

Relation b/w i/p & o/p  $\rightarrow$  Assum  $\rightarrow$  Linear relation

Linear  
Regress  
 $y_{\text{out}}(x)$   
 $\downarrow$   
Linear

$$x = \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}$$

$x_1$  = no. of gfs

$x_2$  = no. of hrs he studied

$x_3$  = parents

$y_1$  = marks - phy

$y_2$  = Chem

$y_3$  =

$$\begin{aligned} y_1' &= w_{11}x_1 + w_{12}x_2 + w_{13}x_3 + b_1 \\ y_2' &= w_{21}x_1 + w_{22}x_2 + w_{23}x_3 + b_2 \\ y_3' &= w_{31}x_1 + w_{32}x_2 + w_{33}x_3 + b_3 \end{aligned}$$

$$y' = Wx + b = \begin{bmatrix} w_{11} & w_{12} & w_{13} \\ w_{21} & w_{22} & w_{23} \\ w_{31} & w_{32} & w_{33} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} b_1 \\ b_2 \\ b_3 \end{bmatrix}$$

$(m \times n)$        $(n \times 1)$

$$y = \text{gff} \cdot (h \dots (n))$$

$$y = w_1 [w_2 [w_3 \dots x]]$$

$w_1, w_2, \dots$

matrix  $\rightarrow$  linear

$$y = \sigma_2 \left\{ w_2 \left[ \sigma_1(w_1 x) \right] \right\}$$

(activation function)

Bias

$$\begin{bmatrix} w_{11} & w_{12} & w_{13} & b_1 \\ \dots & \dots & \dots & \dots \\ \dots & \dots & \dots & \dots \\ \underbrace{w_{31} \quad w_{32} \quad w_{33} \quad b_3}_w \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ 1 \end{bmatrix}$$

Input

m training exs.  $\rightarrow (x_1, x_2, \dots, x_m)$

$(x_1, x_2, x_3, x_n)$

$$\begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_m \end{bmatrix} = \begin{bmatrix} x_{11} & x_{12} & \dots & x_{1n} \\ x_{21} & x_{22} & \dots & x_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ x_{m1} & x_{m2} & \dots & x_{mn} \end{bmatrix} \begin{bmatrix} w_1 \\ w_2 \\ \vdots \\ w_n \end{bmatrix}$$

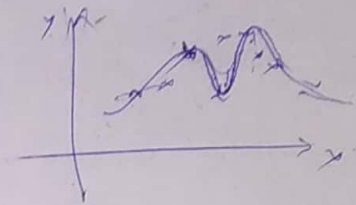
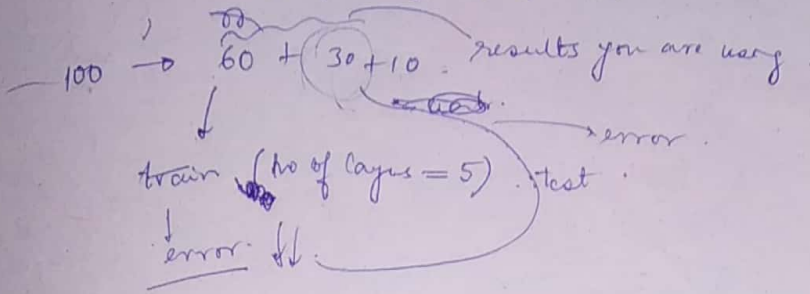
$$X \rightarrow 3 \times 1$$

$$Y \rightarrow 5 \times 1$$

$$W_1 \rightarrow 6 \times 3$$

$$W_2 \rightarrow 4 \times 6$$

$$Y = \begin{bmatrix} w_3 & w_2 & w_1 \end{bmatrix} \begin{bmatrix} 5 & 5 & 5 \end{bmatrix} \begin{bmatrix} 6 \times 5 & 5 \times 5 & 3 \times 5 \end{bmatrix} \begin{bmatrix} 1 \end{bmatrix} \begin{bmatrix} X \end{bmatrix}$$



