Bin Packing for Efficient Compression of Large Bacterial **Genomes Collection**

Tam Truong, Dominique Lavenier, Pierre Peterlongo, Karel Břinda





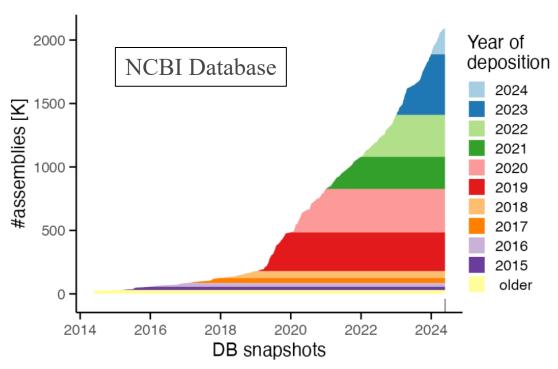




Introduction & State Of The Art

Motivation: Rapidly Growing Bacteria Genome Data

Fast Growth Of Bacterial Genomes Data¹



Karel Brinda, 2024 (CC) https://doi.org/10.6084/m9.figshare.25879258

Increasing Availability of Larger Bacterial Genome Collections

2021 Mar	661k Collection ²	n = 661,405
2024 Mar	AllTheBacteria ³ v0.1	n = 1,932,812
2024 Nov	AllTheBacteria ³ v0.2	n = 2,440,377
Next decade	Collections	10^{7}

Moreover, improvements in biological and technological diversity, MAG,...

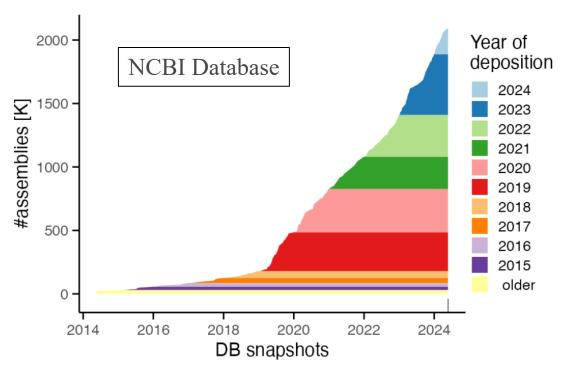
^[1] Břinda et al., Efficient and Robust Search of Microbial Genomes via Phylogenetic Compression. To appear in Nature Methods. 2025

^[2] Blackwell et al., Exploring bacterial diversity via a curated and searchable snapshot of archived DNA sequences. PLOS Biology 19, 11. 2021

^[3] Hunt et a.l,. AllTheBacteria - all bacterial genomes assembled, available and searchable. bioRxiv. 2024

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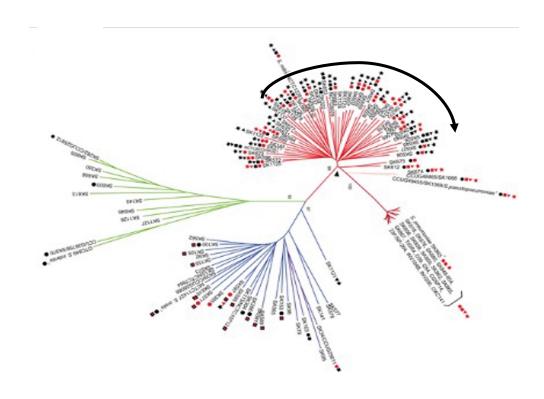
Challenging: efficient compression and search within those collections

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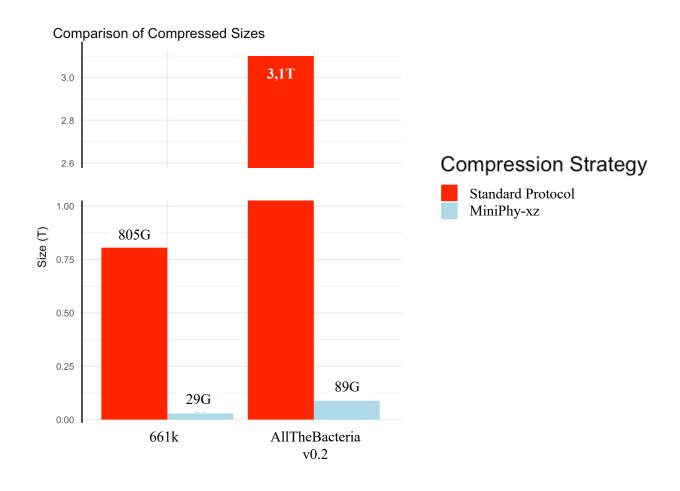
Recent Innovation: Phylogenetic Compression



Difficulty: Compression of genomes is challenging due to the widespread redundancy in the data.

