LAF+ARG

November 8, 2016

1 Minimize the cost of shipment, given that Brazil can not manufacture.

```
In [11]: using JuMP
```

2 2016

```
In [12]: ORIG = ["LAF", "MDP", "PAB-LAF", "PAB-MDP"];
         DEST = ["ILN", "BLG", "JPN", "CHN", "MEX", "PER", "SINK"];
         supply = [16 16 15 15];
         BR=15
         demand = [8.86 \ 0.74 \ 8.26 \ 8.86 \ 2.96 \ 4.42 \ 0]
         #@assert sum(supply) == sum(demand);
         bl = 700
         ba=150
         cost = [
         120
                    1250
                               2580
                                         2300
                                                   450
                                                            720 0;
                    1330
                             1550
                                         1450
                                                   450
                                                            220
                                                                  0;
         120+bl 1250+bl 2580+bl 2300+bl
                                                450+bl
                                                         720+bl
                                                                  0;
         720+ba
                 1330+ba
                          1550+ba 1450+ba
                                              450+ba
                                                         220+ba
        1
         m = Model();
         @variable(m, Trans[i=1:length(ORIG), j=1:length(DEST)] >= 0);
         @objective(m, Min, sum{cost[i,j] * Trans[i,j], i=1:length(ORIG), j=1:length(DEST)});
         @constraint(m, xyconstr[i=1:1:length(ORIG)], sum{Trans[i,j], j=1:length(DEST)} == supply[i]);
         @constraint(m, xyconstr[j = 1:length(DEST)], sum{Trans[i,j], i=1:length(ORIG)} >= demand[j]);
         @constraint(m, xyconstr[j = 1:length(DEST)], sum{Trans[i,j], i=3:(length(ORIG)-1)} <= BR);</pre>
         println("Solving original problem...")
         status = solve(m);
```

```
if status == :Optimal
             @printf("Optimal!\n");
             @printf("Objective value: %.2f\n", getobjectivevalue(m));
             @printf("Transpotation:\n");
             for j = 1:length(DEST)
                  @printf("\t%s", DEST[j]);
             end
             @printf("\n");
             for i = 1:length(ORIG)
                  @printf("%s", ORIG[i]);
                  for j = 1:length(DEST)
                      @printf("\t%.2f", getvalue(Trans[i,j]));
                  @printf("\n");
             end
         else
              @printf("No solution\n");
         end
Solving original problem...
Optimal!
Objective value: 30773.60
Transpotation:
        ILN
                    BLG
                               JPN
                                           CHN
                                                       \texttt{MEX}
                                                                   PER
                                                                              SINK
           8.86
                        0.74
                                     0.00
                                                 0.00
                                                              2.96
                                                                           0.00
                                                                                        3.44
LAF
           0.00
                                                                                        0.00
MDP
                        0.00
                                     8.26
                                                 7.74
                                                              0.00
                                                                           0.00
PAB-LAF
                0.00
                            0.00
                                         0.00
                                                      0.00
                                                                   0.00
                                                                               0.00
                                                                                            15.00
                            0.00
PAB-MDP
               0.00
                                         0.00
                                                      1.12
                                                                   0.00
                                                                               4.42
                                                                                            9.46
    2017
3
In [13]: ORIG = ["LAF", "MDP", "PAB-LAF", "PAB-MDP"];
         DEST = ["ILN", "BLG", "JPN", "CHN", "MEX", "PER", "SINK"];
         supply = [16 18 18 18];
         BR=18
         demand = [8.86 \ 0.74 \ 8.26 \ 8.86 \ 2.96 \ 4.42 \ 0]
         #@assert sum(supply) == sum(demand);
         bl = 700
         ba=150
         cost = [
         120
                      1250
                                2580
                                           2300
                                                      450
                                                               720
                                                                      0;
         720
                      1330
                                 1550
                                           1450
                                                      450
                                                               220
                                                                      0;
                   1250+bl
                                                  450+bl
         120+bl
                             2580+bl
                                        2300+bl
                                                            720+bl
                                                                      0;
         720+ba
                   1330+ba
                             1550+ba
                                       1450+ba
                                                  450+ba
                                                            220+ba
         ٦
         m = Model();
         @variable(m, Trans[i=1:length(ORIG), j=1:length(DEST)] >= 0);
```

```
@objective(m, Min, sum{cost[i,j] * Trans[i,j], i=1:length(ORIG), j=1:length(DEST)});
         @constraint(m, xyconstr[i=1:1:length(ORIG)], sum{Trans[i,j], j=1:length(DEST)} == supply[i]);
         @constraint(m, xyconstr[j = 1:length(DEST)], sum{Trans[i,j], i=1:length(ORIG)} >= demand[j]);
         @constraint(m, xyconstr[j = 1:length(DEST)], sum{Trans[i,j], i=3:(length(ORIG)-1)} <= BR);</pre>
         println("Solving original problem...")
         status = solve(m);
         if status == :Optimal
             @printf("Optimal!\n");
             Oprintf("Objective value: %.2f\n", getobjectivevalue(m));
             Oprintf("Transpotation:\n");
             for j = 1:length(DEST)
                 @printf("\t%s", DEST[j]);
             end
             @printf("\n");
             for i = 1:length(ORIG)
                 @printf("%s", ORIG[i]);
                 for j = 1:length(DEST)
                     @printf("\t%.2f", getvalue(Trans[i,j]));
                 end
                 @printf("\n");
             end
         else
             @printf("No solution\n");
         end
Solving original problem...
Optimal!
Objective value: 30473.60
Transpotation:
                   BLG
                                                                 PER
        ILN
                               JPN
                                          CHN
                                                     MEX
                                                                            SINK
                                                0.00
LAF
           8.86
                       0.74
                                    0.00
                                                             2.96
                                                                         0.00
                                                                                      3.44
                                    8.26
                                                                                      0.00
MDP
           0.00
                       0.00
                                                8.86
                                                             0.00
                                                                         0.88
PAB-LAF
               0.00
                           0.00
                                        0.00
                                                    0.00
                                                                 0.00
                                                                             0.00
                                                                                          18.00
PAB-MDP
               0.00
                           0.00
                                        0.00
                                                    0.00
                                                                 0.00
                                                                             3.54
                                                                                          14.46
    2018
4
In [14]: ORIG = ["LAF", "MDP", "PAB-LAF", "PAB-MDP"];
         DEST = ["ILN", "BLG", "JPN", "CHN", "MEX", "PER", "SINK"];
         supply = [21 18 12 12];
```

