

DEEP NETWORK DEVELOPMENT

Imre Molnár

PhD student, ELTE, AI Department

☑ imremolnar@inf.elte.hu

curiouspercibal.github.io

Tamás Takács

PhD student, ELTE, AI Department

☑ tamastheactual@inf.elte.hu

getlar.github.io



Lecture 2.

Linear Regression & Artificial Neural Networks

Budapest, 17th September 2024

1 Linear Regression

2 Artificial Neural Networks



Previously on Lecture 1

Artificial Intelligence

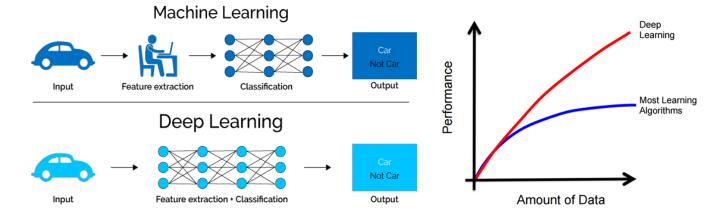
Any technique that enables computers to imitate human behavior.

Machine Learning

Computers capable of learning without explicitly being programmed.

Deep Learning

Computers that learn from data using Deep Neural Networks



Google DeepMind

originally published Nov. 2023; updated Jan. 2024

Levels of AGI: Operationalizing Progress on the Path to AGI

Meredith Ringel Morris¹, Jascha Sohl-dickstein¹, Noah Fiedel¹, Tris Warkentin¹, Allan Dafoe¹, Aleksandra Faust¹, Clement Farabet¹ and Shane Legg¹ 1Google Despirind

We propose a framework for classifying the capabilities and behavior of Artificial General Intelligence (AGI) models and their precursors. This framework introduces levels of AGI performance, generality, and autonomy. It is our hope that this framework will be useful in an analogous way to the levels of autonomous driving, by providing a common language to compare models, assess risks, and measure progress along the path to AGI. To develop our framework, we analyze existing definitions of AGI, and distill six principles that a useful ontology for AGI should satisfy. These principles include focusing on capabilities rather than mechanisms; separately evaluating generality and performance; and defining stages along the path toward AGI, rather than focusing on the endpoint. With these principles in mind, we propose "Levels of AGI" based on depth (performance) and breadth (generality) of capabilities, and reflect on how current systems fit into this ontology. We discuss the challenging requirements for future benchmarks that quantify the behavior and capabilities of AGI models against these levels. Finally, we discuss how these levels of AGI interact with deployment considerations such as autonomy and risk, and emphasize the importance of carefully selecting Human-AI Interaction paradigms for responsible and safe deployment of highly capable AI systems.

Keywords: Al, AGI, Artificial General Intelligence, General AI, Human-Level AI, HLAI, ASI, frontier models, benchmarking, metrics, AI safety, AI risk, autonomous systems, Human-AI Interaction

Futuristic Skeptical

Political Enterprise

[cs.AI]

2v2

Deep Network Development



Lecture 2.

Linear Regression

Budapest, 17th September 2024

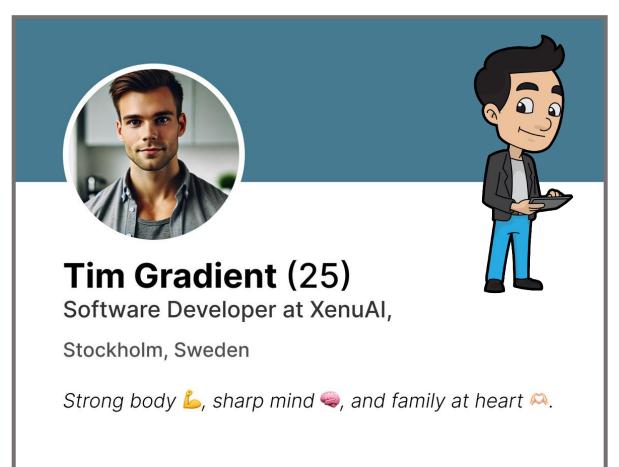
1 Linear Regression

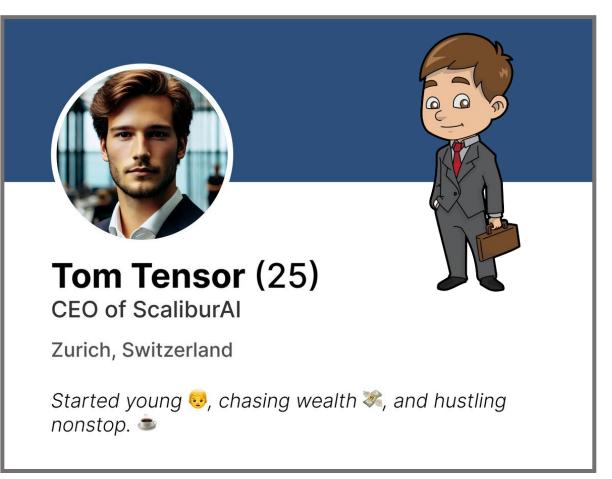
2 Artificial Neural Networks



Meet Tim and Tom

Once childhood friends, but now on different life paths







One day they met and...

Tim was mad at Tom for not spending time with him anymore.

Tim, emotionally said: "You're probably going to end up dead alone..."

"No way! I am healthier than you!"



Tom was mad at Tim for living in his comfort zone and not use his full potential.

Tom, emotionally replied: "But you will die first..."

"No way! I am wealthier than you!"

... and that is when they had an idea ...



Meet Tim and Tom







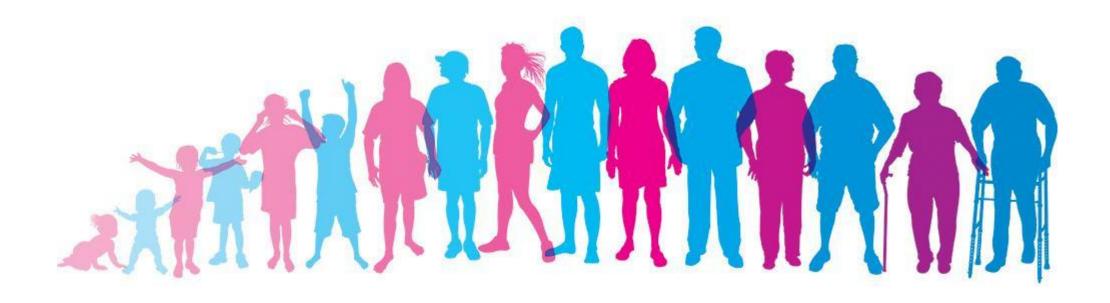
TO USE ARTIFICIAL INTELLIGENCE TO PREDICT THEIR LIFE EXPECTANCY!

