

DAY  
125  
DSA

HashMap  
and  
Heap  
continued

Date \_\_\_\_\_  
Page No. \_\_\_\_\_

Date - 29 Jan  
Day → Saturday

Module → HashMap and Heap

Questions →

1. Merge K Sorted Lists
2. Sort K-Sorted Array.
3. Median priority Queue.

Ques. 1

## MERGE K-SORTED LISTS

Approach 1 → यहाँ सारी list के एवेल  
element pq में से ऑर्डे झोड़ पर के  
remove करें AL result AL +

But here Space  
complexity is very high.

list here is ArrayList. basically Ed  
of ArrayList ArrayList  
green Ed;

ईं K sorted list green Ed।

इसे इन K sorted lists को merge करके 1 sorted list  
करना है; TC → n log n SC → K.

K=4

List l1 = 10, 20, 30, 40.

List l2 = 5, 7, 9, 11, 19, 55, 57.

List l3 = 1, 2, 3.

List l4 = 32, 39

MergedList = 1, 2, 3, 5, 7, 9, 10, 11,  
19, 20, 30, 32, 39, 40, 50, 55,  
57

Approach 2.

तो हम K lists जैसे हैं जो कि sorted होनी।

\* तो हम एक Priority Queue बनाएंगे जिसमें हर list का first element स्टोल करेंगे, Priority Queue में priority की रूट है smaller elements को।

तो हमारे पास priority queue में K element हैं

Because of K  
number of lists

Now, we will remove the element with highest priority and add 1 element in the priority queue (from the same array list to which the removed element belongs)

This will be done in a loop unless the priority queue becomes empty.

In this way, we will have our final sorted list

Result

→ We will return an ArrayList

→ This ArrayList will be the final ArrayList to trace the sorted list of all elements of all ArrayList.

इस element के साथ इ ब्रैक रखना पड़ेगा  
Ab वो ऐसी ArrayList का data है  
और क्या वो ArrayList का last index है?

Because  
ArrayList  
list  
of  
next  
element  
Eg PQ  
add  
remove  
get  
next  
element  
null  
Because  
this element  
is the  
last element  
(which is  
removed)  
get  
null pointer  
exception  
Eg SPCL

इन सभी बातों का ब्रैक रखने के  
लिए हम I Pair class बनाएंगे  
Pair class में हम रखेंगे data → data is the value at index  
data index (di) of list index (li) li  
To store the index of arraylist  
the index of data in the li  
list of arraylist

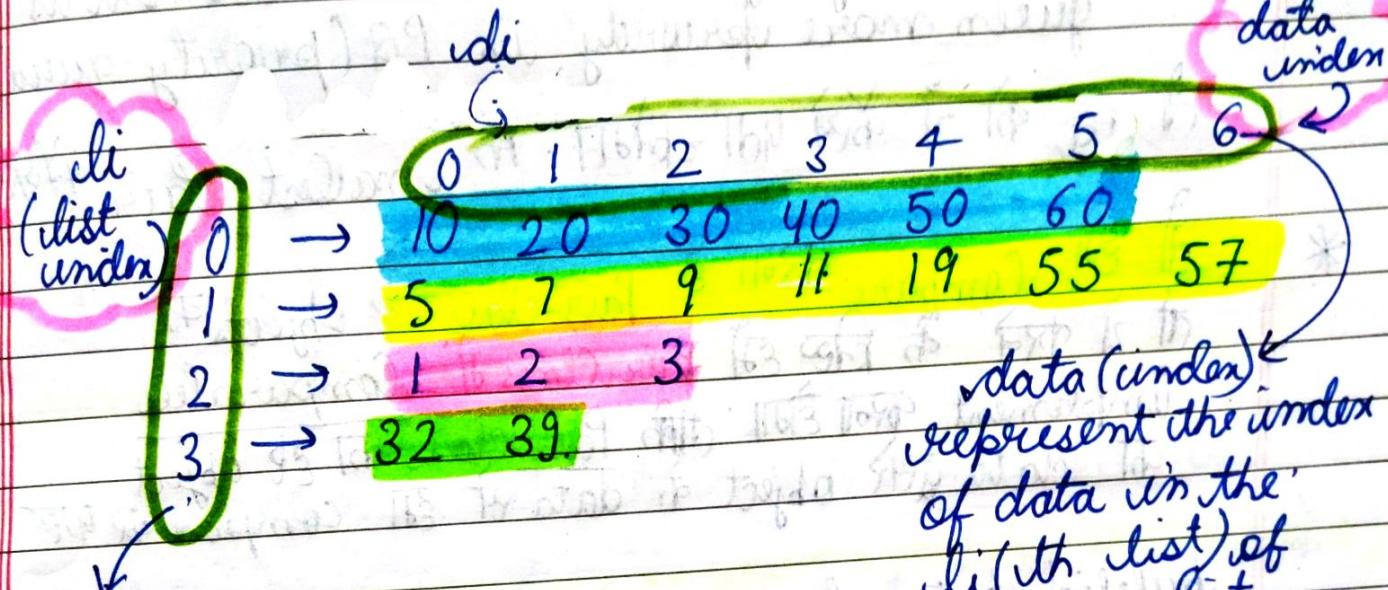
→ The result will be  
Eg SPCL

## Approach

① ~~ETI का Pair class कैसे होता है~~

(list index)  $\rightarrow$  li  
 (data index)  $\rightarrow$  di  
 (data)  $\rightarrow$  data

} we have these  
3 things  
in the pair class



data index  
represent the index  
of data in the  
li(th list) of  
ArrayList.

K list are  
surrounded in

ArrayList. So li(list index).  
will store the index of  
li(th) list of ArrayList.

And therefore, it helps us to  
keep track of the position in the ArrayList.

(ETI ArrayList में कौन सी लिस्ट पर travel करते हैं)

Data is the value, which is an element of li(th)  
list of ArrayList.

नि एके Pair class के 3 कोड शाफ्ट हैं

li (list index)  
di (list index)  
data

data is the value at  
di index of li list

③ हम एक Priority Queue बनाएंगे of type Pair class, तो हम Priority queue में Pair class के objects संलग्न। But Priority Queue में हमें ऐसा data संलग्न एवं प्रियोटी Priority Queue को पता करना है।

तो by default the smallest element is queen more priority in PQ (priority queue).

तो PQ को ये कैसे पता करेगा? As smallest Pair की ओर।

\* तो हमें Compare करना है Pair class के objects के तो ये करने के लिए हमें Pair class में Comparable implement करना होगा। तभी Pair class का हरे object की data दूसरे object की data से pair की compare कर पाये।

static class Pair implements Comparable<Pair>

```
{ int li;
  int di;
  int data; }
```

public int compareTo(Pair o)

```
{ return this.data - o.data; }
```

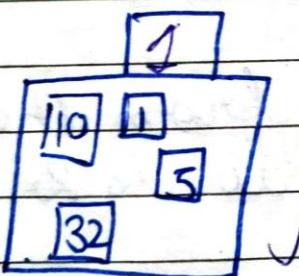
STATE IT difference +ve if this is bigger..

if smaller elements of Pair difference is -ve if this is smaller  
elements are queen more priority

difference is 0 if this and other is equal

static class Pair implements Comparable<Pair>  
 {  
 int li;  
 int di;  
 int data;  
 public int compareTo(Pair o)  
 {  
 return o.data - this.data;  
 }  
 }  
 अब यह other.data - this.data return करता है, so this means that we are giving priority to greater element.