Key Idea: Reordering genomes based on evolutionary history enhances local compressibility¹

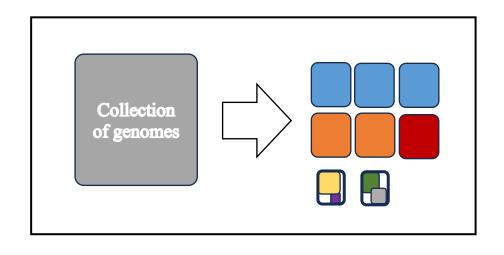
Resulting Improvement Using Phylogenetic Compression (MiniPhy¹)



Lossless compression of 1-3 orders of magnitude over standard protocol

[1] https://github.com/karel-brinda/miniphy

In Practice: Phylogenetic compression involves two steps:

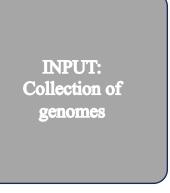


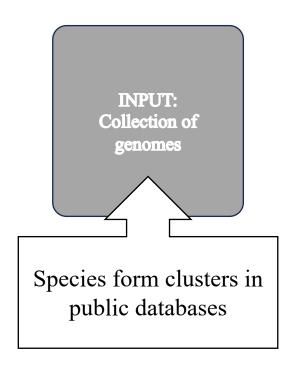
Step 1 : Phylogenetic Batching

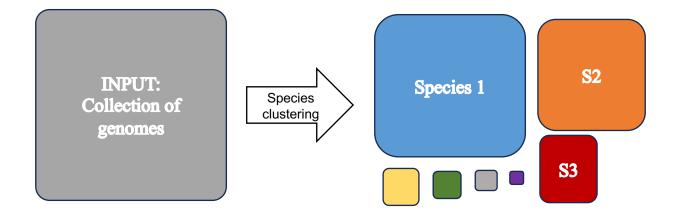


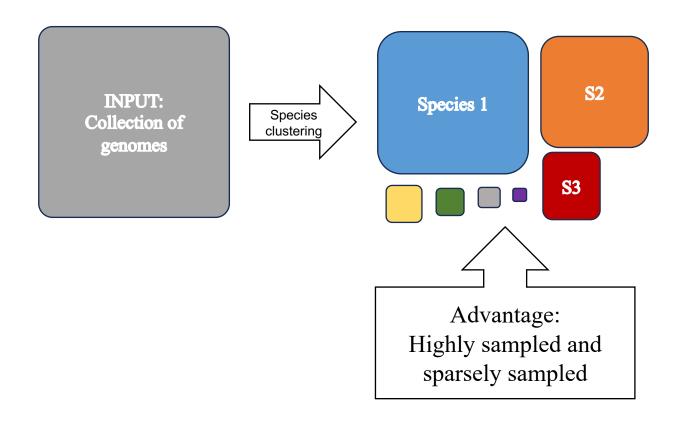
Starting point of my PhD

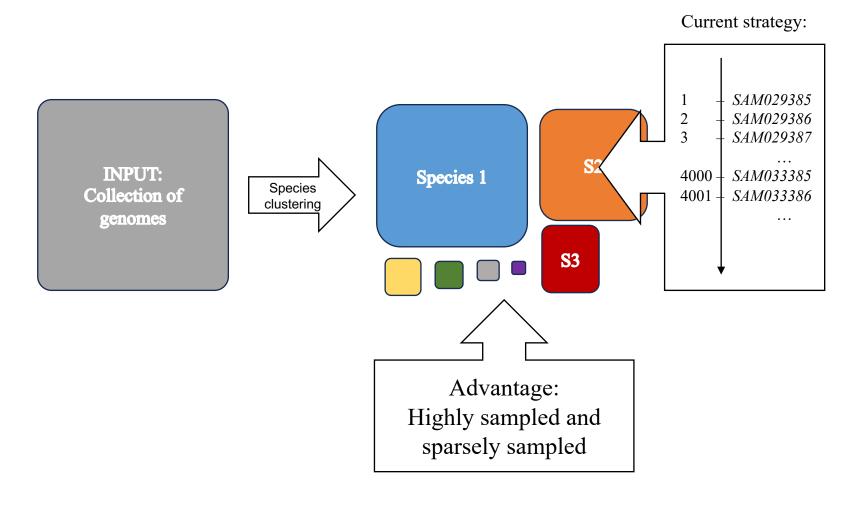
Step 2 : Phylogenetic Reordering



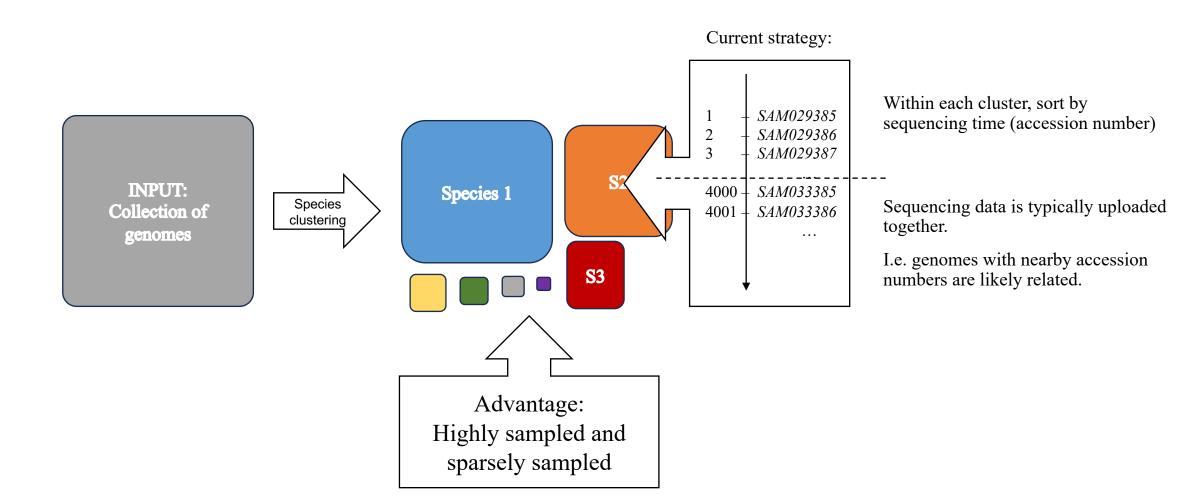








Within each cluster, sort by sequencing time (accession number)