demand = [11.88 0.99 11.09 11.88 3.96 5.94 0]

BR=12

```
bl = 700
         ba=150
         cost = [
         120
                     1250
                                2580
                                          2300
                                                     450
                                                              720
                                                                    0;
         720
                     1330
                                1550
                                          1450
                                                     450
                                                              220
                                                                    0;
         120+bl
                  1250+bl
                             2580+bl
                                       2300+bl
                                                 450+bl
                                                           720+bl
                                                                    0:
         720+ba
                                       1450+ba
                  1330+ba
                             1550+ba
                                                 450+ba
                                                           220+ba
                                                                    0
         1
         m = Model();
         @variable(m, Trans[i=1:length(ORIG), j=1:length(DEST)] >= 0);
         @objective(m, Min, sum{cost[i,j] * Trans[i,j], i=1:length(ORIG), j=1:length(DEST)});
         @constraint(m, xyconstr[i=1:1:length(ORIG)], sum{Trans[i,j], j=1:length(DEST)} == supply[i]);
         @constraint(m, xyconstr[j = 1:length(DEST)], sum{Trans[i,j], i=1:length(ORIG)} >= demand[j]);
         @constraint(m, xyconstr[j = 1:length(DEST)], sum{Trans[i,j], i=3:(length(ORIG)-1)} <= BR);</pre>
         println("Solving original problem...")
         status = solve(m);
         if status == :Optimal
             Oprintf("Optimal!\n");
             Oprintf("Objective value: %.2f\n", getobjectivevalue(m));
             Oprintf("Transpotation:\n");
             for j = 1:length(DEST)
                 @printf("\t%s", DEST[j]);
             @printf("\n");
             for i = 1:length(ORIG)
                 @printf("%s", ORIG[i]);
                 for j = 1:length(DEST)
                     @printf("\t%.2f", getvalue(Trans[i,j]));
                 @printf("\n");
             end
         else
             @printf("No solution\n");
         end
Solving original problem...
Optimal!
Objective value: 41803.90
Transpotation:
                   BLG
                               JPN
                                          CHN
                                                     MEX
                                                                 PER
                                                                            SINK
                                     0.00
           11.88
                         0.99
                                                 0.00
LAF
                                                              3.96
                                                                           0.00
                                                                                       4.17
MDP
           0.00
                       0.00
                                    11.09
                                                 6.91
                                                              0.00
                                                                           0.00
                                                                                       0.00
```

#@assert sum(supply) == sum(demand);

