Homework 4, ECE 1570/2595 Robot Control, Spring 2022 (Due Wednesday Feb. 23)

Problem 1. Please make modifications to the MATLAB codes shown below and reproduce the simulation results on Slides 41 ($k_P = 0.5$) and Slides 42 ($k_P = 2$) of Lecture 5. You only need to submit two plots for this problem.

```
clear all;
T = 12;
                 % Time of simulation
                 % Sampling time interval
dt = 0.01;
x(1) = 0;
                 % Initial x location
y(1) = 0;
                 % Initial y location
phi(1) = pi;
                 % Initial heading
v0 = 10;
                 % Speed of the mobile robot
k_P = 0.5;
                 % Gain of P control
                 % Desired x location
x_d = 40;
y_d = 40;
                 % Desired y location
plot(x_d, y_d, 'rd'); hold on;
                                   % Plot the target location as a red diamond
%%%% Start simulation:
for i = 1 : T/dt
         % Controller:
         phi_d = atan((y_d-y(i))/(x_d-x(i)));
         u(i) = k_P*(phi_d-phi(i)); % This might cause angle problem!
         % Dynamics of mobile robot:
         x(i+1) = x(i) + dt*v0*cos(phi(i));
         y(i+1) = y(i) + dt*vo*sin(phi(i));
         phi(i+1) = phi(i) + dt*u(i);
         plot(x(i),y(i),'b.'); hold on; % Plot the trajectory of the mobile robot
end
```

Problem 2. Consider an LTI system:
$$\dot{\mathbf{x}} = \begin{bmatrix} 3 & -2 \\ 4 & -3 \end{bmatrix} \mathbf{x} + \begin{bmatrix} 1 \\ 1 \end{bmatrix} u$$
; $y = \begin{bmatrix} 1 & 1 \end{bmatrix} \mathbf{x}$.

Given $\mathbf{x}(0) = [3, 3]'$ and $u(t) = 3 \cdot 1(t)$, please compute y(t).