



University of Pittsburgh

ECE 1150: Computer Networks

Performance Measures: Delay and Throughput

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Objectives

- What are the main components of delay?
- Perform computations to calculate delay
- Difference between bit rate and throughput

Units

- Bits: Data
- Byte is 8 bits
- Data Rate, unit is bits per second (bps):
 - How many bits you can transmit in one sec?

Table 2.1 Units used to express data rates

Unit	Equivalent in bits per second
Bits per second (bps)	–
Kilobits per second (Kbps)	1,000 (10^3 bps)
Megabits per second (Mbps)	1,000,000 (10^6 bps)
Gigabits per second (Gbps)	1,000,000,000 (10^9 bps)
Terabits per second (Tbps)	1,000,000,000,000 (10^{12} bps)

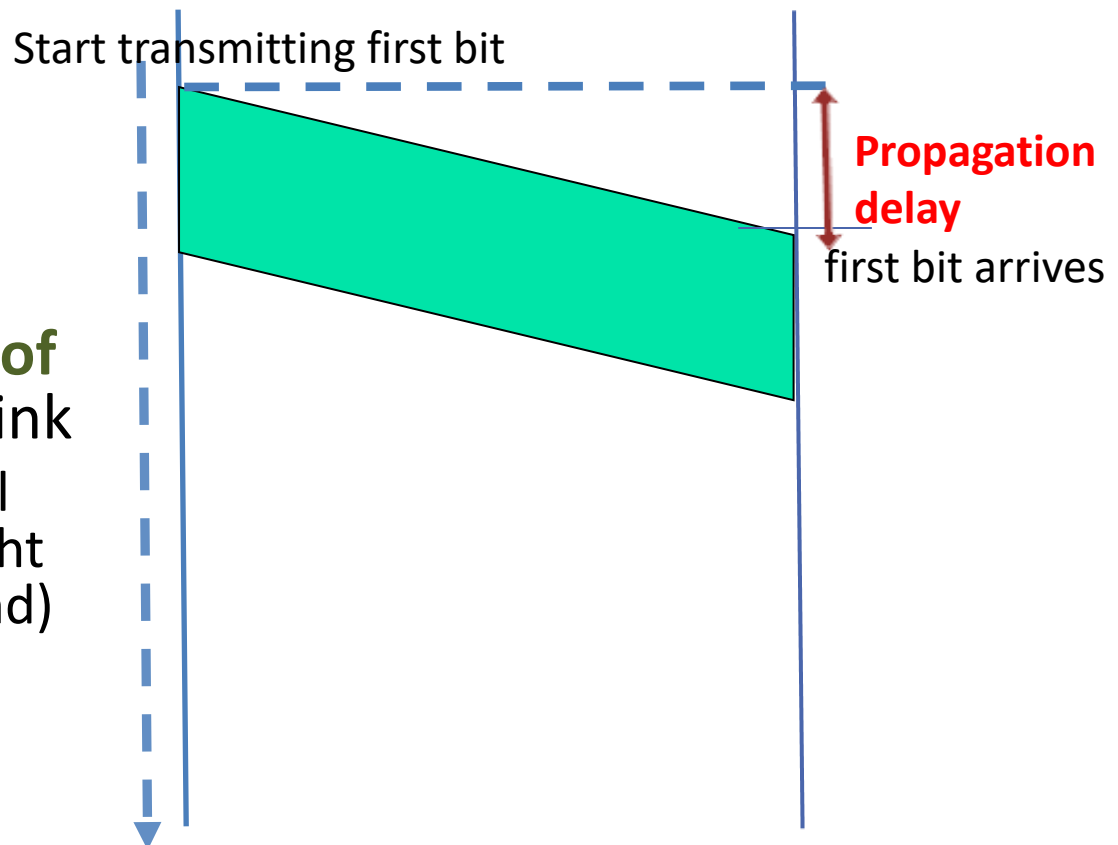
Exp.	Explicit	Prefix	Exp.	Explicit	Prefix
10^{-3}	0.001	milli	10^3	1,000	Kilo
10^{-6}	0.000001	micro	10^6	1,000,000	Mega
10^{-9}	0.000000001	nano	10^9	1,000,000,000	Giga
10^{-12}	0.0000000000001	pico	10^{12}	1,000,000,000,000	Tera
10^{-15}	0.0000000000000001	femto	10^{15}	1,000,000,000,000,000	Peta

Delay

- Propagation delay
- Transmission delay
- Processing delay
- Queuing delay

Propagation Delay

- How long does it take for **a bit to travel** from the source to the destination?
- Let L be the physical **length of the link**
- Let V be the propagation **velocity of the signal** along the link
 - Wireless signal travel with the speed of light (3×10^8 meters/second)
- **Propagation delay** is:
$$T_p = L/V$$



Thunderstorm:

