```
In [ ]: import numpy as np
In [ ]: I = np.array([[154,123,123,123,123,123,123,136],
                       [192,180,136,154,154,154,136,110],
                       [254,198,154,154,180,154,123,123],
                       [239, 180, 136, 180, 180, 166, 123, 123],
                       [180,154,136,167,166,149,136,136],
                       [128, 136, 123, 136, 154, 180, 198, 154],
                       [123,105,110,149,136,136,180,166],
                       [110,136,123,123,123,136,154,136]])
In []: M = I -128
In []: T = np.zeros((8,8))
        for i in range(8):
            for j in range(8):
                 if i == 0:
                     T[i,j] = np.sqrt(1/8)
                 else:
                     T[i,j] = np.sqrt(1/4) * np.cos((2*j + 1)*i*np.pi/16)
In [ ]: D = np.dot(np.dot(T,M),np.transpose(T))
In [ ]: Q = np.array([
            [16, 11, 10, 16, 24, 40, 51, 61],
            [12, 12, 14, 19, 26, 58, 60, 55],
            [14, 13, 16, 24, 40, 57, 69, 56],
            [14, 17, 22, 29, 51, 87, 80, 62],
            [18, 22, 37, 56, 68, 109, 103, 77],
            [24, 35, 55, 64, 81, 104, 113, 92],
            [49, 64, 78, 87, 103, 121, 120, 101],
            [72, 92, 95, 98, 112, 100, 103, 99]
        ])
In []: C = np.round(D/Q)
        R = Q * C
        N = np.round(np.dot(np.transpose(T),R),T)+128)
In [ ]: |print("M",M)
        print()
        print("Q",Q)
        print()
        print("D",D)
        print()
        print("C",C)
        print()
        print("R",R)
        print()
        print("I",I)
        print()
        print("N",N)
```

```
M [[ 26 -5 -5 -5 -5 -5
 [ 64 52
              26 26 26
                           8 -18]
           8
 [126
      70
          26
              26
                  52
                      26
                         -5
                              -5]
                 52
                      38
                         -5
 [111
      52
           8
             52
                              -5]
 <sup>52</sup>
      26
           8
             39
                  38
                      21
                           8
                               8]
                          70
       8 -5
                  26
                      52
                              26]
   0
               8
 [ -5 -23 -18
              21
                   8
                       8 52
                              38]
       8 -5
 [-18
             -5
                  -5
                       8 26
Q [[ 16 11 10 16 24 40 51 61]
[ 12 12 14 19
                  26 58 60
                             55]
     13 16
             24
                 40 57 69
 <sup>[</sup> 14
      17
          22
             29
                  51 87 80
                              62]
      22
          37
              56 68 109 103
 [ 18
                              77]
      35
          55
             64 81 104 113
                             92]
 [ 24
 [ 49
      64
          78
             87 103 121 120 101]
[ 72 92 95 98 112 100 103 99]]
D [[ 1.62250000e+02 4.05989816e+01 2.00026918e+01 7.23294009e+01
   3.02500000e+01 1.24848354e+01 -1.96505043e+01 -1.14971452e+01]
 [ 3.04792937e+01 1.08415970e+02 1.04730992e+01 3.22925175e+01
   2.76990885e+01 -1.55048925e+01 1.84075948e+01 -1.99566961e+00]
 [-9.41445075e+01 -6.00511329e+01 1.22980970e+01 -4.34188963e+01
 -3.12878702e+01 6.06690905e+00 -3.33058262e+00 7.14403453e+00]
 [-3.85675018e+01 -8.33575149e+01 -5.41238759e+00 -2.21698602e+01
  -1.35195286e+01 1.54918916e+01 -1.33187181e+00 3.53461026e+00]
 [-3.12500000e+01 1.79340053e+01 -5.52404638e+00 -1.23555600e+01
   1.42500000e+01 -5.96236717e+00 1.14884686e+01 -6.02384997e+00]
 [-8.64681444e-01 -1.17637950e+01 1.27762672e+01 1.81231416e-01
   2.80712006e+01 1.25731431e+01 8.35255975e+00 2.93590135e+00]
 [ 4.62997947e+00 -2.42141001e+00 1.21694174e+01 6.56145155e+00
  -1.87001117e+01 -1.27532960e+01 7.70190296e+00 1.20313688e+01]
 [-9.95302906e+00 1.11936702e+01 7.81185357e+00 -1.62885238e+01
   2.14648676e+01 2.17022289e-02 5.90622636e+00 1.06807473e+01]]
C [[10. 4. 2. 5. 1. 0. -0. -0.]
 [3. 9. 1. 2. 1. -0. 0. -0.]
 [-7. -5. 1. -2. -1. 0. -0. 0.]
 [-3. -5. -0. -1. -0. 0. -0.
 [-2. 1. -0. -0. 0. -0.
                         0. -0.]
 [-0. -0. 0. 0. 0. 0.
                         0.
 [ 0. -0. 0. 0. -0. -0.
                         0.
                              0.]
 [-0. 0. 0. -0. 0. 0.
                         0.
                              0.11
R [[160. 44. 20. 80. 24.
                              0. -0. -0.]
 [ 36. 108. 14. 38.
                     26.
                          -0.
                                 0.
                                    -0.]
 [-98. -65.
           16. -48. -40.
                            0.
                               -0.
                                      0.]
 [-42. -85.
            -0. -29.
                                -0.
                      -0.
                            0.
 [-36.
       22.
            -0.
                 -0.
                       0.
                           -0.
                                 0.
                                     -0.]
 [ -0.
       -0.
             0.
                  0.
                       0.
                            0.
                                 0.
                                      0.]
       -0.
             0.
                  0.
                      -0.
                           -0.
   0.
                                 0.
                                      0.]
 [ -0.
        0.
             0.
                 -0.
                       0.
                            0.
                                      0.]]
I [[154 123 123 123 123 123 123 136]
 [192 180 136 154 154 154 136 110]
 [254 198 154 154 180 154 123 123]
 [239 180 136 180 180 166 123 123]
 [180 154 136 167 166 149 136 136]
 [128 136 123 136 154 180 198 154]
 [123 105 110 149 136 136 180 166]
```

```
[110 136 123 123 123 136 154 136]]

N [[149. 134. 119. 116. 121. 126. 127. 128.]
        [204. 168. 140. 144. 155. 150. 135. 125.]
        [253. 195. 155. 166. 183. 165. 131. 111.]
        [245. 185. 148. 166. 184. 160. 124. 107.]
        [188. 149. 132. 155. 172. 159. 141. 136.]
        [132. 123. 125. 143. 160. 166. 168. 171.]
        [109. 119. 126. 128. 139. 158. 168. 166.]
        [111. 127. 127. 114. 118. 141. 147. 135.]]

In []:
```