



University of Pittsburgh

# ECE 1150: Computer Networks

## Data Link Layer – Error & Flow Control

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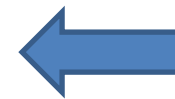
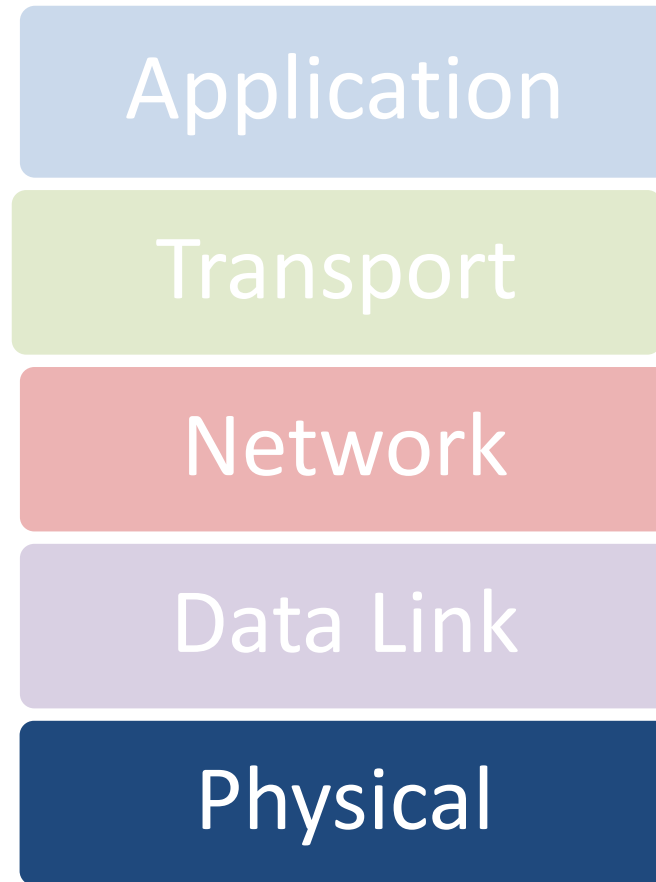
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# Previous Unit

- Data link layer functions
- Medium access control (MAC) protocols

# Context



We are here  
(Layer 2)

# Error Control

- Errors occur in transmissions
  - **Imperfections** of the physical **medium**
    - Noise from power spikes, outages etc.
  - **Collisions**
- Networks should be designed with:
  - Error prevention
  - Error detection
  - Error correction

# Impact of error on throughput

- Let  $P$  be the probability that a frame will be corrupted (e.g. due to collisions)
  - $1-P$  is the probability of successful transmission
- $\text{Throughput} = (1-P) \times \text{Useful data} / (\text{Delay when attempt is successful})$

# Objectives of the rest of this unit

- Explain the how errors control strategies at the link layer
  - Error detection
  - Error correction
  - Flow control