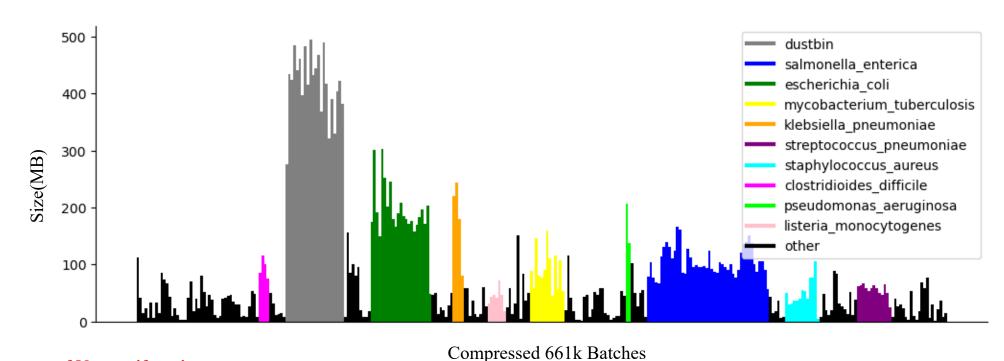


Split big clusters into smaller batches

Merge small clusters together into *dustbins*

Current Limitation: Non-uniform post-compression sizes

Batches are then reordered and compressed



Consequences of Non-uniformity

Unbalanced Workloads

Inefficient Transmission

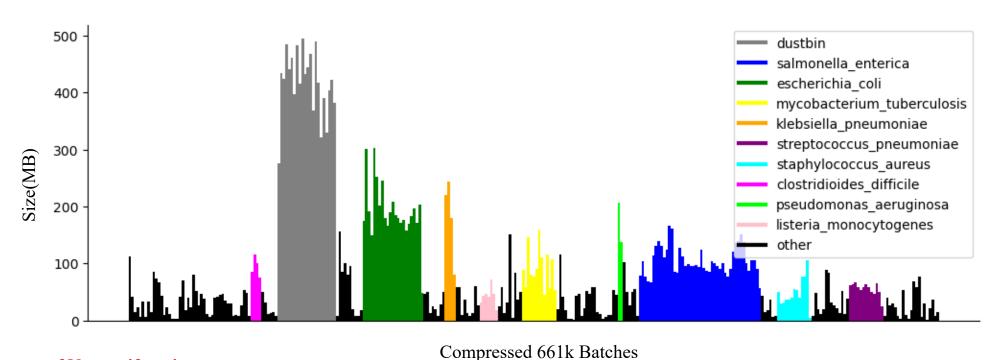
Hinder Parallelization

Memory Overuse

Inconsistent Query Time

Current Limitation: Non-uniform post-compression sizes

We than proceed to reorder and compress all batches individually



Consequences of Non-uniformity

Unbalanced Workloads

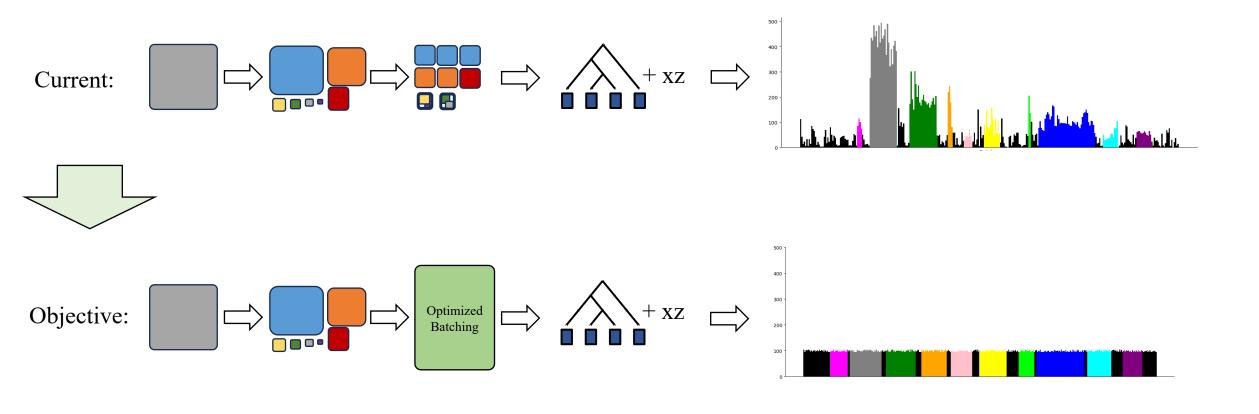
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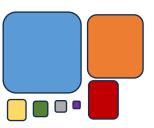
Inconsistent Query Time

Our Goal: Design A Balancing Batching Strategy

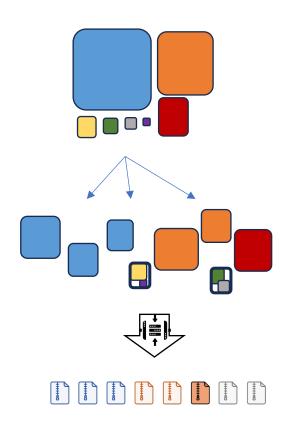


Toward The First Optimization Problem

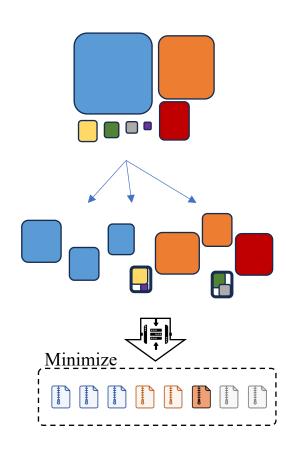
• Clusters of genomes: genomes from the same species, uneven in size



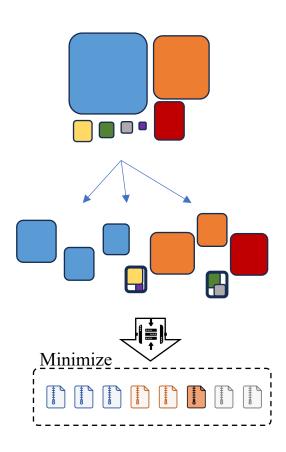
- Clusters of genomes: genomes from the same species, uneven in size
- We want to group them into batches while ensuring:
 - Requirements on batches: number of genomes, uncompressed size, ...