1. Linear Regression



Collect a dataset

- Life Expectancy (WHO) Dataset
- Statistical Analysis on factors influencing Life Expectancy across different countries
- https://www.kaggle.com/kumarajarshi/life-expectancy-who



1. Linear Regression



Exploring the dataset

- Dataset has 2938 data points, each having 20 factors influencing Life Expectancy, the country name and the actual Life Expectancy value
- Adult Mortality Adult Mortality Rates of both sexes, probability of dying between 15 and 60 years per 1000 population;
- BMI Average Body Mass Index of entire population;
- GDP Gross Domestic Product per capita (in USD);

<class 'pandas.core.frame.DataFrame'> RangeIndex: 2938 entries, 0 to 2937 Data columns (total 22 columns): Non-Null Count Dtype Column Country object 2938 non-null Year 2938 non-null int64 Status 2938 non-null object 2928 non-null Life expectancy float64 Adult Mortality 2928 non-null float64 infant deaths 2938 non-null int64 Alcohol 2744 non-null float64 percentage expenditure 2938 non-null float64 Hepatitis B 2385 non-null float64 Measles 2938 non-null int64 BMT 2904 non-null float64 under-five deaths 2938 non-null int64 Polio 2919 non-null float64 Total expenditure 2712 non-null float64 Diphtheria 2919 non-null float64 HIV/AIDS 2938 non-null float64 **GDP** 2490 non-null float64 16 Population 2286 non-null float64 thinness 1-19 years float64 2904 non-null thinness 5-9 years 2904 non-null float64 Income composition of resources 2771 non-null float64 Schooling 2775 non-null float64 dtypes: float64(16), int64(4), object(2)

memory usage: 505.1+ KB

Deep Network Development



Exploring the dataset

Country	Year	Status	Life expectancy	Adult Mortality	Infant Deaths	Alcohol	Percentage Expenditure	Hepatitis B	Measles	вмі
Hungary	2014	Developed	75.6	137	0	0.01	160.9449		0	64.2

Under-five Deaths	Polio	Total expenditure	Diphtheria	HIV/AIDS	GDP	Population		Thinness 5- 9 years	Income composition of resources	Schooling
0	99	7.4	99	0.1	14117.98	9866468	1.7	1.6	0.834	15.8

ELTE EÖTVÖS LORÁND UNIVERSITY

Feature Selection

Tim chose BMI (independent variable) for predicting Life expectancy (dependent variable)

X = BMI

Y = Life Expectancy





Tom chose GDP (independent variable) for predicting Life expectancy (dependent variable)

X = GDP Y = Life Expectancy



Supervised Learning: Linear Regression

Life Expectancy function

$$f(x) = y$$

- Have: (x, y)
 - \circ x data
 - \circ y label
- Goal: Learn a function to map

- Regression Predict real valued / continuous output: $y \in \mathbb{R}$
 - What is the height of person B?
 - What is going to be the price of a share tomorrow?
 - How many cars are in a city?
 - What is the life expectancy of person A?



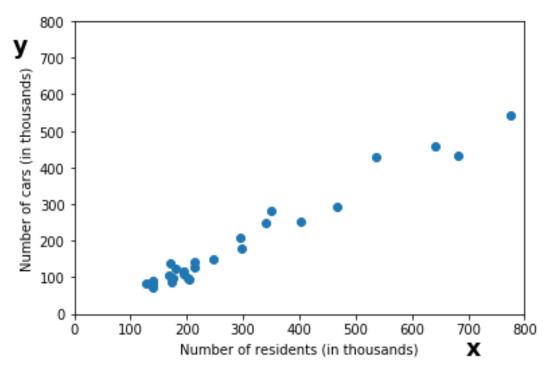


Example

How many cars are in a city?

- **x** (input) number of residents
- **y** (output) number of cars

Cars and residents (Poland 2017)





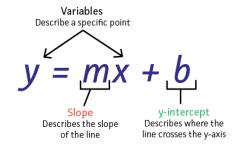
Example

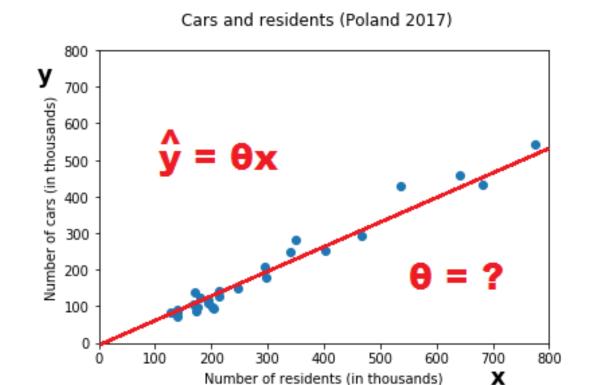
x – (input) number of residents

y – (output) number of cars

Seems to have a linear relationship (we try to fit a line):

$$\hat{y} = heta_0 + heta_1 x = heta x$$







Supervised Learning: Linear Regression

x – (input) number of residents

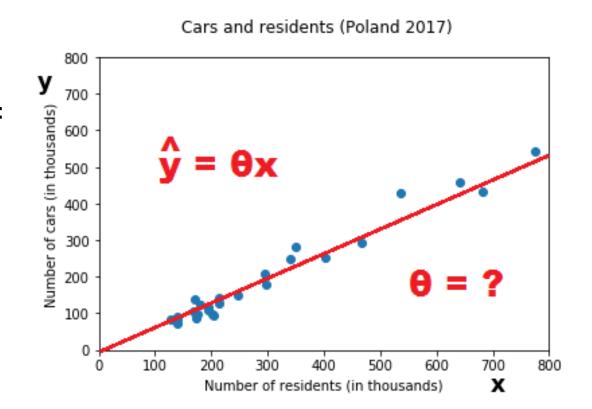
y – (output) number of cars

Seems to have a linear relationship. We want to find a function:

$$h\left(x\right)=\hat{y}=\theta_{0}+\theta_{1}x=\theta x$$
 To select best, that minimize the loss:
 θ

$$J\left(heta
ight) = rac{1}{n} \sum_{i=1}^{n} \left(\hat{y}^{(i)} - y^{(i)}
ight)^{2}$$

$$J\left(heta
ight) = rac{1}{n} \sum_{i=1}^{n} \left(heta x^{(i)} - y^{(i)}
ight)^2$$



Vectorization

Say we have 200 data points:

$$x = egin{bmatrix} 1 & x^{(1)} \ 1 & x^{(2)} \ \dots & \dots \ 1 & x^{(200)} \end{bmatrix}, y = egin{bmatrix} y^{(1)} \ y^{(2)} \ \dots \ y^{(200)} \end{bmatrix}$$

We want to find

$$egin{aligned} oldsymbol{ heta}_{(2,1)} &= egin{bmatrix} oldsymbol{ heta}_0 \ oldsymbol{ heta}_1 \end{bmatrix} \end{aligned}$$

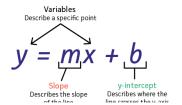
$$egin{aligned} heta &= egin{bmatrix} heta_0 &= egin{bmatrix} heta_0 &= egin{bmatrix} 1 \cdot heta_0 + x^{(1)} heta_1 \ 1 \cdot heta_0 + x^{(2)} heta_1 \ & \ldots \ 1 \cdot heta_0 + x^{(200)} heta_1 \end{bmatrix} \end{aligned}$$