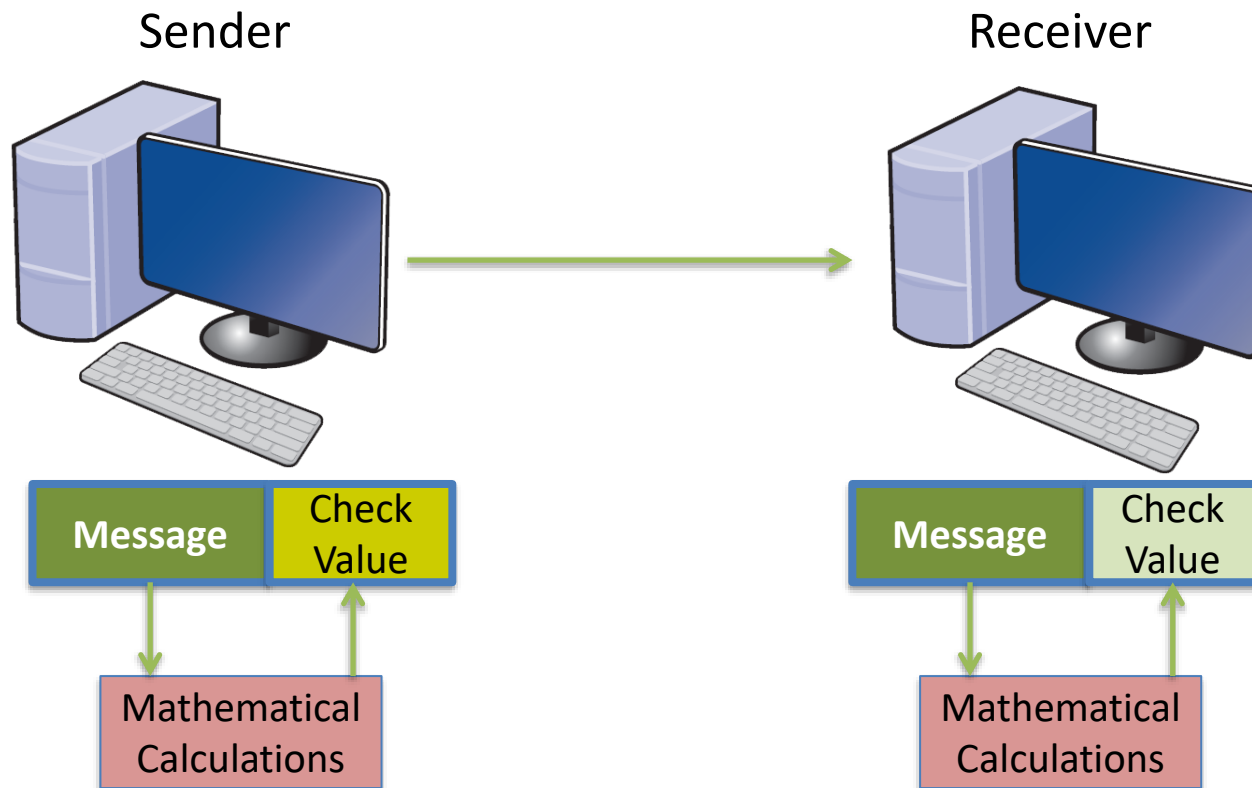
# Error correction in computer communication by adding metadata

- The general approach to error detection in data communications is to **add some meta-data to the original data**
  - The meta-data is generated from the data itself
  - The receiver use the meta-data to check if error exists



# Error Detection

- Both sender and receiver calculate check value
- Receiver tests whether the check values match



Ref.: Fitzgerald et al.



- Can metadata be of any size?

# Error Detection Schemes

- Parity check
- Checksum
- Cyclic redundancy check (CRC)

# Error Detection: Parity Check

- Parity check
  - 1-bit check value
  - Based on the number of 1's in the message
  - Two techniques:
    - Even parity: total number of 1's with remains even
    - Odd parity: total number of 1's remains odd
  - Simple, but only detects odd number of errors

## Example (Even Parity)

Character: 'A'  
Binary: 01000001

Character: 'C'  
Binary: 01000011

Parity Bit = 1

Add Parity Bit: 0  
(to make total even)

'C' has odd number of ones (3 ones), if we use even parity we add 1 to make the total even ( 4 instead of 3)

# Tophat



## Q\_Odd parity

If we are using odd parity, then for the sequence 01000011 we append

**A**

bit '0'

**B**

bit '1'

# Error Detection: Vertical and Longitudinal Parity Checks

- **Two-dimensional parity:**  
data is divided into rows and columns
- Parity is computed for each row and column
- **Can identify where is the error**

	Bit 1	Bit 2		Bit $n$	Parity
Character 1	$b_{11}$	$b_{21}$		$b_{n1}$	$R_1$
Character 2	$b_{12}$	$b_{22}$		$b_{n2}$	$R_2$
Character $m$	$b_{1m}$	$b_{2m}$		$b_{nm}$	$R_m$
Parity	$C_1$	$C_2$		$C_n$	$C_{n+1}$

← LRC

VRC

# Error Detection: Vertical and Longitudinal Parity Checks - Example

- Identify errors and correct them
  - Example: Even parity is used for each row and each column

No errors

1	0	1	0	1	1
1	1	1	1	0	0
0	1	1	1	0	1
0	0	1	0	1	0

Correctable single-bit error

1	0	1	0	1	1
1	0	1	1	0	0
0	1	1	1	0	1
0	0	1	0	1	0

Parity error

Parity error

# Error Detection: Checksum

- 1-byte (typically) is used as check value
- Checksum algorithms vary in the creation of check values
- Common approach: adds the decimal representation of each character (8 bits), then divide by 256
  - Append the remainder to data

