

## # Relational Model

- behind every db is a data model
- behind relational db is relational model
- data  $\rightarrow$  table of values or <sup>file</sup> or records
- A row/a record  $\rightarrow$  describes an entity / association of entities
- Each col has col name  $\rightarrow$  table name & col name help to interpret the data

STUDENT

ROLL	NAME	Dob

DEPT

DCODE	DNAME	HOD

STUDENT\_DEPT

ROLL	DCODE
1	D <sub>1</sub>

STUDENT & DEPT db rows represent entities while rows of STUDENT-DEPT db represent association b/w entities of other 2 db

## # Formal correspondence

Row  $\rightarrow$  Tuple  
Column  $\rightarrow$  Attribute  
Table  $\rightarrow$  Relation

# Each attribute has a domain

# Domain is a set of atomic values

# Relation Schema of a Relation

$R \rightarrow$  name of relation

$R(A_1, A_2 \dots A_n)$  is a relation schema with  $R$  as reln. name &  $A_1, A_2 \dots A_n$  are the attributes.  $A_i$  is the name of the role played by its corresponding domain  $D_i$  ( $\text{DOM}(A_i)$ ).

# Intension of a relation  $\Rightarrow$  Schema

# Degree of reln  $\rightarrow$  no. of attr.  $\rightarrow n$   
in the schema.

or

# Reln state of a reln, of schema  $R(A_1, A_2 \dots A_n)$  is denoted as  $r(R)$  is a set of  $n$ -tuples  $\{t_1, t_2 \dots t_m\}$  <sup>(each tuple contains  $n$  values)</sup> where  $t_i$  is an ordered list of values  $\langle v_1, v_2 \dots v_n \rangle$ .  $v_j$  belongs to  $\text{DOM}(A_j)$

	R			
	$A_1$	$A_2$	$\dots$	$A_n$
$t_1$	$v_1$	$v_2$		$v_n$
$t_2$				

\* State of a relation is called extension of a relation.  
It is instance-based & changes with time-stamp.

• Mathematically,  $n(R)$  is a collection of  $n$ -degree mappings on  $\text{DOM}(A_1), \text{DOM}(A_2), \dots, \text{DOM}(A_n)$   $\rightarrow n$ -ary relation schema

$$n(R) \subseteq \text{DOM}(A_1) \times \text{DOM}(A_2) \times \dots \times \text{DOM}(A_n)$$

## • Characteristics of relation

- Tuples are unordered i.e. it doesn't assume any order in which the tuples are present only that a set of tuples is there
- Attr. in a tuple may be ordered or unordered
  - ORDERED  $\rightarrow$  tuple is an ordered list of values
  - UNORDERED  $\rightarrow$   $\pi(R)$  is a set of mappings  $\{t_1, t_2, \dots, t_m\}$  where  $t_i$  is a mapping from  $R$  to  $D$ ,  $D$  is union of  $\text{DOM}(A_1), \text{DOM}(A_2), \dots, \text{DOM}(A_n)$   
i.e. In tuple  $t_i$ ,  $\{ \langle A_j, v_j \rangle \}$  set of attribute-value pairs

- Values & null values - attribute value is atomic & for a tuple it is single-valued (i.e. for a tuple, an attribute can have only one value)  
Value of an attr. either belongs to its domain or is null  $\text{VALUE} \in \text{DOMAIN}$
- # any schema that satisfies relational model is 1st normal form

<u>ROLL</u>	<u>SCORE</u>
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1	75
---	----

2	85
---	----

3	90
---	----

4	50
---	----

5	0/NULL
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$$\text{avg} = \frac{300}{4} = 75$$

if it is 0 then

$$\text{avg} = \frac{300}{5} = 60$$

# NULL values ignored for statistical operation

# Interpretation of NULL value

- $\rightarrow$  Not applicable
- $\rightarrow$  Applicable but unknown
- $\rightarrow$  Intentionally not stored

# Constraints in relational model

Model-based constraint

⇒ inherent in the model

- no 2 tuples are same
- no ordering of tuple can be assumed
- attr. in a tuple may be unordered or ordered

Data-Dependency Conds.

Functional dependency

Multivalued dependency

- Testing goodness &

Schema-based constraint

⇒ can be specified at the time of defining the schema (using DDL)

Application-based constraint

⇒ can't be specified using DDL but using logic within the appl.

→ The special constraints including multiple relations may require application level validations

# GUI is event-driven. Normally execution of statements is sequential in order but in GUI, when event occurs, the registered ActionListener listens & corresponding method is invoked.

# To the listener, the event object is sent denoting the src, thus single listener may handle multiple events

e.g,

ROLL	SCORE

LOW-LIMIT	HIGH-LIMIT	GRADE

This design ensures that discrepancy in assigning grade for score is prevented

• Domain constraint (type of Schema constraint)

— Attribute  $\in$  its domain

• Key constraint

$S_K$  be a subset of attributes of a schema  $R$  if for any 2 tuple  $t_1, t_2 \in r(R)$  such that

$$t_1[S_K] \neq t_2[S_K]$$

then  $S_K$  is the super key of  $R$

Worst case: entire tuple constitutes the super key

— Minimal super key of which no proper subset is a super key is called CANDIDATE KEY

$$\sigma_{P_1 \text{ AND } P_2}(R) \\ \equiv \sigma_{P_1}(\sigma_{P_2}(R)) \text{ or } \sigma_{P_2}(\sigma_{P_1}(R))$$

