

Design and Analysis of Algorithms Practical File

Design And Analysis Of Algorithms (University of Delhi)



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UNIVERSITY OF DELHI

ARYABHATTA COLLEGE BSC (HONS) COMPUTER SCIENCE SEMESTER - 4

DESIGN AND ANALYSIS OF ALGORITHMS

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Note: For the algorithms at S.No 1 to 3 test run the algorithm on 100 different inputs of sizes varying from 30 to 1000. Count the number of comparisons and draw the graph. Compare it with a graph of nlogn.

Question 1:

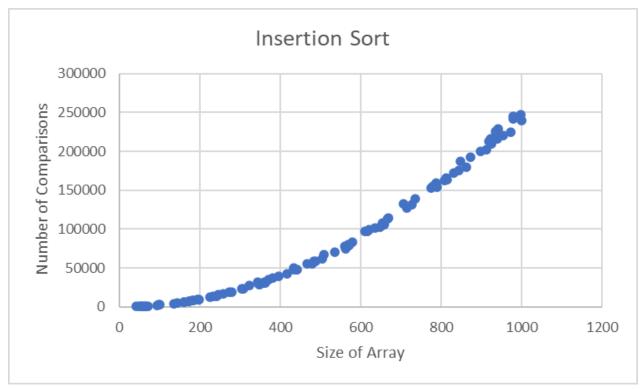
A. Implement Insertion Sort (The program should report the number of comparisons)

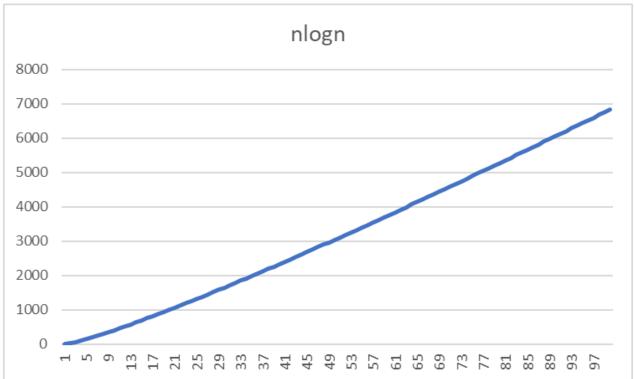
Solution 1.A:

```
# Created By : DEVANSH SHARMA
#include <iostream>
#include <fstream>
using namespace std;
int insertionSort(T arr[], int size)
   T key;
   int i, j, comp = -1;
    for (i = 0; i < size; i++)
        key = arr[i];
        while (j \ge 0 \&\& arr[j] > key)
           comp++;
            arr[j + 1] = arr[j];
        arr[j + 1] = key;
    return comp; // Returns no. of comparisons
int main()
    int n = 100;
```

```
ofstream outputFile("data.csv");
    int size;
        size = rand() % 1000;
    } while (size < 30 || size > 1000);
    int *arr = new int[size];
    for (int j = 0; j < size; j++)
        arr[j] = rand() % 1000;
    int comp = insertionSort<int>(arr, size);
    outputFile << "\n"<< size << "," << comp;</pre>
outputFile.close();
cout << endl;</pre>
return 0;
```

Output 1.A:





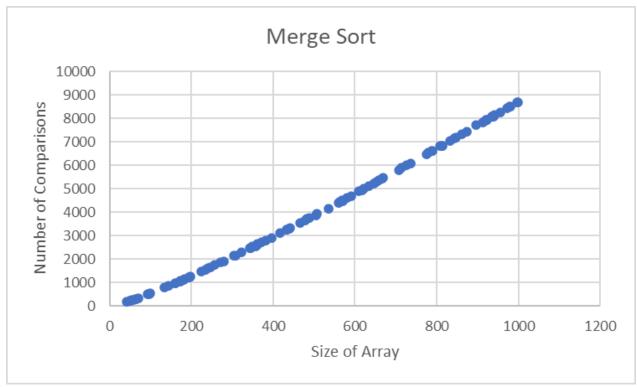
Solution 1.B:

