

# Data Link Layer I

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Semester 1, 2021

# Q1

Consider the case of transmitting 1250 Bytes frame over on a link with a delay of 200ms (millisecond) when the length of the link is 200km. Assume that acknowledgment packets are of negligible size, processing time at a node is negligible, and the link is error-free.

Calculate the transmission efficiency of the following ARQ methods if the transmission rates are 1Kbps, 1Mbps, 1Gbps and the lengths of the same link are 20Km, 200Km, 2000Km, 20000Km respectively.

- a. Stop-and-wait ARQ?
- b. Go-Back-N ARQ where  $W$  is large enough to keep the channel fully busy?
- c. Selective-Repeat ARQ where  $W$  is 7?

# Q1

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Frame Size =  $L = 1250 * 8 \text{ bits} = 10000 \text{ bits}$

Prop rate =  $200\text{km}/(200*10^{-3}\text{s}) = 1000 \text{ km/s}$

$T_{\text{frame}} = L / (\text{Transmission rate}) \text{ (in seconds)}$

$T_{\text{prop}} = \text{Distance} / (\text{Prop rate}) \text{ (in seconds)}$

# Stop-and-wait ARQ

$$S = \frac{1}{1 + 2a}$$

i)  $T_{\text{frame}} = L / (\text{Transmission rate}) = 10000 / 1000 = 10\text{s}$

$T_{\text{prop}} = \text{Distance} / (\text{Prop rate}) = 20 / 1000 = 0.02\text{s}$

$a = T_{\text{prop}} / T_{\text{frame}} = 0.02 / 10 = 0.002$

$s = 1 / (1 + 2a) = 1 / 1.002 = 0.996 \text{ (99.6\%)}$

ii)  $T_{\text{frame}} = L / (\text{Transmission rate}) = 10000 / 1000000 = 0.01\text{s}$

$T_{\text{prop}} = \text{Distance} / (\text{Prop rate}) = 2000 / 1000 = 2\text{s}$

$a = T_{\text{prop}} / T_{\text{frame}} = 2 / 0.01 = 200$

$s = 1 / (1 + 2a) = 1 / 401 = 0.0025 \text{ (0.25\%)}$

Distance \ Transmission rate	20Km	200Km	2000Km	20000Km
1Kbps	99.8%			
1Mbps			0.25%	
1Gpbs				

# Go-Back-N ARQ with a large W

..... ( $W \geq 2a + 1$ ) to keep the channel fully busy?

$$S = \begin{cases} 1, & W \geq 2a + 1 \\ \frac{W}{(2a + 1)}, & W < 2a + 1 \end{cases}$$

$$s = 1$$

# Selective-Repeat ARQ where $W = 7$

$$S = \begin{cases} 1, & W \geq 2a + 1 \\ \frac{W}{(2a + 1)}, & W < 2a + 1 \end{cases}$$

i)  $T_{\text{frame}} = L / (\text{Transmission rate}) = 10000 / 1000 = 10\text{s}$

$T_{\text{prop}} = \text{Distance} / (\text{Prop rate}) = 20 / 1000 = 0.02\text{s}$

$a = T_{\text{prop}} / T_{\text{frame}} = 0.02 / 10 = 0.002 \quad W \geq 2a + 1 \quad s = 1$

ii)  $T_{\text{frame}} = L / (\text{Transmission rate}) = 10000 / 1000000 = 0.01\text{s}$

$T_{\text{prop}} = \text{Distance} / (\text{Prop rate}) = 2000 / 1000 = 2\text{s}$

$a = T_{\text{prop}} / T_{\text{frame}} = 2 / 0.01 = 200 \quad W < 2a + 1 \quad s = w / (1 + 2a) = 7 / 401 = 0.0175 \text{ (1.75\%)}$

Distance \ Transmission rate	20Km	200Km	2000Km	20000Km
1Kbps	100%			
1Mbps			1.75%	
1Gpbs				