- ③ So, first of all, we will create a Priority Queue.  
 और उसमें हर list के first element के लिए pair को PQ में डालेंगे।



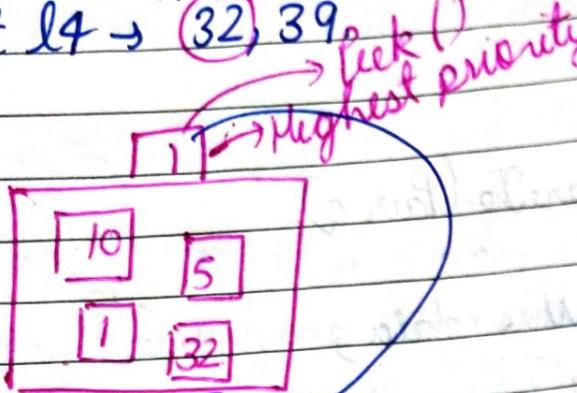
तो याने हर element के लिए pair की तरफ  
 where the li (list index)  
 will be the index of list to which the element belongs.

- ④ Now, we will also create a result ArrayList.  
 अब हम PQ में एक element remove करेंगे।  
 और एक new element PQ में सेंगे (from the same list to which removed element belong).  
 Only if the removed element was not the last element of the list it belonged to.

## DRY RUN

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- li=0 list l1 → 10, 20, 30, 40, 50.
- li=1 list l2 → 5, 7, 9, 11, 19, 55, 57.
- li=2 list l3 → 1, 2, 3.
- li=3 list l4 → 32, 39

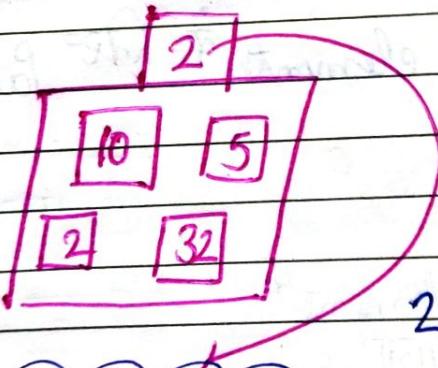


Result ArrayList

1

→ 1 is removed from list where index is 2.

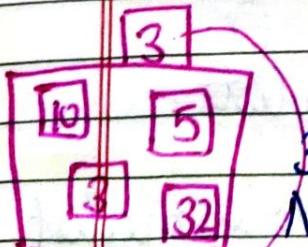
Now, next element will be added from the same list where li=2.



2 is removed from the list where li is 2.

Result ArrayList 1 2

→ Now, 3 will be added from list where li is 2.



3 is removed from the list where li is 2. Now 3 is the last element from this list. So now no element will be added.

Result ArrayList 1 2 3

5 is removed from AL where li is 1, now next element will be added from the same list. So now 7 will be added in the list.

Result AL  $\rightarrow$  1 2 3 5

7 is from list where li is 1.

Now 7 is at the peak of priority in the PQ, so 7 will be removed now next element 9 will be added in the PQ which is from the same list.

So now, 9 will be added.

Result AL  $\rightarrow$  1 2 3 5 7

9

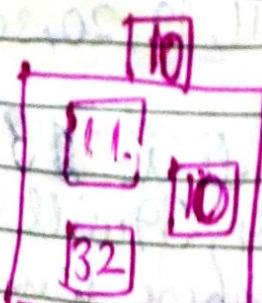
9 is from list where li is 1.

So 9 will be removed & now 11 is added which is next element from the list where li is 1.

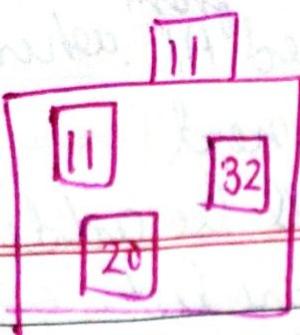
Result AL  $\rightarrow$  1 2 3 5 7 9

10 is from list where li is 0.

So, 10 will be removed from PQ & now next element (10) will be added from the list where li is 0.

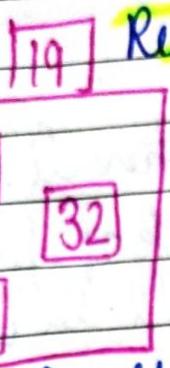


Result AL  $\rightarrow$  1 2 3 5 7 9 10



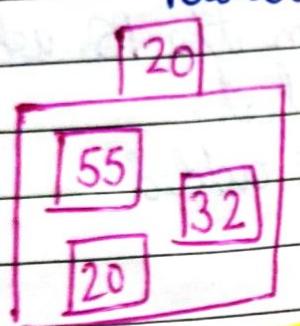
11 is from list where li is 1.  
So next element (19) will be added from list where li is 1.

Result AL  $\rightarrow 1 \ 2 \ 3 \ 5 \ 7 \ 9 \ 10 \ 11$



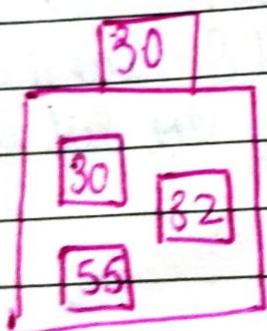
19 is from list where li is 1.  
So next element 55 will be added from list where li is 1.

Result AL  $\rightarrow 1 \ 2 \ 3 \ 5 \ 7 \ 9 \ 10 \ 11 \ 19$



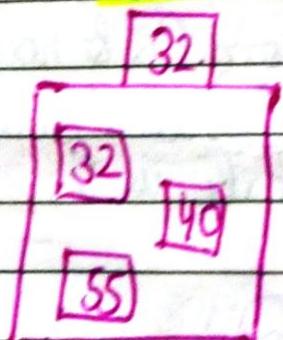
20 is from list where li is 0.  
So, next element 30 will be added from list where li is 0.

Result AL  $\rightarrow 1 \ 2 \ 3 \ 5 \ 7 \ 9 \ 10 \ 11 \ 19 \ 20$



30 is from list where li is 0.  
So, next element is 40, 40 will be added from list where li is 0.

Result AL  $\rightarrow 1, 2, 3, 5, 7, 9, 10, 11, 19, 20, 30$

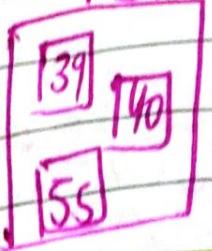


32 is from list where li is 3  
So, next element is 39, 39 will be added from list where li is 3.

Result AL  $\rightarrow 1 \ 2 \ 3 \ 5 \ 7 \ 9 \ 10 \ 11 \ 19 \ 20 \ 30 \ 32$

39

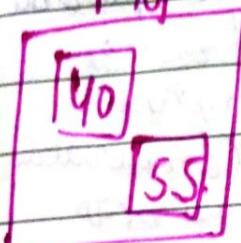
39 is removed from PQ.



