Tanay Saxena (001586302) Program Structures & Algorithms Fall 2021 Assignment No. 3

- Task (List down the tasks performed in the Assignment)
 - Added missing code in 4 methods -Class UF_HWQUPC.java find() -

```
public int find(int p) {
    validate(p);
    int root = p;
    // TO BE IMPLEMENTED
    if (pathCompression) doPathCompression(root);
    while (root != parent[root]) {
        root = parent[root];
    }
    return root;
}
```

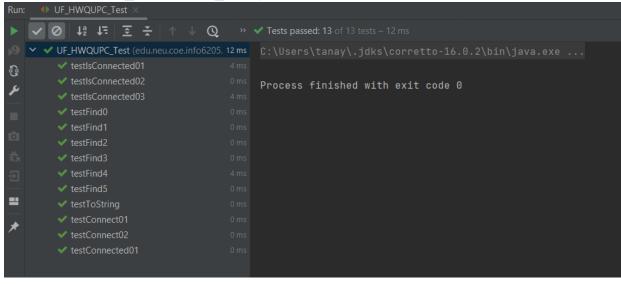
mergeComponents() -

```
private void mergeComponents(int i, int j) {
    // TO BE IMPLEMENTED make shorter root point to taller one
    if (i == j) return;
    if (height[i] < height[j]) {
        updateParent(i, j);
    }
    else {
        updateParent(j, i);
    }
    if (height[i] == height[j]) {
        height[i]++;
    }
}</pre>
```

doPathCompression()

```
private void doPathCompression(int i) {
    // TO BE IMPLEMENTED update parent to value of grandparent
    while (i != parent[i]) {
        parent[i] = parent[parent[i]];
        i = parent[i];
    }
}
```

o Ran tests for UF_HWQUPC_Test.java-



o Created a new class UnionFindClient.java for the analysis -

o Generated the output by executing the main method -

```
Number of steps n = 64, number of unions required m = 160.6
Number of steps n = 94, number of unions required m = 235.4
Number of steps n = 124, number of unions required m = 324.5
Number of steps n = 154, number of unions required m = 449.4
Number of steps n = 184, number of unions required m = 525.0
Number of steps n = 214, number of unions required m = 638.2
Number of steps n = 244, number of unions required m = 651.8
Number of steps n = 274, number of unions required m = 836.9
Number of steps n = 304, number of unions required m = 999.8
Number of steps n = 334, number of unions required m = 963.6
Number of steps n = 364, number of unions required m = 1147.3
Number of steps n = 394, number of unions required m = 1351.5
Number of steps n = 424, number of unions required m = 1483.7
Number of steps n = 454, number of unions required m = 1590.9
Number of steps n = 484, number of unions required m = 1734.1
Number of steps n = 514, number of unions required m = 1644.6
```

.

```
Number of steps n = 9694, number of unions required m = 50195.4

Number of steps n = 9724, number of unions required m = 45784.3

Number of steps n = 9754, number of unions required m = 47330.9

Number of steps n = 9784, number of unions required m = 49748.8

Number of steps n = 9814, number of unions required m = 45638.3

Number of steps n = 9844, number of unions required m = 46525.4

Number of steps n = 9874, number of unions required m = 50509.1

Number of steps n = 9904, number of unions required m = 46921.9

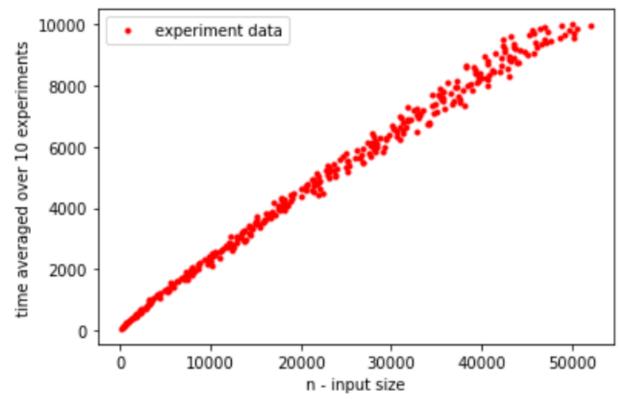
Number of steps n = 9934, number of unions required m = 48843.1

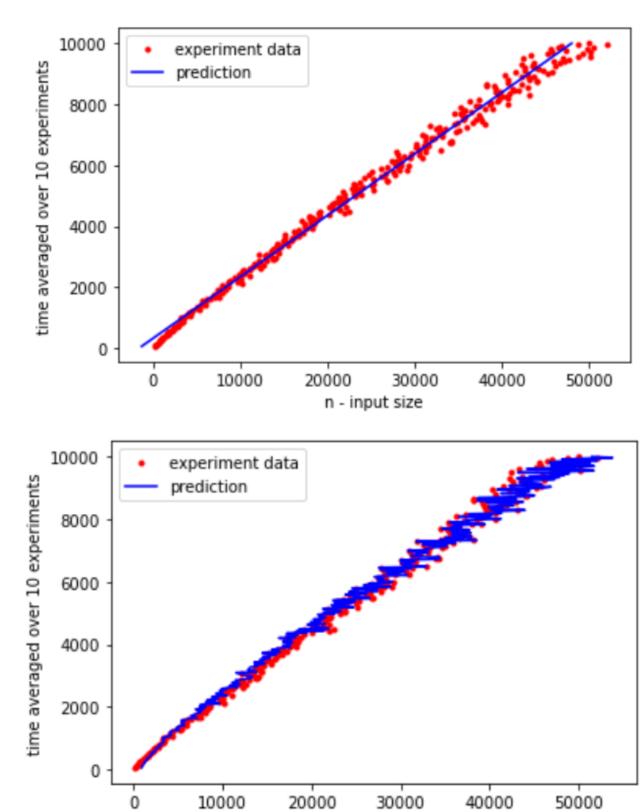
Number of steps n = 9964, number of unions required m = 52037.7

Number of steps n = 9994, number of unions required m = 49968.8

Process finished with exit code 0
```

