

ARG+BRZ

November 8, 2016

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In [1]: using JuMP
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1 2016

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In [2]: ORIG = ["MDP", "PAB", "LAF-MDP", "LAF-PAB"];
        DEST = ["ILN", "BLG", "JPN", "CHN", "MEX", "PER", "SINK"];

        supply = [16 15 16 16];
        US=16
        demand = [8.86 0.74 8.26 8.86 2.96 4.42 0]

        #@assert sum(supply) == sum(demand);
        la = 750
        lb = 650
        cost = [
        720          1330          1550          1450          450          220      0;
        670          1350          1550          1450          400          200      0;
        720+la    1330+la    1550+la    1450+la    450+la    220+la    0;
        670+lb    1350+lb    1550+lb    1450+lb    400+lb    200+lb    0;
        ]

        m = Model();

        @variable(m, Trans[i=1:length(ORIG), j=1:length(DEST)] >= 0);

        @objective(m, Min, sum{cost[i,j] * Trans[i,j], i=1:length(ORIG), j=1:length(DEST)});

        @constraint(m, xyconstr[i=1:1:length(ORIG)], sum{Trans[i,j], j=1:length(DEST)} == supply[i]);

        @constraint(m, xyconstr[j = 1:length(DEST)], sum{Trans[i,j], i=1:length(ORIG)} >= demand[j]);

        @constraint(m, xyconstr[j = 1:length(DEST)], sum{Trans[i,j], i=3:(length(ORIG)-1)} <= US);

        println("Solving original problem...")
        status = solve(m);

        if status == :Optimal
            @printf("Optimal!\n");
            @printf("Objective value: %.2f\n", getobjectivevalue(m));
            @printf("Transpotation:\n");
```

```

    for j = 1:length(DEST)
        @printf("\t%s", DEST[j]);
    end
    @printf("\n");
    for i = 1:length(ORIG)
        @printf("%s", ORIG[i]);
        for j = 1:length(DEST)
            @printf("\t%.2f", getvalue(Trans[i,j]));
        end
        @printf("\n");
    end
end
else
    @printf("No solution\n");
end

```

Solving original problem...

Optimal!

Objective value: 36653.40

Transpotation:

	ILN	BLG	JPN	CHN	MEX	PER	SINK	
MDP	0.00	0.74	8.26	7.00	0.00	0.00	0.00	0.00
PAB	5.76	0.00	0.00	1.86	2.96	4.42	0.00	0.00
LAF-MDP	0.00	0.00	0.00	0.00	0.00	0.00	0.00	16.00
LAF-PAB	3.10	0.00	0.00	0.00	0.00	0.00	0.00	12.90

2 2017

```

In [3]: ORIG = ["MDP", "PAB", "LAF-MDP", "LAF-PAB"];
        DEST = ["ILN", "BLG", "JPN", "CHN", "MEX", "PER", "SINK"];

        supply = [18 18 16 16];
        US=16
        demand = [9.66 0.81 9 9.66 3.22 4.83 0]

        #@assert sum(supply) == sum(demand);
        la = 750
        lb = 650
        cost = [
            720      1330      1550      1450      450      220      0;
            670      1350      1550      1450      400      200      0;
            720+la  1330+la  1550+la  1450+la  450+la  220+la  0;
            670+lb  1350+lb  1550+lb  1450+lb  400+lb  200+lb  0;
        ]

        m = Model();

        @variable(m, Trans[i=1:length(ORIG), j=1:length(DEST)] >= 0);

        @objective(m, Min, sum{cost[i,j] * Trans[i,j], i=1:length(ORIG), j=1:length(DEST)});

        @constraint(m, xyconstr[i=1:1:length(ORIG)], sum{Trans[i,j], j=1:length(DEST)} == supply[i]);

```

```

@constraint(m, xyconstr[j = 1:length(DEST)], sum{Trans[i,j], i=1:length(ORIG)} >= demand[j]);