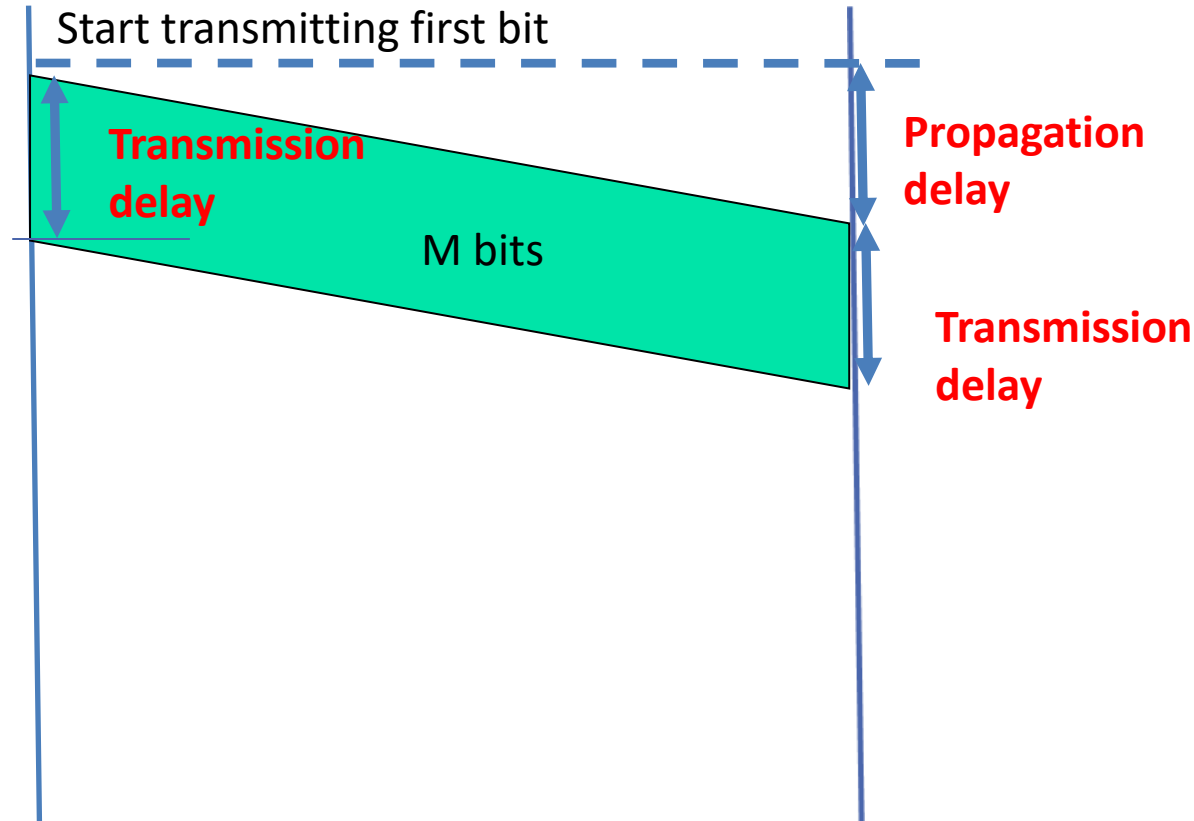
Do you hear first thunder or see first the lightning? Why?

Sample Calculation – Propagation Delay

Question: How long does it take for one bit to travel from New York to San Francisco, over a link of length 4500 km and signal travels with speed $0.8 * \text{speed of light}$. Speed of light is $3 * 10^8$ m/sec

Transmission Delay

- Time required to get message of M bits over a link of bit rate B



- $T_t = M/B$
 - Number of bits/bit rate of link

Question

- Assume a 100 Kbyte file and a link (channel) of 28.8Kb/s, how long does it take to transmit the file?

Tophat: Q_Transmission delay

Get Link Speed based on Maximum Delay

- If you know the maximum delay your application can tolerate, then you can choose the speed of the link accordingly
 - Know max delay T_t and file size (M)
- What is the bit rate of a link that can send an M bit message in T_t seconds?
 - $B = M/T_t$

Question

- Assume an application that requires a maximum transmission delay of 100msec and a channel of 28.8kbps, what is the maximum file size?