39 is the last element of list where  $li = 3$ . So now, no new element will be added.

**Result AL  $\rightarrow$  1, 2, 3, 5, 7, 9, 10, 11, 19, 20, 30, 32, 39**

40



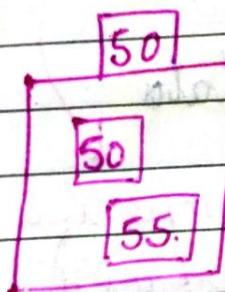
40 is removed from PQ.

40 is from list where  $li$  is  $= 0$ .

So, next element 50 will be added in PQ from list where  $li = 0$ .

**Result AL  $\rightarrow$  1 2 3 5 7 9 10 11 19 20 30 32 39 40**

50



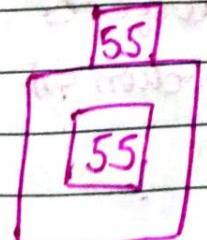
50 is removed from PQ.

50 is from AL where  $li$  is 0.

Now no new element is added in PQ because 50 is last element of list where  $li$  is 0.

**Result AL  $\rightarrow$  1, 2, 3, 5, 7, 9, 10, 11, 19, 20, 30, 32, 39, 40, 50.**

55

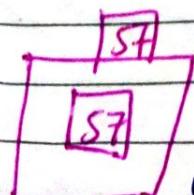


55 is removed from PQ, the  $li$  of 55 is 1.

57 is the next element to be added in PQ because as  $li$  of 57 is 1.

**Result AL  $\rightarrow$  1 2 3 5 7 9 10 11 19 20 30 32 39 40**

57



57 is removed from PQ. 57 is the last element of list where  $li$  is 1. So there is no next element to be added in PQ, so PQ becomes empty.

**Result AL  $\rightarrow$  1 2 3 5 7 9 10 11 19 20 30 32 39 40 50 55 57**

We get our final arraylist

import java.util.\*;

public class Main

{

public class Pair implements Comparable

{

int data;  
int id;  
int li;

Pair को compare  
करने के लिए Comparable  
interface का use करा  
पड़ेगा

public int compareTo (Pair o)

{

return this.data - other.data

Comparable  
Interface में  
compareTo function

का वर्ता नाम है।

उत्तर एवं PQ में integers

data नहीं स्टोर होती।

PQ assume करती है

कि PQ के data की

class में हमने Comparable

implement किया है।

अब यह Comparable implement करना पड़ता है

ताकि PQ Pairs को compare कर पाय

Interface में function

की Body नहीं हो। Interfaces

में किसी नाम दोनों function की

function की

public static ArrayList < Integer > mergeKSortedLists  
 (ArrayList < ArrayList < Integer > ) lists  
 {  
 ↗ हमने result AL का नाम दिया है जो कि ArrayList पर भी  
 ↗ उसके रूप में दिया गया है जो कि ArrayList पर भी

ArrayList < Integer > resultAL = new ArrayList < >();  
 Priority Queue < Pair > pq = new Priority Queue < >();  
 ↗ यह एक Priority Queue है जिसमें हम

for (int li = 0; li < lists.size(); li++)  
 {

Pair p = new Pair();

p.li = li;

p.di = 0;

p.data = lists.get(li).get(0);

pq.add(p);

हमने सभी

list के  
first element

के लिए

Pair बनाये

और उन Pairs

को PQ में add

कर दिया

while (pq.size() > 0)

पहला तक

PQ empty न हो तक तब तक

loop-लिया

और ए

1 element की

remove करते

with highest priority

और इसी element का list

का next element लेते

Pair removedPair = pq.peek();

pq.remove();

result AL.add (removedPair.data);

removedPair.di++;

if (removedPair.di < lists.get(removedPair.li).size())

removedPair.data = lists.get(removedPair.li)

.get(removedPair.di);

pq.add(removedPair);

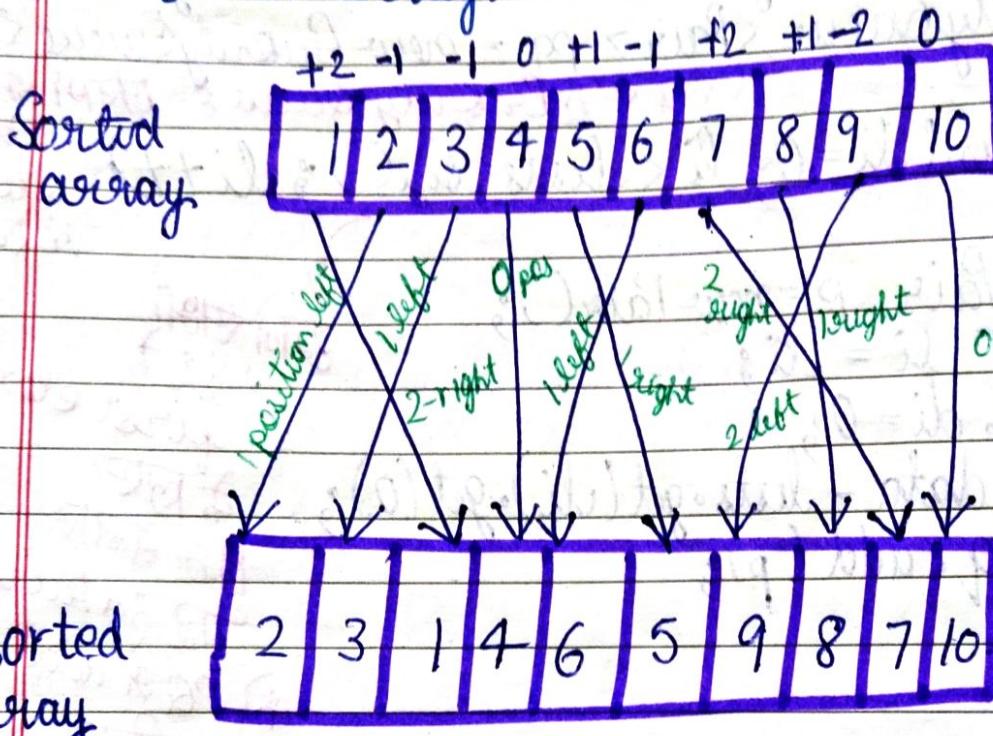
last में AL को  
return करदे।

3 return resultAL;

## Ques. 2. SORT K-SORTED ARRAY

इसे कहा दोगा और यह integer  $K$  given होगा।

The integer  $K$  denotes that the array is a  $k$ -sorted array.



इसे कहा k-sorted array given होगा।

K-sorted array में एक element अपनी position पर  
(0 to  $k$ ) K-position left वा K-position right के move

हो सकता है।

If  $K=2$ , तो  
एक element 1 वा 2 position left वा right move  
कर सकता है।

It is also possible that element does not move  
from their position.

So we can move 0/ 1/ 2. positions if  $K=2$ .