# Q2

Consider a sliding window protocol (Go-Back-N ARQ) used for flow control on a given data link where the data rate is 8,000 bits/second, the propagation delay is 0.25 second, and the frame size is 1600 bits. Assume that acknowledgment packets are of negligible size, processing time at a node is negligible, and the link is error-free. What is the minimum window size which will allow full utilization (efficiency) of the link?

$$\text{Frame Size} = L = 1600 \text{ bits}$$

$$T_{\text{prop}} = 0.25 \text{ s}$$

$$T_{\text{frame}} = 1600 / 8000 = 0.2 \text{ s}$$

$$a = 0.25 \text{ s} / T_{\text{frame}} = 1.25$$

In order to have a full link utilization:  $W \geq 2a + 1$

$$W_{\text{min}} = \text{round\_up}(2 * 1.25 + 1) = 4$$



# Q3

Assume data in 8-bit words as shown below:

10011001 11100010 00100100 10000100

- a. Calculate the checksum at the sender's end and the receiver's end

Refer to lecture notes for binary calculation

## Sender's End

$$b1 = 10011001 = 153$$

$$b2 = 11100010 = 226$$

$$b3 = 00100100 = 36$$

$$b4 = 10000100 = 132$$

$$x = (b1 + b2 + b3 + b4) \bmod 2^8 - 1$$

$$37 = 547 \bmod 255$$

$$\text{checksum } c = -x \bmod 255$$

$$c = -37 \bmod 255$$

$$c = 218$$

$$c = 11011010$$

## Receiver's End

$$b1 = 10011001 = 153$$

$$b2 = 11100010 = 226$$

$$b3 = 00100100 = 36$$

$$b4 = 10000100 = 132$$

$$b5 = 11011010 = 218 \text{ (checksum block)}$$

$$x = (b1 + b2 + b3 + b4 + b5) \bmod 2^8 - 1$$

$$0 = 765 \bmod 255$$

$$\text{checksum } c = -0 \bmod 255$$

$$c = -0 \bmod 255$$

$$c = 0$$

$$c = 0$$

Codeword = 10011001 11100010 00100100 10000100 11011010



# Q3

**Assume data in 8-bit words as shown below:**

10011001 11100010 00100100 10000100

**b.** State an example of an error that checksum fails to detect?

Sender sent                    10011001 11100010 00100100 10000100 11011010

Receiver received            11100010 10011001 00100100 10000100 11011010

Can't be detected by checksum

# Q4

Given the data word (1011011), or data polynomial  $D(x) = x^6 + x^4 + x^3 + x^1 + 1$  and given the generator polynomial  $G(x) = x + 1$

- a. Find the codeword  $C(x)$
- b. Assume the received message  $H(x)$  is  $H(x) = C(x) + E(x)$ , where  $E(x)$  is the error polynomial
  - i. When  $H(x)$  contains no errors show that  $H(x)$  is divisible by  $G(x)$
  - ii. Determine whether the error is detectable when:
    - $E(x) = 1$
    - $E(x) = x + 1$
    - $E(x) = x^3 + x$

# Q4

Given the data word (1011011), or data polynomial  $D(x) = x^6 + x^4 + x^3 + x^1 + 1$  and given the generator polynomial  $G(x) = x + 1$  (11)

- a. Find the codeword  $C(x)$  (For detailed explanation please see lecture notes)

			1	1	0	1	1	0	0	
1	1	1	0	1	1	0	1	1	0	
		1	1							
		1	1							
		0	0	1	0					
				1	1					
				0	1	1				
					1	1				
					0	0	1	0		
							1	1		
									1	

Remainder

Codeword = 10110111

# Q4

Given the data word (1011011), or data polynomial  $D(x) = x^6 + x^4 + x^3 + x^1 + 1$  and given the generator polynomial  $G(x) = x + 1$

- b. Assume the received message  $H(x)$  is  $H(x) = C(x) + E(x)$ , where  $E(x)$  is the error polynomial
- i. When  $H(x)$  contains no errors show that  $H(x)$  is divisible by  $G(x)$