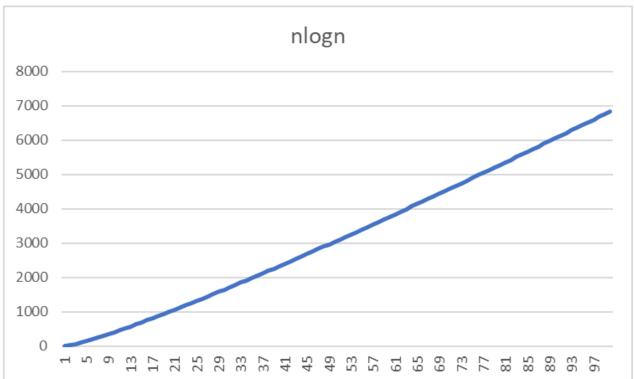
```
#include <iostream>
#include <fstream>
using namespace std;
int comps;
void merge(int arr[], int left, int mid, int right)
    int n1 = mid - left + 1;
    int n2 = right - mid;
    int L[n1], M[n2];
    for (int i = 0; i < n1; i++)
        L[i] = arr[left + i];
    for (int j = 0; j < n2; j++)
        M[j] = arr[mid + 1 + j];
    int i = 0, j = 0, k = left;
    while (i < n1 \&\& j < n2)
        if (L[i] \le M[j])
            arr[k] = L[i];
```

```
i++;
        else
           arr[k] = M[j];
        comps++; // Increment comparison counter
        k++;
   while (i < n1)
       arr[k] = \overline{L[i]};
       i++;
       k++;
   while (j < n2)
       arr[k] = M[j];
       k++;
void mergeSort(int arr[], int left, int right)
   if (left < right)</pre>
        int mid = left + (right - left) / 2;
       mergeSort(arr, left, mid);
       mergeSort(arr, mid + 1, right);
       merge(arr, left, mid, right);
```

```
int main()
    int n = 100;
    ofstream outputFile("data.csv");
    for (int i = 0; i \le n; i++)
        int size;
            size = rand() % 1000;
        } while (size < 30 || size > 1000);
        int *arr = new int[size];
        for (int j = 0; j < size; j++)
           arr[j] = rand() % 1000;
        comps = 0;
        mergeSort(arr, 0, size - 1);
        outputFile << "\n" << size << "," << comps;</pre>
    outputFile.close(); // Close the file
    cout << endl;</pre>
    return 0;
```

Output 1.B:





Question 2:

Implement Heap Sort(The program should report the number of comparisons)

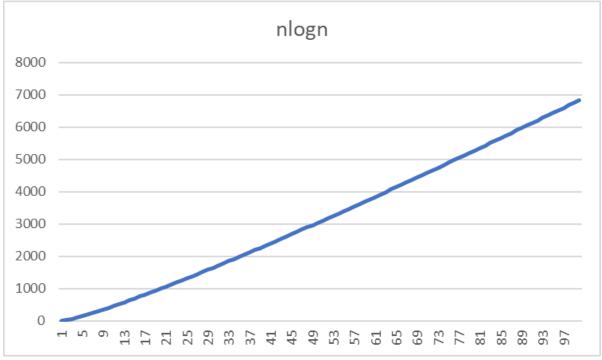
Solution 2:

```
#include <iostream>
#include <fstream>
using namespace std;
// Max Heapify function
int max_heapify(int arr[], int i, int size)
   int count = 0; // comparison counter
   int maxIndex = i;
   int 1 = 2 * i + 1; // left child
   int r = 2 * i + 2; // right child
   // Comparisons with left child
   if (1 < size && arr[1] > arr[maxIndex])
       maxIndex = 1;
    // Comparisons with left child
    if (r < size && arr[r] > arr[maxIndex])
       maxIndex = r;
    // Main logic
   if (i != maxIndex)
        count++;
       swap(arr[i], arr[maxIndex]);
        count += max heapify(arr, maxIndex, size);
    return count;
   Build Heap function - iterating over all the
    non leaf nodes and applying max heapify
int buildMaxHeap(int arr[], int size)
   int count = 0;
   for (int i = size / 2 - 1; i \ge 0; --i)
        count += max heapify(arr, i, size) + 1;
```

```
return count;
   Heap Sort function - iterates (size-1) times,
   swap max element (root) and last element and then
   applying max heapify on root element (and decrease size by 1)
int heapSort(int arr[], int size)
    int count = buildMaxHeap(arr, size);
   for (int i = size - 1; i > 0; i--)
    {
        swap(arr[0], arr[i]);
        count += max heapify(arr, 0, i) + 1;
    return count;
int main()
   // Number of iterations
   int n = 100;
   // Opening and initializing file
   ofstream outputFile("data.csv");
    for (int i = 0; i < n; i++)
    {
        int size;
       // Taking a random size between 30 and 1000
        do
        {
            size = rand() % 1000;
        } while (size < 30 || size > 1000);
        int *arr = new int[size];
        // Initializing array with random values
        for (int j = 0; j < size; j++)
            arr[j] = rand() % 1000;
        }
        // Initializing comps and applying heap sort
        int comps = heapSort(arr, size);
```