## Approach

1. We create a priority queue of size  $K+1$ . Now, we will remove 1 element from the priority queue. (Priority Queue से 1 element remove करना और उस removed element को print करना)
 

K+1 size of arraylist

This will be the smallest element as the removal from the priority queue gives the smallest element or the element of highest priority. Now, we have  $K$  elements remaining in the priority queue. The removed element will be

3. So, we insert the next element in the Priority Queue and the size again becomes  $K+1$ .

Unless the PQ becomes empty of

Now, we will keep on removing the element from PQ and adding next element of the array (unless we have no next element in the array to be added in the PQ).

- \* So, we repeat the same procedure until we cover the entire array.

→ Out Priority Queue में से 1 element remove करके PQ empty करें।  
 → और Array की 1 element PQ में add करें।  
 → तब तक कि Array के सब elements की visit कर दी जाए।

प्रियोरिटी क्वीन  
प्रियोरिटी क्वीन  
empty of  
एयरे  
& print  
the  
removed  
element.

4. If the array is completely visited & some elements are left in the Priority Queue, we empty the PQ completely (to print the removed element) and then this procedure stops here.

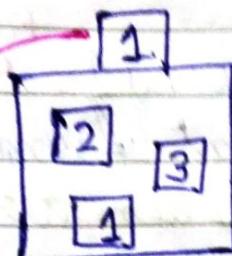
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①

|   |   |   |   |   |   |   |   |   |    |
|---|---|---|---|---|---|---|---|---|----|
| 2 | 3 | 1 | 4 | 6 | 5 | 9 | 8 | 7 | 10 |
|---|---|---|---|---|---|---|---|---|----|

1 element  
will be  
removed  
and  
printed



→ 1

K=2

} Added  $K+1$  i.e. 3 elements  
in the PQ.

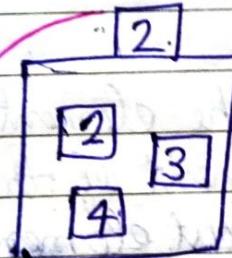
} 1 is removed & printed  
Next element (4) will be added  
in the PQ.

|   |   |   |   |   |   |   |   |   |    |
|---|---|---|---|---|---|---|---|---|----|
| 2 | 3 | 1 | 4 | 6 | 5 | 9 | 8 | 7 | 10 |
|---|---|---|---|---|---|---|---|---|----|

↓  
1 has  
already been printed

②

1 element  
will  
be  
removed  
and  
printed



1 2.

} We still have 3 elements in  
the PQ.

2 has the maximum Priority.

So we will remove 2 from PQ & print it.

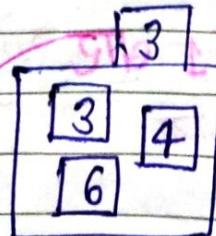
Now next element (6) will be added

in the PQ.

→ 2 is also printed

③

1 element  
will be  
removed  
and  
printed



→ 1 2 3.

|   |   |   |   |   |   |   |   |   |    |
|---|---|---|---|---|---|---|---|---|----|
| 2 | 3 | 1 | 4 | 6 | 5 | 9 | 8 | 7 | 10 |
|---|---|---|---|---|---|---|---|---|----|

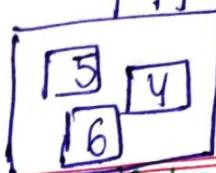
} 1 and 2  
has already  
been printed

Now 3 is printed

& removed.

So the next  
element of array  
(5) will be added  
in the PQ.

④



1 element will be removed & printed

1 2 3 4

2 3 0 4 6 5 9 8 7 10

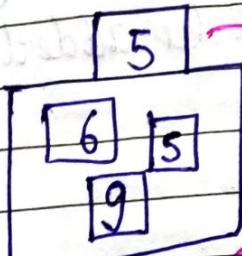
1,2,3 have been printed

Now 4 is also printed

& removed from the PQ.

So next element of Array (9) will be added in the PQ.

⑤



1

2 3 0 4 6 5 9 8 7 10

element will be removed

1,2,3,4 have already been printed.

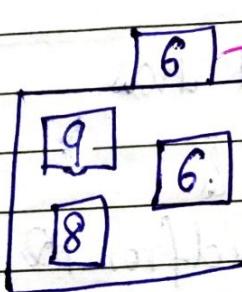
1 2 3 4 5.

and printed

New, 5 is printed and removed from PQ.

So, next element of Array (8) will be added in the PQ.

⑥



1 element will be removed.

and printed.

2 3 0 4 6 5 9 8 7 10

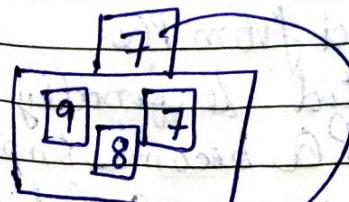
1 2 3 4 5 6

1,2,3,4,5 have already been printed

Now, 6 is printed and removed from PQ.

So, next element of Array (7) will be added in the PQ.

⑦



2 3 0 4 6 5 9 8 7 10

1,2,3,4,5,6 have already been printed

1 2 3 4 5 6 7 Now, 7 is printed and removed from PQ.

So, next element of Array (10) will be added in the PQ.

(8)

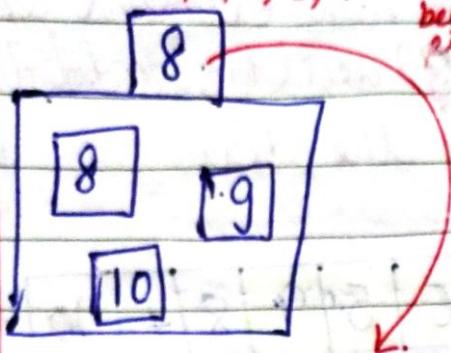
|   |   |   |   |   |   |   |   |   |    |
|---|---|---|---|---|---|---|---|---|----|
| 2 | 3 | 1 | 4 | 6 | 5 | 9 | 8 | 7 | 10 |
|---|---|---|---|---|---|---|---|---|----|

1, 2, 3, 4, 5, 6, 7

have  
been  
printed

Now, 8 will be printed and removed from PQ.

So, next element of array  
Something will be added.



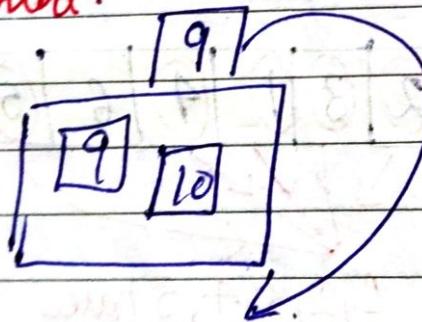
1 2 3 4 5 6 7 8

(9)

|   |   |   |   |   |   |   |   |   |    |
|---|---|---|---|---|---|---|---|---|----|
| 2 | 3 | 1 | 4 | 6 | 5 | 9 | 8 | 7 | 10 |
|---|---|---|---|---|---|---|---|---|----|

Now, 9 will be printed & removed from PQ.