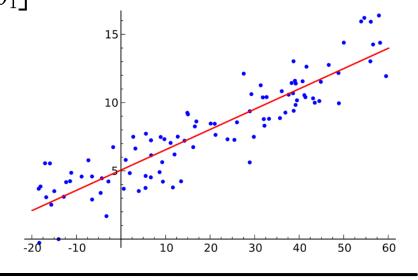
That minimizes loss:

$$J\left(heta
ight) = rac{1}{n}\sum_{i=1}^{n}\left(\hat{y}^{(i)}-y^{(i)}
ight)^2 = rac{1}{n}\sum_{i=1}^{n}\left(heta_1x^{(i)}+ heta_0-y^{(i)}
ight)^2$$

(vectorized form):

$$J(heta) = (\hat{Y} - Y)^T(\hat{Y} - Y) = (heta X - Y)^T(heta X - Y)$$







Supervised Learning: Linear Regression

The problem can be summarized:

$$heta^* = \operatorname*{argmin}_{ heta} J(heta)$$

Find the optimal θ^* that minimizes the loss (in this case the Mean Squared Error):

$$J\left(heta^{*}
ight)=rac{1}{n}\sum_{i=1}^{n}\left(heta^{*}x^{\left(i
ight)}-y^{\left(i
ight)}
ight)^{2}$$

How to find optimal θ^* ?

- Analytical solution: Normal equation
- Numerical solution: Gradient Descent

1. Linear Regression



Analytical solution: Normal Equation

Say we have 200 data points:

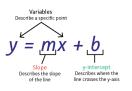
$$x = egin{bmatrix} 1 & x^{(1)} \ 1 & x^{(2)} \ \cdots & \cdots \ 1 & x^{(200)} \end{bmatrix}$$

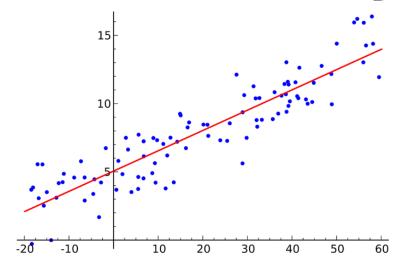
$$heta = [heta_0, heta_1]^T$$

$$\mathbf{y} = [y^{(1)}, y^{(2)}, \dots, y^{(200)}]^T$$

$$\hat{\mathbf{y}} = X\theta$$

$$J(\theta) = (\theta X - Y)^T (\theta X - Y)$$





Normal Equation [1]:
$$heta^* = (X^TX)^{-1}(X^TY)$$

 $heta^*$ is the optimal parameter that minimizes the loss function J(heta)

[1] Normal equation derivation (different): https://eli.thegreenplace.net/2014/derivation-of-the-normal-equation-for-linear-regression/

ELTE EÖTVÖS LORÁND UNIVERSITY

Feature selection (recap)

Tim chose BMI (independent variable) for predicting Life expectancy (dependent variable)

X = BMI Y = Life Expectancy



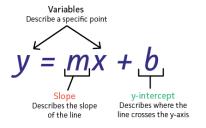


Tom chose GDP (independent variable) for predicting Life expectancy (dependent variable)

X = GDP Y = Life Expectancy

ELTE EÓTVŐS LORÁND Life expectancy vs BMI

Analytical solution: Normal Equation (Tim)



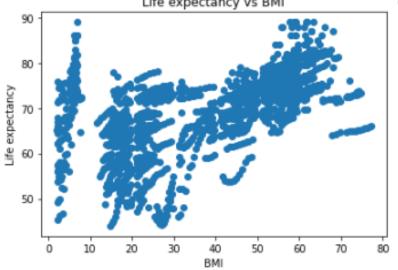
$$\theta^* = (X^TX)^{-1}(X^TY)$$

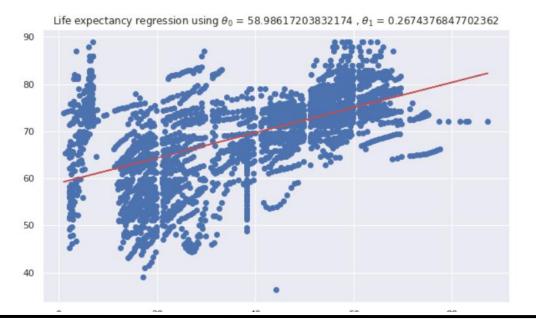
```
def normal_equation(X,Y):
    return np.linalg.inv(X.T @ X) @ (X.T @ Y)

tim_theta = normal_equation(tim_data_ready, Y)
print(f'y = mx + b')
print(f'y = {tim_theta[1]}x + {tim_theta[0]}')
```



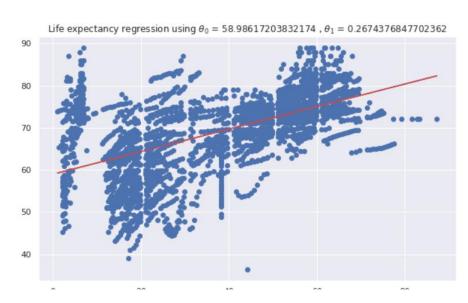
```
y = mx + b \ y = 0.26743768477023727x + 58.98617203832164
```







Analytical solution: Normal Equation (Tim)





```
def life_expectancy(X, theta):
    X = np.concatenate((np.ones(1),np.array(X)),axis=0)
    return round(np.dot(X, theta),1)

height = 1.82 #float(input("Please input your height (in meters): ")) #1.82
weight = 80 #float(input("Please input your weight (in kilograms): ")) #80
bmi = weight / height**2
print("BMI:",bmi)
life_exp_tim = life_expectancy([bmi], tim_theta)
print("Tim's life expectancy is", life_exp_tim , "years.")
```

BMI: 24.151672503320853

Tim's life expectancy is 65.4 years.

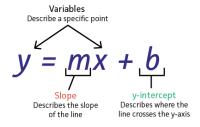
```
height = 1.80 #float(input("Please input your height (in meters): ")) #1.82
weight = 73 #float(input("Please input your weight (in kilograms): ")) #80
bmi = weight / height**2
print("BMI:",bmi)
life_exp_tim_tom = life_expectancy([bmi], tim_theta)
print("Tom's life expectancy predicted by Tim's model is", life_exp_tim_tom , "years.")
```

BMI: 22.530864197530864

Tom's life expectancy is 65.0 years.