Output 2:







Question 3:

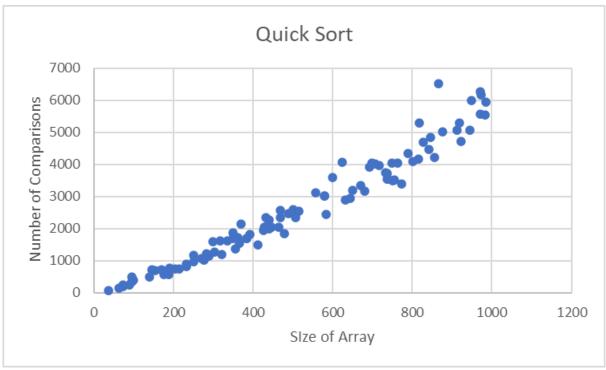
Implement Randomized Quick sort (The program should report the number of comparisons)

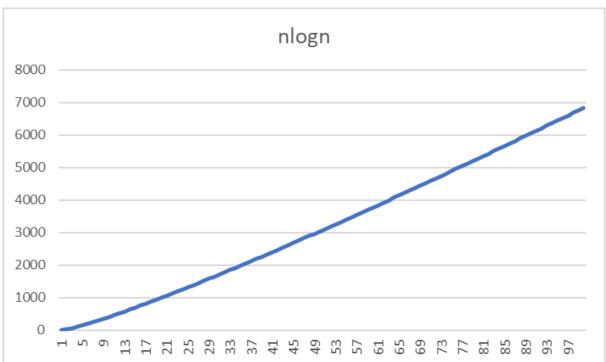
Solution 3:

```
# Created By : DEVANSH SHARMA
#include <iostream>
#include <fstream>
using namespace std;
int comps;
int partition(int array[], int low, int high)
    int pivot = array[high];
    int i = (low - 1);
    for (int j = low; j < high; j++)
        if (array[j] <= pivot)</pre>
            i++;
            swap(array[i], array[j]);
            comps++; // Comparison + 1
    swap(array[i + 1], array[high]);
    return (i + 1);
int randomPartition(int arr[], int low, int high)
    int random = low + rand() % (high - low);
    swap(arr[random], arr[high]);
    return partition(arr, low, high);
roid quickSort(int array[], int low, int high)
```

```
if (low < high)</pre>
        int pi = randomPartition(array, low, high);
        quickSort(array, low, pi - 1);
       quickSort(array, pi + 1, high);
int main()
   int n = 100;
   ofstream outputFile("data.csv");
   for (int i = 0; i < n; i++)
        int size;
       do{
            size = rand() % 1000;
        } while (size < 30 || size > 1000);
        int *arr = new int[size];
        for (int j = 0; j < size; j++)
            arr[j] = rand() % 1000;
        comps = 0;
        quickSort(arr, 0, size);
        outputFile << "\n" << size << "," << comps;</pre>
   outputFile.close(); // Close the file
   cout << endl;</pre>
   return 0;
```

Output 3:





Question 4:

Implement Radix Sort

Solution 4:

```
#include <iostream>
using namespace std;
// Get maximum value from array.
int getMax(int arr[], int n)
   int max = arr[0];
   for (int i = 1; i < n; i++)
        if (arr[i] > max)
            max = arr[i];
   return max;
// Count sort of arr[].
void countSort(int arr[], int n, int exp)
    // Count[i] array will be counting the number of array values having
that 'i' digit at their (exp) th place.
   int output[n], i, count[10] = {0};
    // Count the number of times each digit occurred at (exp)th place in
every input.
   for (i = 0; i < n; i++)
        count[(arr[i] / exp) % 10]++;
   // Calculating their cumulative count.
   for (i = 1; i < 10; i++)
        count[i] += count[i - 1];
    // Inserting values according to the digit '(arr[i] / exp) % 10'
fetched into count[(arr[i] / exp) % 10].
    for (i = n - 1; i >= 0; i--)
    {
        output[count[(arr[i] / exp) % 10] - 1] = arr[i];
        count[(arr[i] / exp) % 10]--;
    // Assigning the result to the arr pointer of main().
    for (i = 0; i < n; i++)
```

```
arr[i] = output[i];
// Sort arr[] of size n using Radix Sort.
void radixsort(int arr[], int n)
    int exp, m;
    m = getMax(arr, n);
    // Calling countSort() for digit at (exp)th place in every input.
    for (\exp = 1; m / \exp > 0; \exp *= 10)
        countSort(arr, n, exp);
int main()
    cout << endl;</pre>
    int n = 8;
    int arr[] = {170, 45, 75, 90, 802, 24, 2, 66};
    cout << "Original Data : " << endl;</pre>
    for (int i = 0; i < n; i++)
        cout << arr[i] << " ";</pre>
    cout << endl;</pre>
    radixsort(arr, n);
    // Printing the sorted data.
    cout << "Sorted Data : " << endl;</pre>
    for (int i = 0; i < n; i++)
        cout << arr[i] << " ";
    cout << endl;</pre>
    return 0;
```

