Q. From the figure and the data given below, using Bayes Rule and calculate:

Pneumonia			Smoking		
True	0.1			Yes	0.2
False	0.9			No	0.8

Solution:

Let c, be the event for the cough. (Here, c represents to not cough)

Let p, be the event for pneumonia. (Here, p represents to not pneumonia)

Let s, be the event for smoking. (Here, \underline{s} represents to not smoking)

i.
$$P(c/(p \& s)) = 0.95$$

ii.
$$P(c/(p \& s)) = 0.05$$

iii.
$$P(c/(\underline{p \& s})) = 0.6$$

iv.
$$P(c/(p \& \underline{s})) = 0.8$$

$$P(c) = [P(c/p \cap s)] * P(p) * P(s) + [P(c/p \cap s)] * P(p) * P(s) + [P(c/p \cap \underline{s})] * P(p) * P(\underline{s}) + [P(c/p \cap \underline{s})] * P(\underline{p}) * P(\underline{s})$$

$$= 0.95 * 0.1 * 0.2 + 0.6 * 0.9 * 0.2 + 0.8 * 0.1 * 0.8 + 0.05 * 0.9 * 0.8$$

$$= 0.019 + 0.108 + 0.064 + 0.036$$

$$= 0.227$$

$$P(c/s) = [P(c/p \cap s)] * P(p) + [P(c/\underline{p} \cap s)] * P(\underline{p})$$

$$= 0.95 * 0.1 + 0.6 * 0.9$$

$$= 0.095 + 0.54$$

$$= 0.635$$

$$P(s/c) = [P(c/s) * P(s)] / P(c)$$
$$= [0.635*0.2] / 0.227$$
$$= 0.55$$

$$P(c/\underline{s}) = [P(c/p \cap \underline{s})] * P(p) * 1 + [P(c/p \cap s)] * P(\underline{p}) * 1$$
$$= 0.8 * 0.1 + 0.05 * 0.9$$
$$= 0.08 * 0.045$$

$$=0.125$$