

Indian Institute of Technology Delhi
Department of Computer Science and Engineering

CXL226

Programming Languages

Quiz 4

March 16, 2017

10 minutes

Maximum Marks: 10

Q1 (10 marks) Unification.

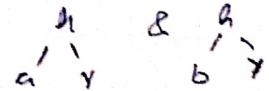
For each of the following pairs of terms, provide the most general unifier if it exists, and otherwise indicate why unification fails. The unifier must be given in its reduced form (as a finite domain function from variables to terms).

1. $f(h(a, Y), X)$ and $f(X, h(b, Y))$.

The unification fails, because if we proceed with the algorithm we get
 $\sigma_1 = \{ X \mapsto h(a, Y) \}$

Now finding mgu of $(t_2, u_2) \Rightarrow$ we need to find the mgu of

which fails as $a \neq b$ (different constants)



2. $f(h(X, a), Y)$ and $f(Z, h(b, X))$.

The most general unifier is

$$Z \mapsto h(X, a)$$

$$Y \mapsto h(b, X)$$

3. $f(h(a, X), X)$ and $f(Y, h(Y, b))$.

The unification fails as when we first apply unification on $h(a, X)$ & Y we get $Y \mapsto h(a, X)$ but on applying on X & $h(Y, b)$ we need to get unification on X & $h(h(a, X), b)$ which fails as it contains X .

4. $f(h(a, X), h(X, b))$ and $f(h(a, b), h(Z, X))$.

The unification is.

$$\text{mgu} = \begin{matrix} X \mapsto b \\ Z \mapsto b \end{matrix}$$