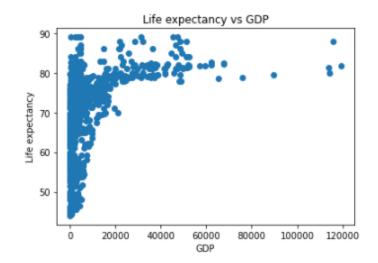
Analytical solution: Normal Equation (Tom)

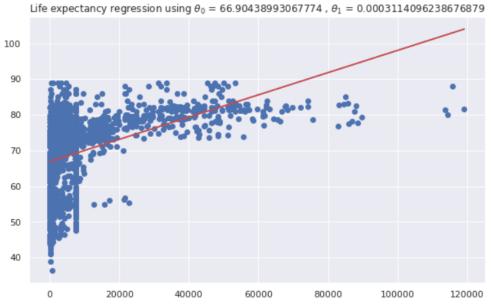


```
tom_theta = normal_equation(tom_data_ready, Y)
print(f'y = mx + b')
print(f'y = {tom_theta[1]}x + {tom_theta[0]}')
```

```
y = mx + b \ y = 0.0003114096238676778x + 66.90438993067785
```



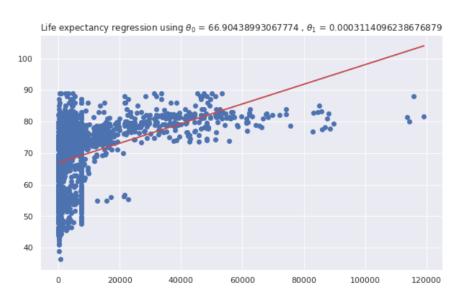




1. Linear Regression



Analytical solution: Normal Equation (Tom)





```
def life_expectancy(X, theta):
    X = np.concatenate((np.ones(1),np.array(X)),axis=0)
    return round(np.dot(X, theta),1)

gdp = 8500 #float(input("Please input the GDP of your country: ")) #8500
life_exp_tom = life_expectancy([gdp], tom_theta)
```

Tom's life expectancy is 69.6 years.

```
gdp = 5000 #float(input("Please input the GDP of your country: ")) #5000
life_exp_tom_tim = life_expectancy([gdp], tom_theta)
print("Tim's life expectancy predicted by Tom is", life_exp_tom_tim , "years.")
```

Tim's life expectancy predicted by Tom is 68.5 years.



Results

Tim's Life Expectancy predictions:

- Tim 65.4 years
- Tom -65 years

Tom's Life Expectancy predictions:

- Tim -68.5 years
- Tom 69.6 years



NO AGREEMENT!!

- Metrics?
- Further explore dataset?
- Better feature selection?

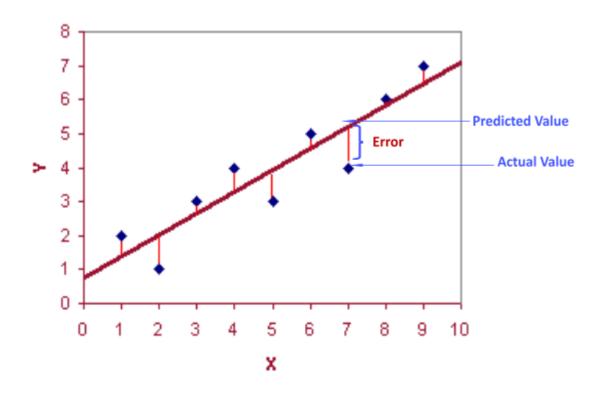


NO! Mine is better! I'll live longer!

My model is better! I'll live longer!



Metrics (Loss): Root Mean Squared Error



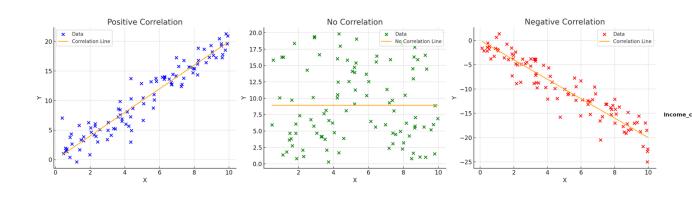
$$RMSE = \sqrt{rac{1}{n}\sum_{i=1}^{n}\left(\hat{y}_i - y_i
ight)^2}$$

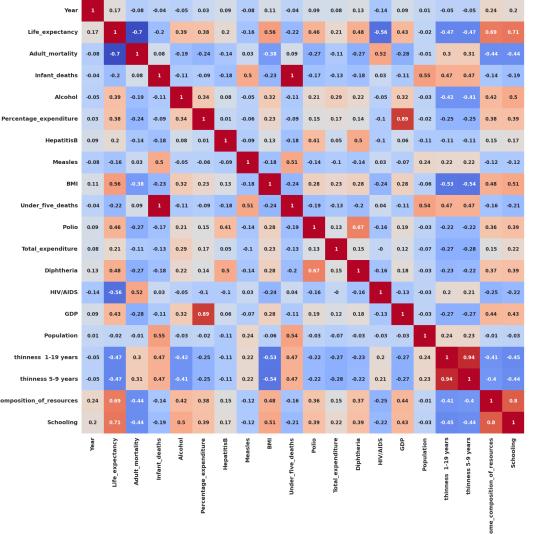


Exploring the dataset part 2

Correlation matrix

 What is the relationship between the different features and the Life expectancy?



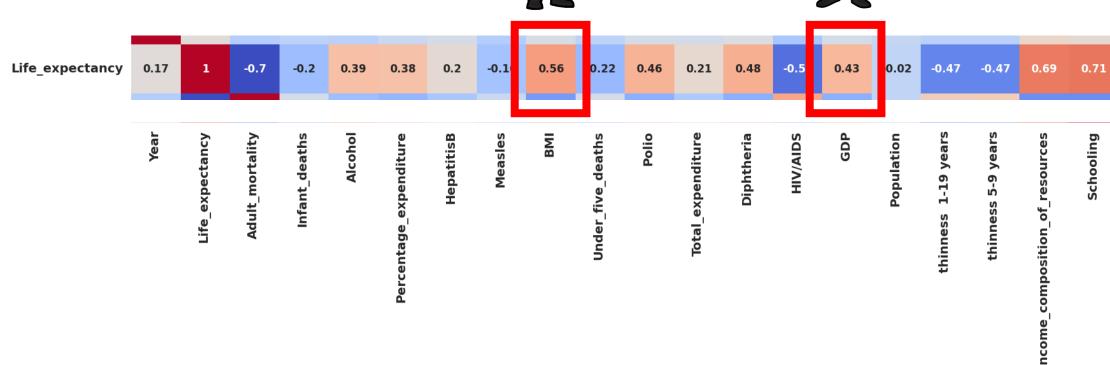


ELTE EÖTVÖS LORÁND UNIVERSITY

Exploring the dataset part 2





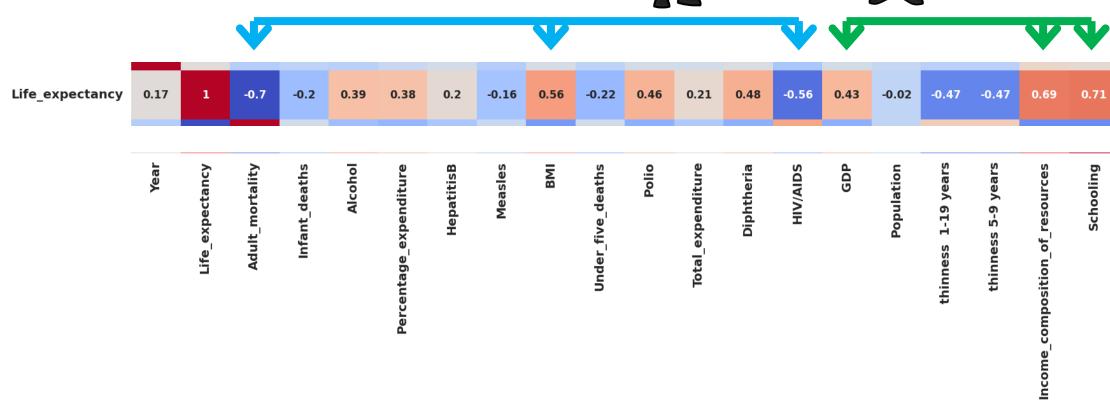


Exploring the dataset part 2









ELTE EÖTVŐS LORÁND UNIVERSITY

Exploring the dataset part 2

Tim chose BMI, Adult Mortality and HIV/AIDS (independent variables) for predicting Life expectancy (dependent variable)