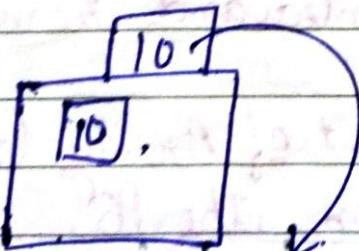
1, 2, 3, 4, 5, 6, 7, 8 have been printed.



1 2 3 4 5 6 7 8 9

Now 9 has been printed & removed from PQ,  
so only 10 is remaining in PQ.

(10)



1 2 3 4 5 6 7 8 9 10.

Now 10 will be removed from PQ & printed & finally our PQ becomes empty.  
and we have our sorted array.

See we have pushed element in PQ & then removed them

So the TC for removing an element from PQ  
Time complexity  $\rightarrow O(\log k)$ .

So, TC for K elements  $\rightarrow O(n \log k)$

Space Complexity  $\rightarrow O(k)$

Because only K Elements were stored in PQ.

# SORT K-SORTED ARRAY

## <code>

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```
import java.util.*;  
public class Main {  
    public static void main(String[] args) {  
        Scanner scan = new Scanner(System.in);  
        int n = scan.nextInt();  
        int arr[] = new int[n];  
        for (int i = 0; i < n; i++) {  
            arr[i] = scan.nextInt();  
        }  
        int k = scan.nextInt();  
    }  
}
```

} एक K  
sorted array  
input  
लिया

} की value  
output का.

```
PriorityQueue<Integer> pq = new PriorityQueue<>();
```

```
for (int i = 0; i <= k; i++) {  
    pq.add(arr[i]);  
}  
}
```

} array के  
K+1  
elements को  
pq में डाला

```
for (int i = k + 1; i < arr.length; i++) {
```

प्रक्रिया  
peek  
element  
को print  
प्रिंट  
remove  
दूसरे

