Exist the determinant of 
$$A \neq 0$$

2 dimension =>  $\begin{bmatrix} a & b \\ c & d \end{bmatrix}^{-1} = \frac{1}{ad-bc} \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$ 

3 dimension =>  $red[A \mid I] = [I|A^{-}]$ 

To find intosection of 2 subspaces:

Let 
$$\overrightarrow{x_0} \in U \cap V$$
,  $U = \text{span} \{ [ : ], [ : ] \}$   $V = \text{span} \{ [ : ], [ : ] \}$ 
 $\overrightarrow{x_0} \in U \longrightarrow \overrightarrow{x_0} = \alpha, [ : ] + \kappa_2 [ : ]$ 
 $\overrightarrow{x_0} \in V \longrightarrow \overrightarrow{x_0} = \beta, [ : ] + \beta_2 [ : ]$ 
 $\alpha, [ : ] + \kappa_2 [ : ] - \beta_2 [ : ] : \overrightarrow{0}$ 

Then ab is & and &2 is x0 &U.

0 1 1 1 0

Similarly A affine shapees null [m1(A.').'; w1 (B').']

Linear Map: 
$$\phi(x_1+x_2)=\phi(x_1)+\phi(x_2)$$
 (incl integration, differentiation,  $\phi(\lambda x)=\lambda \phi(x)$  matrices)

# non-zeo nows in REF, or

Rank 
$$(A_{min})$$
 = # linearly independent column vectors = dimension of  $Im(A_{min})$  dim $(Im(a))$  + dim $(ker(a))$  = # of columns of A

$$\overline{\Phi}_{TS} \Rightarrow \text{transfirmation motion from } S \text{ to } T \Longrightarrow [\omega]_{T} = \overline{\Phi}_{TS}[\upsilon]_{S}$$
To find  $\overline{\Phi}_{TS} : \text{ref}(T|S) = (I|\underline{\Phi}_{TS}) \Longrightarrow I_{Ev} = [v_1...v_n]$ 

$$\overline{\Phi}_{TS} = (\overline{\Phi}_{ST})^{-1}$$

Determinant: Cotactor expension / Triangular Matrix

GE method: Multiply on by constant => Det multiple by some constant

Add two rows => Det don't change

Sup two rows => Det multiple resorve 1

Eigenvectors:  $A \stackrel{?}{\times} = _{\lambda} I \stackrel{?}{\times} = > (A - _{\lambda}I) \stackrel{?}{\times} = 0$ 

For eigenvectors to exists,  $det(A-\lambda I)=0$  , whose  $det(A-\lambda I)$  is the charpoly of A Sub-lack eigenvalue into  $(A-\lambda I)$  to find eigenvectors.

Any point moves towards eigenvelor with largest eigenvolve (PCA, Rogerank)

Diagonolization: IEV DIVE = A => D= IVE A IEV

 $= 2P^{-1}AP = 0 \quad \text{There columns of } P \text{ or eigenvectors and } D \text{ or circulates}$   $\text{Cayley Hamilton Theorem: Let } \text{ char-poly}(A) = a_0 + a_1 \lambda + a_2 \lambda^2 + \dots + a_n \lambda^n$   $\text{Hhen } a_0 + a_1 M + a_2 M^2 + \dots + a_n M^n = \vec{0}$ 

M-1 = aI+a2M+...+en MA-1

Dot Parduct: 
$$\vec{a} \cdot \vec{b} = \sum_{n=1}^{\infty} a_n x_n b_n : = (\vec{a})^n \vec{b} = |\vec{a}| |\vec{b}|_{COS} 0$$

Projection Matrix at  $\vec{a}$  onto  $\vec{b}$ :  $8(8^n 8)^{-1} \vec{b}$   $\vec{b}$  must be a basic (lineth independent)

B<sup>T</sup>  $(\vec{a} - 6\pi^2) = \vec{0}$   $(6\pi^2 = 7\pi_8 a^2)$ 
 $(7\pi^2)^{-1} \vec{b} = \vec{b} \vec{a}$ 
 $(97\pi^2)^{-1} \vec{b} = \vec{b} \vec{a}$ 

Ration of Vectors:  $(7\pi^2)^{-1} \vec{b} = \vec{b} \vec{a}$ 

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