Output 4:

```
Original Data :
170 45 75 90 802 24 2 66
Sorted Data :
2 24 45 66 75 90 170 802
```

Question 5:

Implement Bucket Sort

Solution 5:

```
#include <iostream>
#include <string>
using namespace std;
struct bucket
   int ptr;
   float *value;
void insertionSort(T arr[], int size)
   T key;
    for (i = 0; i < size; ++i)
        key = arr[i];
        while (j \ge 0 \&\& arr[j] > key) {
            arr[j + 1] = arr[j];
        arr[j + 1] = key;
void print(float ar[], int size, string str)
    cout << str << "[";</pre>
    for (int i = 0; i < size; ++i)
        cout << (i == 0 ? "" : ", ") << ar[i];
    cout << "]" << endl;
void bucketSort(float ar[], int n)
    struct bucket B[n];
```

```
for (int i = 0; i < n; i++)
       B[i].ptr = -1;
       B[i].value = new float[n];
    for (int i = 0; i < n; i++)
       int idx = n * ar[i];
        B[idx].value[++B[idx].ptr] = ar[i];
   for (int i = 0; i < n; i++)
        insertionSort<float>(B[i].value, B[i].ptr + 1);
   int idx = 0;
    for (int i = 0; i < n; i++)
        for (int j = 0; j < B[i].ptr + 1; j++)
            ar[idx++] = B[i].value[j];
        delete[] B[i].value; // and free the memory
int main()
   int size = rand() % 15 + 5;
   float *arr = new float[size];
digits after decimal
   for (int j = 0; j < size; j++)
        arr[j] = (float)(rand() % 100) / 100;
   print(arr, size, "\nUnsorted Array = ");
   bucketSort(arr, size);
   print(arr, size, "\nSorted Array = ");
   cout << endl;</pre>
    return 0;
```

Output 5:

```
Unsorted Array = [0.67, 0.34, 0, 0.69, 0.24, 0.78, 0.58, 0.62, 0.64, 0.05, 0.45, 0.81, 0.27, 0.61, 0.91, 0.95]

Sorted Array = [0, 0.05, 0.24, 0.27, 0.34, 0.45, 0.58, 0.61, 0.62, 0.64, 0.67, 0.69, 0.78, 0.81, 0.91, 0.95]
```

Question 6:

Implement Randomized Select

Solution 6:

```
#include <iostream>
using namespace std;
int Partition(int A[], int p, int r) {
   int i = p - 1;
    for (int j = p; j < r; j++) {
        if (A[j] \le A[r]) {
            i++;
            swap(A[i], A[j]);
   swap(A[i + 1], A[r]);
   return i + 1;
int RandomizedPartition(int A[], int p, int r) {
   int i = p + rand() % (r - p + 1);
   swap(A[r], A[i]);
   return Partition(A, p, r);
int RandomizedSelect(int A[], int p, int r, int i) {
   if (p == r) {
        return A[p];
   int q = RandomizedPartition(A, p, r);
    int k = q - p + 1;
```

```
if (i == k) {
    return A[q];
} else if (i < k) {
    return RandomizedSelect(A, p, q - 1, i);
} else {
    return RandomizedSelect(A, q + 1, r, i - k);
}

int main() {
    int A[] = { 3, 5, 2, 7, 6, 1, 4 };
    int n = sizeof(A) / sizeof(A[0]);
    int i = 3;
    int order_statistic = RandomizedSelect(A, 0, n - 1, i);
    cout << "The " << i << "th order statistic is: " << order_statistic
<< endl;
    return 0;
}</pre>
```