XOR (since  $E(x)$  here just indicates which bits are in error during transmission)

Divide  $H(x)$  by  $G(x)$  and show that the remainder = 0

# Q4

Determine whether the error is detectable when:

- $E(x) = 1$

Received: 10110111 + 00000001 = 10110110

			1	1	0	1	1	0	1	
1	1	1	0	1	1	0	1	1	0	
		1	1							
		1	1							
		0	0	1	0					
				1	1					
				0	1	1				
					1	1				
					0	0	1	0		
							1	1		
									1	

Error detected

# Q4

Determine whether the error is detectable when:

- $E(x) = x^3 + x$

$$\begin{array}{r} \text{Received: } 10110111 \\ + 00001010 \\ \hline = 10111101 \end{array}$$

			1	1	0	1	0	1	0
1	1	1	0	1	1	1	0	1	
		1	1						
			1	1					
			0	0	1	1			
					1	1			
					0	0	1	0	
							1	1	
							0	1	1
								1	1
									0

Error undetected

# Q5

**Show byte-stuffing & destuffing steps for the following data bits if PPP frame is used?**

01000001 01111101 01000010 01111110 01010000 01110000 01000110

Convert to Hex: 41 7D 42 7E 50 70 46

Look for the Flag (7E) and Control Escape (7D): 41 7D 42 7E 50 70 46

Stuffing

7D will be replaced by the byte 7D and  $(7D \text{ XOR } 20) = 5D$

7E will be replaced by the byte 7D and  $(7E \text{ XOR } 20) = 5E$

Hence the complete byte string to be sent: 7E 41 7D 5D 42 7D 5E 50 70 46 7E

Received bits after Hex Conversion: 7E 41 7D 5D 42 7D 5E 50 70 46 7E

Look for the bytes 7E and 7D: 7E is the flag; If 7D is encountered, look into the next byte

7E 41 7D 5D 42 7D 5E 50 70 46 7E

Replace (7D <next byte>) with (<next byte> XOR 20)

7E 41 7D 42 7E 50 70 46 7E

Destuffing



## Q6 (Optional. For information only)

In some networks the data link layer requests all damaged frames to be retransmitted. Assume that the acknowledgement frame is never lost. If the probability of a frame being damaged on a particular link is  $p$ , what is the normalized throughput of the link if stop-and-wait ARG is used?

Hint:

$$\sum_{i=1}^{\infty} (i \times x^{i-1}) = \frac{1}{(1-x)^2} \quad \text{for } (-1 < x < 1)$$

# Q6 (Optional)

The time to transmit a frame successfully is

$$T = T_{frame} + 2 T_{prop}$$

Suppose the frame or ACK *is lost*, two transmission attempts are required, therefore,

$$T = T_{frame} + \text{timeout} + T_{frame} + 2 T_{prop}$$

Assume  $\text{timeout} = 2 T_{prop}$

Therefore

$$T = 2 (T_{frame} + 2 T_{prop}) \quad \text{for two transmissions}$$

# Q6 (Optional)

Suppose for successful transmission each frame has to be transmitted  $k$  times on average, then

$$T = N_x (T_{frame} + 2 T_{prop})$$

The probability of a frame requires exactly  $k$  transmissions,  $P(k)$ , equals the probability of the first  $k-1$  attempts failing,  $(p^{k-1})$ , multiplies the probability of the  $k$ -th transmission succeeding,  $(1-p)$ .

Therefore the mean number of transmission is

$$N_x = \sum_{k=1}^{\infty} (k \times T(k)) = \sum_{k=1}^{\infty} (k \times (1-p) \times p^{k-1}) = \frac{1}{(1-p)^2} (1-p) = \frac{1}{(1-p)}$$

# Q6 (Optional)

Normalized throughput

$$S = \frac{T_{frame}}{N_x (T_{frame} + 2T_{prop})} = \frac{1}{N_x (1 + 2a)}$$

$$\mathbf{S} = \frac{1 - \mathbf{P}}{1 + 2\mathbf{a}}$$