# Machine Problem 4: Virtual Memory Management and Memory Allocation

### Introduction

In this machine problem we complete our memory manager. For this we extend our solution from previous MPs in three directions:

Part I: We will extend the page table management to support very large numbers and sizes of address spaces. This is currently not possible because both the page directory and the page table pages are stored in directly-mapped memory, which is very small. We need to move the page table pages and maybe the page table directory, from the directly-mapped kernel memory (kernel memory pool) into "virtual" memory (process memory pool). As you will see, this will slightly complicate the page table management and the design of the page fault handlers.

Part II: We will prepare the page table to support virtual memory as described in Part III.

**Part III:** We will implement a simple virtual-memory allocator (similar to the frame pool allocator in a previous MP) and hook it up to the new and delete operators of C++.

As a result we will have a flexible simple memory management system that we can use for later machine problems. Most importantly, we will be able to **dynamically allocate memory** in a fashion that is familiar to us from standard user-level C++ programming.

## Part I: Support for Large Address Spaces

The page table management in the previous machine problem was rather simple because we stored the *directory page* and any *page table pages* in directly-mapped memory (the kernel pool). Since the logical address of these pages was identical to their physical address, it was very easy to manipulate the content of the directory and of the page table frames. This approach works fine when the number of address spaces and the size of the requested memory is small; otherwise, we very quickly run out of frames in the directly-mapped frame pool.

In this machine problem, we allocate page table pages (and even page table directories if you want) in mapped memory, i.e. memory above 4MB in our case. These frames are handled by the process frame pool.

### Help! My Page Table Pages are in Mapped Memory!

Given a working implementation of a page table in direct-mapped memory, it is pretty straightforward to move it from directly-mapped memory to mapped memory.

When paging is turned on, the CPU issues logical addresses, and you will have problems working with the page table when you place it in mapped memory. In particular, you will want to modify entries in the page directory and page table pages. You know where these are in physical memory, but the CPU can only issue logical addresses. You can maintain a complicated table that maintains which logical addresses point to which page directory or page table page. Fortunately, this is not necessary, as you already have the page table, which that does exactly this mapping for you. You simply need to find a way to make use of it.

Ver. 2024C Page 1

The Canvas module on "Recursive Table Lookup on the x86" addresses this problem. We will use the trick described in the module: Have the last entry in the page directory point back to the beginning of the page directory. Make sure that you understand the trick. If you don't, ask. Once you understand this trick, the rest of this part of the machine problem will take very little time.

# Recursive Page Table Look-up

Here we summarize again the recursive table-lookup mechanism described in the Canvas module: Both the page table directory and the page table pages contain physical addresses. If a logical address of the form

```
| X : 10 | Y : 10 | offset : 12 |^{1}
```

is issued by the CPU, the memory management unit (MMU) will use the first 10 bits (value X) to index into the page directory (i.e., relative to the Page Directory Base Register) to look up the Page Directory Entry (PDE). The PDE points to the appropriate page table page. The MMU will use the second 10 bits (value Y) of the address to index into the page table page pointed to by the PDE to get the Page Table Entry (PTE). This entry will contain a pointer to the physical frame that contains the page.

If we set the last entry in the page directory to point to the page directory itself, we can play a number of interesting tricks. For example, the address below will be resolved by the MMU as follows:

```
| 1023 : 10 | 1023 : 10 | offset : 12 |
```

- The MMU will use the first 10 bits (value 1023) to index into the page directory to look up the PDE. PDE number 1023 (the last one) points to the page directory itself. *The MMU does not know about this* and treats the page directory like any other page table page.
- The MMU then uses the second 10 bits to index into the (supposed) page table page to look up the PTE. Since the second 10 bits of the address also have value 1023, the resulting PTE points again to the page directory itself. Again, the MMU does not know about this and treats the page directory like any frame: It uses the offset to index into the physical frame. This means that the offset is an index to a byte in the page directory. If the last two bits of the offset are zero, the offset becomes an index to the (offset DIV 4)'th entry in the page directory. In this way you can manipulate the page directory if you store it in logical memory. Neat!

Similarly, the address

```
| 1023 : 10 | X : 10 | Y : 10 | 0 : 2 |
```

gets processed by the MMU as follows:

• The MMU will use the first 10 bits (value 1023) to index into the page directory to look up the PDE. PDE number 1023 points to the page directory itself. Just as in the example above the MMU does not know about this and treats the page directory like any other page table page.

<sup>&</sup>lt;sup>1</sup>This expression represents a 32-bit value, with the first 10 bits having value X, the following 10 bits having value Y, and the last 12 bits having value offset.

• The MMU then uses the second 10 bits (value X) to index into the (supposed) page table page to look up the PTE (which in reality is the Xth PDE). The offset is now used to index into the (supposed) physical frame, which is in reality the page table page associated with the Xth directory entry. Therefore, the remaining 12 bits can be used to index into the Yth entry in the page table page.

The two examples above illustrate how one can manipulate a page directory that is stored in virtual memory (i.e., not stored in directly-mapped memory in our case) or a page table that is stored in virtual memory, respectively.

