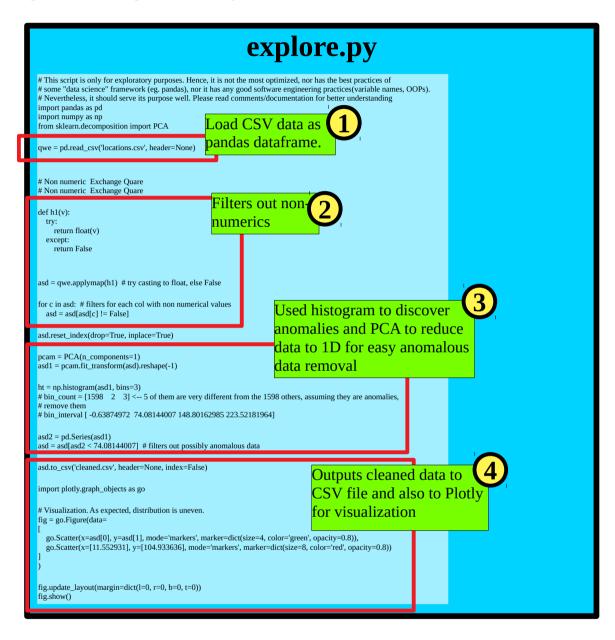
Efficient path solution for N workers

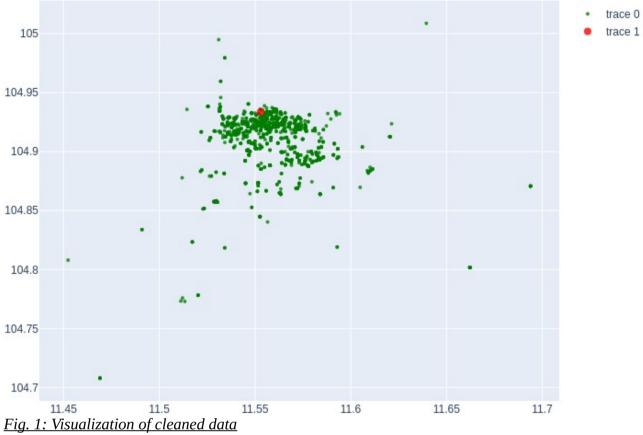
Table of Contents

1. Data cleaning	2
2. Path finding solution	
2.1. Downsample data	
2.2. Partition data to N worker count in a radial manner with evenly distributed points	
2.3. Implement actual path search algo for each partition	9
2.4. Optimize the total distance travelled for each worker and their adjacent neighbours	.10
2.5. Use optimized path search from downsampled data to find shorter paths for original data	.11
2.6. Summary	.12
3. Scaling up	.13
4. Other recommendations.	.14

1. Data cleaning

The data cleaning workflow is depicted in the following diagram. This workflow <u>is specific to the data given</u> in the assignment and <u>may not work for other cases.</u>

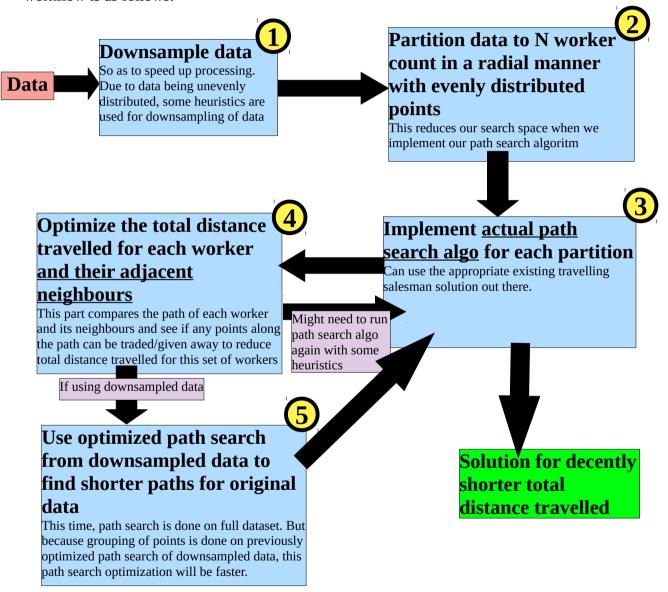




2. Path finding solution

We assume the optimization goal is to ensure total distance travelled by all workers is as short as possible (not the same as evenly distance travelled)

For the purpose of sheer processing speed and multithreading, Golang is used for this part here. The workflow is as follows:



2.1. Downsample data

To speed up solution search, downsampling is done. This downsamping method seeks to reduce data points that are similar, while keeping dissimilar data points, hence the downsampled data still maintain a fairly accurate representation of original data

