

Assignment #6: Database Design - Normalization (Solution)

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Due: 8:00 PM, Nov. 12, 2020.

1. [30 points] Consider the relation $R(A,B,C,D,E,F)$. Use **synthesis method** to construct a set of 3NF relations from the following functional dependencies. Indicate the primary key for each relation in the result.

$$AB \rightarrow E$$

$$B \rightarrow ED$$

$$E \rightarrow D$$

$$DF \rightarrow A$$

$$C \rightarrow F$$

$$DC \rightarrow A$$

Solution:

- (a) Find the canonical cover of F:

- i. Transform all FDs to canonical form (i.e., one attributes on the right):

$$AB \rightarrow E$$

$$B \rightarrow E$$

$$B \rightarrow D$$

$$E \rightarrow D$$

$$DF \rightarrow A$$

$$C \rightarrow F$$

$$DC \rightarrow A$$

- ii. Drop extraneous attributes: A in $AB \rightarrow E$ is extraneous, since we have $B \rightarrow E$.

The complete proof is as follows:

Considering the minimality of LHS of $AB \rightarrow E$

First we need to compute: A^+ using minimal cover

$A^+ = A$ (Initialization)

$= A$

Done.

$\Rightarrow E$ is not subset of A^+ . So attr B is necessary.

Then, we need to compute: B^+ using minimal cover

$B^+ = B$ (Initialization)

$= BD$ ($B \rightarrow D$)

$= BDE$ ($B \rightarrow E$)

...

Done.

$\Rightarrow E$ is a subset of $(AB - A)^+$. So A is NOT necessary

The set of FDs becomes:

$B \rightarrow E$
 $B \rightarrow D$
 $E \rightarrow D$
 $DF \rightarrow A$
 $C \rightarrow F$
 $DC \rightarrow A$

iii. Drop (transitive) redundant FDs:

$B \rightarrow E$ and $E \rightarrow D$ implies $B \rightarrow D$, so we drop $B \rightarrow D$.

$C \rightarrow F$ implies $CD \rightarrow FD$. We also have $DF \rightarrow A$, so we drop $DC \rightarrow A$.

The set of FDs becomes:

$B \rightarrow E$
 $E \rightarrow D$
 $DF \rightarrow A$
 $C \rightarrow F$

which is the canonical cover of F.

(b) Find the primary key of R: Observations:

- i. B and C do not appear on the right hand side of any FD, so they have to appear in all keys of R.
- ii. BC^+ : $BC \rightarrow BCE$ (since $B \rightarrow E$) $\rightarrow BCED$ (since $E \rightarrow D$) $\rightarrow BCEDF$ (since $C \rightarrow F$) $\rightarrow BCEDFA$ (since $DF \rightarrow A$). So BC is a key of R.

In this case, we do not need to consider any other combination, because any other combination containing BC (e.g., BCD) is a super key and not minimal.

(c) We do not need to group the FDs in the canonical cover because all the determinants on the left side are unique.

(d) Construct a relation for each group:

R1 (B, E)
R2 (E, D)
R3 (D, F, A)
R4 (C, F)

(e) If none of the relations contain the key for the original relation, add a relation with the key:

R5 (B, C)

R1, R2, R3, R4, and R5 are in 3NF and in BCNF.

2. [30 points] Consider the relation R(A,B,C,D) and the following set of functional dependencies F. Apply the **decomposition method** on R to end up with BCNF relations and dependency preserving. Indicate the primary key for each relation in the result.

$A \rightarrow B$
 $B \rightarrow CD$
 $A \rightarrow D$
 $B \rightarrow C$
 $AB \rightarrow CD$

Solution:

- (a) Find the canonical cover of F:

$$A \rightarrow B$$

$$B \rightarrow D$$

$$B \rightarrow C$$

- (b) Apply the decomposition method on R to end up with BCNF relations:

- i. Using $A \rightarrow B$ to decompose R, we can get:

$$R1' (\underline{A}, C, D) \text{ in BCNF}$$

$$R2' (\underline{A}, B) \text{ in BCNF}$$

Note that this decomposition does not preserve dependencies $B \rightarrow D$ and $B \rightarrow C$, so we choose another dependency and try again from the start.