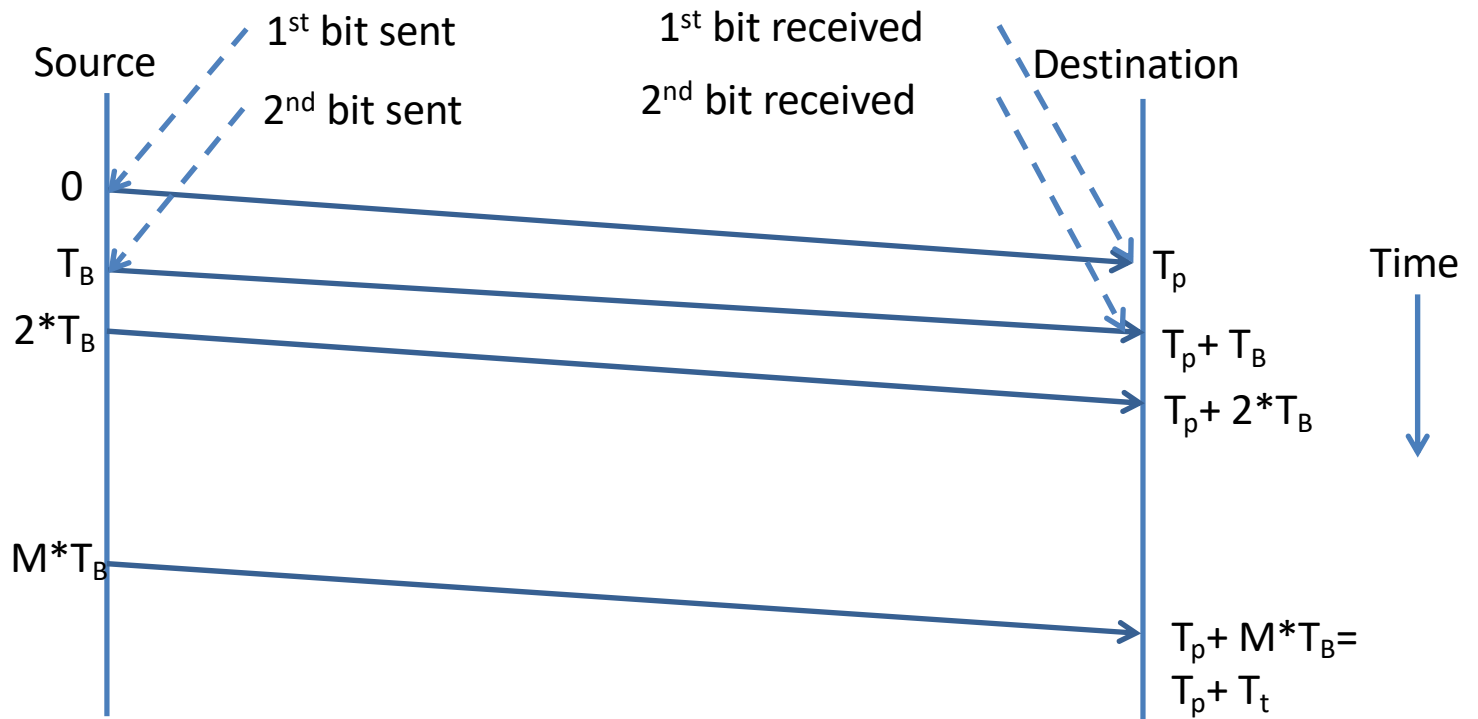
Final answer: 360 bytes

Total delay over a link

- How long would it take for a receiver to get an M bits file sent over a link of L meters, along which a signal propagates at speed V m/sec. The bit rate over the link is B bits. Time is calculated from start of transmission of first bit

Tophat: Q_{Total} delay over a link

$$T_p + T_T?$$



Note that a bit is sent every $1/B \text{ sec} = T_B$

In this case this is every $1/128 * 10^5 = 8 \text{ microseconds } (\mu\text{sec})$

Question 4

- How long would it take to receive a 10 megabyte file over a 5 km channel. The signal propagates with speed of $V=0.9 \times \text{speed of light}$, and bit rate is 128kbps (single link)? Find the delay in seconds. Round to nearest integer.

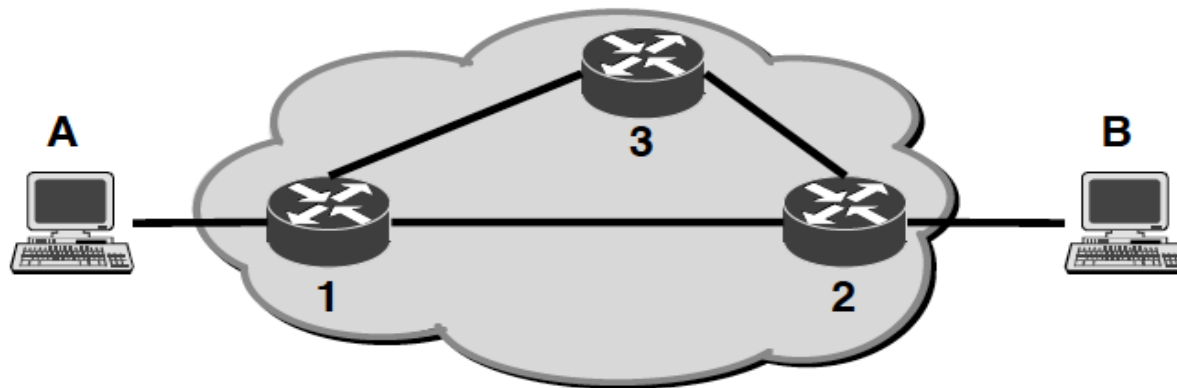
Solution

- How long would it take to receive a 10 megabyte file over a 5 km channel ($V=0.9 \times \text{speed of light}$) on a 128kbps channel?
- Answer
 - Total time = Propagation delay (T_p) + Transmission delay (T_t)
 - $T_p = L/V = (5 \times 10^3 \text{ m}) / (0.9 \times 3 \times 10^8 \text{ m/s})$
 - $T_t = M \text{ (bits)} / B = 8 \times 10^6 / (128 \times 10^3) = 8/128 \times 10^4 = 0.0625 \times 10^4 = 625 \text{ sec.}$
 - Total time =

Transmission delay is much larger than propagation delay

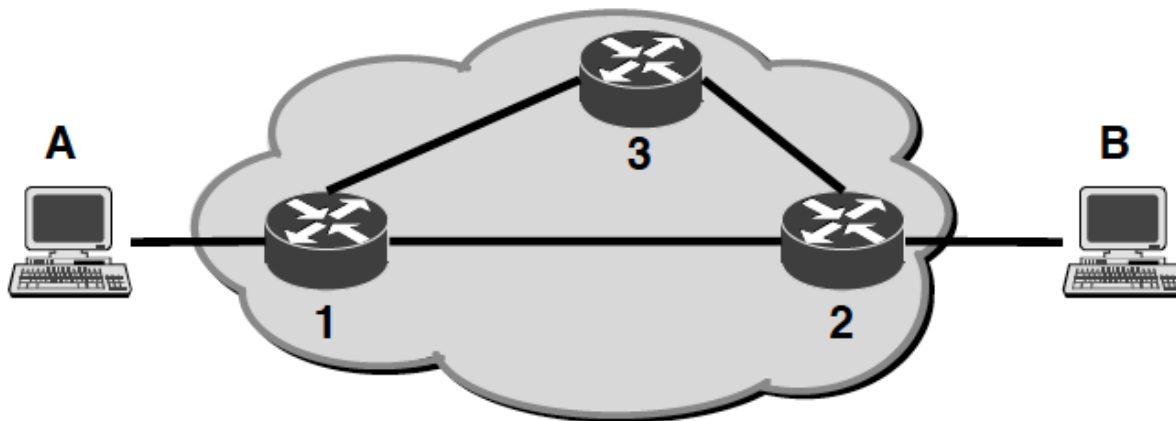
Multiple Hops Network

- End-to-end delay is the **sum of the delay encountered at each hop** from the source to the destination
 - There could be multiple hops..
 - E.g. Laptop to switch, switch to router, router to router, router to destination/server
 - E.g. A to router 1, to router 2, to destination B