```
    int val = pq.peek();  
    System.out.println(val);
```

```
    pq.remove();  
    pq.add(arr[i]);  
}
```

} array के  
next element  
in pq के साथ  
loop चलता है।

while ( $hpq.size() > 0$ )

अगर pq में अब श्रीकृष्ण  
elements हों तो print  
करदा) और उन्हें pq में से

1 init val =  $hpq.peek()$ ;

remove करदा)

System.out.println(val);

$hpq.remove();$

2

3

3

③

# MEDIAN PRIORITY QUEUE

Date \_\_\_\_\_  
Page No. \_\_\_\_\_

We have to create our own priority queue but this is not a normal priority queue. This is a median Priority Queue.

मतलब इस Priority Queue में Smaller तक greater element की अपनी Priority, नहीं होती। Median Priority Queue की median की सबसे ऊपरी Priority होती।

तो इसके remaining elements का median ही return किया जाएगा।

10 20 30 40 50

## NORMAL PRIORITY QUEUE      Median Priority Queue

peek() → 10.

peek() → 30

remove() → 10.

remove() → 30.

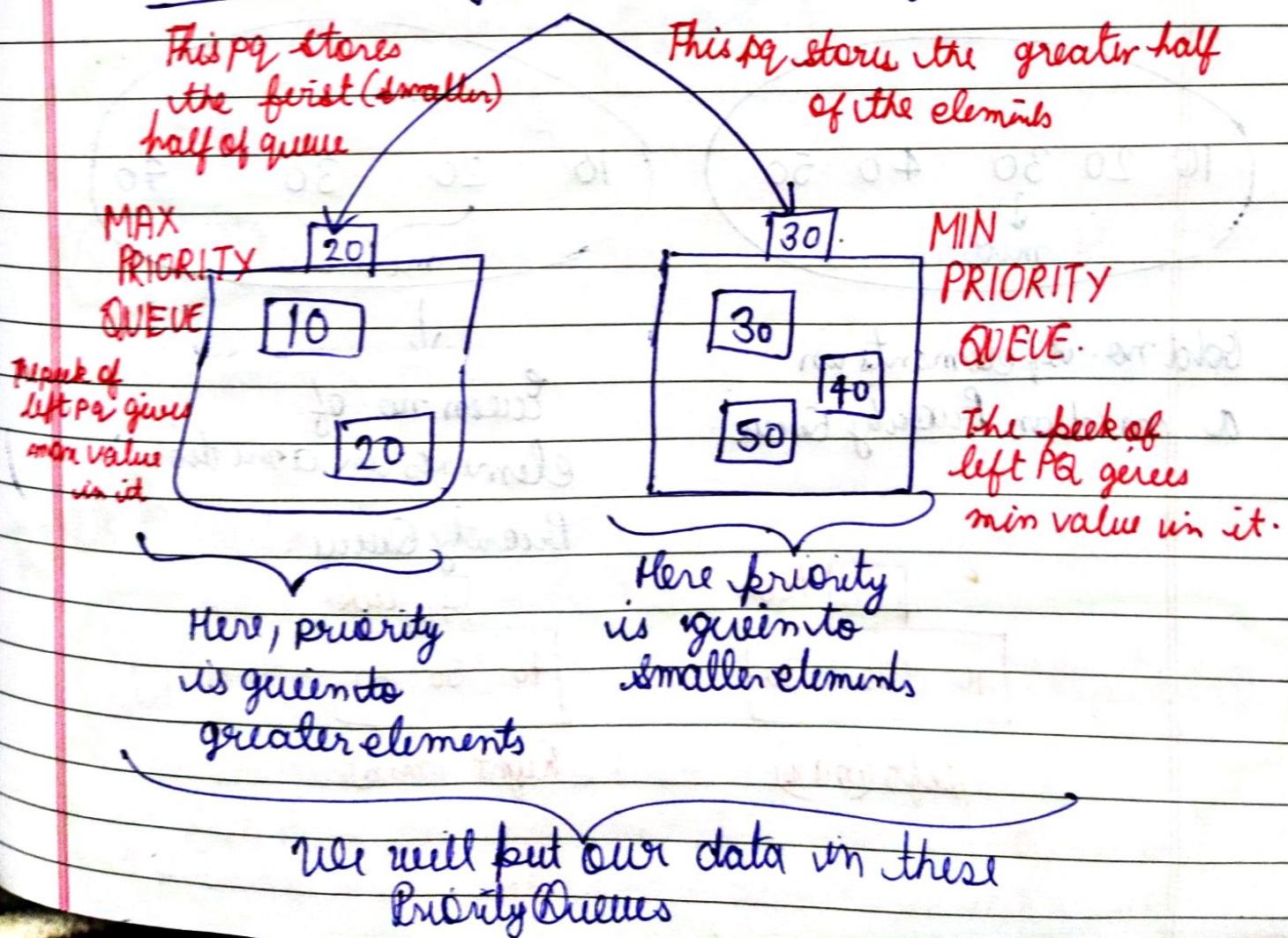
In A median priority will see just like a normal priority queue, but in the <sup>normal</sup> priority queue when we call the remove function, it removes the smallest element (10) from the queue because By default In Priority Queue, the smallest element has the highest priority queue.

But, In case of Median Priority Queue, when we call the remove() function, the function will remove the median of all elements similarly the peek() function returns the median of all elements.

\* The Time Complexity of peek() and remove() function should be same as of a normal priority queue  $O(1)$   $\downarrow$   $O(\log n)$

### Approach

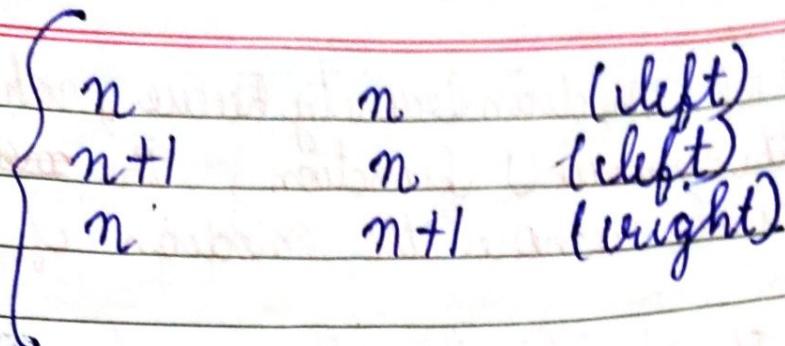
1. Median Priority Queue is basically 2 priority queues



Lift PQ.

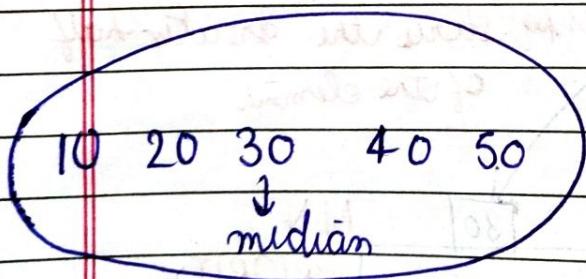
Right PQ.

Peek

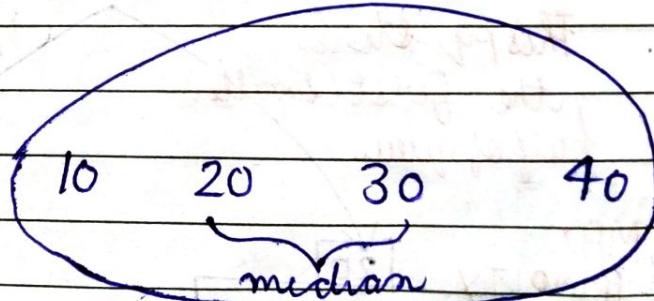


→ If the median queue has even no. of elements i.e. If both Left PQ & Right PQ has equal size  
Left PQ if 1st element remove still and that element will be printed as a median.

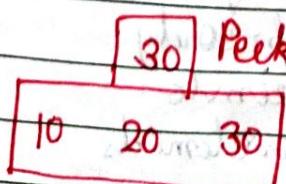
→ If there are odd number of elements in the pq, if the left priority / right priority queue has  $n+1$  elements & the other priority queue (right / left pq) has  $n$  elements, then in this case, the pq with  $n+1$  elements will remove an element.



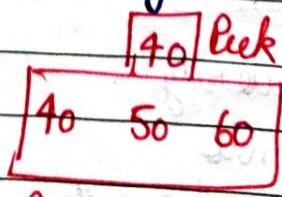
Odd no. of elements in a median Priority Queue.



Even no. of elements in a median Priority Queue.



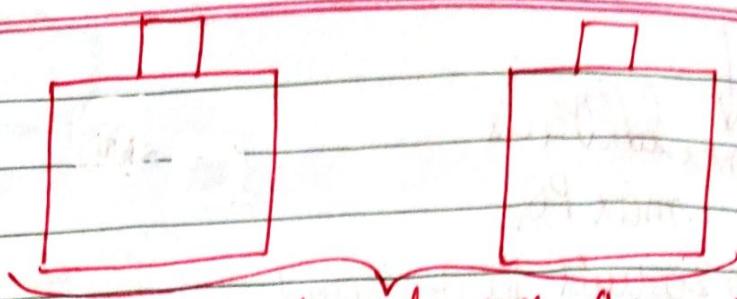
Left (max)



Right (min)

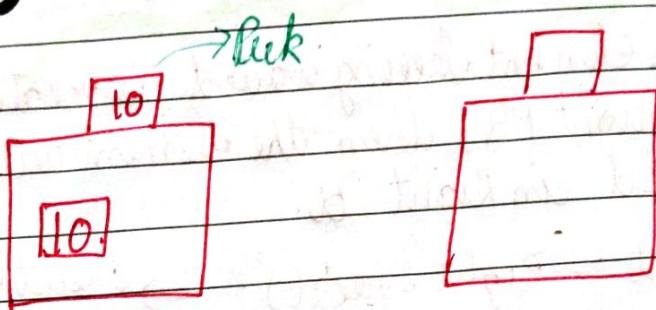
# DRYRUN

Date \_\_\_\_\_  
Page No. \_\_\_\_\_



Our median priority Queue is empty.  
Initially, both our left and right priority  
were empty.

**ADD(10)**

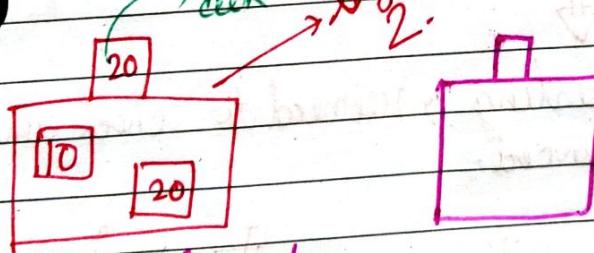


→ Pick

By default,  
an element is  
inserted in the left PQ.

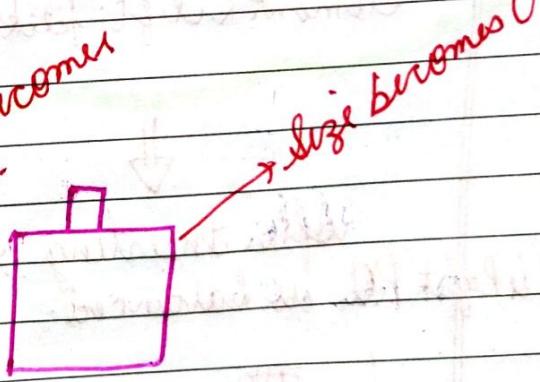
**RULE 1**

**ADD(20)**



→ Pick

Size becomes  
2.



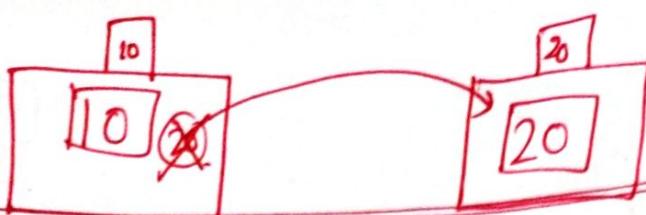
Size becomes 0

**RULE 2**

By default, element  
is inserted in left PQ

But if, The difference in size of Left and Right PQ  
Should be 1

But here the difference becomes 2. So, remove  
1 element from queue having more element & put it in another



↓  
since left PQ is  
max PQ

so 20 will be removed  
from it & it will be  
pushed in right PQ.

3rd Left  $\neq$  Right PQ & Size equal  $\neq$

### RULE 3

When the element being added is greater than peek() of right PQ, then the element will get inserted in right PQ.

element  $>$  Right.peek()  $\Rightarrow$  Insert in  
Right PQ.

When the element being added is lesser than the peek() of left PQ, then the element will be inserted in left PQ.

element  $<$  Left.peek()  $\Rightarrow$  Insert in left  
PQ.



After inserting, we need to check whether the left & right PQ is balanced.

↳ 3rd Rule Difference 2 दूरी नहीं

Left queue में विकल्प एवं Right queue में एवं  
element remove करके दूसरी queue में add करें।

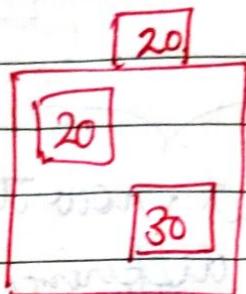
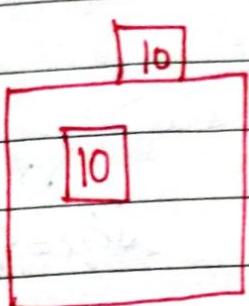
If the element  $<$  Right.peek() & element  $>$  Left.peek()

By default, 3rd element of left PQ. It add करेंगे।

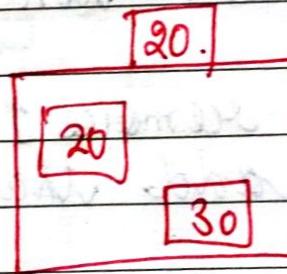
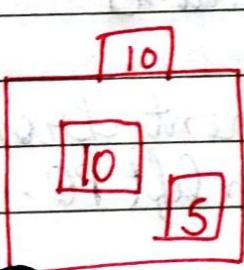
Then, we will check if the PQ has size difference  $< -1$

**ADD(30)**

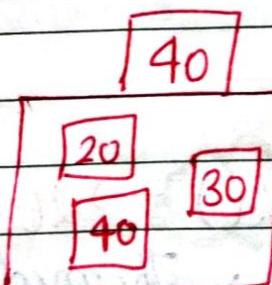
