

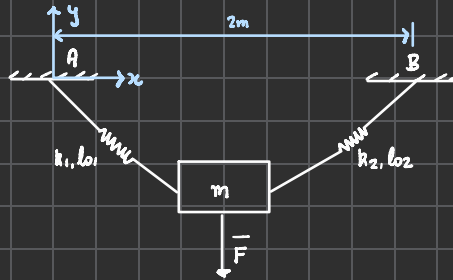
Homework-1

Problem 1

Due: 16-Jan-2025

Time Spent: 2.5 Hours

Sketch:



Given:  $k_1 = 10 \text{ N/m}$ ;  $k_2 = 20 \text{ N/m}$ ;  $m = 5 \text{ kg}$ ;  $\mathbf{r}(0) = [1 \ -2]^T \text{ m}$ ;  $\mathbf{\bar{r}}_{AM} = [2 \ 0]^T \text{ m}$   
 $l_{01} = 1 \text{ m}$ ;  $l_{02} = 1.414 \text{ m}$ ;  $g = 10 \text{ m/s}^2$ ;  $\mathbf{v}(0) = [0 \ 0]^T \text{ m/s}$ ;  $\mathbf{\bar{F}} = [5 \ 1]^T \text{ N}$

To Find:  $\mathbf{r}(t)$

Apply LMB,

$$\sum \bar{\mathbf{F}}_i = m\bar{\mathbf{a}}$$

$$\Rightarrow \bar{\mathbf{F}} + \bar{\mathbf{F}}_{s1} + \bar{\mathbf{F}}_{s2} - mg\hat{\mathbf{j}} = m\bar{\mathbf{a}}$$

$$\bar{\mathbf{F}}_{s1} = k_1 (|\bar{\mathbf{r}}_{AM}| - l_{01}) \frac{(\bar{\mathbf{r}}_{AM})}{|\bar{\mathbf{r}}_{AM}|} = -k_1 (|\bar{\mathbf{r}}(t)| - l_{01}) \frac{\bar{\mathbf{r}}(t)}{|\bar{\mathbf{r}}(t)|}$$

$$\bar{\mathbf{F}}_{s2} = k_2 (|\bar{\mathbf{r}}_{BM}| - l_{02}) \frac{(\bar{\mathbf{r}}_{BM})}{|\bar{\mathbf{r}}_{BM}|} = -k_2 (|\bar{\mathbf{r}}(t) + \bar{\mathbf{r}}_{AB}| - l_{02}) \frac{(\bar{\mathbf{r}}(t) + \bar{\mathbf{r}}_{AB})}{|\bar{\mathbf{r}}(t) + \bar{\mathbf{r}}_{AB}|}$$

FBD: Mass