 - Post-compression batch sizes must fit within a memory constraint (balance)



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- **→** Optimization Problem: Bin Packing

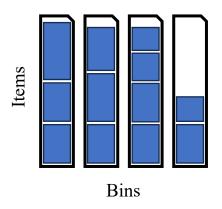


Bin Packing Problem: Definition

Bin Packing Problem:

Given a list of items i = 1, ..., n, each having a size $ci \in Z+$, and an integer value CAPACITY.

Find the minimum number of bin to pack all items in such a way that the sum of the item sizes in one bin is always smaller than CAPACITY.



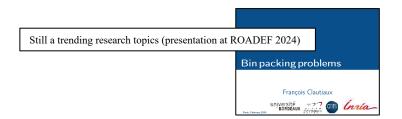
A classic combinatorial optimization problem.

The problem is NP-complete

Classical heuristics are ordered-based algorithms.

Initially, an empty bin is created. At each step, the next item is selected and packed in a bin. A new bin may be created at each step.

- First-fit: choose the first possible bin
- Best-fit: choose largest remaining CAPACITY bin
- Worst-fit: choose smallest remaining CAPACITY bin



- Let $G = \{g_1, g_2, ..., g_n\}$ be the set of genomes.
- $B = \{b_1, b_2, ..., b_m\}$ be the set of batches, where $b_j \subseteq G$. All genomes need to be assigned, one genome in one batch.