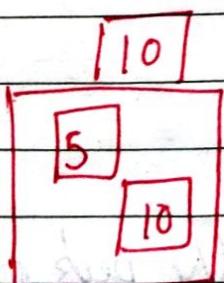
↳ 30 is greater than Right peek().  
So 30 will be inserted in the Right PQ

**ADD(5)**

↳ 5 is lesser than Left peek()  
So 5 will be inserted in the Left PQ.

**ADD(40)**

↳ 40 is greater than Right peek()  
So 40 will be inserted in Right PQ.



Left PQ

Maximum

Priority Queue

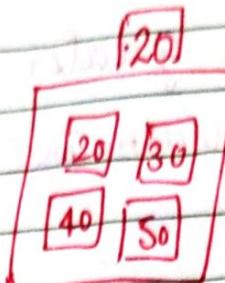
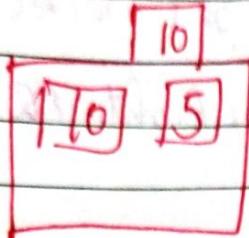
Right PQ

Minimum

Priority Queue

**ADD (50)**

50 is greater than Right peek()  
so 50 is added to the Right PQ



size = 2

But now the size difference is 2. size = 4.

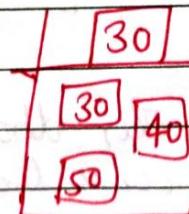
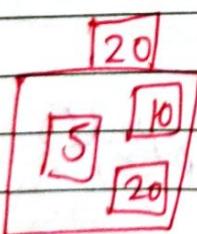
So there isn't the accurate balance between size.

So the Right PQ has size 4.

and the Left PQ has size 2.

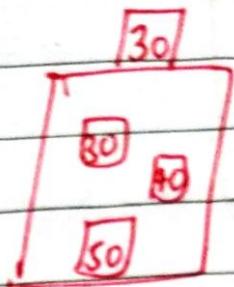
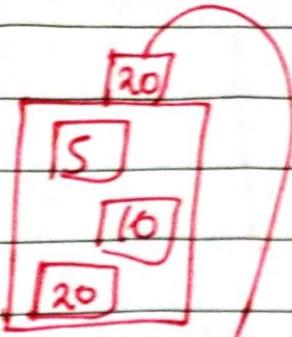
So, there is an imbalance.

So, just remove 1 element from Right PQ and add that in Left PQ.



**Median PQ . peek() → 20.**

The median is the peek of PQ with more elements if there are odd no. of elements in total. But if in total there are even number of elements, then median is the peek of left PQ.



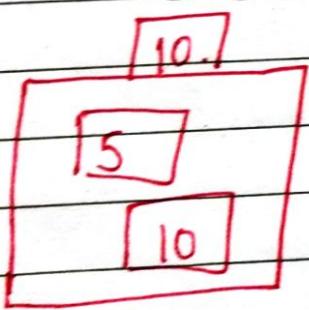
Median PQ Remove() → 20

Median Remove() → When there are equal elements in both Left & Right PQ  
(Even no. of elements in total).

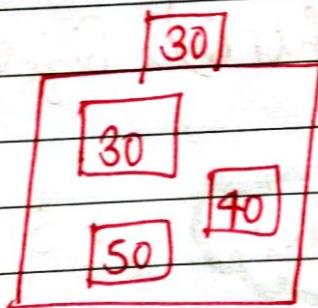
Then we will remove the element from Left PQ.

Right.remove() → 20 is removed.

MEDIAN PQ REMOVE() → 30.



↓  
Size = 2



↓  
Size = 3

5 element → When the size is odd  
(when size of left & right PQ.  
is not equal)

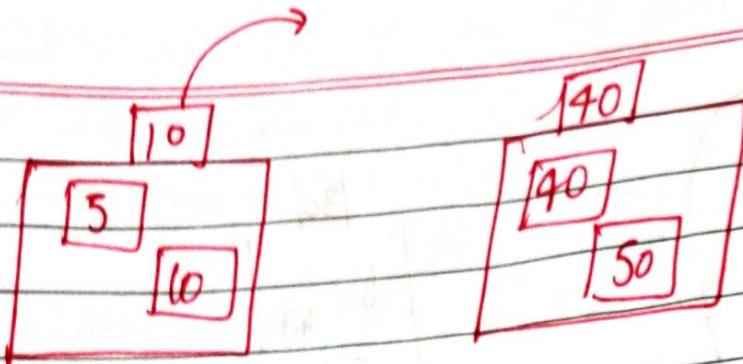
Then remove the element from PQ having more elements.

Right Size > left Size

So Remove element from Right PQ..

MEDIANPQ::REMOVE() → 10.

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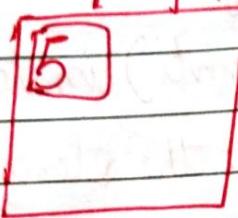


Now again the Elements are even.  
So remove the element from left PQ.

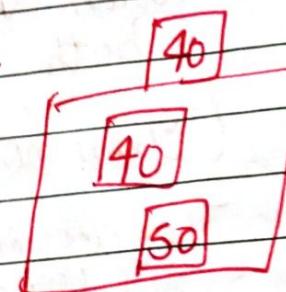
MEDIANPQ::REMOVE

→ 40

15.



Size → 1



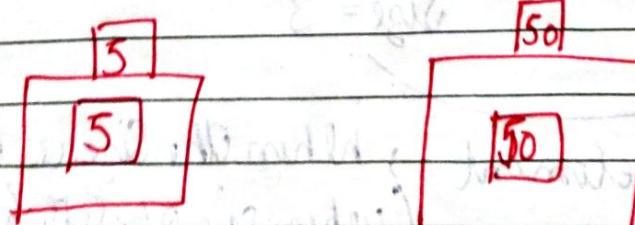
→ Size → 2

Now, as the elements are odd.  
So the element will be removed from PQ  
where the Size is more.

Size of Right PQ > Size of Left PQ

MedianPQ::Remove()

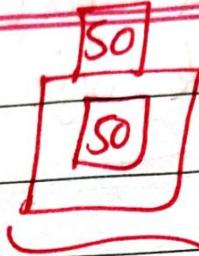
→ 5



Even element So, element will be  
removed from left PQ.

Median PQ · remove() → 50.

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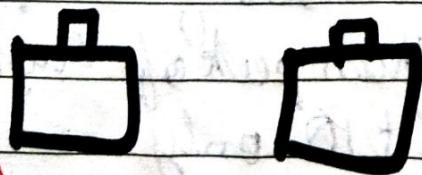
Left PQ has  
0 element

Right PQ -  
has 1 element

Size of Right PQ > Size of Left PQ.

So remove the element from Right PQ.

Now, Both our left & Right PQ is empty.



Empty PQ's

Page No. \_\_\_\_\_

In the Question, we need to write the following functions  
Add, Remove, Peek, Size

Add() → Add an element in Median PQ;



Basically we have 2 PQ behind

1. The elements are added by default in left PQ.
2. The difference b/w size of 2 PQ should be maintained to 1.  
If the difference increases, shift one element from the queue with higher no. of elements to the one with the lower.
3. If the input element is greater than peek<sup>(V)</sup> of right PQ, then it is added to Right PQ only.

Peek() → 1. If there are even number of elements (equal in both PQ) then the median is the peek() of the left Priority Queue. else if there are odd number of elements, then the median is the peek of the Queue with more elements.

Remove() → 1) If there is equal no. of elements in left & right PQ (total even no. of elements in both PQ) then the median will be removed from the left PQ else we remove from the PQ which has more number of elements.

Size() → If we will just to add the size of left PQ & Right PQ.

## Time Complexity

1.  $\text{Add}() \rightarrow O(\log n)$
2.  $\text{remove}() \rightarrow O(\log n)$
3.  $\text{peek}() \rightarrow O(1)$
4.  $\text{Size}() \rightarrow O(1)$ .

} Similar to normal  
pq.

## Space Complexity

• The Space Complexity is  $O(1)$  as we have not used any extra space for any function ( $\text{add}$ ,  $\text{remove}$ ,  $\text{peek}$ ,  $\text{size}$ ).  
We have just taken 2 PQ but they will not be counted in Space Complexity as it is not extra space.

The question asked to create a Median Priority Queue and we have just done that using 2 PQ's.

# MEDIAN PRIORITY QUEUE <code>

Page No.