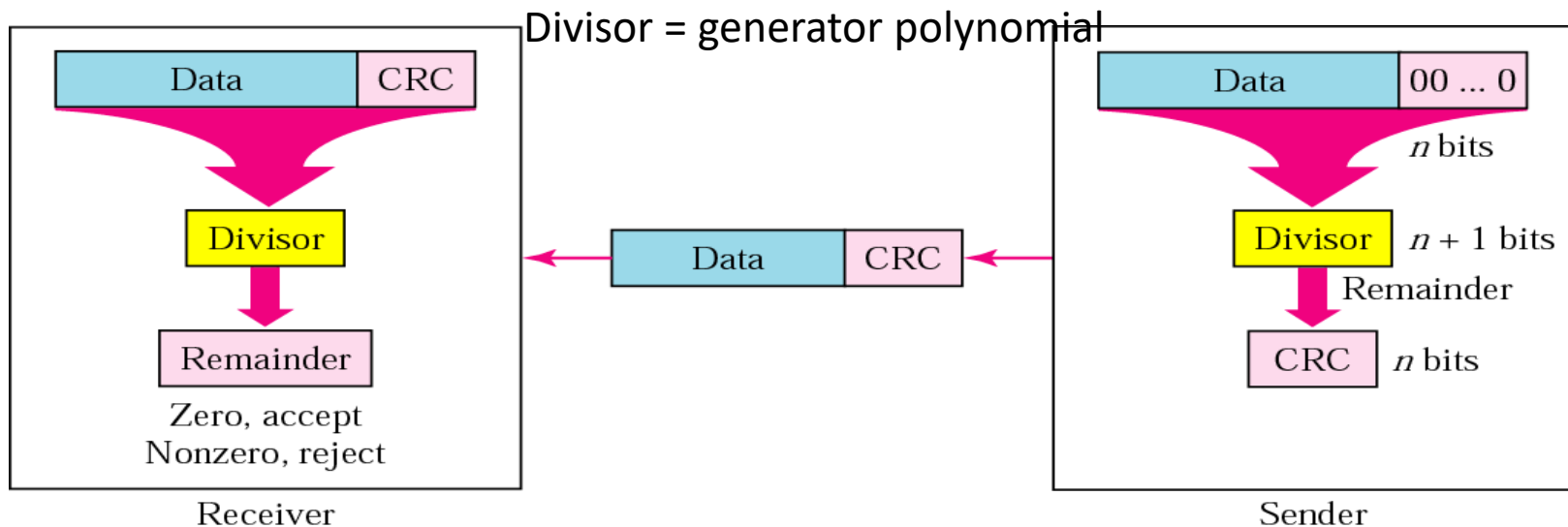
# Polynomials

- Each bit sequence can be represented as a polynomial
  - $[b_{n-1} \dots b_2 b_1 b_0] \Rightarrow m(x) = b_{n-1} x^{n-1} + \dots + b_1 x^1 + b_0 x^0$
  - Note that  $x^0 = 1$
  - Example: represent 11000101 in a polynomial
    - $11000101 \Rightarrow x^7 + x^6 + x^2 + 1$
    - 8 bits  $\Rightarrow$  Degree of polynomial (largest power of  $x$ ) is = 7
- When the generator polynomial  $g = [1 \ 1 \ 0 \ 1] \Rightarrow$ 
  - $g(x) = x^3 + x^2 + 1$ ,
  - Generator polynomial is  $g(x)$  of degree  $n = 3$



