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CSL302

Programming Languages

Quiz 2

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10 minutes

Maximum Marks: 10

Q1. (10 marks) Definitional interpreter for boolean expressions. Consider a simple language for boolean expressions consisting of boolean constants T and F, propositional variables P_1, P_2, \dots ; and closed under (unary) negation, and binary operations of conjunction ("and") and disjunction ("or"). Specify a definitional interpreter for this language, filling in the spaces below.

Abstract Syntax

$b, b_1, b_2 \in B ::=$

- T | F /* const */
- P /* prop variables */
- $\neg b$ /* negation */
- $b_1 \wedge b_2$ /* and */
- $b_1 \vee b_2$ /* or */

Semantic Domain

Boolean.

Auxiliary Concepts

$v \in \text{TruthAssign} \equiv$

$T \rightarrow \text{True}$
 $F \rightarrow \text{False}$
 $\neg b \rightarrow \neg(\text{TruthAssign } v)$

Semantic Functions

truth:

$(B \rightarrow \text{TruthAssign}) \rightarrow \text{Boolean}$

value [T] : T \rightarrow Bo
 value [F] : F \rightarrow Bo

Definition of function truth

$T \rightarrow \text{True}$
 $F \rightarrow \text{False}$
 $\neg b \rightarrow \neg(\text{truth } b)$
 $b_1 \wedge b_2 \rightarrow (\text{truth } b_1) \wedge (\text{truth } b_2)$
 $b_1 \vee b_2 \rightarrow (\text{truth } b_1) \vee (\text{truth } b_2)$