→ Project Opern.

$$\pi_{\text{ROLL, NAME}}(\text{STUDENT})$$

$$\pi_{\text{List}}(R)$$

$$\pi_{L_2}(\pi_{L_1}(R))$$

$$= \pi_{L_2}(\pi_{L_1}(R))$$

$$\text{iff } L_{\text{List } 2} \subseteq L_{\text{List } 1}$$

Q. select roll & name of all students with score  $\geq 80$

$$\pi_{\text{ROLL, NAME}}(\sigma_{\text{SCORE} \geq 80}(\text{STUDENT}))$$

→ Rename Opern. (Assignment)

$$\begin{array}{c} \text{TEMP} \leftarrow \sigma_{\text{SCORE} \geq 80}(\text{STUDENT}) \\ \uparrow \\ \text{ASSIGNMENT} \end{array}$$

$$\begin{array}{l} T \leftarrow \text{reln. algebra exp.} \\ \text{o/p is assigned to } T \\ T(A, B, C) \leftarrow \\ \text{Assignment involving} \\ \text{renaming of attr. to} \\ A, B, C \end{array}$$

o Notations:

- For reln.  $R(A_1, A_2, \dots, A_n)$

→  $\rho_S(B_1, B_2, \dots, B_n)(R)$  : renaming of reln. & attr.

→  $\rho_S(R)$  : renaming of reln. only

→  $\rho(B_1, B_2, \dots, B_n)(R)$  : renaming of attr. only

→ Cartesian Product

$$R_1(X, A, B) \times R_2(X, P, Q)$$

## → Equijoin

STUDENT  $\bowtie$  DEPT  
STUDENTS.DCODE  
= DEPT.DCODE

→ o/p schema: student & dept rels combined, but only those tuples retained for which predicate satisfies

→ equivalent to cartesian prod. + filtering

## # Fundamental oper.

- select
- projection
- rename
- cartesian prod.
- union
- set min
- intersection

## Extension

- equijoin
- natural join

## → Natural join

STUDENT \* DEPT

based on the equality of the common attr. → should appear only once in o/p schema

DEPT	
DCODE	DNAME
D1	—
D2	—
D3	—

STUDENT	
ROLL NAME	DCODE
_____	D1
_____	D1
_____	D2
_____	NULL
_____	D3

Now, equi join

DEPT  $\bowtie$  STUDENT

DEPT.DCODE = STUDENT.DCODE

IF joining attr. is NULL  $\rightarrow$  no match

\* when data from multiple relations reqd.  $\rightarrow$  go for joining:

IF we want those tuple, for which, for the attr under consideration values of one reln. don't match with values of the other, go for outer join

### • Outer Join

$R1 \bowtie R2$   
 $R1.A = R2.A$

Left  
outer  
Join

$\Downarrow$   
 Tuples of R1 with no match in R2 will be matched with a null tuple of R2

Right  
Outer  
Join

$R1 \bowtie R2$

For R2 all tuples appear

Full  
outer  
Join

$R1 \bowtie R2$

All tuples of R1 & R2 appear assuming null tuple of other reln. where necessary



## • Outer Union



Tuples of  $R1$  &  $R2$  match if

$$t_1[X] = t_2[X]$$

$$t_1 \in r_1(R_1), t_2 \in r_2(R_2)$$

$R1$  outer union  $R2$

For matched tuples, value of  $Y$  taken from  $R1$  & value of  $Z$  from  $R2$

Matched pair  $\Rightarrow$  one output tuple

For unmatched tuple  $\Rightarrow$  it takes null for either attr.

# Full outer join & outer union are equivalent -  
if full outer join taken w/ all columns attr.  
and not any specific subset

## • Division op<sup>n</sup>

ATTENDANCE (ROLL SCORE)

SUB (SCORE)

$ATTENDANCE \div SUB \Rightarrow$  ROLL nos for which tuples combine  
with an SCORE of SUB are  
in ATTENDANCE

$$R(X, Y) = R(Z) \div S(Y) \quad Y \subset Z, \quad X = Z - Y$$

Output schema: X

in its state, we have set of tuples  $\{t\}$ ,  $t$  is such that corresponding to  $t$  there are tuples  $t_R$  in  $r(R)$  with  $t[X] = t_R[X]$  &  $t_R[Y] = t_s[Y]$   
 $\forall t_s \in r_s(S)$

$t$  will be in output if it appears in  $r(R)$  with combination of all  $t_s$  in  $r_s(S)$

Division opern by sequence of fundamental opern.

$$R(X, Y) \quad S(Y)$$

$T1 \leftarrow \pi_X(R) \rightarrow$  duplicate eliminating proj.  $\rightarrow$  gives Roll of student that appeared for atleast 1 sub.

$T2 \leftarrow T1 \times S \rightarrow$  all combinations of roll & subj.

$T3 \leftarrow T2 - R \rightarrow$  missing roll, some comb.

$T4 \leftarrow \pi_X(T3) \rightarrow$  roll of stts missed atleast one sub.

$T \leftarrow T1 - T4 \rightarrow$  roll of students who missed no sub.

$$T \equiv R \div S$$

• To find out students with same score in same subjects (i.e. to determine students who have copied off of each other.)

RESULT, ROLL, COPY, ROLL (RESULT  $\bowtie$  COPY (RESULT))

RESULT, SCORE

= COPY, SCORE

AND RESULT, ROLL < COPY, ROLL