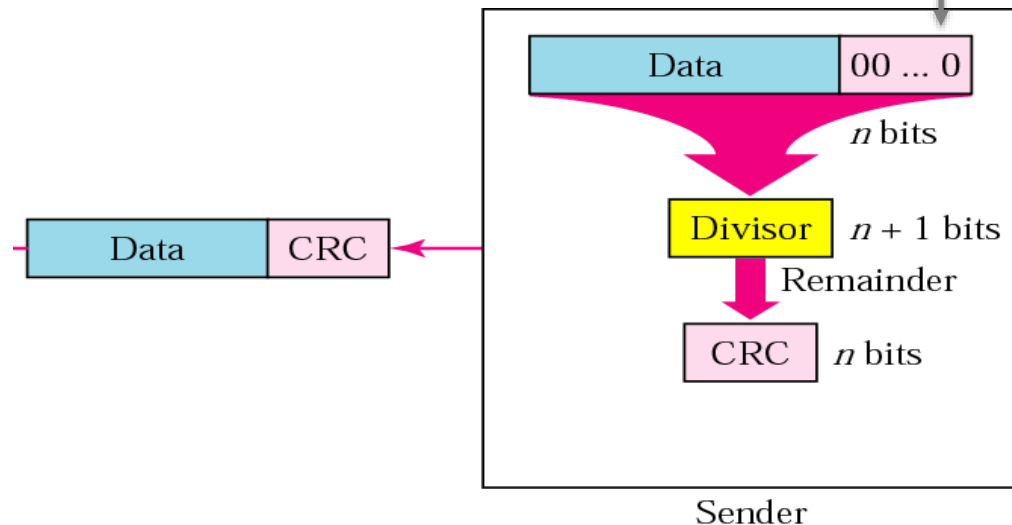
# Error Detection: CRC

- Treats message as a single binary number
- Sender and receiver must **agree** on a **pattern** of  $n+1$  bits, known as **generator polynomial or divisor**
  - $n$  is degree of the polynomial
- **CRC** is the **remainder** with data is divided by divisor
- International standards define: **8, 12, 16** and **32 bits** CRC
  - degree of polynomial = number of bits appended



# CRC Sender Procedure

- **Step 1:** User data is dividend, technology specifies a **divisor**
- **Step 2:** At sender, **add  $n$  zeros** to the **end** of the data (divisor has  $n+1$  bits)
- **Step 3:** At sender, **perform modulo-2 division** of appended data with divisor
- **Step 4:** At sender, **append remainder** to data as CRC and send to receiver



# CRC Receiver Procedure

- Step 5: At receiver, perform modulo-2 division of entire frame (data & CRC) with same divisor
  - Divisor is known because it is specified by technology
- Step 6: At receiver, if remainder = 0, accept data (no errors).
  - Else remainder  $\neq 0$ , error detected => reject data

# Error Detection: CRC

- Divisions in the CRC operations are modulo-2:
  - Like regular long division, however addition and subtraction are equivalent to bitwise XOR (Exclusive OR)
    - $0 - 0 = 0$
    - $0 - 1 = 1$
    - $1 - 0 = 1$
    - $1 - 1 = 0$

# Example

- Example: Message: [ 101010],  
divisor =  $g = [1101]$ ,  
get CRC bits.

# CRC – Sender Operation

Message: [ 101010], divisor = [1101] →  $n+1=4$ ,  $n=3$

$n=3$ , 0's appended

User data (Message)

							1	1	0	1	1	1
1	1	0	1	1	0	1	0	1	0	0	0	0
				1	1	0	1	⋮	⋮	⋮	⋮	⋮
					1	1	1	1	⋮	⋮	⋮	⋮
					1	1	0	1	⋮	⋮	⋮	⋮
							1	0	0	0	⋮	⋮
							1	1	0	1	⋮	⋮
								1	0	1	0	⋮
								1	1	0	1	⋮
									1	1	1	0
									1	1	0	1
										0	1	1

