Implementation of Shor's factorization algorithm

Project No.4

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software development kits: IBM Qiskit and Microsoft Q#.

21 --- Quantum ---- 3 X 7

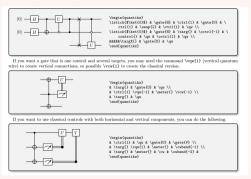
Objectives

- To simulate a quantum circuit of Shor's factorization algorithm.
- To factor composite numbers (represented in no more than 6 bits) of two small prime numbers.
- To break simple encryption involving prime factorization.
- To break RSA encryption.

Scope

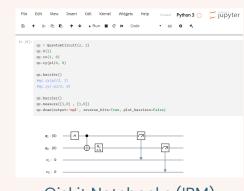
- Use IBM Qiskit and Microsoft Q# for simulation.
- The number to be factored is a composite number (represented in no more than 6 bits) of two small prime numbers.

Software tools

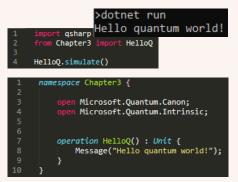




To factor N = p*q

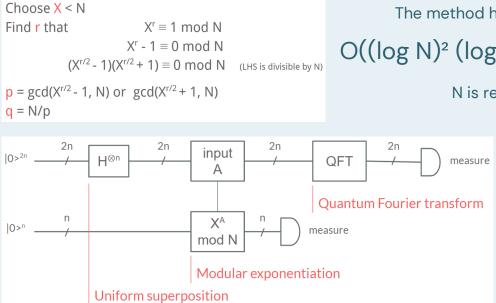


Qiskit Notebooks (IBM)



Microsoft Q# and .NET SDKs

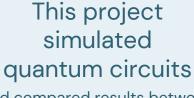
Order finding: a clever method to factor a number N



The method has polynomial complexity

 $O((log N)^2 (log log N) (log log log N))$

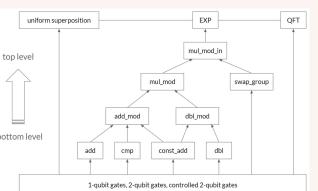
N is represented in n bits



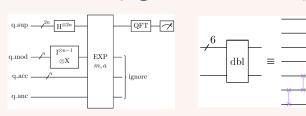
and compared results between IBM Qiskit and Microsoft Q#.

Qiskit

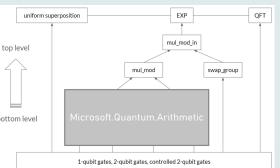
Circuit design: IBM Qiskit



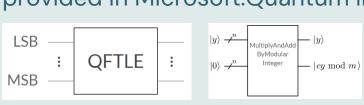
Implement everything from elementary gates to the top level.



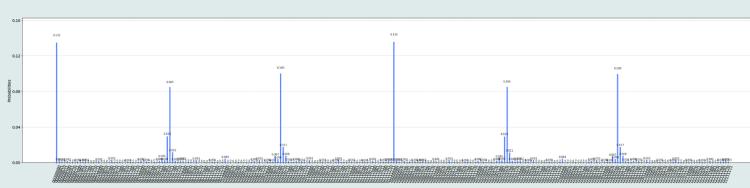
Circuit design: Micosoft Q#



There are some built-in operations provided in Microsoft.Quantum library.



Results



Quantum computer is different from classical computer.

There are several quantum algorithms which solve some

problems better than those algorithms in classical computer.

Factoring is one of the problems proposed by Peter Shor who

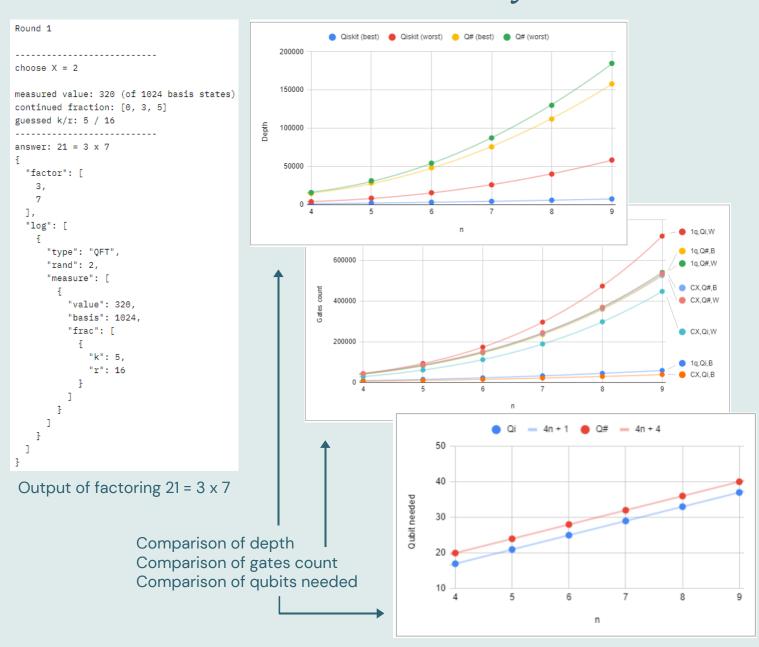
discovered the quantum algorithm to solve it. This project

tried to simulate a quantum computer to implement Shor's

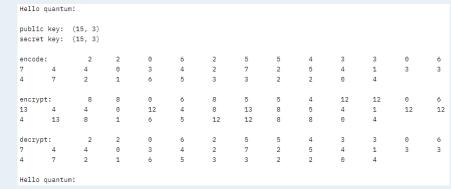
factorization algorithm using two different open-source

Histogram of measurement results. 6 peaks mean the order is 6.

IBM Qiskit vs Microsoft Q#



RSA encryption demonstration



The encryption/decryption of the text "Hello quantum!". Assume that the attacker is the man in the middle between encryption and decryption processes. He knows the public key, and he also knows the private key because RSA encryption involves prime factorization that is a critical part of the encryption.

Conclusion

Criteria	IBM Qiskit	Microsoft Q#
maximum length (bits)	6	5
times to random	indeterminate	indeterminate
times to do measurement	indeterminate	indeterminate
running time	lower	higher
depth	lower	higher
width	lower	higher
gates count	looser	tighter
demonstrate RSA breaking	yes	yes

There is an unsolved problem of too much running time consumed in Microsoft Q#. This project also tried to break a simple encryption involving no-more-than-5-bit composite number.

MSB — Sumarized comparison between two SDKs

< Q# >



• IBM Qiskit logo - https://pennylane.readthedocs.io/en/user-docs-refactor/introduction/plugins.html