X = BMI, Adult Mortality, HIV/AIDS Y = Life Expectancy





Tom chose GDP, Income composition of resources and Schooling (independent variables) for predicting Life expectancy (dependent variable)

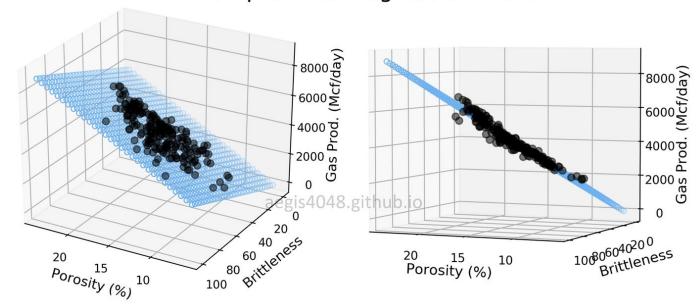
X = GDP, Income comp. resources, Schooling Y = Life Expectancy



Multiple Linear Regression

- How many cars are in a city?
- x1 (input) number of residents (in thousands)
- x2 (input) distance to capital (in km)
- y (output) number of cars
- We can add more... x3,...,xn

3D multiple linear regression model





Multiple Linear Regression (Vectorization)

- Similar (only dimensions change)
- Generalizable

$$X_{(m,n)} = egin{bmatrix} 1 & x_1^{(1)} & \dots & x_n^{(1)} \ 1 & x_1^{(2)} & \dots & x_n^{(2)} \ \dots & \dots & \dots & \dots \ 1 & x_1^{(m)} & \dots & x_n^{(m)} \end{bmatrix} egin{bmatrix} heta & = & egin{bmatrix} heta_0 \ heta_1 \ \dots \ heta_n \end{bmatrix} y & = & egin{bmatrix} y^{(1)} \ y^{(2)} \ \dots \ y^{(m)} \end{bmatrix}$$

$$y=X hinspace W = (m,n)(n,1)$$



Multiple Linear Regression: Normal equation (Tim)

```
tim_theta = normal_equation(tim_data_ready, Y)
print(f'theta = {tim_theta}')
theta = [ 6.95250308e+01    1.58686254e-01 -3.38199840e-02 -4.58041192e-01]
```

$$RMSE = \sqrt{rac{1}{n}\sum_{i=1}^{n}\left(\hat{y}_i - y_i
ight)^2}$$



```
def RMSE(y_pred, y):
    return np.sqrt(metrics.mean_squared_error(y, y_pred))

tim_y_pred = np.dot(tim_data_ready, tim_theta)
tim_rmse = RMSE(tim_y_pred, Y)

print("Tim's RMSE: ", tim_rmse)

Tim's RMSE: 5.784750918898876
```



Multiple Linear Regression: Normal equation (Tim)



```
height = 1.82 #float(input("Please input your height (in meters): "))
weight = 80 #float(input("Please input your weight (in kilograms): "))
bmi = weight / height**2
print("BMI:",bmi)
adult mortality = 53
hiv = 0.1
life_exp_tim = life_expectancy([bmi,adult_mortality,hiv], tim_theta)
print("Tim's life expectancy is", life exp tim , "years.")
BMI: 24.151672503320853
Tim's life expectancy is 71.5 years.
height = 1.80 #float(input("Please input your height (in meters): "))
weight = 73 #float(input("Please input your weight (in kilograms): "))
bmi = weight / height**2
print("BMI:",bmi)
adult mortality = 70
hiv = 0.1
life exp tim tom = life expectancy([bmi,adult mortality,hiv], tim theta)
print("Tom's life expectancy predicted by Tim is", life_exp_tim_tom , "years.")
BMT: 22.530864197530864
Tom's life expectancy predicted by Tim is 70.7 years.
```



Multiple Linear Regression: Normal Equation (Tom)

```
tom_theta = normal_equation(tom_data_ready, Y)
print(f'theta = {tom_theta}')
theta = [4.49681347e+01 8.26882411e-05 1.42744076e+01 1.22489350e+00]
```

$$RMSE = \sqrt{rac{1}{n}\sum_{i=1}^{n}\left(\hat{y}_i - y_i
ight)^2}$$



```
def RMSE(y_pred, y):
    return np.sqrt(metrics.mean_squared_error(y, y_pred))

tom_y_pred = np.dot(tom_data_ready, tom_theta)
tom_rmse = RMSE(tom_y_pred, Y)

print("Tom's RMSE: ", tom_rmse)

Tom's RMSE: 6.288890108092894
```



Multiple Linear Regression: Normal equation (Tom)



```
gdp = 8500
income = 0.8
school = 16.5
life_exp_tom = life_expectancy([gdp,income,school], tom_theta)
print("Tom's life expectancy is", life exp tom , "years.")
Tom's life expectancy is 77.3 years.
gdp = 5000
income = 0.77
school = 15.5
life exp tom tim = life expectancy([gdp,income,school], tom theta)
print("Tim's life expectancy predicted by Tom is", life exp tom tim , "years.")
Tim's life expectancy predicted by Tom is 75.4 years.
```

ELTE EČTIVOS LORÁND UNIVERSITY

Results part 2



Tim's Life Expectancy predictions:

- Tim -71.5 years
- Tom -70.7 years

im's RMSE: 5.79



Tom's Life Expectancy predictions:

- Tom -77.3 years
- Tim -75.4 years

Tim's RMSE: 6.29



ELTE EČTVÖS LORÁND UNIVERSITY

Next steps...



- Normalization? Standardization?
- Gradient Descent?
- Artificial Neural Networks?



Tim vs Tom to be continued...

ELTE EÖTVÖS LORÁND UNIVERSITY

Normalization vs Standardization

Normalization

Consider a dataset containing two features:

- Age
- Income

The range of age can go from 0-100 years old, whereas the range of income can go from 0-1,000,000 HUF

If we would do linear regression, income would have the highest influence because of its large values.

$$z_i = rac{x_i - \min(x)}{\max(x) - \min(x)}$$



https://towardsai.net/p/data-science/how-when-and-why-should-you-normalize-standardize-rescale-your-data-3f083def38ff

ELTE EÔTYÔS LORÁND UNIVERSITY

Normalization vs Standardization

Standardization

Consider a dataset containing two features:

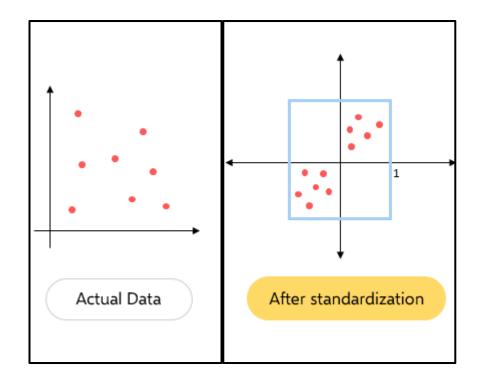
- Weight (Kg)
- Height (cm)

The range might be similar, but the meaning is different. For example, 100 Kg is different than 100 cm.