Output 6:

```
The 3th order statistic is: 3
```

Question 7:

Implement Breadth-First Search in a graph

Solution 7:

```
# Created By : DEVANSH SHARMA
#include <bits/stdc++.h>
using namespace std;
   int V;
    vector<list<int> > adj;
public:
   Graph(int V);
   void addEdge(int v, int w);
   void BFS(int s);
};
Graph::Graph(int V)
    this->V = V;
    adj.resize(V);
void Graph::addEdge(int v, int w)
    adj[v].push back(w);
void Graph::BFS(int s)
    vector<bool> visited;
    visited.resize(V, false);
    list<int> queue;
    visited[s] = true;
    queue.push back(s);
```

```
while (!queue.empty()) {
       s = queue.front();
       cout << s << " ";
       queue.pop front();
       for (auto adjacent : adj[s]) {
           if (!visited[adjacent]) {
               visited[adjacent] = true;
               queue.push back(adjacent);
int main()
   cout<<endl;cout<<endl;</pre>
   Graph g(4);
   g.addEdge(0, 1);
   g.addEdge(0, 2);
   g.addEdge(1, 2);
   g.addEdge(2, 0);
   g.addEdge(2, 3);
   g.addEdge(3, 3);
   cout << "Following is Breadth First Traversal "</pre>
       << "(starting from vertex 2) \n";
   g.BFS(2);
   cout<<endl;cout<<endl;</pre>
   return 0;
```

Output 7:

```
Following is Breadth First Traversal (starting from vertex 2) 2 0 3 1
```

Question 8:

Implement Depth-First Search in a graph

Solution 8:

```
# Created By : DEVANSH SHARMA
#include <bits/stdc++.h>
using namespace std;
   map<int, bool> visited;
   map<int, list<int> > adj;
   void addEdge(int v, int w);
    void DFS(int v);
};
void Graph::addEdge(int v, int w)
    adj[v].push back(w); // Add w to v's list.
void Graph::DFS(int v)
    visited[v] = true;
    cout << v << " ";
    list<int>::iterator i;
    for (i = adj[v].begin(); i != adj[v].end(); ++i)
        if (!visited[*i])
            DFS(*i);
int main()
```

Output 8:

```
Following is Depth First Traversal (starting from vertex 2) 2 0 1 3
```

Question 9:

Write a program to determine the minimum spanning tree of a graph using both Prims and Kruskal's algorithm

Solution 9.A: Kruskal Algorithm

```
# Created By : DEVANSH SHARMA
#include <algorithm>
#include <vector>
#include <vector>
using namespace std;

#define edge pair<int, int>

class Graph {
   private:
   vector<pair<int, edge> > G; // graph
   vector<pair<int, edge> > T; // mst
   int *parent;
   int V; // number of vertices/nodes in graph
   public:
```

```
Graph(int V);
 void AddWeightedEdge(int u, int v, int w);
 int find set(int i);
 void union set(int u, int v);
 void kruskal();
 void print();
Graph::Graph(int V) {
 parent = new int[V];
 for (int i = 0; i < V; i++)
   parent[i] = i;
 G.clear();
 T.clear();
void Graph::AddWeightedEdge(int u, int v, int w) {
 G.push back(make pair(w, edge(u, v)));
int Graph::find set(int i) {
 if (i == parent[i])
   return i;
 else
   return find set(parent[i]);
void Graph::union set(int u, int v) {
 parent[u] = parent[v];
void Graph::kruskal() {
 int i, uRep, vRep;
 sort(G.begin(), G.end()); // increasing weight
 for (i = 0; i < G.size(); i++) {
   uRep = find set(G[i].second.first);
   vRep = find set(G[i].second.second);
   if (uRep != vRep) {
     T.push back(G[i]); // add to tree
```

```
union set(uRep, vRep);
void Graph::print() {
 cout << "Edge\t:"</pre>
     << " Weight" << endl;
 for (int i = 0; i < T.size(); i++) {
    cout << T[i].second.first << " - " << T[i].second.second << "\t: "</pre>
       << T[i].first;
   cout << endl;</pre>
int main() {
 Graph q(6);
 g.AddWeightedEdge(0, 1, 4);
 g.AddWeightedEdge(0, 2, 4);
 g.AddWeightedEdge(1, 2, 2);
 g.AddWeightedEdge(1, 0, 4);
 g.AddWeightedEdge(2, 0, 4);
 g.AddWeightedEdge(2, 1, 2);
 g.AddWeightedEdge(2, 3, 3);
 g.AddWeightedEdge(2, 5, 2);
 g.AddWeightedEdge(2, 4, 4);
 g.AddWeightedEdge(3, 2, 3);
 g.AddWeightedEdge(3, 4, 3);
 g.AddWeightedEdge(4, 2, 4);
 g.AddWeightedEdge(4, 3, 3);
 g.AddWeightedEdge(5, 2, 2);
 g.AddWeightedEdge(5, 4, 3);
 g.kruskal();
 g.print();
 return 0;
```