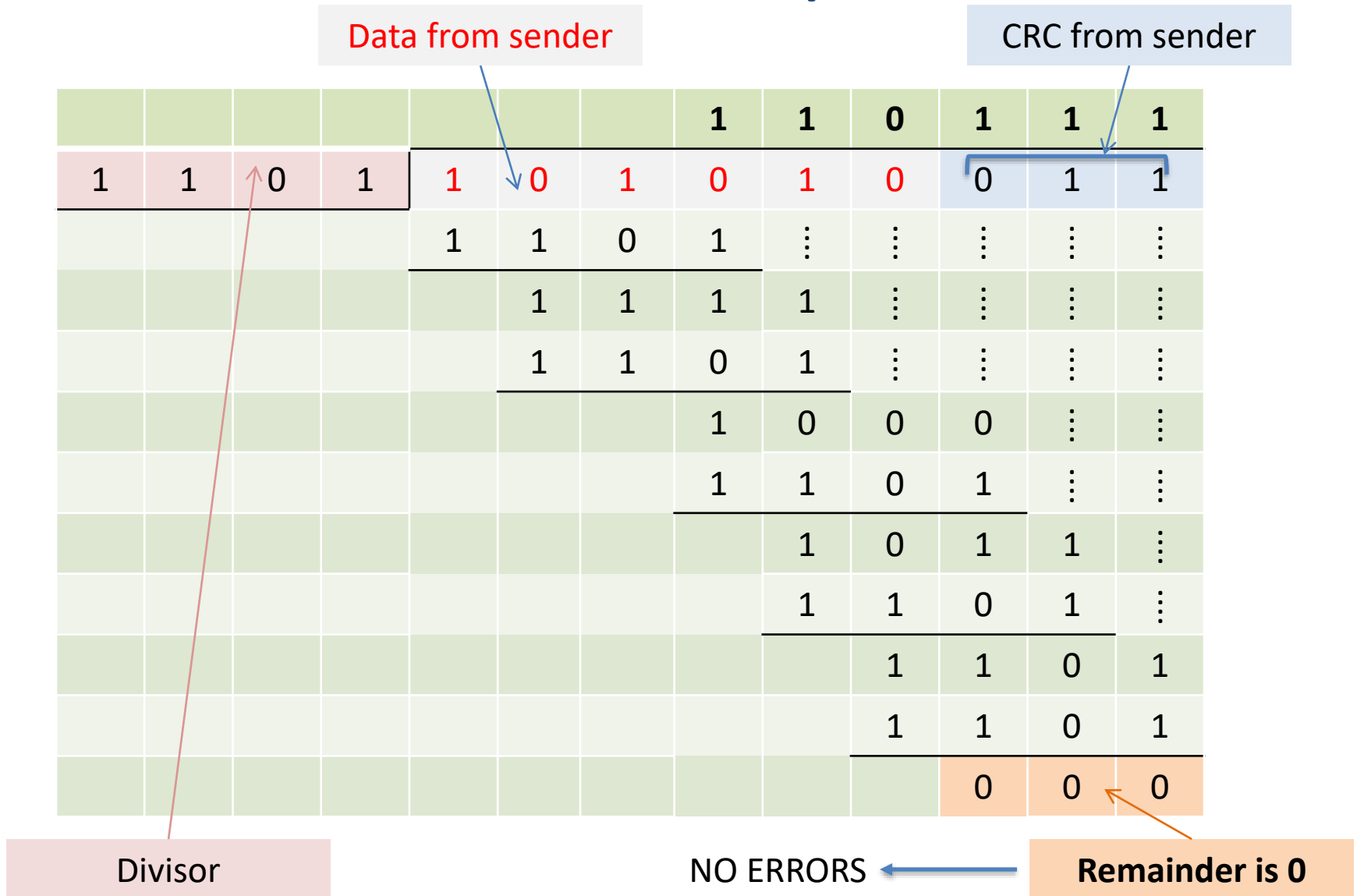
Divisor

$$g(x)=x^3+x^2+1$$

Send: 101010 011

CRC remainder

# CRC – Receiver Operation



# Another Method: Get CRC using Polynomials

- Generator polynomial:  $g = [1\ 1\ 0\ 1] \Rightarrow g(x) = x^3 + x^2 + 1$ 
  - Degree:  $n = 3$
- Append  $n$  zeros to the message then get polynomial representation
  - Message|000:  $[1\ 0\ 1\ 0\ 1\ 0\ 0\ 0\ 0] \Rightarrow m(x) = ?$ 
    - OR we can get the polynomial of message then multiply by  $x^n$
- Divide by  $g(x)$
- The remainder is the CRC =  $x+1 \Rightarrow [0\ 1\ 1]$ 
  - It should be  $n$  bits, so we add zero at the most significant bit
- Similarly, the received sequence with no errors is:  
 $[101010\ 011] \Rightarrow r(x) = ?$ 
  - When you divide by  $g(x)$  the remainder will be zero. Try it.