### Enough Theory! How do I Implement This?!

One side effect of this recursive page-table lookup is that we give a fixed logical address to the PDE or the PTE for a given logical memory address. This logical address of the PDE can be therefore easily computed. For this you should define two functions,

```
unsigned long * PageTable::PDE_address(unsigned long addr);
unsigned long * PageTable::PTE_address(unsigned long addr);
```

which return the address of the PDE or PTE. Once you have the address, you can easily access the content of the PDE or the PTE. For example,

```
unsigned long * pde = my_page_table->PDE_address(myaddr);
```

assigns the **address** of the PDE for myaddr to variable pde. The **content** of the PDE can now be accessed at \*pde. In some way, finding the PTEs and PDEs is now easier than it was in MP3 because we don't need to walk the page table to get of the PDE or PTE.

### Part II: Preparing class PageTable to handle Virtual Memory Pools

You will modify the class PageTable to support virtual memory allocation pools. We describe the class VMPool in detail in Part III below.

### Modifications to Class PageTable

In order to support virtual memory pools, make the following modifications to the page table. (A new version of the file page\_table.H is part of the source package. Feel free to use your own file, just add the two new functions register\_pool and free\_page.)

The page table must know all created virtual memory pools. This is because the page fault handler of the page table must know if the page fault has been caused by a legitimate access to memory that just happens to be not "in memory", or whether the user is trying to access unallocated memory, and the fault should be treated as a segmentation fault. For this, the page table must have a list of all memory pools.

You are to add support for (1) **registering** a virtual memory pool with the page table, (2) **checking the legitimacy** of a logical address, and (3) **freeing pages from memory**:

1. Add support for registration of virtual memory pools. In order to do this, the following function is to be provided:

Ver. 2024C Page 3

```
void PageTable::register_pool(VMPool * _pool);
```

The page table object shall maintain a list of registered pools. <sup>2</sup>

- 2. Add support for region check in page fault handler. Whenever a page fault happens, check with registered pools to see whether the address is legitimate. This can be done by calling the function VMPool::is\_legitimate for each registered pool. If the address is legitimate, proceed with the page fault. Otherwise, abort.
- 3. Add support for virtual memory pools to request the release of previously allocated pages. The following function is to be provided:

```
void PageTable::free_page(unsigned long _page_no);
```

If the page is valid, the page table releases the frame and marks the page invalid. Do not forget to appropriately flush the TLB whenever you mark a page invalid! (see below)

### Page Table Entries and the TLB

Recall that in the x86 architecture the TLB is **not coherent** with memory accesses. Therefore, you must flush all relevant entries in the TLB (or flush the entire TLB) each time you modify page table entries that may be contained in the TLB. This is mostly the case when you invalidate a page table entry. If you don't do that, the CPU may use a stale entry in the TLB, and your program will likely crash in very mysterious ways. The easiest way to flush the (entire) TLB is to reload the CR3 register (the page table base register) with its current value. The CPU thinks that a new page table is loaded, and it therefore flushes the TLB. (Note that stale TLB entries were not a problem in the previous MPs: If an invalid page is marked as valid as part of the page fault, the TLB gets updated.)

## Part III: An Allocator for Virtual Memory

In the third part of this machine problem we will design and implement an allocator for virtual memory. This allocator will be realized in form of the following virtual-memory pool class VMPool:

<sup>&</sup>lt;sup>2</sup>You will note that this will lead to a confused compiler: The PageTable object refers to the VMPool, and the VMPool in turn refers to the PageTable. This circular dependence will need to be broken. This is typically done through so-called *forward declarations*. For example, in the file page\_table.H we add the line class VMPool;. This line declares the class VMPool, which will then be defined later in file vm\_pool.H. You do the same with class PageTable in file vm\_pool.H. Google "forward declarations in C++" or similar for more details.

```
virtual-memory pool.]
   _base_address is the logical start address of the pool.
  _size is the size of the pool in bytes.
   _frame_pool points to the frame pool that provides the virtual
  memory pool with physical memory frames.
  _page_table points to the page table that maps the logical memory
   references to physical addresses. */
unsigned long allocate(unsigned long _size);
/* Allocates a region of _size bytes of memory from the virtual
   memory pool. If successful, returns the virtual address of the
   start of the allocated region of memory. If fails, returns 0. */
void release(unsigned long _start_address);
/* Releases a region of previously allocated memory. The region
   is identified by its start address, which was returned when the
   region was allocated. */
bool is_legitimate(unsigned long _address);
/* Returns FALSE if the address is not valid. An address is not valid
   if it is not part of a region that is currently allocated. */
```

An address space can have **multiple virtual memory pools** (created by constructing multiple objects of class VMPool). Each pool can have **multiple regions**, which are created by the function allocate and destroyed by the function release.

Our virtual-memory pool will be a somewhat lazy allocator: Instead of immediately allocating frames for a newly allocated memory region, the pool will simply "remember" that the region exists by storing start address and size in a local table. Only when a reference to a memory location inside the region is made, and a page fault occurs because no frame has been allocated yet, the page table (this is a separate object) finally allocates a frame and makes the page valid.