@constraint(m, xyconstr[j = 1:length(DEST)], sum{Trans[i,j], i=3:(length(ORIG)-1)} <= US);

println("Solving original problem...")
status = solve(m);

if status == :Optimal
    @printf("Optimal!\n");
    @printf("Objective value: %.2f\n", getobjectivevalue(m));
    @printf("Transpotation:\n");
    for j = 1:length(DEST)
        @printf("\t%s", DEST[j]);
    end
    @printf("\n");
    for i = 1:length(ORIG)
        @printf("%s", ORIG[i]);
        for j = 1:length(DEST)
            @printf("\t%.2f", getvalue(Trans[i,j]));
        end
        @printf("\n");
    end
else
    @printf("No solution\n");
end

```

Solving original problem...

Optimal!

Objective value: 38527.50

Transpotation:

	ILN	BLG	JPN	CHN	MEX	PER	SINK	
MDP	0.00	0.81	9.00	8.19	0.00	0.00	0.00	0.00
PAB	8.48	0.00	0.00	1.47	3.22	4.83	0.00	0.00
LAF-MDP	0.00	0.00	0.00	0.00	0.00	0.00	0.00	16.00
LAF-PAB	1.18	0.00	0.00	0.00	0.00	0.00	0.00	14.82

3 2018

```

In [4]: ORIG = ["MDP", "PAB", "LAF-MDP", "LAF-PAB"];
        DEST = ["ILN", "BLG", "JPN", "CHN", "MEX", "PER", "SINK"];

```

```
supply = [12 18 21 21];
```

```
US=21
```

```
demand = [11.88 0.99 11.09 11.88 3.96 5.94 0]
```

```
#@assert sum(supply) == sum(demand);
```

```
la = 750
```

```
lb = 650
```

```
cost = [
```

```
720      1330      1550      1450      450      220  0;
```

```
670      1350      1550      1450      400      200  0;
```

```
720+la  1330+la  1550+la  1450+la  450+la  220+la  0;
```

```

670+1b    1350+1b    1550+1b    1450+1b    400+1b    200+1b    0;
]

m = Model();

@variable(m, Trans[i=1:length(ORIG), j=1:length(DEST)] >= 0);

@objective(m, Min, sum{cost[i,j] * Trans[i,j], i=1:length(ORIG), j=1:length(DEST)});

@constraint(m, xyconstr[i=1:1:length(ORIG)], sum{Trans[i,j], j=1:length(DEST)} == supply[i]);

@constraint(m, xyconstr[j = 1:length(DEST)], sum{Trans[i,j], i=1:length(ORIG)} >= demand[j]);

@constraint(m, xyconstr[j = 1:length(DEST)], sum{Trans[i,j], i=3:(length(ORIG)-1)} <= US);

println("Solving original problem...")
status = solve(m);

if status == :Optimal
    @printf("Optimal!\n");
    @printf("Objective value: %.2f\n", getobjectivevalue(m));
    @printf("Transpotation:\n");
    for j = 1:length(DEST)
        @printf("\t%s", DEST[j]);
    end
    @printf("\n");
    for i = 1:length(ORIG)
        @printf("%s", ORIG[i]);
        for j = 1:length(DEST)
            @printf("\t%.2f", getvalue(Trans[i,j]));
        end
        @printf("\n");
    end
else
    @printf("No solution\n");
end
end

```

Solving original problem...

Optimal!

Objective value: 56694.80

Transpotation:

	ILN	BLG	JPN	CHN	MEX	PER	SINK	
MDP	0.00	0.99	7.23	3.78	0.00	0.00	0.00	0.00
PAB	0.00	0.00	0.00	8.10	3.96	5.94	0.00	0.00
LAF-MDP	0.00	0.00	0.00	0.00	0.00	0.00	0.00	21.00
LAF-PAB	11.88	0.00	3.86	0.00	0.00	0.00	0.00	5.26

4 2019

```

In [5]: ORIG = ["MDP", "PAB", "LAF-MDP", "LAF-PAB"];
        DEST = ["ILN", "BLG", "JPN", "CHN", "MEX", "PER", "SINK"];

```

```

supply = [20 20 22 22];
US=22
demand = [12.56 1.04 11.64 12.47 4.16 6.24 0]

#@assert sum(supply) == sum(demand);
la = 750
lb = 650
cost = [
720          1330          1550          1450          450          220    0;
670          1350          1550          1450          400          200    0;
720+la      1330+la      1550+la      1450+la      450+la      220+la    0;
670+lb      1350+lb      1550+lb      1450+lb      400+lb      200+lb    0;
]

m = Model();