# Cyclic redundancy check (CRC)

- Most commercial data communication technologies use CRC
- CRC-32 is used in Ethernet
  - CRC-32: generator polynomial of degree 32. This also means that 32 CRC bits will be appended to data

- The generator polynomial is

$$g(x) = 1 + x + x^2 + x^4 + x^5 + x^7 + x^8 + x^{10} + x^{11} + x^{12} + x^{16} + x^{22} + x^{23} + x^{26} + x^{32}$$

See also: [http://www.xilinx.com/support/documentation/application\\_notes/xapp209.pdf](http://www.xilinx.com/support/documentation/application_notes/xapp209.pdf)

# CRC-32 capabilities

- CRC-32 can detect all errors affecting less than 33 [which is  $n + 1$ ] bits
- CRC-32 can reasonably detect errors affecting more than 33 bits

# Error Correction

- Once detected, errors must be corrected
- Error correction techniques
  - **Retransmission** (or backward error correction)
    - Retransmission is simple and most common
    - **Automatic Repeat reQuest (ARQ)**
      - Stop-and-wait ARQ
      - Continuous ARQ
  - Forward error correction
    - Receiving device can correct messages without retransmission.. Instead use channel coding techniques(think of repetition code)

# Error Correction: Stop-and-Wait ARQ

- Stop-and-wait ARQ

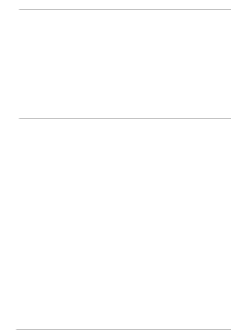
1. Receiver receives frame and sends:

- Acknowledgement (ACK)  
if no error
- Negative  
acknowledgement (NAK)  
if error

2. If NAK, sender re-sends data

Sender

Receiver



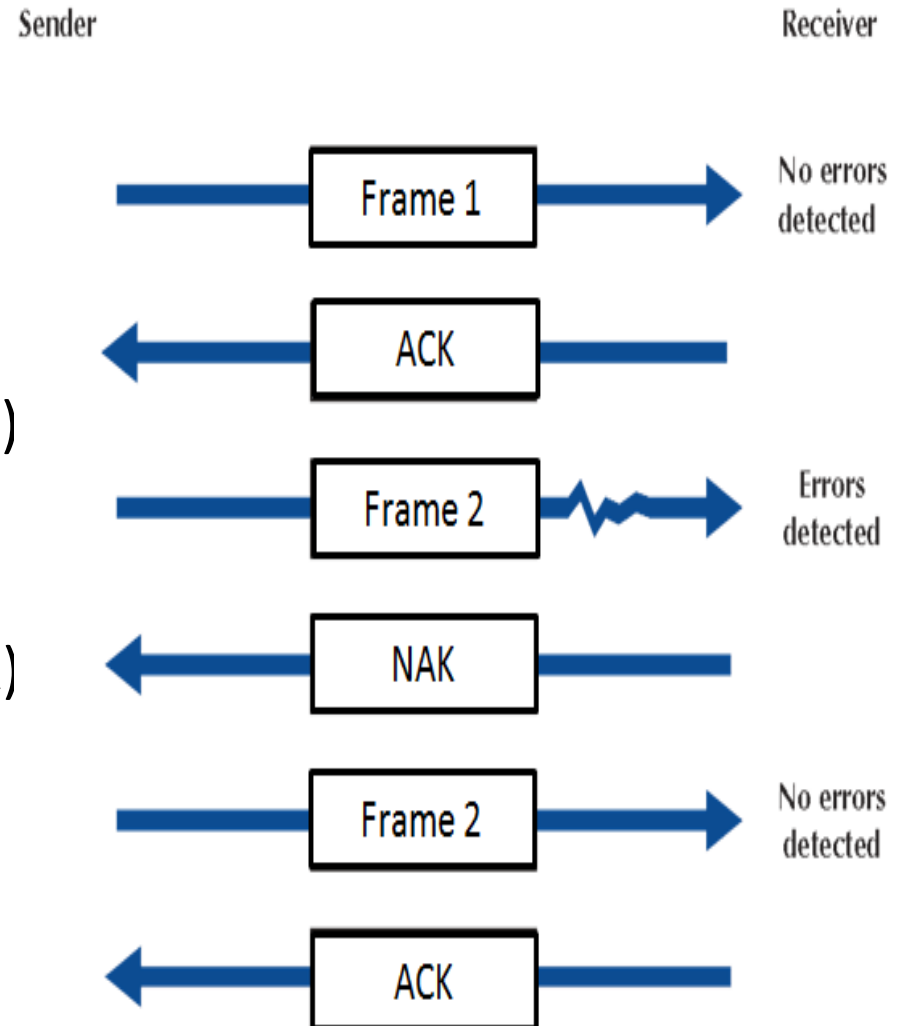
# Error Correction: Stop-and-Wait ARQ

- Stop-and-wait ARQ

1. Receiver receives frame and sends:

- Acknowledgement (ACK) if no error
- Negative acknowledgement (NAK) if error

2. If NAK, sender re-sends data



# Error Correction: Stop-and-Wait ARQ

- Stop-and-wait ARQ

3. If no ACK or NAK, Sender retransmits frame after "timeout"
4. If no ACK, sender re-sends data, receiver sends ACK and deletes duplicate frame