PAB-LAF	0.00	0.00	0.00	0.00	0.00	0.00	12.00
PAB-MDP	0.00	0.00	0.00	4.97	0.00	5.94	1.09

5 2019

```
In [15]: ORIG = ["LAF", "MDP", "PAB-LAF", "PAB-MDP"];
         DEST = ["ILN", "BLG", "JPN", "CHN", "MEX", "PER", "SINK"];
         supply = [22 20 20 20];
         BR=20
         demand = [12.56 \ 1.04 \ 11.64 \ 12.47 \ 4.16 \ 6.24 \ 0]
         #@assert sum(supply) == sum(demand);
         bl = 700
         ba=150
         cost = [
         120
                     1250
                                2580
                                          2300
                                                    450
                                                              720
                                                                    0;
         720
                     1330
                                1550
                                          1450
                                                    450
                                                              220
                                                                    0;
         120+bl
                 1250+bl
                            2580+bl
                                       2300+bl
                                                 450+bl
                                                          720+bl
                                                                    0;
         720+ba
                  1330+ba
                            1550+ba
                                     1450+ba
                                                 450+ba
                                                          220+ba
         m = Model();
         @variable(m, Trans[i=1:length(ORIG), j=1:length(DEST)] >= 0);
         @objective(m, Min, sum{cost[i,j] * Trans[i,j], i=1:length(ORIG), j=1:length(DEST)});
         @constraint(m, xyconstr[i=1:1:length(ORIG)], sum{Trans[i,j], j=1:length(DEST)} == supply[i]);
         @constraint(m, xyconstr[j = 1:length(DEST)], sum{Trans[i,j], i=1:length(ORIG)} >= demand[j]);
         @constraint(m, xyconstr[j = 1:length(DEST)], sum{Trans[i,j], i=3:(length(ORIG)-1)} <= BR);</pre>
         println("Solving original problem...")
         status = solve(m);
         if status == :Optimal
             @printf("Optimal!\n");
             @printf("Objective value: %.2f\n", getobjectivevalue(m));
             Oprintf("Transpotation:\n");
             for j = 1:length(DEST)
                 @printf("\t%s", DEST[j]);
             @printf("\n");
             for i = 1:length(ORIG)
                 @printf("%s", ORIG[i]);
                 for j = 1:length(DEST)
```

```
Oprintf("\t%.2f", getvalue(Trans[i,j]));
                 end
                 @printf("\n");
             end
         else
             @printf("No solution\n");
         end
Solving original problem...
Optimal!
Objective value: 43728.00
Transpotation:
        ILN
                   BLG
                               JPN
                                           CHN
                                                      MEX
                                                                  PER.
                                                                             SINK
LAF
           12.56
                         1.04
                                     0.00
                                                  0.00
                                                               4.16
                                                                           0.00
                                                                                        4.24
MDP
           0.00
                        0.00
                                    11.64
                                                  8.36
                                                              0.00
                                                                           0.00
                                                                                        0.00
PAB-LAF
               0.00
                            0.00
                                        0.00
                                                     0.00
                                                                  0.00
                                                                              0.00
                                                                                           20.00
PAB-MDP
               0.00
                            0.00
                                        0.00
                                                     4.11
                                                                  0.00
                                                                              6.24
                                                                                           9.65
6
    2020
In [16]: ORIG = ["LAF", "MDP", "PAB-LAF", "PAB-MDP"];
         DEST = ["ILN", "BLG", "JPN", "CHN", "MEX", "PER", "SINK"];
         supply = [28 24 21 21];
         BR=21
         demand = [14.02 \ 1.17 \ 13.09 \ 14.02 \ 4.67 \ 7.01 \ 0]
         #@assert sum(supply) == sum(demand);
         bl = 700
         ba=150
         cost = [
         120
                      1250
                                2580
                                           2300
                                                     450
                                                              720
                                                                     0;
         720
                     1330
                                           1450
                                                     450
                                                               220
                                1550
                                                                     0;
         120+bl
                  1250+bl
                             2580+bl
                                       2300+bl
                                                  450+bl
                                                           720+bl
                                                                     0;
         720+ba
                  1330+ba
                                                           220+ba
                            1550+ba
                                      1450+ba
                                                  450+ba
                                                                     0
         1
         m = Model();
         @variable(m, Trans[i=1:length(ORIG), j=1:length(DEST)] >= 0);
         @objective(m, Min, sum{cost[i,j] * Trans[i,j], i=1:length(ORIG), j=1:length(DEST)});
         @constraint(m, xyconstr[i=1:1:length(ORIG)], sum{Trans[i,j], j=1:length(DEST)} == supply[i]);
         @constraint(m, xyconstr[j = 1:length(DEST)], sum{Trans[i,j], i=1:length(ORIG)} >= demand[j]);
         @constraint(m, xyconstr[j = 1:length(DEST)], sum{Trans[i,j], i=3:(length(ORIG)-1)} <= BR);</pre>
         println("Solving original problem...")
```

```
status = solve(m);
         if status == :Optimal
             @printf("Optimal!\n");
             @printf("Objective value: %.2f\n", getobjectivevalue(m));
             @printf("Transpotation:\n");
             for j = 1:length(DEST)
                 @printf("\t%s", DEST[j]);
             @printf("\n");
             for i = 1:length(ORIG)
                 @printf("%s", ORIG[i]);
                 for j = 1:length(DEST)
                     @printf("\t%.2f", getvalue(Trans[i,j]));
                 end
                 @printf("\n");
             end
         else
             @printf("No solution\n");
         end
Solving original problem...
Optimal!
Objective value: 48925.10
Transpotation:
        ILN
                   BLG
                              JPN
                                          CHN
                                                     MEX
                                                                PER
                                                                           SINK
                                                             4.67
                                    0.00
                                                                         0.00
                                                                                      8.14
LAF
           14.02
                        1.17
                                                 0.00
MDP
           0.00
                       0.00
                                    13.09
                                                 10.91
                                                              0.00
                                                                          0.00
                                                                                       0.00
               0.00
                           0.00
                                       0.00
                                                    0.00
                                                                0.00
                                                                            0.00
                                                                                         21.00
PAB-LAF
                           0.00
                                       0.00
                                                    3.11
                                                                0.00
                                                                                         10.88
PAB-MDP
               0.00
                                                                            7.01
```