## Loss

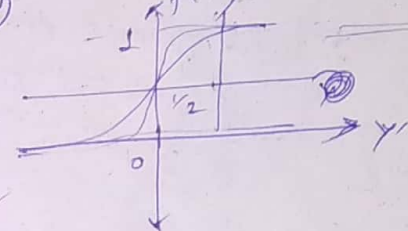
Correct -  $y$  o/p from net  $\rightarrow y'$

Error Regression  $\rightarrow$  mean sq. error  $\frac{1}{n} \sum (y - y')^2$

Class  $\rightarrow$  logistic function  $f(x) = \frac{1}{1 + e^{-x}}$

$$y = \frac{1}{1 + e^{-x}}$$

Normalization



## Optimisation

Loss minimise by changing the parameters ( $W$ s)

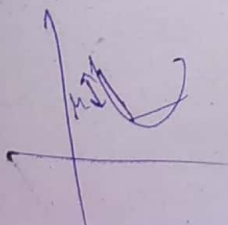
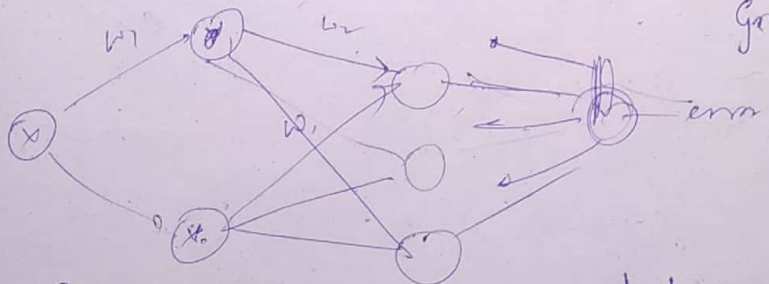
$$W_{i+1} = W_i + \mu \frac{\partial}{\partial W_i} (\text{Loss})$$

Supr.  $y = W_3 [ \sigma_2 (W_2 ( \sigma_1 (W_1 (x)) ) ) ]$

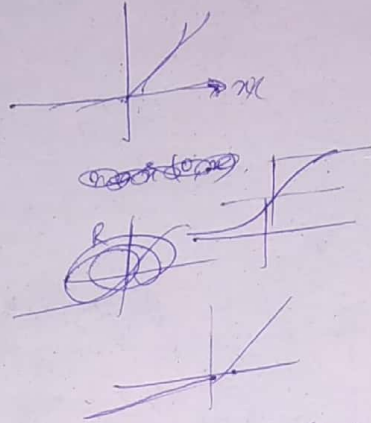
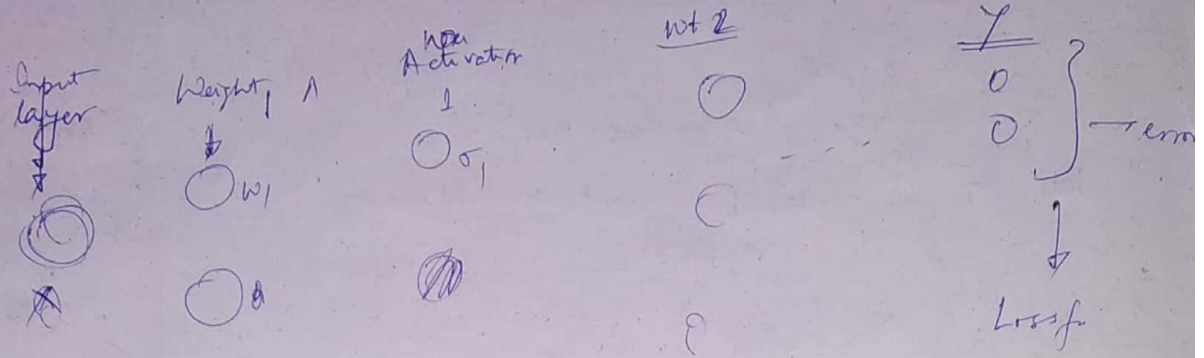
$$\frac{\partial}{\partial W_1} = \frac{\partial (\text{err})}{\partial W_3} \cdot \frac{\partial W_3}{\partial z_2} \cdot \frac{\partial z_2}{\partial W_2} \cdot \frac{\partial W_2}{\partial z_1} \cdot \frac{\partial z_1}{\partial W_1}$$