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• The compression size of each batch must be less than or equal to A MB:

$$|post_compression_size(b_j)| \le A, \forall j \in \{1, ..., m\}$$

Objective function:
$$\min \sum_{i=1}^{m} b_i$$

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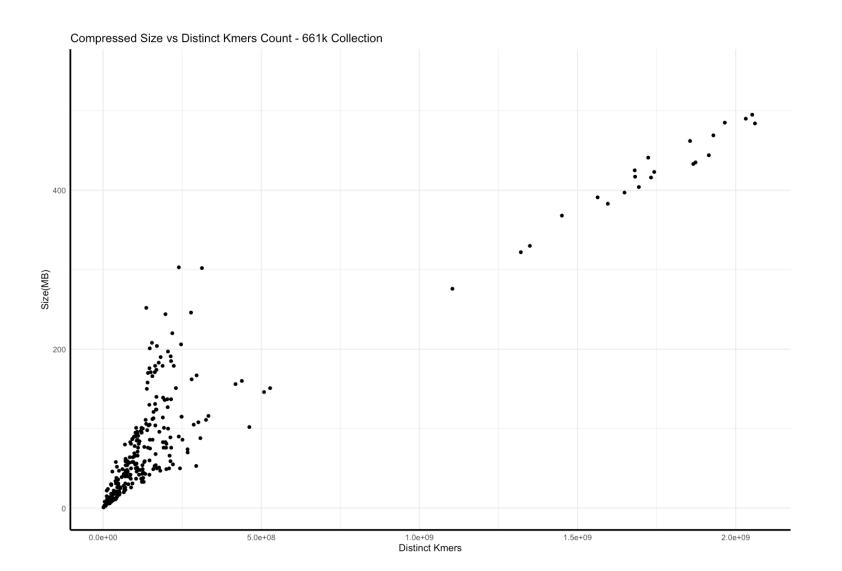
Getting the compression size is non-trivial

- → xz compression speed ≈ 1 genome per sec
- \rightarrow 1h20m for a batch with n = 5000

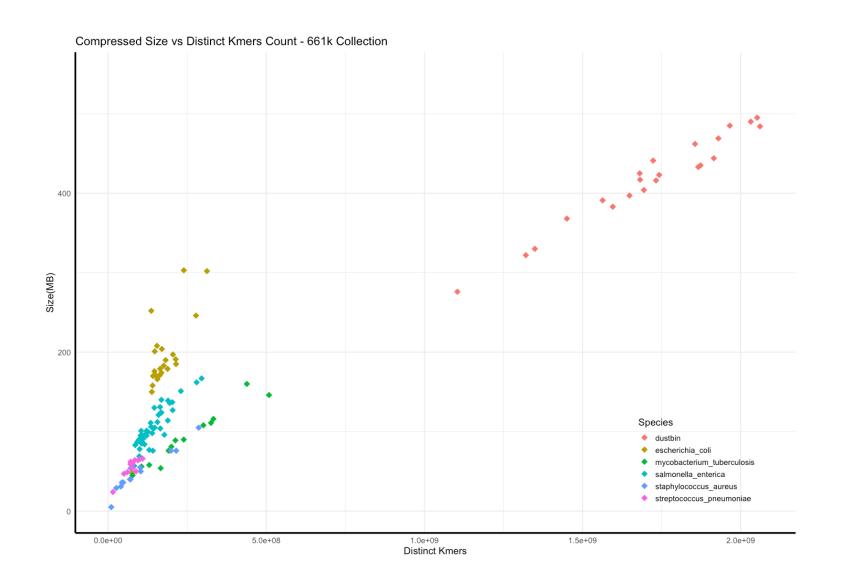
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Implementation Of The Balancing Batching Model

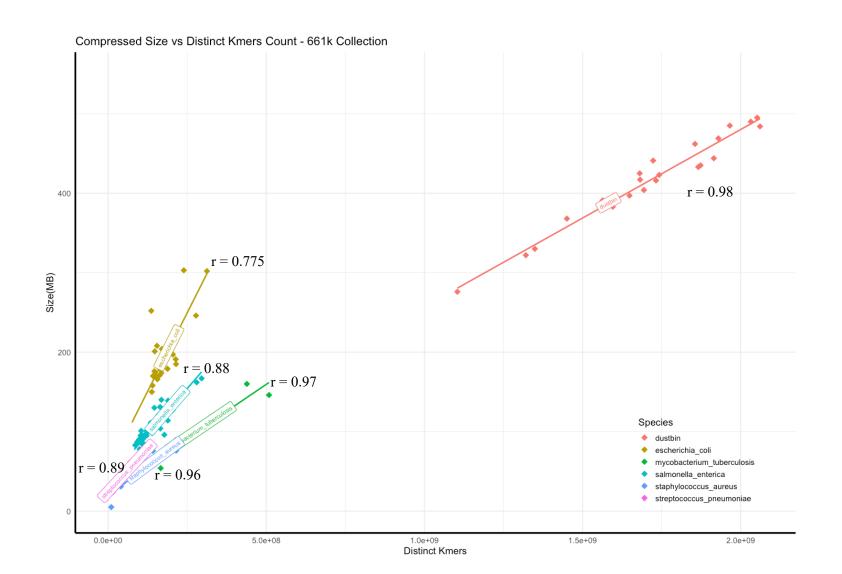
Ingredient 1: Post-compression Sizes Correlates With Distinct Kmers Count In Genomes Collections