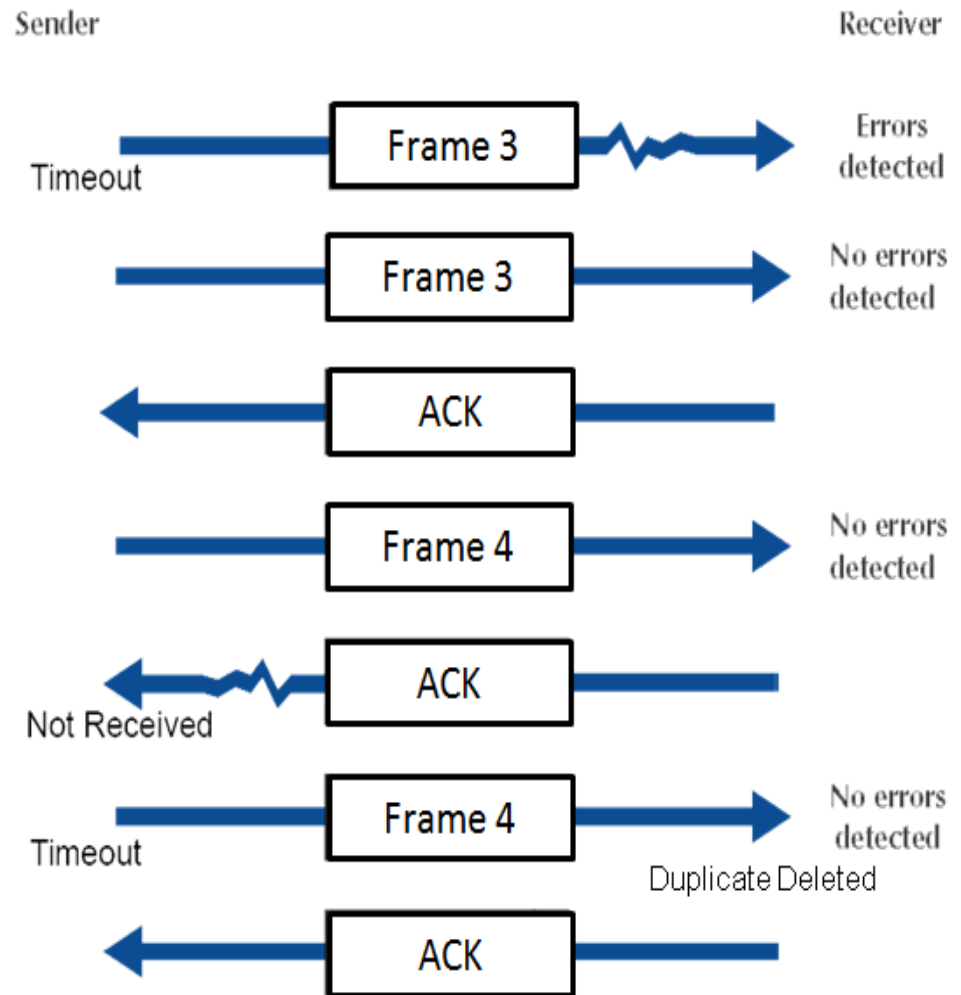
Sender

Receiver

# Error Correction: Stop-and-Wait ARQ

- Stop-and-wait ARQ

3. If no ACK or NAK, Sender retransmits frame after "timeout"
4. If no ACK, sender re-sends data, receiver sends ACK and deletes duplicate frame



# Error Correction

Here, window size is 2

Sender

Receiver

- Continuous ARQ
  - Sender does not wait for ACKs before sending more data
  - **“Sliding window”** is number of frames allowed to be unacknowledged by receiver
    - That is you can send more than one packet before receiving an ACK
  - Number of packets that can be sent depends on window size
    - Window size is **agreed upon by sender and receiver at the beginning**