Backpropagation

Gradient descent

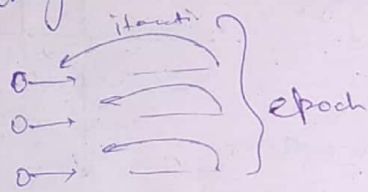


hyperparameters  $\leftarrow$  no. of layers, no. of neurons in a layer



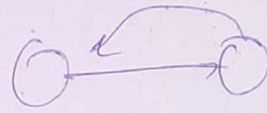
50%  
60%

1. Batch gradient descent

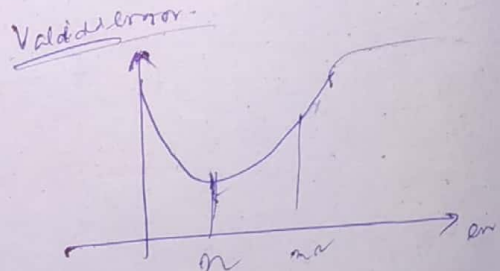
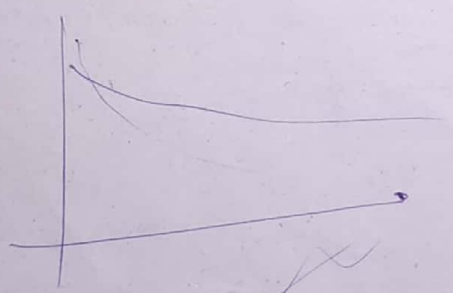
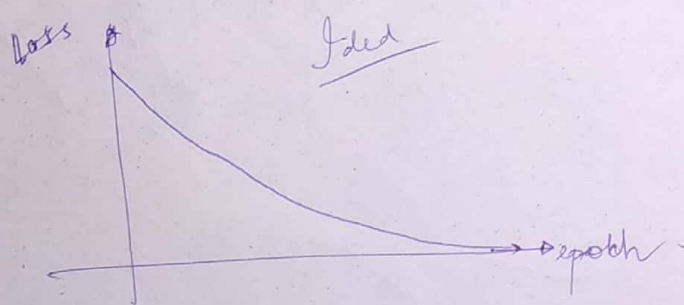
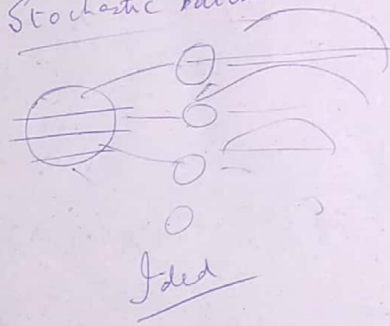


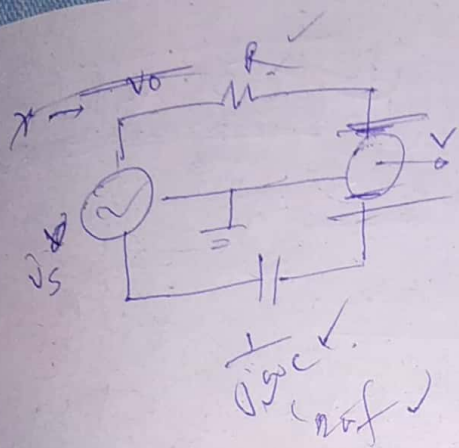
2. Stochastic descent

epoch = iteration



3. Stochastic batch





$$\begin{aligned}
 & \text{Measured } |V| \\
 & \text{Real } |V| \\
 & \text{Error } |V| \\
 & \text{Max } |V| \\
 & \text{Error } |V| \\
 & \text{Error } |V|
 \end{aligned}$$