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Ingredient 2: Fast Distinct Kmers Counting via HyperLogLog

2007 Conference on Analysis of Algorithms, AofA 07

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DMTCS proc. AH, 2007, 127-146

HyperLogLog: the analysis of a near-optimal cardinality estimation algorithm

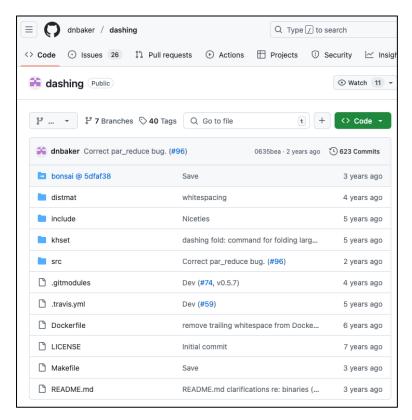
Philippe Flajolet¹ and Éric Fusy¹ and Olivier Gandouet² and Frédéric Meunier¹

¹Algorithms Project, INRIA-Rocquencourt, F78153 Le Chesnay (France)

²LIRMM, 161 rue Ada, 34392 Montpellier (France)

This extended abstract describes and analyses a near-optimal probabilistic algorithm, HYPERLOGLOG, dedicated to estimating the number of distinct elements (the cardinality) of very large data ensembles. Using an auxiliary memory of m units (typically, "short bytes"), HYPERLOGLOG performs a single pass over the data and produces an estimate of the cardinality such that the relative accuracy (the standard error) is typically about $1.04/\sqrt{m}$. This improves on the best previously known cardinality estimator, LOGLOG, whose accuracy can be matched by consuming only 64% of the original memory. For instance, the new algorithm makes it possible to estimate cardinalities well beyond 10^9 with a typical accuracy of 2% while using a memory of only 1.5 kilobytes. The algorithm parallelizes optimally and adapts to the sliding window model.

HyperLogLog Cardinality Estimation¹



Implemented in Dashing^{2,3}

[3] https://github.com/dnbaker/dashing

^[1] Philippe Flajolet, Éric Fusy, Olivier Gandouet, Frédéric Meunier. HyperLogLog: the analysis of a near-optimal cardinality estimation algorithm. AofA: Analysis of Algorithms, Jun 2007

^[2] Baker, D.N., Langmead, B. Dashing: fast and accurate genomic distances with HyperLogLog. Genome Biol 20, 265. 2019

Ingredient 3: Bin Packing Greedy Algorithms – 2 Variations

STRATEGY 1 : given unlimited batches with capacity C

Minimize nb of batch B

s.t.

$$distinct_kmers(bj) < C$$
, for $(j = 1, ..., m)$

Sort the genomes by acession number.

Initially, an empty bin is created.

At each step, the next genomes is selected and packed in the first available bin.

Distinct kmers count in each step is calculated using Dashing

Create new bin as needed.

STRATEGY 2 : given a fixed number of batch n

$$T \ge distinct_kmers(b_j), for j = 1, ..., m$$

Minimize T

Sort the genomes by acession number.

Create n bins.

At each step, the next genomes is selected and packed in the bin with the smallest CAPACITY.

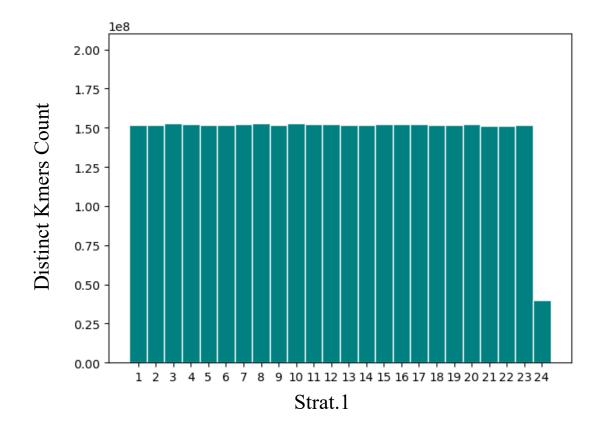
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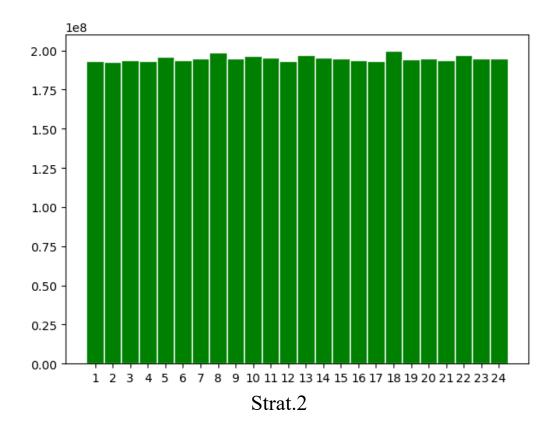
First Results