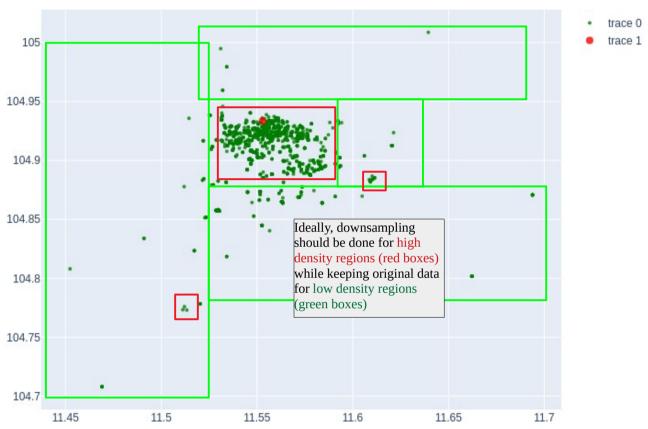
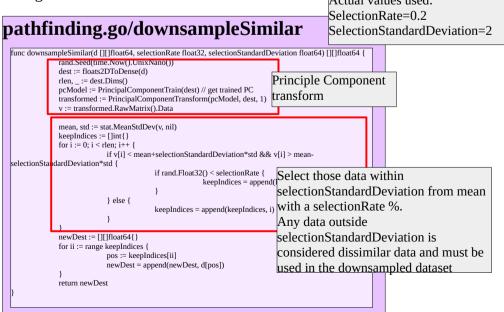


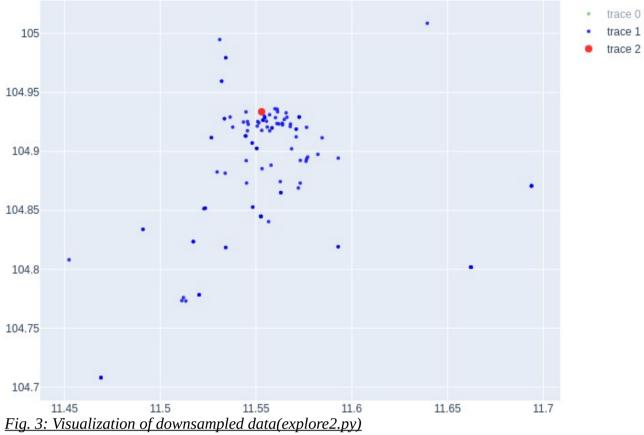
Fig. 2: Possible regions for downsampling

Actual algorithm

In the actual algorithm, data's first principle components and their mean/standard deviation is used for filtering out similar data.

Actual values used:

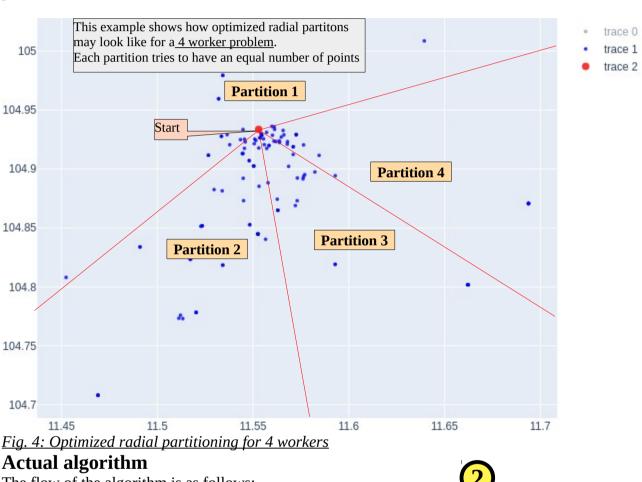


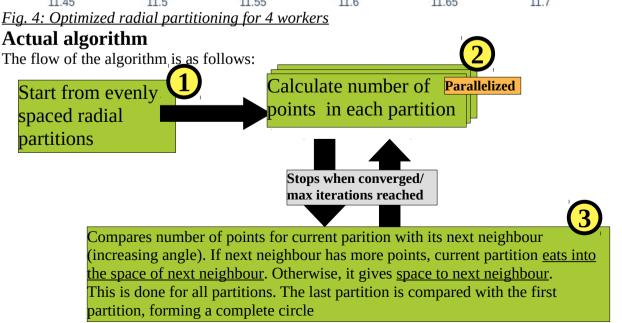


2.2. Partition data to N worker count in a radial manner with evenly distributed points

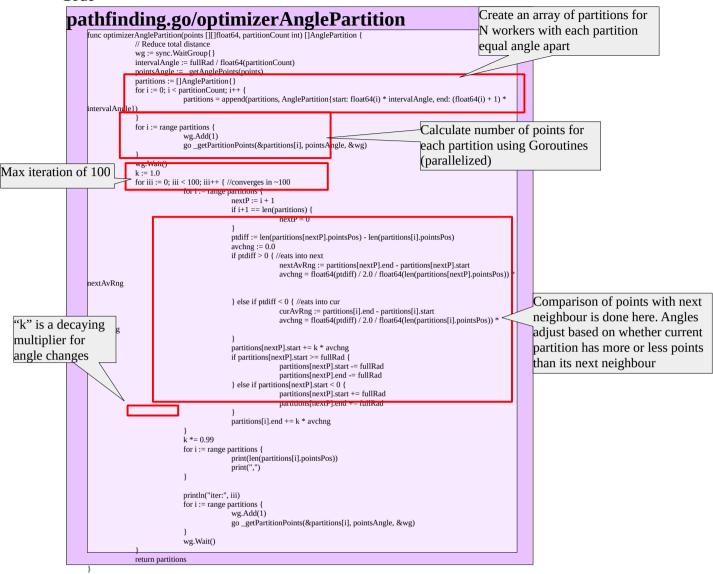
The search space for decently shorter path search for N workers at this point is still too big. Hence, it may be ideal if we start the path search on some pre-optimized partitioning heuristics. The idea is that, the points covered by each worker for decently shorter paths are rather compartmentalized so they have a low chance of cutting through the paths of adjacent workers. We can work out an estimate of this boundary region for each worker using radial lines for boundary lines for each partition.

We then optimize the angles of these radial lines towards an equal number of nodes for each partiton.





Code



Sample output for 4 worker problem:

```
3,12,198,144,iter: 0
   40 85,106,126,iter: 1
   67 91,105,94,iter: 2
   74 93,103,87,iter: 3
      104,82,94,iter: 4
  93 85,108,71,iter: 5
   41 92,85,139,iter: 6
                                 For last 3 iterations,
   72 <mark>85,110,90,iter:</mark> 7
                                 partition sizes are
   80 95,90,92,iter: 8
                                 unchanged. The results have
                                 converged.
  89,89,90,89,iter: 97
  89 90,89,89,iter: 98
  89,90,89,iter: 99
Columns represent different
workers/partitions.
Number of points for <u>partition 1</u> at
each iteration.
```

2.3. Implement actual path search algo for each partition

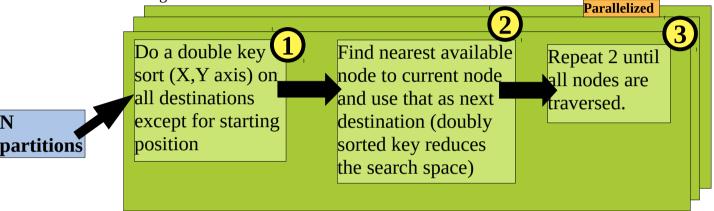
Using the partitioned points from 2.2, we can implement a path search for each worker/partition. In this solution, a naive path search using nearest neighbour approach was used.

This means the solution is **not optimal**, **but reasonable**.

However, it is <u>recommended to look for better existing solutions</u> for this (will need time to find Golang implementations, or will have to write my own)

Actual algorithm

The flow of the algorithm is as follows:



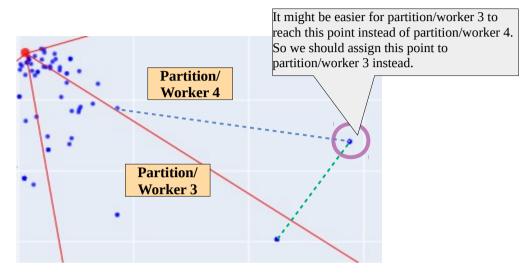
```
pathfinding.go/_findShortestDistanceWalk
          nc _findShortestDistanceWalk(startpt []float64, points [][]float64 [][]float64 {
    // this assumes walk from 0,0
    // double index, sort 1st index, find nearest neigh
                        // branch-and-bound
                                                                                                                                Nearest neighbour path
                        sort.Slice(points, func(i, j int) bool {
                                                                              Double sort
                                        return points[i][1] < poi
                                                                                                                                search using L2 Norm
                        sort.Slice(points, func(i, j int) bool {
                                        return points[i][0] < points[j][0]
                        start := [][]float64{startpt}
                       points = append(start, points...)
                       path := make([]int, len(points))
used := make([]bool, len(points))
                       for ii := 0; ii < len(points)-1; ii++ {
                                        curPathPos := ii
                                        curNode := path[curPathPos]
                                        shortestDist := -1.0
                                        for i := 1; i < len(points); i++ {
                                                         if !used[i] {
                                                                         if shortestDist < 0 {
                                                                                          shortestDist = _distL2(points[curNode], points[i])
                                                                          path[curPathPos+1] = i
} else if math.Abs(points[curNode][0]-points[i][0]) < shortestDist {
                                                                                          d := _distL2(points[curNode], points[i])
if d < shortestDist {</pre>
                                                                                                          path[curPathPos+1] = i
shortestDist = d
                                                                          } else if points[i][0]-points[curNode][0] > shortestDist { //first index already > current shortest dist
        ignore rest
                                        used[path[curPathPos+1]] = true
                       pathNodes := [][]float64{}
for i := range path {
                                        pathNodes = append(pathNodes, points[path[i]])
                       return pathNodes[1:1
```

Sample output for 4 worker problem:

```
Zero centered nearest neighbour path of worker 0
                                                      All these are coordinates
-9.881747e-004 -1.522353e-003
                                                     relative to the starting point
-2.181221e-003 -2.666762e-003
-2.916504e-003 -9.577773e-004
+9.859312e-004 +1.720140e-003
+3.196548e-003 +4.231431e-004
Zero centered nearest neighbour path of worker 1
+5.390953e-003 -2.216627e-003
+5.390953e-003 -2.216627e-003
+7.231544e-003 -4.993727e-003
+6.806206e-003 -5.695631e-003
+6.806206e-003 -5.695631e-003
Zero centered nearest neighbour path of worker 2
+2.107452e-003 -2.857497e-003
+2.107452e-003 -2.857497e-003
+2.108406e-003 -2.857497e-003
+1.387428e-003 -3.788283e-003
+1.387428e-003 -3.788283e-003
Zero centered nearest neighbour path of worker 3
-3.444445e-004 -5.131056e-003
+7.169950e-004 -7.145216e-003
+7.169950e-004 -7.145216e-003
-8.313776e-005 -8.564284e-003
-1.050723e-004 -8.564284e-003
```

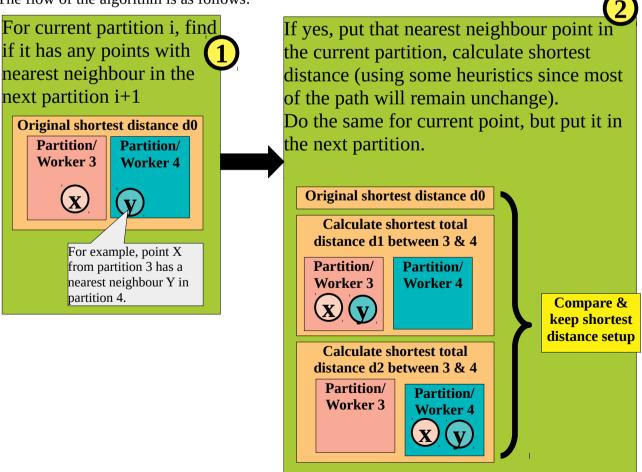
2.4. Optimize the total distance travelled for each worker and their adjacent neighbours

While decently shorter path is implemented within each partition, the total decently shorter travelled distance by all the workers is still unoptimized. Hence we need this step to reduce global decently shorter travelled distance.



Actual algorithm

The flow of the algorithm is as follows:

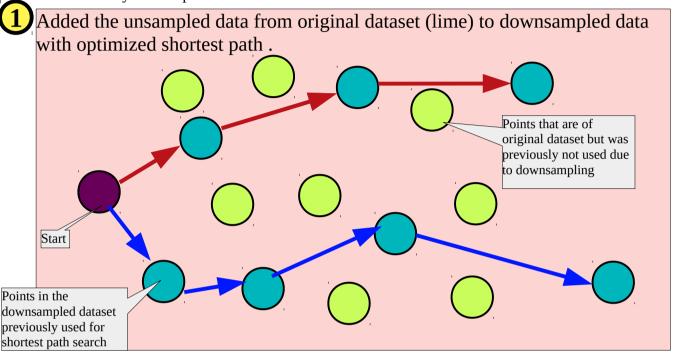


Actual code not yet implemented.