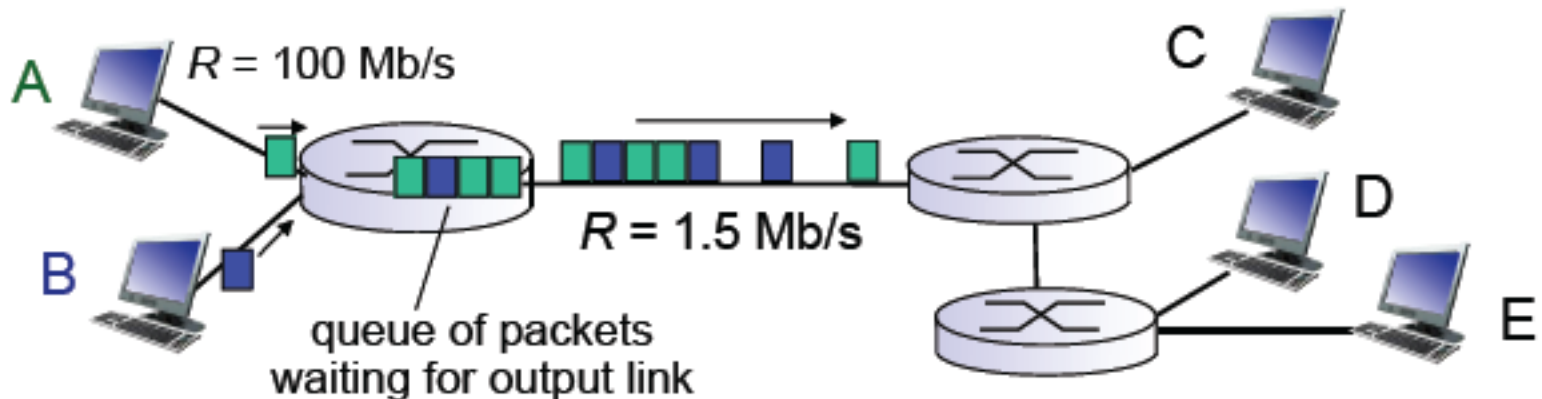
End to End Delay

- Assume path A -- 1 -- 2 -- B
 - Delay (A -> 1) + Delay (1 -> 2) + Delay (2->B)
 - This is called **end-to-end delay**



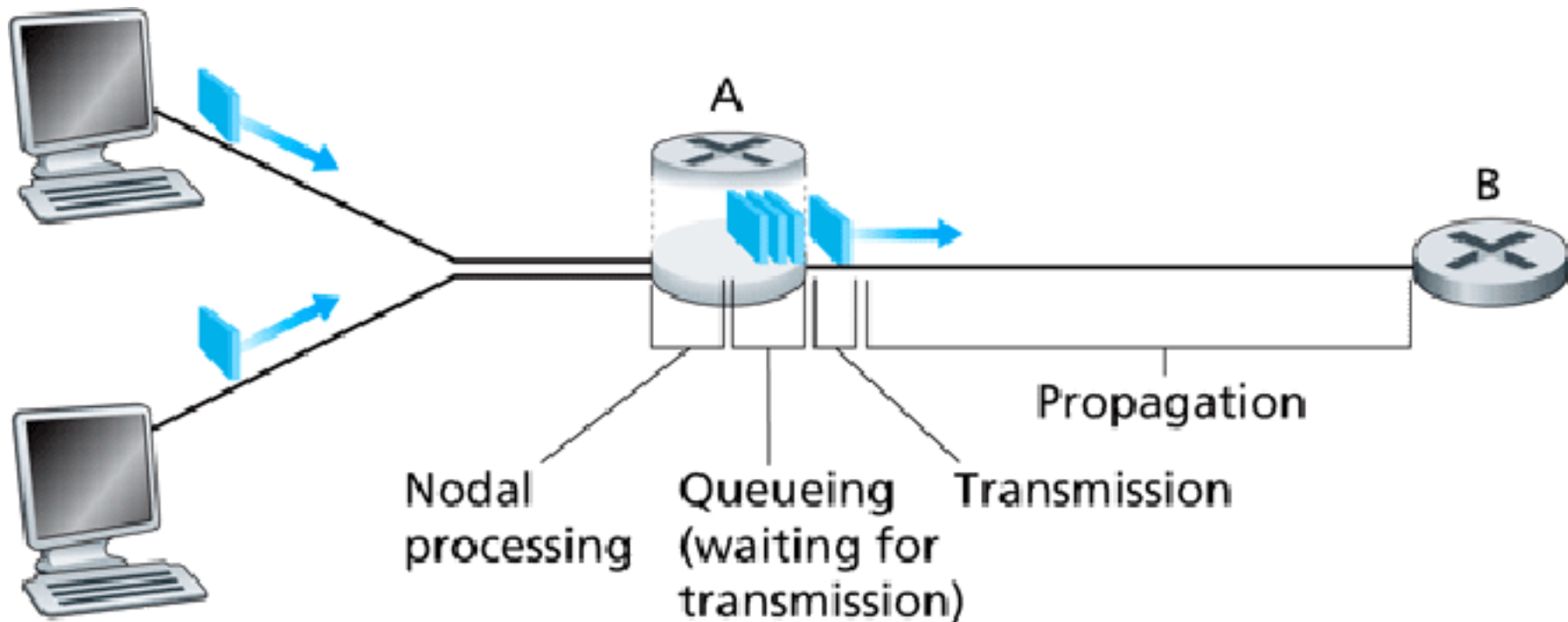
Processing Delay and Queuing Delay

- **Processing delay** is the time to process the packet within each intermediate node
 - for example to find what the next hop will be
- **Queuing delay** is another element where packet needs to wait in queue to be served