Most importantly, the deviation and the mean are different for both attributes.

For instance, it is more common to have people with a mean of 80 Kg and a few people with 100 or 200 Kg, than having people with a mean of 80 cm tall (the majority will have more 160 cm).

$$z=rac{x-ar{x}}{\sigma}$$



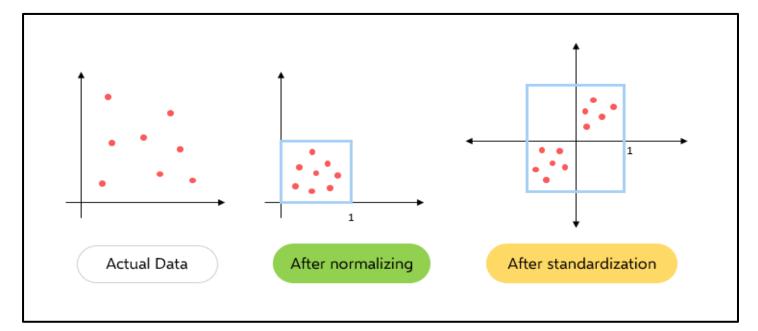
https://towardsai.net/p/data-science/how-when-and-why-should-you-normalize-standardize-rescale-your-data-3f083def38ff



Normalization vs Standardization

Normalization is recommended when your data has varying scales. Standardization is recommended when your data has different units.

$$z_i = rac{x_i - \min(x)}{\max(x) - \min(x)} \qquad \qquad z = rac{x - ar{x}}{\sigma}$$



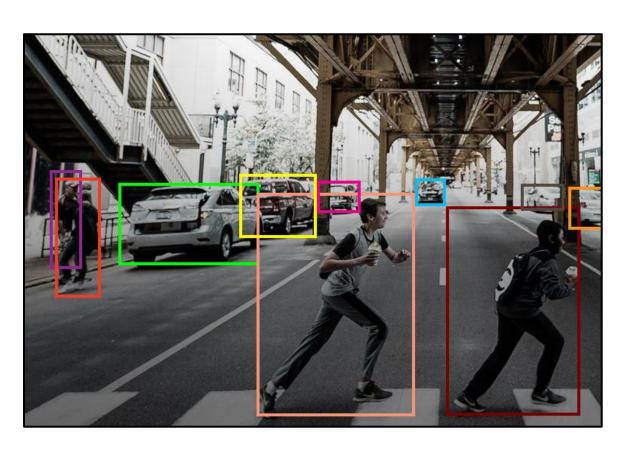
Normalisation	Standardisation
Scaling is done by the highest and the lowest values.	Scaling is done by mean and standard deviation.
It is applied when the features are of separate scales.	It is applied when we verify zero mean and unit standard deviation.
Scales range from 0 to 1	Not bounded
Arrected by outliers	Less directed by Outliers
is applied when we are not sure about	It is used when the data is Gaussian or
The data distribution	Hormany distributed
It is also known as Scaling Normalization	It is also known as Z-Score

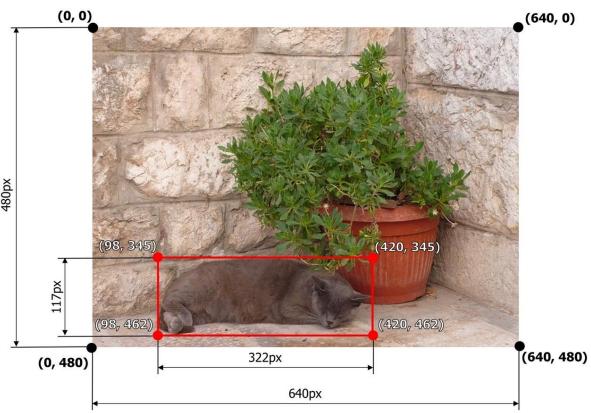
https://towardsai.net/p/data-science/how-when-and-why-should-you-normalize-standardize-rescale-your-data-3f083def38ff



Applications

Object Detection (Bounding Box Regression)







Lecture 2.

Artificial Neural Networks

Budapest, 17th September 2024

1 Linear Regression

2 Artificial Neural Networks

2. Artificial Neural Networks



How do ANNs work?

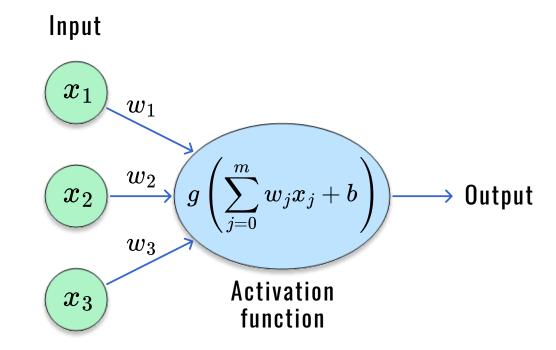
- x the inputs
- **w** weight parameters we will train
- \boldsymbol{b} bias parameter we will train
- \boldsymbol{g} nonlinear activation function

(ReLU, Softmax, ...)

o – the output

One neuron with *m* inputs does the following:

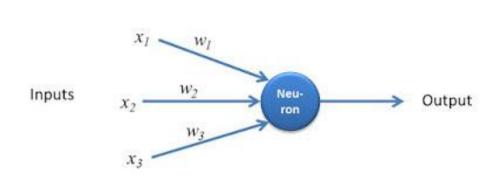
$$o=g\left(\sum_{j=0}^m w_j x_j + b
ight)$$

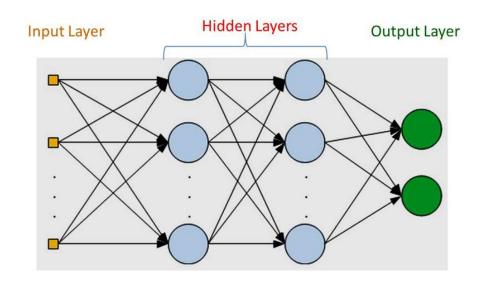




Deep Neural Networks

- Neural networks are built up from neurons, that have inputs and outputs
- Neurons are organised into layers
- Layers refine the output of the previous layers

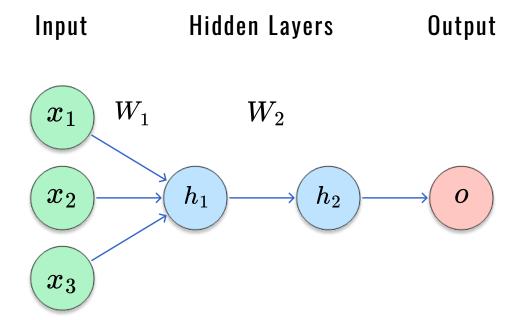






Why do we need nonlinear activation functions?

