

Reward Maximization Perspective

$$X \succeq Y \iff \sum_{t \geq 0} r(X_t) \geq \sum_{t \geq 0} r(Y_t)$$

$$r_{\theta}(q_{<t}, o_t) = \alpha \log \frac{\pi_{\theta}(o_t | q_{<t})}{\pi_{\text{ref}}(o_t | q_{<t})}$$

Question (q)

Alice eats 3 eggs and Bob eats 2 eggs every morning. How many dozens will Alice eat in 4 weeks?

Step 1 (o_1)

Since there are 7 days in a week and Alice eats 3 eggs every day:

3 eggs \times 7 days = 21 eggs/week

...

Step t (o_t)

Now, we take the weekly total and multiply it by 4 weeks:

21 eggs \times 4 weeks = 84 eggs total

Step $t+1$ (o_{t+1})

A dozen is equal to 12 eggs.
1 dozen = 12 eggs

Step $T-1$ (o_{T-1})

Divide the total number by 12:

84 \div 12 = 7

Answer (o_T)

Alice will eat 7 dozen eggs in 4 weeks.



rollout μ

Regret Minimization Perspective

$$X \succeq Y \iff \sum_{t \geq 0} \text{Reg}(X_t) \leq \sum_{t \geq 0} \text{Reg}(Y_t)$$

$$-\text{Reg}_{\theta}^{\mu}(q_{<t}, o_t) = \alpha \log \frac{\pi_{\theta}(o_t | q_{<t})}{\pi_{\text{ref}}(o_t | q_{<t})}$$

Sequential forward KL divergence

$$-\alpha \bar{\mathbb{D}}_{\text{KL}}(\mu || \pi_{\theta}; q_{<t}, o_t)$$

Human evaluate actions via **prospective, counterfactual** reasoning toward a verifiable state.