Total Delay

- Total delay = processing + queuing + transmission + propagation



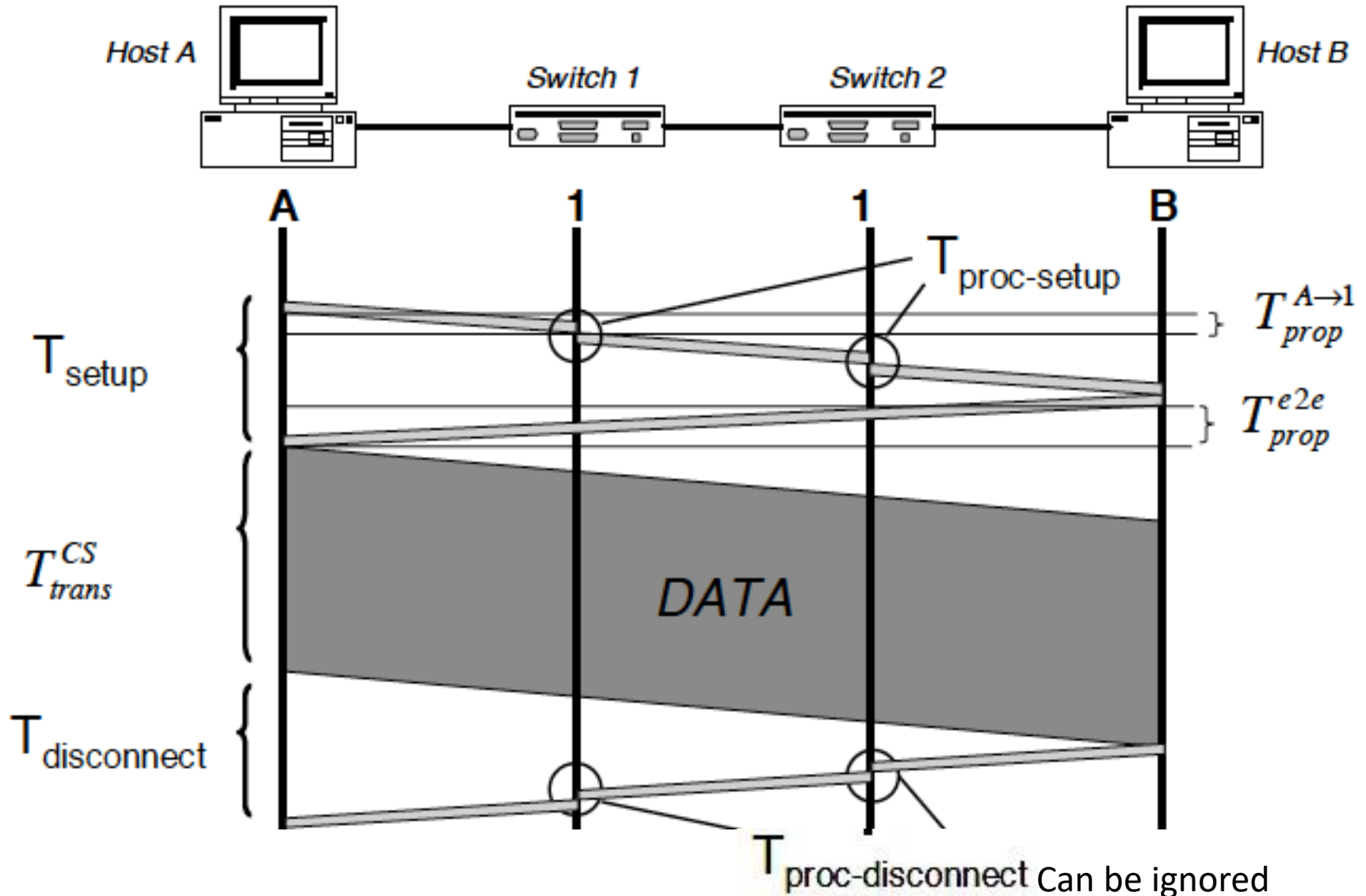
Queuing Delay

- More on queuing delay later

Delay in Circuit Switching

Delay in Circuit Switching

Total delay = time to set-up circuit + transmit message + time to release resources
= total Propagation + total transmission + total processing (to establish circuit)