As we described earlier, in order for the page table object to know about virtual memory pools, we have the pools **register** with the page table by calling the function

```
PageTable::register_pool(VMPool * _pool).
```

This allows the page table object to maintain a collection (a list or an array) of references to virtual memory pools. This comes in handy when a page fault occurs, and the page table needs to check whether the memory reference is legitimate. When a virtual memory region is deallocated (as part of a call to VMPool::release(), the virtual memory pool informs the page table that any frames allocated to pages within the region can be freed and that the pages are to be invalidated. For this, the virtual memory pool calls the function PageTable::free\_page(unsigned int page\_no) for each page that is to be freed.

#### Implementation Issues:

There are no limits to how much you can optimize the implementation of your allocator. We want you to keep the allocator simple! Keep the following points in mind when you design your virtual memory pool in order to keep the implementation simple.

• Ignore the fact that the function allocate allows for the allocation of arbitrary-sized regions. Instead, always allocate multiples of pages. In this way you won't have to deal

with fractions of pages. Except for some internal fragmentation, the user will not know the difference.

- Don't try to optimize the way how frames are returned to the frame pool. Whenever a virtual memory pool releases a region, notify the page table to release the pages (and return any allocated frames to the frame pool).
- Keep the implementation of the allocator simple! There is no need to implement a Buddy-System allocator, for example. See the next point. (Unfortunately, we cannot use the bitmap implementation recommended for the contiguous-frame pool. The bitmap needed to manage a 4GB address space would be huge.)
- A proven and simple-to-implement approach is to store an array of allocated regions (base page and length for each region) and an array of free regions. Initially, there would be one allocated region (see below) and one large free region. As you allocate regions, you add entries in the allocated-region array, by splitting up free regions. Similarly, you would "move" allocated regions to the free-region array whenever you release memory. Don't worry about the external fragmentation that is caused by this. No need to coalesce free regions.
- Where to store your arrays of allocated and free regions? Feel free to use the first one or two page(s) of the pool to store the arrays. This solution limits the number of regions that you can allocate to less than 256 if you use one page to store the arrays (512 if you use two pages). This should be sufficient for now.
- A new virtual memory pool **registers** with the page table object. In this way, whenever the page table experiences a page fault, it can check whether memory references are legitimate (i.e., they are part of previously allocated regions). The page table checks with the registered virtual memory pools whether the address is legitimate by calling the function VMPool::is\_legitimate for each registered pool. If the address is not declared legitimate by any pool, the memory reference is invalid, and the kernel aborts.
- At this time we don't have a backing store yet, and pages cannot be "paged out". This means that we can easily run out of memory if a program references lots of pages in the allocated regions. Don' worry about this for now.

# The Assignment

- 1. (Part I) Extend your page table manager from the previous MP to handle pages in virtual memory. Use the "recursive page table lookup" scheme described in this handout. Remember to get your directory frame and the page table page frames from the process frame pool instead of the kernel frame pool!
- 2. Test your implementation of the new page table manager in virtual memory. Towards the end of file kernel.C you can define or un-define a macro called TEST\_PAGE\_TABLE, which controls whether just the page table is tested, or whether just the VM pools are tested. By default, this macro is defined, and only the page-table implementation is tested. Once you convince yourself that your page table implementation works correctly, uncomment the definition of this macro, and the code will start testing the VM pools.

3. (Part II) Extend your page table manager to (1) handle registration of virtual memory pools, (2) handle requests to free pages, and (3) check for legitimacy of logical addresses during page faults.

4. (Part III) Implement a simple virtual memory pool manager as defined in file vm\_pool.H. Always allocate multiples of pages at a time. This will simplify your implementation.

You should have access to a set of source files and a makefile that should make your implementation easier. In particular, the kernel.C file will contain documentation that describes where to add code and how to proceed about testing the code as you progress through the machine problem. The updated interface for the page table is available in page\_table.H and the interface for the virtual memory pool manager is available in file vm\_pool.H.

#### What to Hand In

You are to hand in a ZIP file, with name mp4.zip, containing the following files:

- 1. A design document, called design.pdf (in PDF format) that describes your implementation of the page table and the virtual memory pool.
- 2. All the source files and the makefile needed to compile the code.
- 3. The assignment should not require modifications to files other than page\_table.H/C and vm\_pool.H/C. In addition, will need to slightly modify kernel.C to turn on/off the provided test functions, or to add new test functionalities. Any modifications to the provided files vm\_pool.H and page\_table.H/C must be documented. Any modification to other files must be clearly motivated and documented. Be very careful when you modify the public interface provided by the .H files. We are using our own test code to check the correctness of your implementations, and we have to ensure that your code is compatible with our tests.
- 4. Grading of these MPs is a very tedious chore. These handin instructions are meant to mitigate the difficulty of grading, and to ensure that the grader does not overlook any of your efforts.

Note: Pay attention to the capitalization in file names. For example, if we request a file called file.H, we want the file name to end with a capital H, not a lower-case one. While Windows does not care about capitalization in file names, other operating systems do. This then causes all kinds of problems when the TA grades the submission.

Failure to follow the handin instructions will result in lost points.

Ver. 2024C Page 7