Output 9.A:

```
Edge : Weight
1 - 2 : 2
2 - 5 : 2
2 - 3 : 3
3 - 4 : 3
0 - 1 : 4
```

Solution 9.B: Prims Algorithm

```
#include <bits/stdc++.h>
using namespace std;
#define V 5
int minKey(int key[], bool mstSet[])
    for (int v = 0; v < V; v++)
        if (mstSet[v] == false && key[v] < min)</pre>
            min = key[v], min index = v;
    return min index;
void printMST(int parent[], int graph[V][V])
    cout << "Edge \tWeight\n";</pre>
        cout << parent[i] << " - " << i << " \t" << graph[i] [parent[i]]</pre>
void primMST(int graph[V][V])
    int parent[V];
    int key[V];
    bool mstSet[V];
    for (int i = 0; i < V; i++)
        key[i] = INT MAX, mstSet[i] = false;
    key[0] = 0;
    parent[0] = -1;
    for (int count = 0; count < V - 1; count++)
        int u = minKey(key, mstSet);
        mstSet[u] = true;
            if (graph[u][v] && mstSet[v] == false && graph[u][v] <</pre>
key[v])
                parent[v] = u, key[v] = graph[u][v];
```

Output 9.B:

```
Edge Weight
0 - 1 9
3 - 2 51
1 - 3 19
3 - 4 31
```

Question 10:

Write a program to solve the weighted interval scheduling problem

Solution 10:

```
# Created By : DEVANSH SHARMA
#include <iostream>
#include <algorithm>
using namespace std;

// A job has start time, finish time and profit.
struct Job
{
   int start, finish, profit;
};

// A utility function that is used for sorting events
// according to finish time
bool jobComparator(Job s1, Job s2)
{
   return (s1.finish < s2.finish);</pre>
```

```
int latestNonConflict(Job arr[], int i)
    for (int j=i-1; j>=0; j--)
        if (arr[j].finish <= arr[i-1].start)</pre>
            return j;
    return -1;
int findMaxProfitRec(Job arr[], int n)
    if (n == 1) return arr[n-1].profit;
    int inclProf = arr[n-1].profit;
    int i = latestNonConflict(arr, n);
    if (i != -1)
    inclProf += findMaxProfitRec(arr, i+1);
    int exclProf = findMaxProfitRec(arr, n-1);
    return max(inclProf, exclProf);
int findMaxProfit(Job arr[], int n)
    sort(arr, arr+n, jobComparator);
    return findMaxProfitRec(arr, n);
```

```
}
// Driver program
int main()
{
    cout<<endl;cout<<endl;
    Job arr[] = {{3, 10, 20}, {1, 2, 50}, {6, 19, 100}, {2, 100, 200}};
    int n = sizeof(arr)/sizeof(arr[0]);
    cout << "The optimal profit is " << findMaxProfit(arr, n);
    cout<<endl;cout<<endl;cout<<endl;
    return 0;
}</pre>
```

Output 10:

```
The optimal profit is 250
```

Question 11:

Write a program to solve the 0-1 knapsack problem

Solution 11:

```
# Created By : DEVANSH SHARMA
#include <bits/stdc++.h>
using namespace std;
int max(int a, int b) { return (a > b) ? a : b; }

// Returns the maximum value that

// can be put in a knapsack of capacity W
int knapSack(int W, int wt[], int val[], int n)

{
    // Base Case
    if (n == 0 || W == 0)
        return 0;

// If weight of the nth item is more

// than Knapsack capacity W, then

// this item cannot be included

// in the optimal solution
if (wt[n - 1] > W)
    return knapSack(W, wt, val, n - 1);
```

Output 11:

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END OF ASSIGNMENT

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