Example: Delay in Circuit Switching

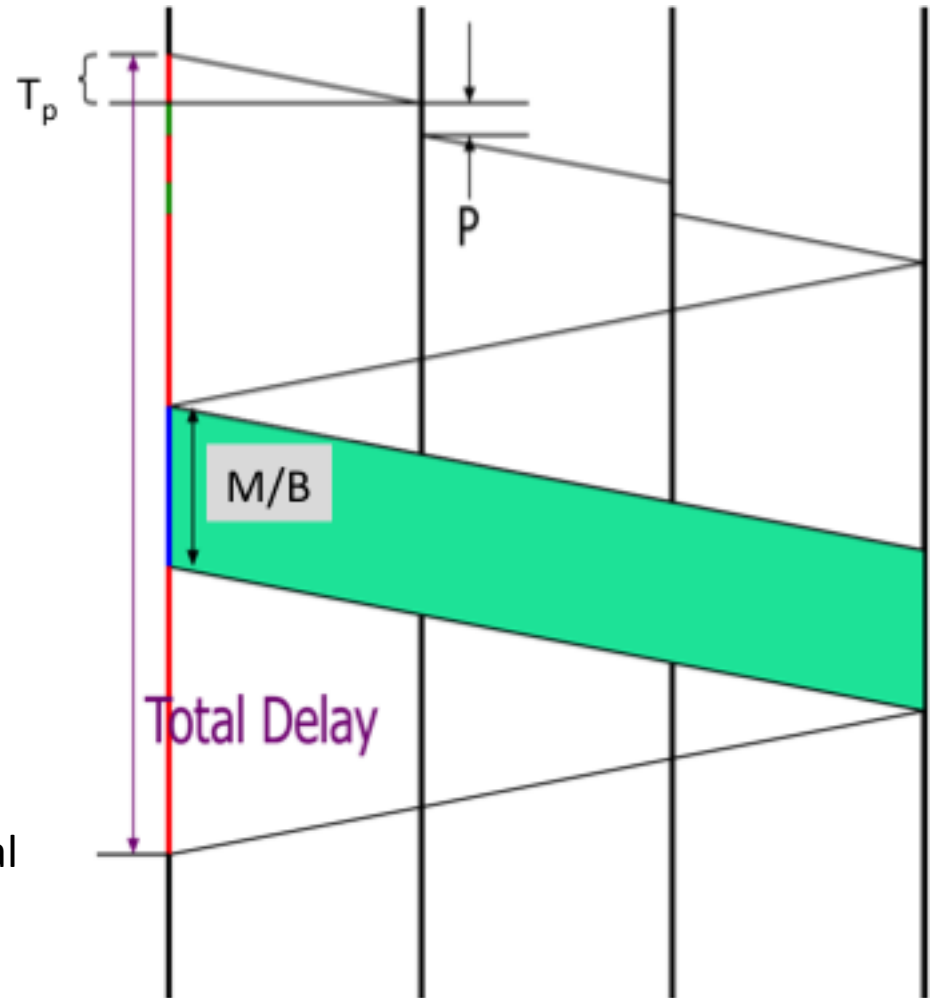
- P: Per hop processing delay
- N_h : number of hops
- T_p : propagation delay per link
- B: Bit rate
- M: message size

