

1. soru

Soru 1

$$A \cdot v = \lambda \cdot v \quad A = \begin{bmatrix} 4 & 1 & -1 \\ 5 & 2 & -3 \\ 0 & -3 & 7 \end{bmatrix}$$

$$A \cdot v - \lambda \cdot v = 0$$

$$(A - \lambda I) \cdot v = 0$$

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$$|A - \lambda I| = 0$$

$$A - \lambda I = \begin{bmatrix} 4 & 1 & -1 \\ 5 & 2 & -3 \\ 0 & -3 & 7 \end{bmatrix} - \begin{bmatrix} \lambda & 0 & 0 \\ 0 & \lambda & 0 \\ 0 & 0 & \lambda \end{bmatrix} = \begin{bmatrix} 4-\lambda & 1 & -1 \\ 5 & 2-\lambda & -3 \\ 0 & -3 & 7-\lambda \end{bmatrix}$$

$$[(4-\lambda)(2-\lambda)(7-\lambda) + 15 + 0] - [0 + 36 - 9\lambda + 35 - 5\lambda] = 0$$

$$[(8 + \lambda - 6\lambda), (7-\lambda) + 15] - (71 - 14\lambda) = 0$$

$$[56 + 7\lambda - 42\lambda - 8\lambda - \lambda^3 + 6\lambda^2 + 15] - (71 - 14\lambda) = 0$$

$$- \lambda^3 + 13\lambda^2 - 38\lambda = 0$$

$$- \lambda^2 + 13\lambda - 38 = 0$$

$$\lambda^2 - 13\lambda + 38 = 0$$

$$(\lambda - 9)(\lambda - 4)$$

$$\lambda_1 = 0$$

en küçük
öz değeri

$$\lambda_2 = 4, \lambda_3 = 9$$

$$\lambda_1 = 0 \text{ için}$$

$$(A - 0 \cdot I) \cdot v = 0$$

$$\begin{bmatrix} 4 & 1 & -1 \\ 5 & 2 & -3 \\ 0 & -3 & 7 \end{bmatrix} \cdot \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

$$\left[\begin{array}{ccc|c} 4 & 1 & -1 & 0 \\ 5 & 2 & -3 & 0 \\ 0 & -3 & 7 & 0 \end{array} \right] \xrightarrow{R_1 \leftarrow \frac{5}{4}R_1 + R_2} \left[\begin{array}{ccc|c} 4 & 1 & -1 & 0 \\ 0 & \frac{3}{4} & -\frac{7}{4} & 0 \\ 0 & -3 & 7 & 0 \end{array} \right] \xrightarrow{4R_2 + R_3 \rightarrow R_3} \left[\begin{array}{ccc|c} 4 & 1 & -1 & 0 \\ 0 & \frac{3}{4} & -\frac{7}{4} & 0 \\ 0 & 0 & 0 & 0 \end{array} \right]$$

$$4x_1 + x_2 - x_3 = 0$$

$$3x_2 - 7x_3 = 0$$

$$-3x_2 - 7x_3 = 0$$

$$x_2 = -\frac{7}{3}x_3$$

$$4x_1 - \frac{7}{3}x_3 = 0$$

$$4x_1 = \frac{7}{3}x_3$$

$$x_1 = \frac{7}{12}x_3$$

$$\begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} \frac{7}{12} \\ -\frac{7}{3} \\ 1 \end{bmatrix}$$

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vektör

2. soru

Soru 2

$$f'(c) = \frac{f(b) - f(a)}{b - a} \quad \frac{1}{4} < 2 - \sqrt{3} < \frac{1}{2\sqrt{3}}$$
$$f'(2 - \sqrt{3}) = \frac{f(\frac{1}{2\sqrt{3}}) - f(\frac{1}{4})}{\frac{1}{2\sqrt{3}} - \frac{1}{4}} =$$

3. soru

Soru 3

$$\frac{x}{y} = \frac{91}{500} \quad \frac{x+5}{y+6} = \frac{105}{500}$$
$$\begin{aligned} 500x + 2500 &= 105y + 630 \\ 500x &\approx 91y \end{aligned} \quad \longrightarrow \quad \begin{aligned} 91y + 2500 &= 105y + 630 \\ 1870 &= 14y \\ 133,57 &\approx y \\ y &\rightarrow 134 \quad y_0 \text{ da } y \rightarrow 133 \end{aligned}$$