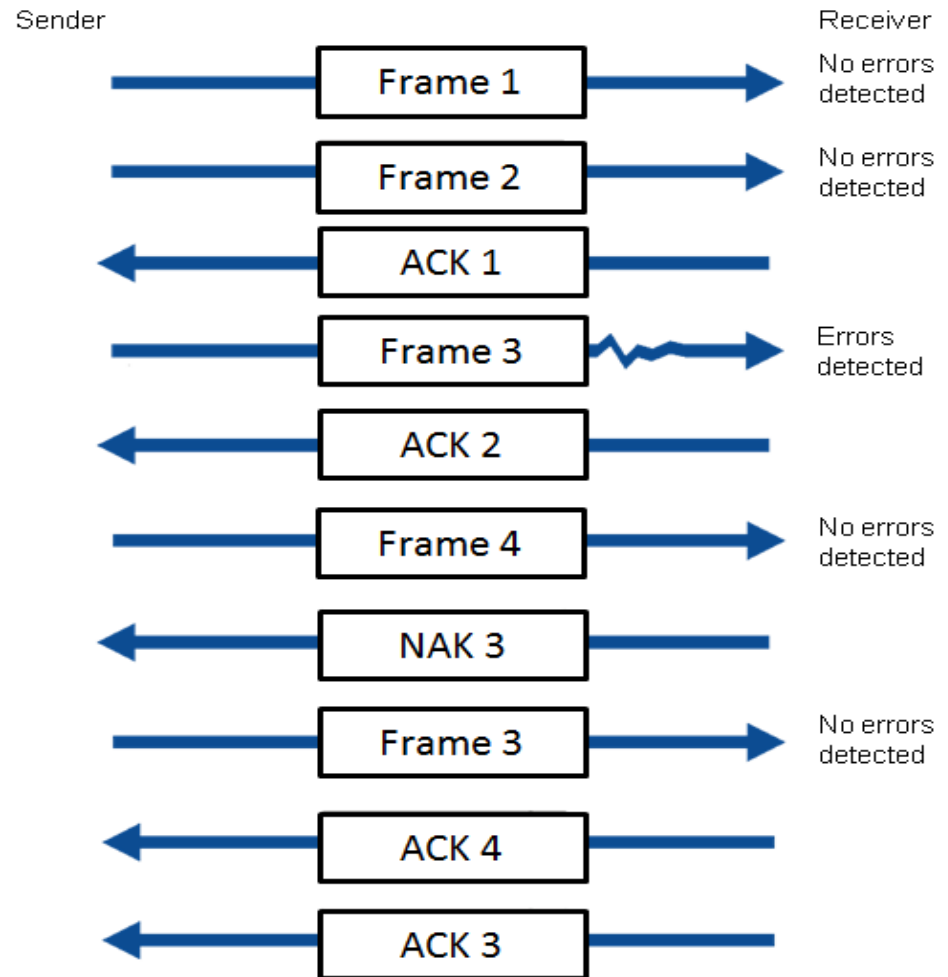
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# Error Correction: Continuous ARQ

- Continuous ARQ
  - Sender does not wait for ACKs before sending more data
  - “Sliding window” is number of frames allowed to be unacknowledged by receiver
  - Agreed upon by sender and receiver at the beginning



Here, window size is 2

# Tophat



## Q\_Throughput of ARQ

We expect that throughput using stop-and-wait ARQ

**A**

is higher than that can be obtained from continuous ARQ

**B**

is lower than that can be obtained from continuous ARQ

- ARQ is useful in flow control by limiting the number of packets received

# Sliding Window

- If an error occurs
  - Transmitter resends everything since the error (Go-Back-N)
  - Only the packet that has errors (Selective Retransmission)

# Sliding Window (Go-Back-N)



# Key Takeaways

- Important function at Data Link layer is error control
- Error detection
  - Append extra bits for error detection
  - Parity, checksum, CRC
  - CRC is commonly used and is more robust
- Error Correction through retransmission
  - Stop and wait ARQ
  - Continuous ARQ
    - Define sliding window, which is maximum number of frames that can be transmitted before an ACK is received
    - Implement flow control by defining limit on the window size