@variable(m, Trans[i=1:length(ORIG), j=1:length(DEST)] >= 0);

@objective(m, Min, sum{cost[i,j] * Trans[i,j], i=1:length(ORIG), j=1:length(DEST)});

@constraint(m, xyconstr[i=1:1:length(ORIG)], sum{Trans[i,j], j=1:length(DEST)} == supply[i]);

@constraint(m, xyconstr[j = 1:length(DEST)], sum{Trans[i,j], i=1:length(ORIG)} >= demand[j]);

@constraint(m, xyconstr[j = 1:length(DEST)], sum{Trans[i,j], i=3:(length(ORIG)-1)} <= US);

println("Solving original problem...")
status = solve(m);

if status == :Optimal
    @printf("Optimal!\n");
    @printf("Objective value: %.2f\n", getobjectivevalue(m));
    @printf("Transpotation:\n");
    for j = 1:length(DEST)
        @printf("\t%s", DEST[j]);
    end
    @printf("\n");
    for i = 1:length(ORIG)
        @printf("%s", ORIG[i]);
        for j = 1:length(DEST)
            @printf("\t%.2f", getvalue(Trans[i,j]));
        end
        @printf("\n");
    end
else
    @printf("No solution\n");
end

```

```

Solving original problem...
Optimal!
Objective value: 54105.40

```

Transpotation:

	ILN	BLG	JPN	CHN	MEX	PER	SINK	
MDP	0.00	1.04	11.64	7.32	0.00	0.00	0.00	
PAB	4.45	0.00	0.00	5.15	4.16	6.24	0.00	
LAF-MDP	0.00	0.00	0.00	0.00	0.00	0.00	22.00	
LAF-PAB	8.11	0.00	0.00	0.00	0.00	0.00	13.89	

5 2020

```
In [6]: ORIG = ["MDP", "PAB", "LAF-MDP", "LAF-PAB"];
        DEST = ["ILN", "BLG", "JPN", "CHN", "MEX", "PER", "SINK"];

        supply = [21 24 28 28];
        US=22
        demand = [14.02 1.17 13.09 14.02 4.67 7.01 0]

        #@assert sum(supply) == sum(demand);
        la = 750
        lb = 650
        cost = [
            720      1330      1550      1450      450      220      0;
            670      1350      1550      1450      400      200      0;
            720+la    1330+la    1550+la    1450+la    450+la    220+la    0;
            670+lb    1350+lb    1550+lb    1450+lb    400+lb    200+lb    0;
        ]

        m = Model();

        @variable(m, Trans[i=1:length(ORIG), j=1:length(DEST)] >= 0);

        @objective(m, Min, sum{cost[i,j] * Trans[i,j], i=1:length(ORIG), j=1:length(DEST)});

        @constraint(m, xyconstr[i=1:1:length(ORIG)], sum{Trans[i,j], j=1:length(DEST)} == supply[i]);

        @constraint(m, xyconstr[j = 1:length(DEST)], sum{Trans[i,j], i=1:length(ORIG)} >= demand[j]);

        @constraint(m, xyconstr[j = 1:length(DEST)], sum{Trans[i,j], i=3:(length(ORIG)-1)} <= US);

        println("Solving original problem...")
        status = solve(m);

        if status == :Optimal
            @printf("Optimal!\n");
            @printf("Objective value: %.2f\n", getobjectivevalue(m));
            @printf("Transpotation:\n");
            for j = 1:length(DEST)
                @printf("\t%s", DEST[j]);
            end
            @printf("\n");
            for i = 1:length(ORIG)
                @printf("%s", ORIG[i]);
```

```

        for j = 1:length(DEST)
            @printf("\t%.2f", getvalue(Trans[i,j]));
        end
        @printf("\n");
    end
else
    @printf("No solution\n");
end

```

Solving original problem...

Optimal!

Objective value: 61275.00

Transpotation:

	ILN	BLG	JPN	CHN	MEX	PER	SINK	
MDP	0.00	1.17	7.09	12.74	0.00	0.00	0.00	
PAB	11.04	0.00	0.00	1.28	4.67	7.01	0.00	
LAF-MDP	0.00	0.00	6.00	0.00	0.00	0.00	22.00	
LAF-PAB	2.98	0.00	0.00	0.00	0.00	0.00	25.02	

In []: