Time Complexity

Searching

$logn=log(n^2) < n^1/2 < n < nlogn$	Search	Runtime		
Recurrence	Runtime	_	Linear	n
T(n) = S(0,n-1)T(i) = 2T(n-1)	2^n		Binary	logn
T(n) = 2T(n/2) + O(n)	nlogn		Quickselect	n
T(n) = T(n/2) + O(n)	n	_	Knuth Shuffle	n
T(n) = 2T(n/2) + O(1)	n	_	Merkel Tree	logn
T(n) = S(0, sqrt(n))T(i) + sqrt(n)	n	_	1/ th. Ch ttl	·
T(n) = 2T(n/4) + O(1)	sqrt(n)	_	Knuth Shuffle: for (1,n-1): swap(i,rand(0,i))
T(n) = T(n/2) + O(1)	logn	-		

Sorting

Algorithm	Best	Average	Worst	Stable	Space	Remarks
Bubble	n	n^2	n^2	Yes	1	Largest k items are in final k positions
Selection	n^2	n^2	n^2	No	1	Smallest k items are in smallest k positions
Insertion	n	n^2	n^2	Yes	1	First k items are sorted
Merge	nlogn	nlogn	nlogn	Yes	n	Groups of 2^x are sorted
Quick	nlogk	Median/ Rand/Check nlogk	Specific nk	No	logn	Array is partitioned around pivot T(n) = pT(n/p) + O(nlogp) = nlogn Duplicate: n^2 if no 3-way partition
Heap	nlogn	nlogn	nlogn	No	1	Build Heap: n, Get Sort: nlogn
Reversal		n(logn)^2				Quicksort with Mergesort around pivot

Data Trees

Structure	Operation	Remark		
Binary Search	h	Full Tree: n = 2^(h+1) - 1 Delete if x has 2 child: replace x with successor(x) Successor right.min() or recurse to (left of parent or root)		
Scapegoat	logn	Rebuild subtree rooted at scapregoat when triggered		
AVL	logn	h < 1.44logn or n > 2^(h/1.44) v.left Left Heavy or Balanced: right(v) v.left Right Heavy: left(v.left), right(v) Insert 2 x R Delete 2logn x R		
Trie	L	More space due to more overhead		
(a,b)	logn	split for insert, merge+share for delete		
kd	h	Alternate splitting horizontally and vertically		
Heap	logn	 Heap Ordering: Pr(parent) >= Pr(child) Complete Binary Tree Delete Swap(last), Bubble Down Array: Left(x)=2x+1, Right(x)=2x+2 		
Leftist Heap	logn	max rightRank = logn, max height = n merge (logn) merge smaller root with right child of other swap if left>right, update rightRank Insert merge with single vertex, swap <= 1 GetMax remove root, merge child Delete update rightRank (stop if left child), swap <= 1		
Augmented Structure	Remark			
Dynamic Orde Statistic	r Select le	Stores weight of subtree. During functions, rank = left.weight + 1 Select left.weight < rank: left.select(k). Else: right.select(k-rank) Rank recurse to root, if node is right child: rank += parent.left.weight + 1		
Interval Tree	Search (Sort by left endpoint. Stores max endpoint in node's subtree Search (logn) If x > max or left is null, search(right). Else: search(left) All Overlap (klogn) search node, add to list, delete node, repeat until null		
Orthogonal Range Search	Range Q 2D Rang	Store all points as leaves of a BST. Internal nodes stores max of left. Range Query (k+logn) find split node. do left & right traversals. 2D Range Query (k+(logn)^2) for node in x-tree, build y-tree using nodes in subtree. Build2D T(nlogn) S(nlogn)		

Hashing

Must redefine **hashCode** default returns address and **equals** for **get** to work

Hash Table	Insert	Search	Space	Remarks
Linked List	h+1 = 1	h+n/m = 1	m+n	Simple Uniform Hashing Assumption: Equally mapped to every bucket Worst case for search = n
Linked List w/ Resize	amor(1)	E(1)	m+n	Ideal: ==m -> Double Table . $n < m/4$ -> Half Table Increment O(n^2) . Double O(n) . Square O(n^2)
Open Addressing	h + 1/(1-a),	where a = n/m a< 1	n	Uniform Hashing Assumption: Equally mapped to every permutation Linear Probing - Clusters Double Hashing - h(k,i) = f(k) + ig(k) mod m, (m,g(k)) -> n^2 permutations !UHA Delete sets node to tombstone value for search
Fingerprint Bloom	k	k		False positive. No false negative. Delete (Counter/Tombstone) -> False negative FHT: $p = P(False\ positive)$. $p = 1-e^(-n/m)$. $n/m <= ln(1/1-p)$ BT: $p = (1-e^(-kn/m)^k)$. $opt(k) = (m*ln2)/n$

Graphs & Trees

Adjacency List O(V+E) Adjacency Matrix O(V^2) Edge List O(E)

SSSP	Runtime	Remarks
Bellman-Ford	VE	No negative cycles
Dijkstra	ElogV(AVL) E+VlogV(Fibo Heap)	No negative edge Vx(insert+deleteMin) + Ex(decreseKey)
Toposort Relax	V+E E	No directed cycles (Directed Acyclic Graph) Post-order DFS or Kahn's(nodes w/o in-edges)
BFS	V+E(Queue)	Same Weight
DFS	V+E(Stack)	No cycle (Tree)
MED	nm	Toposort + Relax

MST	Runt	ime	Idea			
Prim's	Elog E(kno	_	Add min edge on cut		MST Pro	perty
Kruskal's	ElogV Add min edge not in same tree aE(known) Sort + ExUF = ElogE + Ea(n)			M	ax edge in cycles NOT in ST In edge in cut IS in MST	
Boruvska's	Elo	Every step: Add min edge for every node ogV Search min out-edge = V+E using B/DFS Update component ID = V		= V+E	1. Ru 2. Ru	Tree (<2xOPT) In APSP & build new graph In MST and remove Iplicate edges
Rooted Directed	E		Add min incoming edge			
Union-Find	Find	Union	Union-Find	Find	Union	_
Quick Find	1	n	Weighted Union	logn	logn	_
Quick Union	n	n	Weighted Union + Path Compression	a(m,n)	a(m,n)	

Dynamic Programming

DP	Runtime	е	Subproblem		
LIS	n^2	S[i] =	S[i] = max(S[j])+1 for all j>1 and $S[j]>S[i]$. Base: $S[n]=0$		
Lazy Prize	kE		P[v,k] = max(P[w,k-1])+W(w,v) for all w points to v. Base: $P[v,0]=0$		
Vertex Cover	V		S[v,0] = sum S[w,1] , w neighbour of v S[v,1] = 1 + sum min(S[w,0] , S[w,1]) Base: S[leaf,0]=0 S[leaf,1]=1		
APSP	V^3		S[v,w,n] = min(S[v,w,n-1], S[v,n,n-1]+S[n,w,n-1]) $Base: S[v,w,0]=W(v,w)$ $P[v,w,n] = P[v,w,n-1] OR P[v,n,n-1] AND P[n,w,n-1]$		
APSF	P Ru	untime	Method		
Sparse -	+ve (V	^2)logV	Dijkstra's		
Unweigh	nted	VE	BFS		
All		V^3	Floyd-Warshall		