Created a jupyter notebook and performed analysis on the output (csv format)





n - input size

- Relationship Conclusion:
 - The graph appears to be linearithmic,
 M = a * N lg(N) + b
 - N: input size
 - M: average number of pairs
 - o lg: log base 2
 - o a & b are constants
 - The detailed experiment can be found <u>here</u>
- Evidence to support the conclusion:
 - 1. Output (Snapshot of Code output in the terminal)

```
Number of steps n = 64, number of unions required m = 160.6
Number of steps n = 94, number of unions required m = 235.4
Number of steps n = 124, number of unions required m = 324.5
Number of steps n = 154, number of unions required m = 449.4
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Number of steps n = 9694, number of unions required m = 50195.4

Number of steps n = 9724, number of unions required m = 45784.3

Number of steps n = 9754, number of unions required m = 47330.9

Number of steps n = 9784, number of unions required m = 49748.8

Number of steps n = 9814, number of unions required m = 45638.3

Number of steps n = 9844, number of unions required m = 46525.4

Number of steps n = 9874, number of unions required m = 50509.1

Number of steps n = 9904, number of unions required m = 46921.9

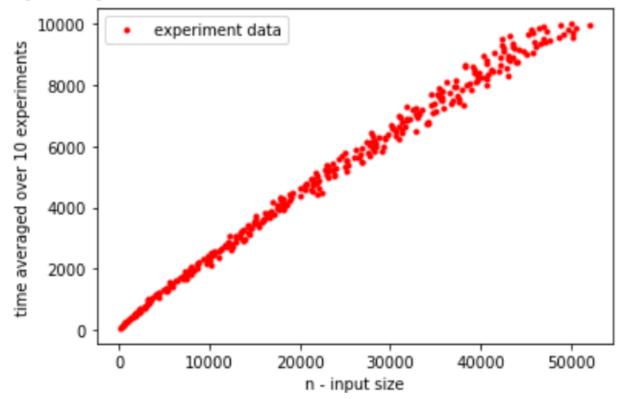
Number of steps n = 9934, number of unions required m = 48843.1

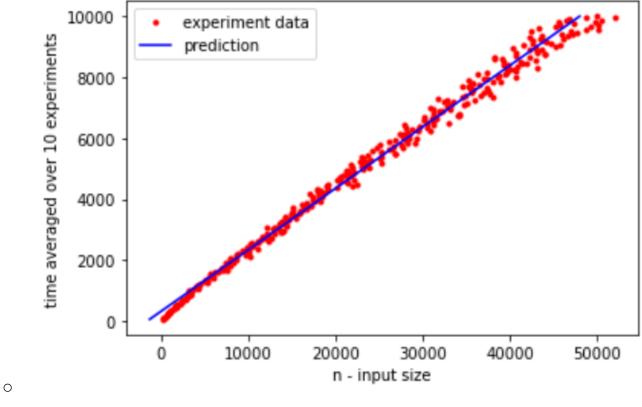
Number of steps n = 9964, number of unions required m = 52037.7

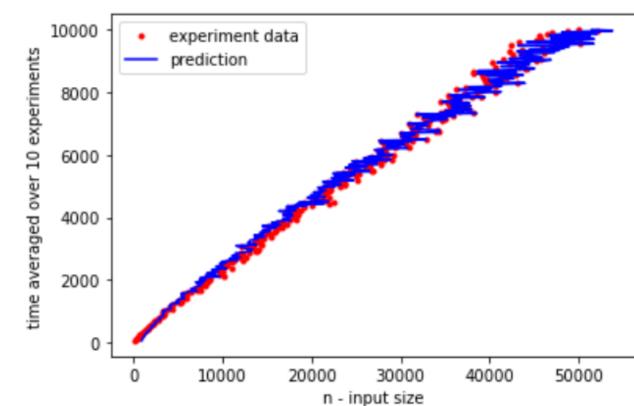
Number of steps n = 9994, number of unions required m = 49968.8

Process finished with exit code 0
```

2. Graphical Representation(Observations)







3. Unit tests result:(Snapshot of successful unit test run)

