

## FCS152 Tutorial 5

### Set Theory

1. List the elements of the following sets; here  $\mathbf{N} = \{1, 2, 3, \dots\}$ 
  - (a)  $A = \{x: x \in \mathbf{N}, 3 < x < 13\}$
  - (b)  $B = \{x: x \in \mathbf{N}, x \text{ is even}, x < 15\}$
  - (c)  $C = \{x: x \in \mathbf{N}, 4 + x = 3\}$
2. Write each of the following sets in the form  $\{x \mid P(x)\}$ :
  - (a)  $\{\text{January, February, May, July}\}$
  - (b)  $\{a, aba, ababa, abababa, \dots\}$
  - (c)  $\{\dots, 1/8, 1/4, 1/2, 1, 2, 4, 8, \dots\}$
3. Given two sets  $A = \{a, \{a\}\}$ ,  $B = \{a, b, \{a, b\}\}$ . Determine  $A \cap B$ ,  $A \cup B$ ,  $P(A)$ ,  $B \cap P(A)$ ,  $A \times B$ .
4. Which of the following is true for all sets  $A$ ,  $B$  and  $C$ ? Prove or give a counter-example.
  - (a)  $A \cap B = B \cap A$
  - (b)  $(A - B) \cap C = (A \cap C) - B$
  - (c)  $(A - B) - C = A - (B - C)$
5. Prove by induction on the size of the set, that the power set  $P(A)$  has cardinality  $2^{|A|}$ .