## Problem5

## November 5, 2016

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In [3]: mysecondorder = (x,h) \rightarrow (f(x+h) - 2.0*f(x) + f(x-h))/(h^2.0)
        ddf = x \rightarrow -1.0*sin(x)
       f = x \rightarrow sin(x)
Out[3]: (anonymous function)
In [4]: x = pi/6.0
       for i=1:16
           h=10.0^{(-i)}
            addf = mysecondorder(x,h)
            err = abs(addf - ddf(x))
            @printf("%.8e %.16f %.5e\n", h, addf, err)
        end
1.00000000e-01 -0.4995834721974234 4.16528e-04
1.00000000e-02 -0.4999958333473664 4.16665e-06
1.00000000e-03 -0.4999999583255033 4.16745e-08
1.00000000e-04 -0.4999999969612645 3.03874e-09
1.00000000e-05 -0.5000005964816977 5.96482e-07
1.00000000e-06 -0.4999334279887080 6.65720e-05
1.00000000e-07 -0.4940492459581947 5.95075e-03
1.00000000e-08 -1.1102230246251563 6.10223e-01
1.00000000e-09 55.5111512312578199 5.60112e+01
1.00000000e-10 0.0000000000000 5.00000e-01
1.00000000e-11 0.0000000000000 5.00000e-01
1.00000000e-12 0.0000000000000 5.00000e-01
1.00000000e-13 5551115123.1257820129394531 5.55112e+09
1.00000000e-14 -555111512312.5782470703125000 5.55112e+11
1.00000000e-15 0.0000000000000 5.00000e-01
1.00000000e-16 -5551115123125783.00000000000000 5.55112e+15
In [5]: @show mysecondorder(x,0.2)
        Oshow mysecondorder(x,0.1)
        Oshow mysecondorder(x,0.05)
mysecondorder(x, 0.2) = -0.49833555396895646
mysecondorder(x,0.1) = -0.4995834721974234
mysecondorder(x,0.05) = -0.4998958420134868
In [7]: h0=0.2
       h1=h0/2.0
       rho0 = mysecondorder(x,h0)
       rho1 = mysecondorder(x,h1)
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```
addf0 = (4/3)*rho1 - (1/3)*rho0
       err = abs(addf0 - ddf(x))
       @printf("%.8e %.16f %.5e\n", h0, addf0, err)
       h0=h1
       h1=h0/2.0
       rho0 = mysecondorder(x,h0)
       rho1 = mysecondorder(x,h1)
       addf1 = (4/3)*rho1 - (1/3)*rho0
       err = abs(addf1 - ddf(x))
       @printf("%.8e %.16f %.5e\n", h0, addf1, err)
       h0=h1
       addf2 = (16/15)*addf1 - (1/15)*addf0
       err = abs(addf2 - ddf(x))
                             %.16f %.5e\n", addf2, err)
       @printf("Combination
2.00000000e-01 -0.4999994449402457 5.55060e-07
1.00000000e-01 -0.4999999652855079 3.47145e-08
Combination
               -0.499999999751921 2.48078e-11
In [8]: using ApproxFun
In [9]: x=pi/6.0
       f = Fun(x->sin(x))
       aprox = f''(x)
       err = abs(aprox - ddf(x))
       @printf("%.16f %.5e\n", aprox, err)
-0.499999999999885 1.14908e-14
In []:
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