total transmission delay = message size/bit rate = M/B

Processing delay = $(N_h - 1) P$

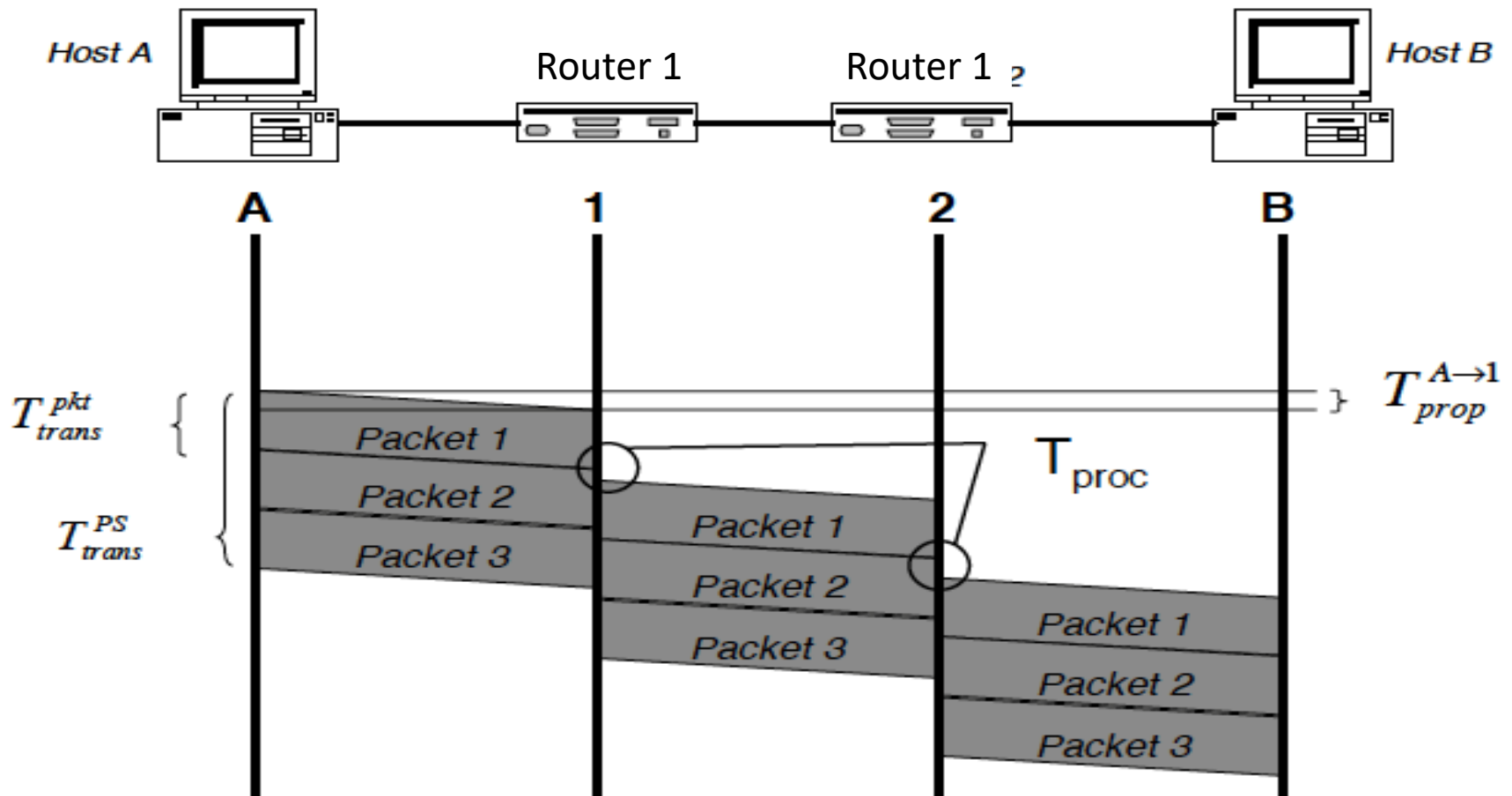
Propagation delay one way = $N_h T_p$

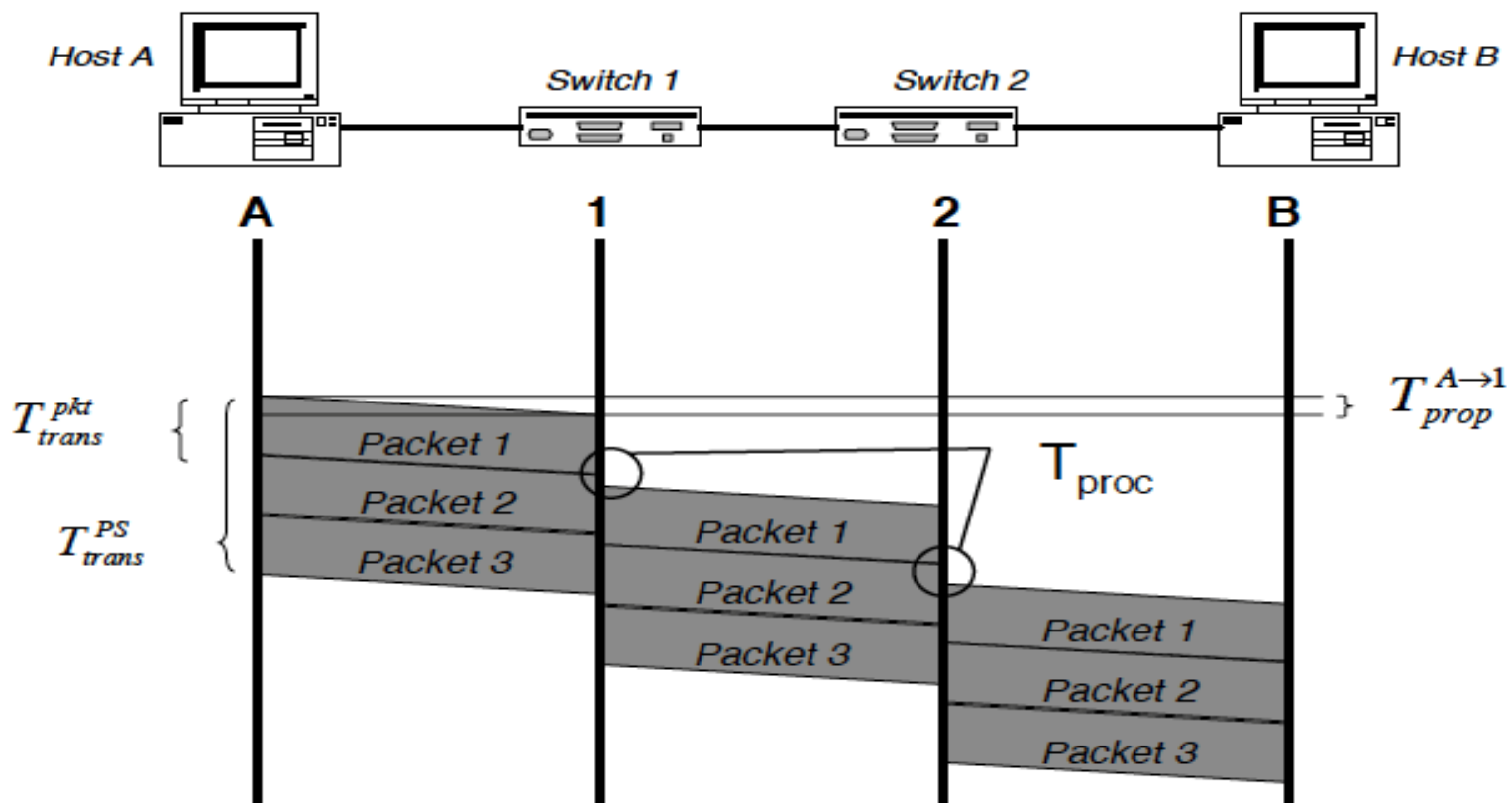
Total delay = time to set up connection + total transmission time + time to release the connection



Delay in Packet Switching

Total delay= total propagation+ total transmission delay of all packets + total queuing + total processing





Example: Delay in Packet Switching

- P : Per hop processing delay
- Q_d : Queuing wait time
- N_h : number of hops
- N_m : number of packets
- T_p : Link propagation delay
- T_t : transmission delay per packet

Total delay= total propagation along all links + total transmission of the N_m packets + delay of store and forward + total processing in intermediate nodes + total queuing wait time

$$= N_h T_p + N_m T_t + (N_h - 1) (T_t + P) + Q_d$$

Note: Total store and forward for the first packet at intermediate routers = $(N_h - 1) T_t$

Tophat



Q_Propagation delay in multihops

If a transmission goes over N hops. Each link along the transmission has propagation delay T_p . Then total propagation delay is

A	$N \times T_p$
B	$(N-1) \times T_p$



Q_ Queuing delay

If a transmission goes over a path of a total of N hops, and each intermediate device adds Q seconds in queuing. Then total queuing delay in the transmission is

A	$N \times Q$
B	$(N-1) \times Q$

Packet Switching - Problem

Alice and Bob are **4 hops** apart on a datagram packet-switched network where each link is **1 mile long**. The speed of light in the wire is approximately **125,000 miles/s**. **Processing delay at intermediate devices is 5ms**. **Packets are 1500 bytes** long. The **bit rate** over each link is **56kbit/s** (original speed of Internet backbone links in the 80s). If Bob sends a **10-packet message to Alice**, how long will it take Alice to receive the entire message. Routers store and forward. Ignore the queuing delay.