Dataset:

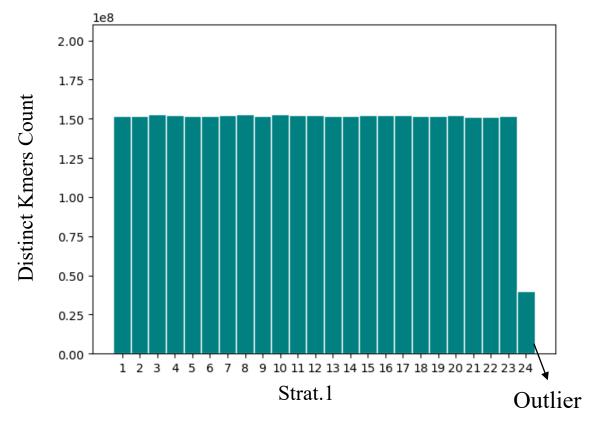
- Assemblies of *Mycobacterium tuberculosis* from 661k collection
- Number of Genomes: around 49,000
- Uncompressed Size: 218 GB
- CAPACITY of batches: 152,000,000

Batching Results Comparison: Distinct Kmers Count





Batching Results Comparison: Distinct Kmers Count

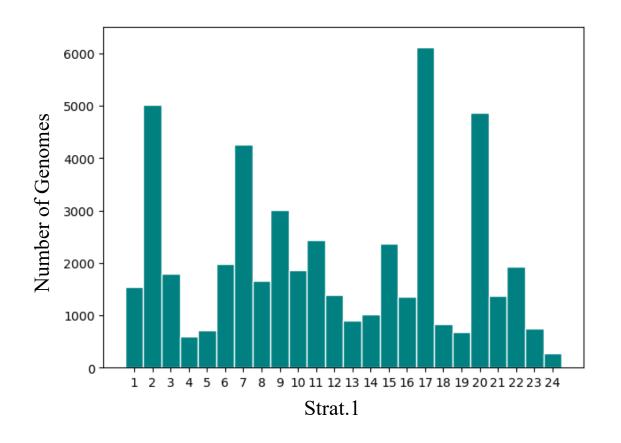


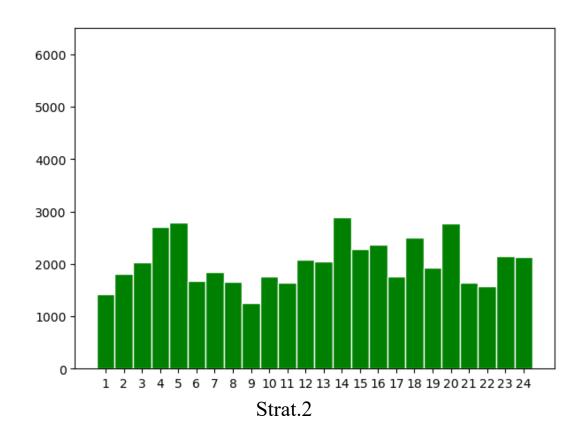
1e8 2.00 1.75 1.50 1.25 1.00 0.75 0.50 0.25 0.00 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 Strat.2

Strat.1 keep the order of accession number

→ Lower number of distinct kmers count per batch

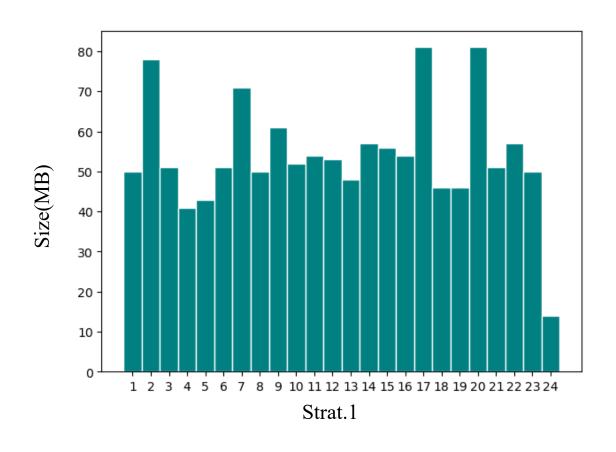
Batching Results Comparison: Number Of Genomes