```
import java.util.*;  
public class Main {
```

```
    public class Main
```

```
        public static class MedianPriorityQueue
```

```
            PriorityQueue<Integer> left = new PriorityQueue<Integer>();  
            PriorityQueue<Integer> right = new PriorityQueue<Integer>();
```

```
            public MedianPriorityQueue() {
```

constructor  
of  
median  
pq  
class

```
            left = new PriorityQueue<Integer>();  
            left.add(0);
```

```
            right = new PriorityQueue<Integer>();  
            right.add(0);
```

```
            } // giving priority  
            // to smaller element
```

```
            public void add (int val) {
```

```
                if (right.size() > 0 & val > right.peek()) {
```

```
                    right.add(val);
```

```
                } else {
```

```
                    left.add(val);
```

```
                }
```

```
            }
```

val  
at value  
ZTR  
right  
pq  
peek  
ZTR  
right  
add  
otherwise  
left pq

ZTR left ZTR  
Right pq at  
size diff 1 ZTR  
at balance  
at ZTR yes

element  
at ZTR  
otherwise  
Right pq is empty  
we will get  
null pointer  
exception

private void handleGap()

{ if (left.size() - right.size() == 2)

int val = left.remove();  
right.add(val);

3TR left की size  
से right की size

में 2 element  
होता है तो

left से 2 का  
element

front का

right

3TR

& vice versa.

else if (right.size() - left.size() == 2)

{ int val = right.remove();  
left.add(val);

public int remove().

3TR remove  
function call

if (this.size() == 0).

3TR का रखा है

प्रोटोकोल  
का बदलाव

3TR medium

PQ की कोई  
element नहीं

(left 3TR Right PQ  
का size check  
होता है)

if (left.size() >= right.size())

3TR size 0 है तो  
we have no

return left.remove();

element to  
remove so  
we will

simply  
print

underflow.  
& return -1

else

return right.remove();

as the removed  
element

else 3TR

Medium PQ size 0 होता है

3TR left PQ की size right PQ से

विवाद होता है

जो we will remove the element from left PQ  
otherwise from right PQ.

```

public int peek() {
    if (this.size() == 0)
        System.out.println("Underflow");
    return -1;
}

if (left.size() >= right.size()) {
    return left.peek();
} else {
    return right.peek();
}
}

public int size() {
}

```

*if (this.size() == 0)* → *if peek function me gft  
size() zero  
function  
and logic ddkhjye*

*if (left.size() >= right.size())* → *if left pg & right pg  
size is equal  
it will return the  
peek of left pg*

*else* → *if size of left pg & right pg  
is not equal  
then we  
will return the  
peek of right pg*

return left.size() + right.size();

The Size of median Priority Queue is the sum of size of left Priority Queue & right Priority Queue.

→ Here this is the closing bracket of median Priority Queue Class Queue

public static void main (String [] args)

{ BufferedReader br = new BufferedReader

(new InputStreamReader  
(System.in));

Date: \_\_\_\_\_  
Page No. \_\_\_\_\_

MediumPriorityQueue queue = new MediumPriorityQueue

String str = br.readLine();

while (str.equals ("quit") == false)

{ if (str.startsWith ("add"))

int val = Integer.parseInt

(str.split (" ") [1]);

queue.add (val);

} Object PQ function call होती है।

else if (str.startsWith ("remove"))

int val = queue.remove ();

if (val != -1)

System.out.println (val);

}

else if (str.startsWith ("fuck"))

int val = queue.remove ();

if (val != -1)

System.out.println (-val);

}

}

else if (str.startsWith("size")).

{ System.out.println(queue.size());

}

str = br.readLine();

3 3 3  
3 3 0