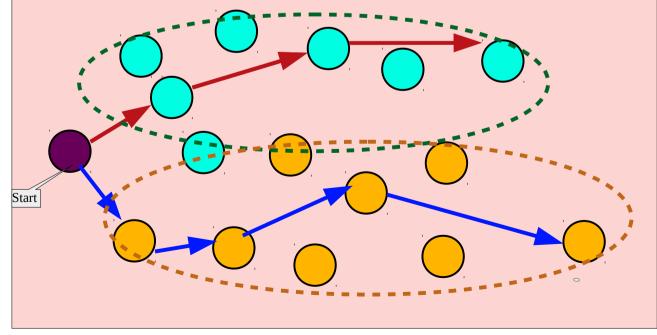
2.5. Use optimized path search from downsampled data to find shorter paths for original data

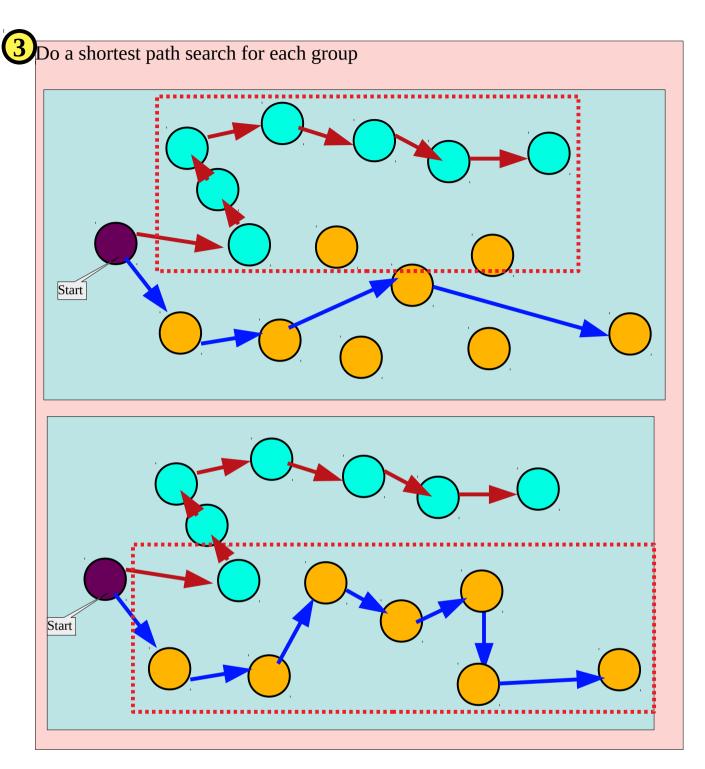
Because we used downsampled points to speed up optimization, the result is not entirely reflective of the actual solution.

Now we have an optimized solution from the downsampled points, we use this result to help us find our decently shorter paths solution for the actual dataset.



Create locally nearest neighbour groups where <u>each previously unsampled point</u> is grouped together with its nearest downsampled point non-starting point(A starting point is common to all paths, so it is pointless to put any points together with it) along with all other downsampled points that share the same path





This will yield a decently "Shorter" path search. To ensure better results, we can perform optimization across neighbouring partitions again as we did in 2.5.

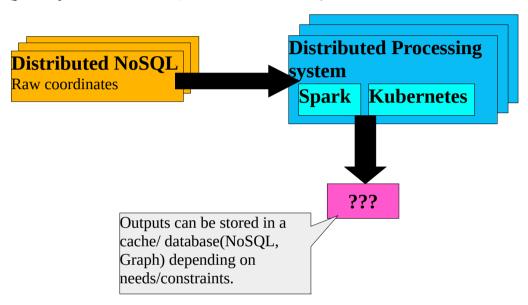
Actual code not yet implemented.

2.6. Summary

The steps taken from 2.1. to 2.5. drastically reduces search space and utilizes parallelism to speed up solution search. The final solution would be a decently shorter total distance travelled. To find actual shortest distance will require computing all possible path permutations for a NP-hard problem, which may not worth to find in reasonable time/resources.

3. Scaling up

- 1) By using a downsampled approach to this problem, we have added a possibly useful technique to reduce search space for much bigger problems. (eg. Finding decently shorter paths with 1 million data points and 1000 workers but using only 10,000 downsampled points to help us find a decently good solution).
- 2) Depending on real world constrains/needs, we may be able to change parallelized logic to distributed codes across multiple machines (Spark), as we could also do with the data storage (possibly distributed NoSQL for raw coordinates)



4. Other recommendations

- 1) Data sanitization should be done upstream. Eg. Coordinates should only contain floats if they are stored in a database.
- 2) Path search solution does not take into account other real life variables such as traffic conditions, laws, personal travelling preference, renumeration package et cetera. So it should not be treated as the only way for delivering packages.