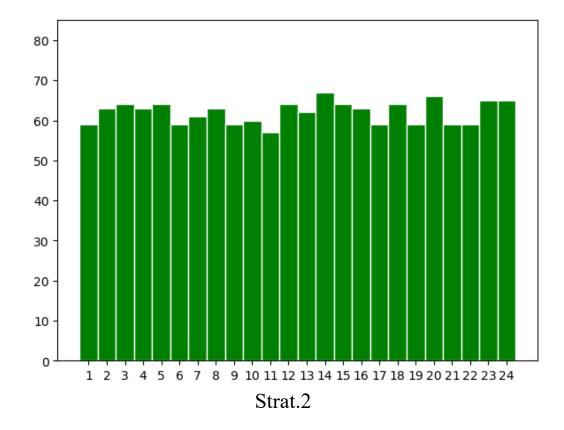




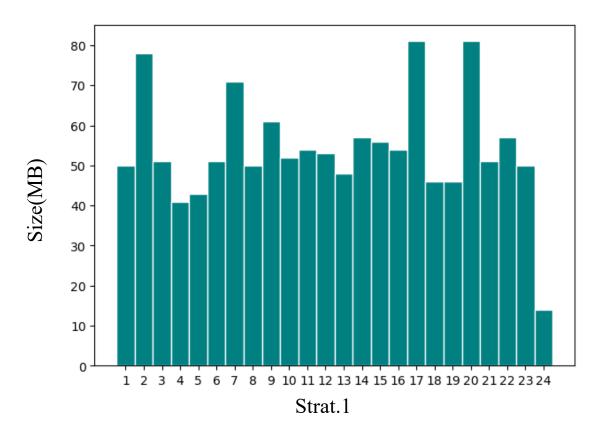
Number of genomes per batch varies, strat.2 to a lesser extent compared to strat.1

Batching Results Comparison: After Compression



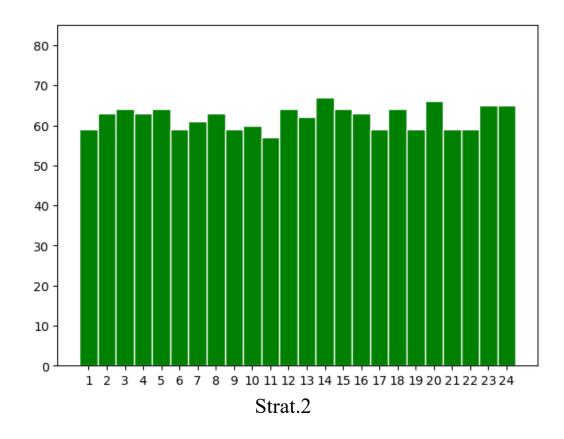


Batching Results Comparison: After Compression



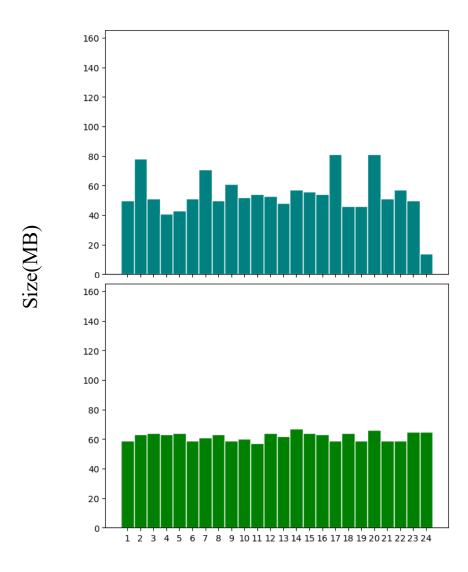
Post-compression size: 1,3G

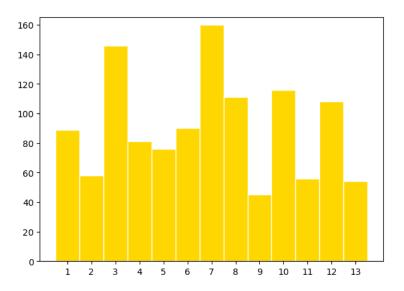
Most of the batches are balanced (between 4050MB, max size 81MB)



Post-compression size: 1,6G All Batches are well balanced (between 59-67MB, max size 67MB)

Batching Results Comparison: Compare With the Original Batching





Post-compression size: 1,2G Highly imbalance

Conclusion & Perspectives

Batching is a crucial step in Phylogenetic Compression.

Batching by estimating compression size via HyperLogLog and Distinct K-mer counts improves balancing of the final compressed sizes *Mycobacterium tuberculosis*.

First results:

- First model for Optimization Batching as a Bin Packing Problem.
- Workflows of the bin packing batching strategies:
 - https://github.com/tam-km-truong/HLL-Binning
 - https://github.com/tam-km-truong/HLL-Balancing

Perspectives:

- Currently scaling up the results and methods to the 661k and the AllTheBacteria Collections
- Introducing new constraints such as Max Number of genomes per batch
- Application in other data structure such as Bloom filter, on PIM and GPU

Thank You