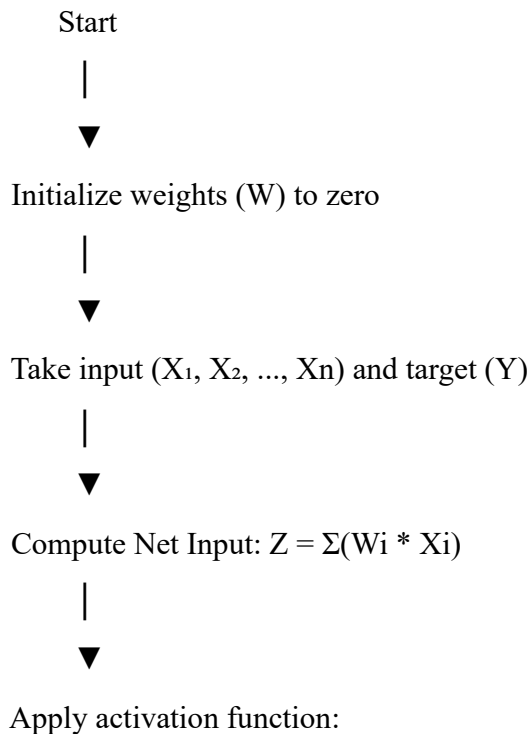
Threshold is the value at which a neuron gets activated in a perceptron model. If the weighted sum of inputs exceeds this threshold, the neuron fires (outputs 1); otherwise, it remains inactive (outputs 0).

- **Formula (for step activation function):**

$$Y=\begin{cases} 1, & \text{if } WX+B \geq \text{Threshold} \\ 0, & \text{otherwise} \end{cases}$$

- **Example:** In a binary classifier, if the weighted sum is greater than the threshold, the model classifies it as positive; otherwise, negative.

17. Flowchart of Hebbian Learning Algorithm



If $Z \geq 0$, Output = 1

Else, Output = -1

|



Update Weights: $W_i = W_i + \eta * X_i * Y$

|



More training samples?

Yes

|



Take next input sample

|

|

|



No

|



Display Final Weights

|



Stop

19. Significance of Weights and Connections in an Artificial Neural Network (ANN):

1. Weights in ANN:

- Weights represent the **strength of the connection** between neurons in different layers.
- Each input is multiplied by a weight before being passed to the next neuron, determining how much influence the input has on the output.
- Adjusting weights during training helps the network learn patterns from data.
- **Example:** In a neural network for image recognition, higher weights may be assigned to pixels representing important features like edges or shapes.

Mathematical Representation:

$$Y = f(WX + B)$$

where **W** = weight, **X** = input, **B** = bias, and **f** = activation function.

2. Connections in ANN:

- Connections link neurons in one layer to neurons in the next, facilitating information flow.
- Stronger connections (higher weights) indicate **more significant relationships** between neurons.
- Different ANN architectures (e.g., **Feedforward, Convolutional, Recurrent**) have different connection structures to process specific types of data.

Why Are Weights and Connections Important?

- ✔ **Learning and Adaptation:** Weights are updated during training to minimize errors and improve accuracy.
- ✔ **Feature Extraction:** Helps detect meaningful patterns in data, such as edges in images or words in text.
- ✔ **Decision Making:** Determines how input data propagates through the network, impacting final predictions.

20. Impact of Activation Function on Learning Capability of a Neural Network

The **choice of activation function** significantly influences how a neural network learns and makes predictions. It affects:

1. **Non-linearity** (ability to model complex relationships)
2. **Gradient flow** (during backpropagation)
3. **Training speed and stability**

Activation Function	Formula	Effect on Learning
Step Function	$f(x)=1 \text{ if } x \geq 0$	Suitable for binary classification but not useful for deep networks as it lacks smooth gradients.
Sigmoid	$f(x)=1/(1+e^{-x})$	Helps in smooth gradient flow but suffers from vanishing gradient for large or small values.
Tanh	$f(x)=(e^{x}-e^{-x})/(e^{x}+e^{-x})$	Works better than Sigmoid by centering outputs around zero, reducing bias.
ReLU (Rectified Linear Unit)	$f(x)=\max(0,x)$	Reduces vanishing gradient problem but can suffer from dying ReLU (neurons becoming inactive).
Leaky ReLU	$f(x)=x \text{ if } x > 0 \text{ else } 0.01x$	Solves dying ReLU by allowing small gradients for negative values.

Activation Function	Formula	Effect on Learning
Softmax	$f(x_i) = \frac{e^{x_i}}{\sum e^{x_j}}$	Used in multi-class classification to output probability distribution.

22. Difference Between Training and Testing in Neural Networks

Feature	Training Phase	Testing Phase
Purpose	The neural network learns patterns from labeled data by adjusting weights and biases.	The trained model is evaluated on unseen data to measure its accuracy and generalization.
Data Used	Uses training dataset , which includes input-output pairs for learning.	Uses testing dataset , which is separate from training data and never seen before.
Process	<ul style="list-style-type: none"> - Forward propagation calculates output. - Backpropagation updates weights using loss function and optimization algorithms like SGD, Adam, RMSprop. 	<ul style="list-style-type: none"> - The trained model takes input and predicts the output without adjusting weights. - The performance is measured using metrics like accuracy, precision, recall, F1-score, and mean squared error (MSE).
Weight Updates	Weights are adjusted iteratively to minimize errors.	Weights remain fixed (no updates).
Outcome	The model learns patterns, relationships, and features in data.	Determines how well the model can generalize to unseen data.