Packet Switching - Solution

Alice and Bob are 4 hops apart on a datagram packet-switched network where each link is 1 mile long. Per-hop processing delay is $5\mu\text{s}$. Packets are 1500 bytes long. All links have a transmission speed of 56kbit/s (original speed of Internet backbone links in the 80s). The speed of light in the wire is approximately 125,000 miles/s. If Bob sends a 10-packet message to Alice, how long will it take Alice to receive the entire message?

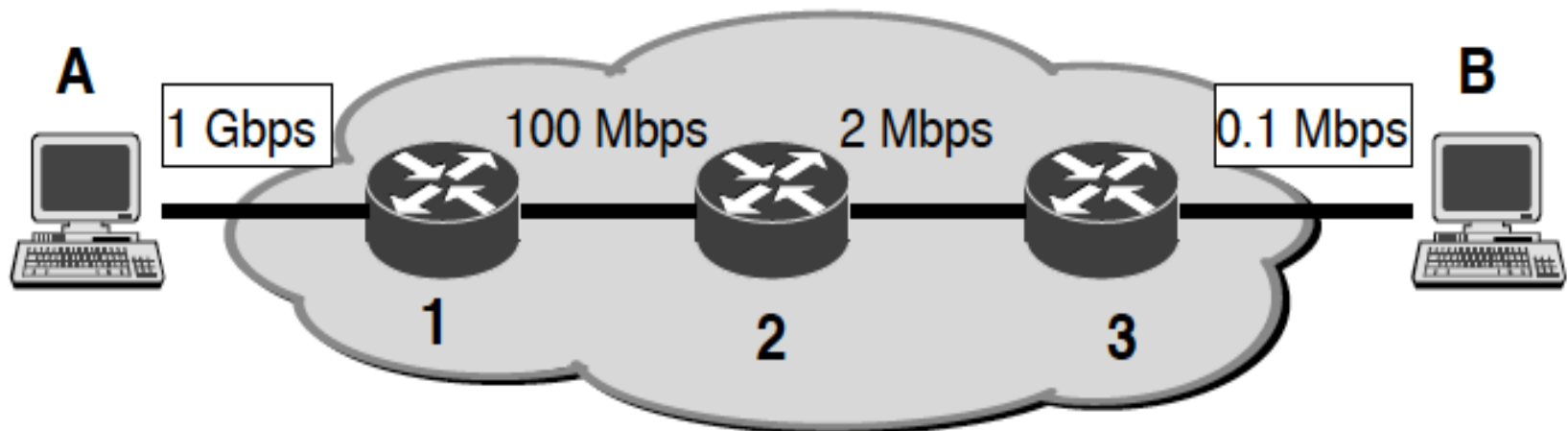
■ Answer:

- Number of hops $N_h=4$,
- Number of packets $N_m=10$,
- Per-hop processing delay $P=5\mu\text{s}=0.00005\text{s}$,
- Link propagation delay $T_p = \text{distance/speed of light} = 1/125,000$
- Packet size = 1500 bytes = $1500*8=12,000$ bits,
- Packet transmission delay $T_t = \text{packet size/transmission speed} = 12,000/56000 = \mathbf{0.214\text{s}}$.

$$\text{Delay} = N_h T_p + N_m T_t + (N_h - 1) (T_t + P) = 0.000032 + 2.14 + 0.642 + 0.000015 = 2.78\text{s}.$$

Bottleneck Link

- In multihop network, the overall rate is determined by the link with the lowest data rate
- Exceeding that rate results in overflow and data loss



Throughput

- Throughput is the effective rate
- In real situations, actual data rate as seen in the system is influenced by many factors besides the transmitter's data rate.
 - Channel access mechanisms, loading, queuing delays etc may affect the actual (average) data rate seen by the user.

Throughput example

- If it takes **10 sec** on an average to send a **1MByte** file from point A to B, what is the effective throughput of the network.

Throughput = amount of useful data (payload)/total time required to transmit this data

$$= (8 \times 10^6) / 10 = 0.8 \text{ Mbps}$$

Note that 10 sec includes all delay sources (transmission, queuing..)

Question: throughput



Q_Throughput

Tophat Q_ throughput

Suppose you want to send a 1000Bytes file as chunks of data (as packets) but in doing so , you add a total of 300 Bytes overhead bit to the file you want to send! The bit rate is 10Kbps. If the delay after adding overhead is 1.04seconds. What is the throughput?

A $(1300 \times 8) / 1.04$

B $(1000 \times 8) / 1.04$

C None of the above

Throughput - Overheads

Question

Suppose you want to send a 1000Bytes file as chunks of data (as packets) but in doing so , you add a total of 300 Bytes overhead bit to the file you want to send! Your transmitter's data rate (also the link data rate) is 10Kbps.

- A) You now transmit 1000B+ 300B through the channel. How long does it take for your to transmit the entire file?
- B) How long will it take you if there were no overheads?
- C) What is the throughput . Compare with the original transmission rate?
- D) How efficient is your sending mechanism (due to the overheads)?

Final Answers

a) 1.04sec b) 0.8 sec c) 7.69kbps d) 76.9%

Exercise

File of size $M=10^6$ bytes. If packet switching is used then the file will be segmented into $N_m=500$ packets, each contains 48 Bytes of header in addition to the data. Bit rate of link is $B=1\text{Mbps}$

- What is the difference in the **transmission delay** between circuit switching and packet switching.
- What is throughput and efficiency of packet switching?
 - Assuming the total delay is approximated by the transmission delay only

Summary

- Delay components
- Delay in circuit switching and packet switching
- Throughput

Next

- Queuing delay analysis