- ii. Using $B \rightarrow D$ to decompose R, we can get:

$$R1 (\underline{A}, B, C) \text{ in 2NF}$$

$$R2 (\underline{B}, D) \text{ in BCNF}$$

- iii. Using $B \rightarrow C$ to decompose R1, we can get:

$$R11 (\underline{A}, B) \text{ in BCNF}$$

$$R12 (\underline{B}, C) \text{ in BCNF}$$

A correct decomposition would be R2, R11 and R12. R2, R11 and R12 are in BCNF and dependency preserving. An efficient one that eliminates an unnecessary join is :

$$T1 (\underline{A}, B)$$

$$T2 (\underline{B}, C, D)$$

where we group R2 and R12 since they share the same primary key. T1 and T2 are in BCNF and dependency preserving.

3. [40 points] Using the table method, check if the following decomposition is good, bad or ugly. Show all steps.

R1: (ProductID, Length, Width, Height, Weight, OrderID, OrderDate, CustomerID, TotalPrice)

R2: (CustomerID, Address, City, State, ZipCode, PhoneNumber)

R3: (ProductID, OrderID, ProductQuantity)

Assume the functional dependency set to be:

FD1: $\text{ProductID} \rightarrow \text{Length, Width, Height, Weight}$

FD2: $\text{OrderID} \rightarrow \text{OrderDate, CustomerID, TotalPrice}$

FD3: $\text{CustomerID} \rightarrow \text{Address, City, State, ZipCode, PhoneNumber}$

FD4: $\text{ProductID, OrderID} \rightarrow \text{ProductQuantity}$

Hint: bad decomposition is a lossy one, while ugly decomposition is lossless but does not preserve some dependencies.

Solution:

Let the attributes be sorted in the following order:

(1) ProductID, (2) Length, (3) Width, (4) Height, (5) Weight, (6) OrderID, (7) OrderDate, (8) CustomerID, (9) TotalPrice, (10) Address, (11) City, (12) State, (13) ZipCode, (14) PhoneNumber, (15) ProductQuantity

Initially the table looks like the following. Note that the table uses simplified marks. “k” means known cell, and empty cell means “U”.

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
R1	k	k	k	k	k	k	k	k	k						
R2								k		k	k	k	k	k	
R3	k					k									k

Using FD1, we can add more “k” marks in the table. New marks are in italic uppercase.

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
R1	k	k	k	k	k	k	k	k	k						
R2								k		k	k	k	k	k	
R3	k	<i>K</i>	<i>K</i>	<i>K</i>	<i>K</i>	k									k

Then we use FD2 to update the table. New marks are in italic uppercase.

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
R1	k	k	k	k	k	k	k	k	k						
R2								k		k	k	k	k	k	
R3	k	k	k	k	k	k	<i>K</i>	<i>K</i>	<i>K</i>						k

Next, we use FD3 to update the table. New marks are in italic uppercase.

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
R1	k	k	k	k	k	k	k	k	k	<i>K</i>	<i>K</i>	<i>K</i>	<i>K</i>	<i>K</i>	
R2								k		k	k	k	k	k	
R3	k	k	k	k	k	k	k	k	k	<i>K</i>	<i>K</i>	<i>K</i>	<i>K</i>	<i>K</i>	k

Finally we use FD4 to update the table. New marks are in italic uppercase.

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
R1	k	k	k	k	k	k	k	k	k	k	k	k	k	k	<i>K</i>
R2								k		k	k	k	k	k	
R3	k	k	k	k	k	k	k	k	k	k	k	k	k	k	k

Now we have 2 rows filled with mark “k”, so it is a lossless decomposition. Since it preserves all FDs, it is a good decomposition.