What happens if we create a deep neural network with 2 hidden layers without an activation function?



(vectorized)

$$egin{aligned} g(x) &= x \ h_1(x) &= g\left(W_1x + b_1
ight) = W_1x + b_1 \ h_2(x) &= g\left(W_2x + b_2
ight) = W_2x + b_2 \end{aligned}$$

$$egin{aligned} o &= h_2(h_1(x)) = h_2(W_1x + b_1) = \ &= W_2(W_1x + b_1) + b_2 = \ &= W_2W_1x + W_2b_1 + b_2 \end{aligned}$$

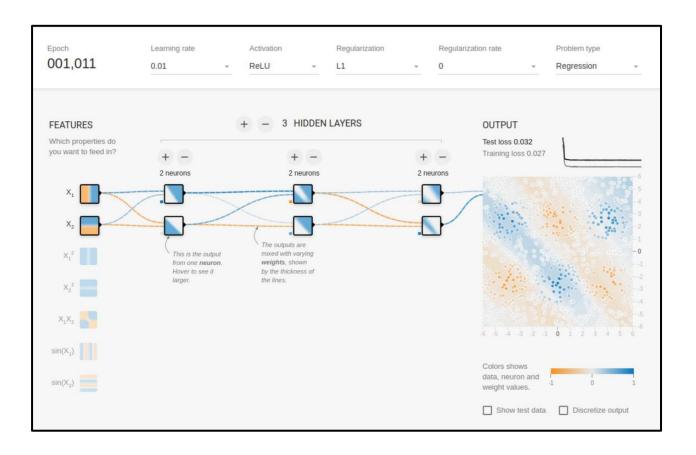
we get a bigger linear regression model



Why do we need nonlinear activation functions?

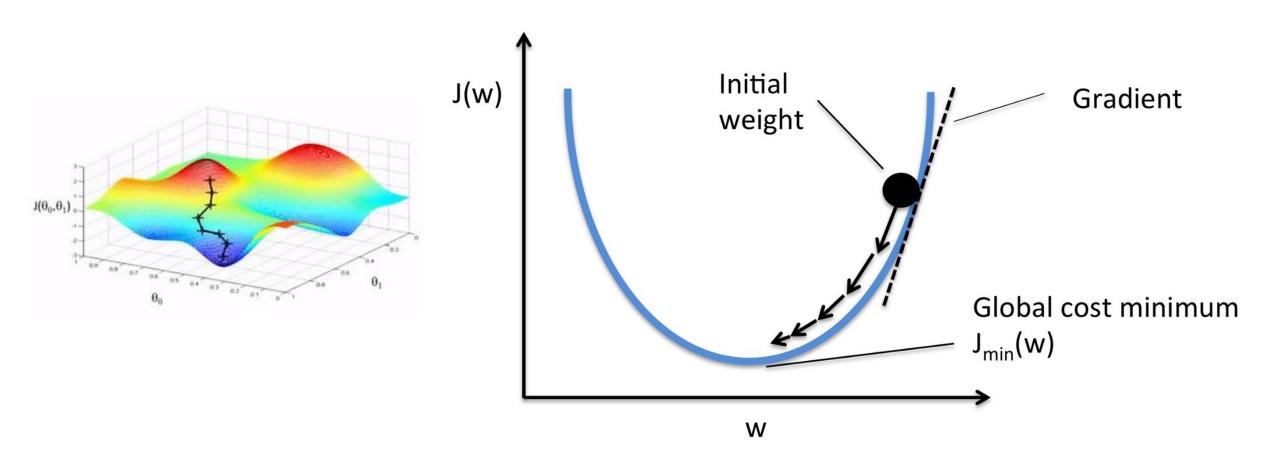
In short it allows the model to learn **complex patterns** and **relationships**

Demo: https://playground.tensorflow.org





Numerical Solution: Gradient Descent



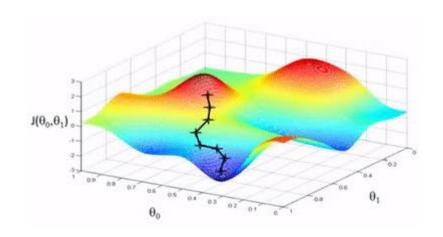
ELTE EÔTYŐS LORÁND UNIVERSITY

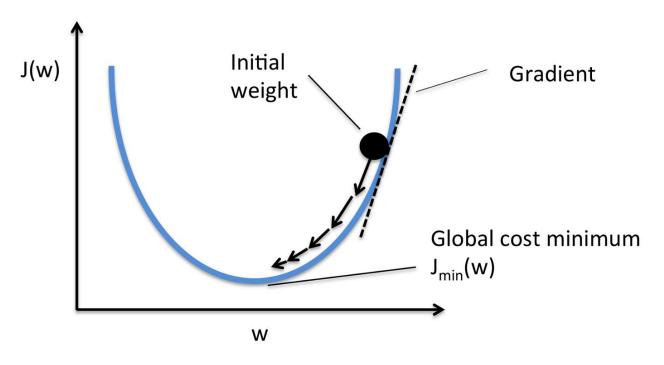
Numerical Solution: Gradient Descent

- 1. Select θ randomly
- 2. Update θ :

$$\theta_t = \theta_{t-1} - \alpha \nabla J(\theta_{t-1})$$

- \circ where $J(\theta)$ is the average error
- 3. Iterate until it converges





$$J(heta) = rac{1}{n} \sum_{i=1}^n ig(\hat{y}_i - y_iig)^2 = rac{1}{n} \sum_{i=1}^n ig(heta_i x_i - y_iig)^2$$

ELTE EÔTVÔS LORÁND UNIVERSITY

Numerical Solution: Gradient Descent

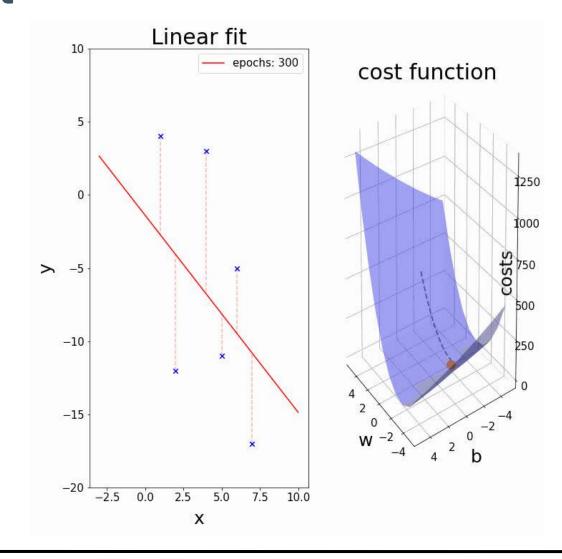
- 1. Select θ randomly
- 2.Calculate \hat{y} for all training examples
- 3. Calculate the gradient of the total loss:

$$abla J(heta_{t-1}) =
abla rac{1}{n} \sum_{i=1}^n L(\hat{y}_i, y_i).$$

4.Update:

$$\theta_t = \theta_{t-1} - \alpha \nabla J(\theta_{t-1})$$

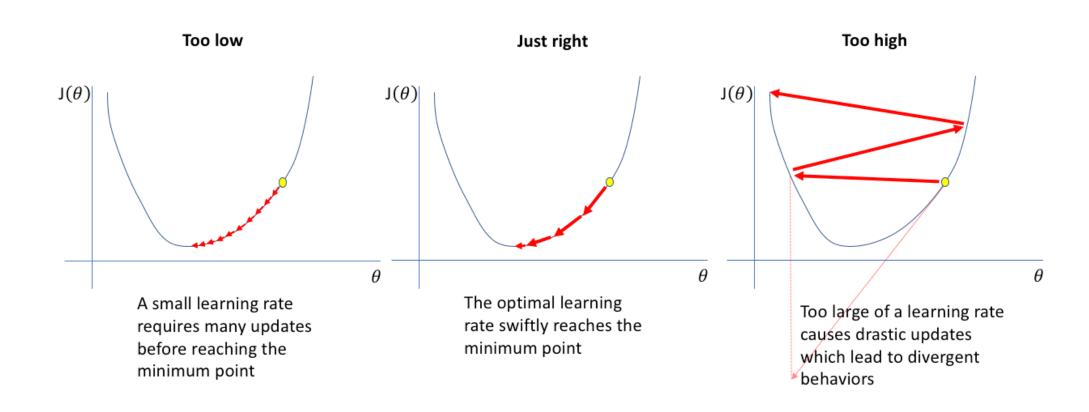
5. Iterate until it converges





Gradient Descent: Learning Rate

1. Update:



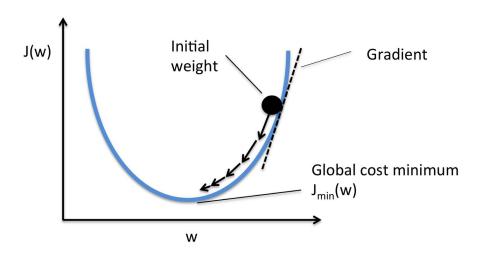


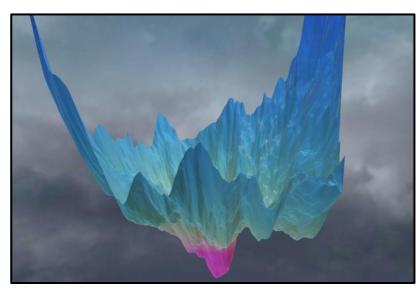
Gradient Descent

Easy visualization in 2D

But can be much harder: (demo) https://losslandscape.com/explorer

More details in the next lecture







Stochastic Gradient Descent (SGD)

- Processing the whole dataset in one batch is straightforward, may not fit into the memory
- Go through the training data in randomly selected batches
- A single pass through on the training data called epoch
- batch size can be:
 - Dataset size (full-batch)
 - 1, 2, 4, 8, 16, ... (mini-batch)

"SGD is like a drunkard trying to find his way home."

— Geoffrey Hinton

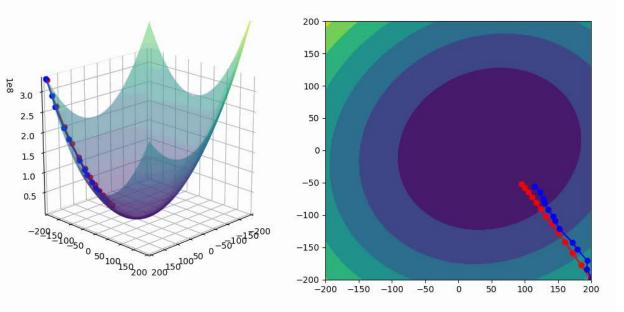


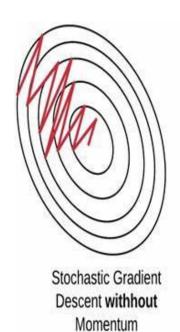
Image from: https://towardsdatascience.com/stochastic-gradient-descent-for-machine-learning-clearly-explained-cadcc17d3d11

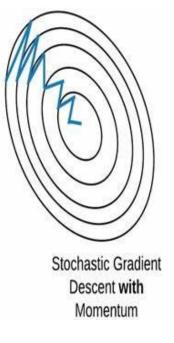
ELTE EČTIVÕS LORÁND UNIVERSITY

SGD with Momentum

- To get a smoother trajectory and reduce oscillations in valleys lets introduce momentum
- β controls the smoothing (weighted average)

4. Update:



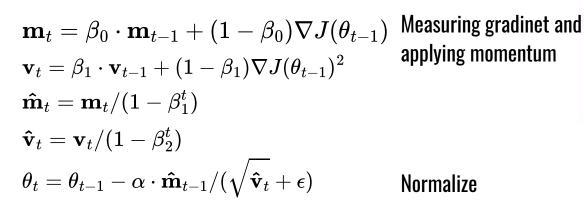




Adaptive Moment Estimation (Adam)

- Gradient descent makes large adjustments to parameters with large gradients
- **Solution**: Normalize the gradients so we move fix distances (learning rate)

4. Update:



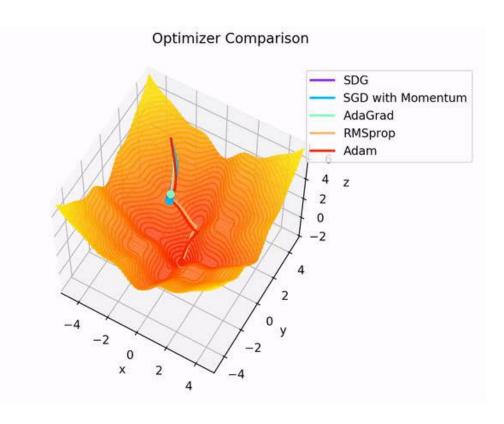


Image from: https://eloquentarduino.github.io/2020/04/stochastic-gradient-descent-on-your-microcontroller/



Summary

- Linear regression is a supervised learning method
- It tries to find the best-fitting linear model that minimizes the error
- Used when the output is continuous (not discrete)
- Can be solved with analytical or numerical solution

Analytical (Normal equation)

- Closed-form, provides a direct solution <u>Numerical (Gradient Descent)</u>
- Iterative approach, provides an approximation
- Fully Connected Networks (Feed Forward Networks) are inspired by the biological neural networks in the brain (but there are some differences)
- Can be used in tasks like Linear Regression where we optimize the weights and biases



Resources

Books:

- Courville, Goodfellow, Bengio: Deep Learning Freely available: https://www.deeplearningbook.org/
- Zhang, Aston and Lipton, Zachary C. and Li, Mu and Smola, Alexander J.: Dive into Deep Learning Freely available: https://d2l.ai/

Courses:

- Deep Learning specialization by Andrew NG
- https://www.coursera.org/specializations/deep-learning



That's all for today!

