

# TOUSE: A Fair User Selection Mechanism Based on Dynamic Time Warping for MU-MIMO Networks

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## Abstract

Multi-user Multiple-Input and Multiple-Output (MU-MIMO) has potential for prominently enhancing the capacity of wireless network by simultaneously transmitting to multiple users. User selection is an unavoidable problem which bottlenecks the gain of MU-MIMO to a great extent. Major state-of-the-art works focused on improving network performance by using Channel State Information (CSI), however, the overhead of CSI feedback becomes unacceptable when the user population is large. Some work does well in balancing tradeoff between complexity and achievable capacity but lack of consideration of fairness. Current work universally ignore the rational utilizing of time resource, bring the improvement of network throughput to a standstill. In this paper, we propose TOUSE, a scalable and fair user selection scheme for MU-MIMO. The core design of TOUSE is its dynamic time warping based user selection mechanism for downlink MU-MIMO, which could make full use of concurrent transmitting time. TOUSE also presents a novel data-rate estimation method without any CSI feedback, which provide supports for user selection. Simulation result shows that TOUSE significantly outperforms traditional contention-based user selection schemes in both throughput and fairness in indoor condition.

*Keywords:* MU-MIMO, user selection, fairness, dynamic time warping

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## 1. Introduction

Multi-user Multiple Input Multiple Output (MU-MIMO) have attracted a huge amount of attention already because it enables better spatial reuse. The network capacity is enhanced by send frames to multiple single-stream users concurrently. Prior to 802.11ac, traditional 802.11 protocol limits every transmission was only sent to a single user, which cannot full utilizing spatial resources supported by multiple antennas AP. Multi-user transmissions are a new technology within 802.11. By using MU-MIMO [1], AP is equipped with multiple antennas, and could transmit to multiple users at one time. Due to these abilities, MU-MIMO has the potential to change the way Wi-Fi networks are built and achieve improved capacity gains.

A MU-MIMO downlink system, in theory, its capacity gains increases linearly with the number of transmit and receive antennas. But in practice, the number of antennas is limited for several reasons, and the inter-user interference could not be ignored. These lead a series of important problems emerged. First, how an AP select a beamforming group of users which could transmit simultaneously. Second, how to determine the size of the beamforming group. Different beamforming group selection lead to variant transmitting rate, then influence the overall network performance. Unwise selecting method may results in a huge waste of space-time at every single transmitted slot, and causes the problems of fairness and complexities. To make an optimal selection, we should choose a metric like sum rate as a criterion to process the feedback information like CSI (Channel State Information) or SNR (Signal-Noise Ratio), design an efficient scheduling scheme based on various data we obtained.

Substantial research [2] has provided the solving method to the user selection problem for MU-MIMO. Most solutions select the optimal beamforming groups based on understanding the full CSI of all the potential user. CSI presents the characteristics of the channel including fading distribution, average channel gain and spatial correlation, all are important to beamforming group select. However, CSI is calculated by estimating the training sequence from AP, then users

feedback it to the AP. Reducing the CSI overhead becomes an important issue in MU-MIMO since this is a long and complexity process [3]. Although numerous optimization schemes of feedback are proposed, like compression algorithms [4], the overhead of CSI feedback still huge sometimes and severely affect the performance of network, since the overhead grows linearly with the number of users. Even worse, infrequent CSI feedback results in outdated, which may lead to the inter-user interference. It is convenient to select beamforming group within CSI, but intolerable for MU-MIMO system with unacceptable feedback overhead.

In fact, these challenges have motivated previous works to find better possible solutions for user selection. In [3], the author proposed a distributed contention mechanism that singles out the best user to feedback its CSI. Narendra [5] present pre-sounding user selection algorithm using only available pre-sounding information instead of post channel sounding information, solved the problem of feedback overhead at a certain extent.

In this paper, we propose *Time Optimal User Selection based on Effective SNR* (TOUSE), a scalable and fair user selection scheme for MU-MIMO networks to achieve higher capacity. To sum up, our main contributions are as follows:

- We design a novel dynamic time warping based user selection mechanism to increasing throughput under the fairness constraint, and propose a algorithm to solve it.
- We adopt a low complexity feedback mechanism to obtain the available channel information and presents a novel data-rate estimation method base on the information of effective SNR [6] without any CSI feedback.
- TOUSE has ability to adapt different network channel quality, no matter low SNR region and high link qualities. It also suitable to dynamic network, since it select user after channel sounding is completed and acquiring real-time information.

- Finally we experimentally evaluate the performance of TOUSE. Result shows that, on average, the gain of TOUSE is  $1.5\times$  over traditional Random user selection scheme in 3-antennas AP scenarios. Compared with PUMA scheme [5], network capacity gain is similar but TOUSE provides users fair selection opportunities.

The rest of this paper is organized as follows. In Section II, we present background of user selection in MU-MIMO. Section III provides an overview of the components of TOUSE. Section IV evaluates the performance of TOUSE with experimentation. Then we describe related work in Section V and Section VI concludes the paper.

## 2. BACKGROUND AND CHALLENGES

### 2.1. MU-MIMO System Model

In a downlink MU-MIMO systems, consider a single-cell MIMO with a single base station serves for  $N$  users. The base station is equipped with  $M$  antennas and the client with one or more receive antennas. We assume that AP send frames to a set of selected single antenna users  $S$  called beamforming group at the same time, which satisfies  $K = |S|$ ,  $K \leq M$ . Due to the multi-user interference at the client side, it is essential for AP to precode outgoing signals to minimize interference among simultaneous streams. Owing to its low complexity, AP apply ZFBF (Zero-forcing beamforming) [7]. In ZFBF, user streams are separated by different beamforming direction. Let  $x_k$  denotes the data symbol sending to user  $k$ ,  $\mathbf{w}_k$  be the beamforming weight vector, and the  $\mathbf{p}_k$  presents the transmit power. Assume  $\mathbf{h}_k$  is the  $1 \times M$  channel state vector between transmit antennas and receiver  $k$ . Define  $\mathbf{W} = [\mathbf{w}_1, \mathbf{w}_2, \dots, \mathbf{w}_K]$ ,  $S = \{s_1, s_2, \dots, s_K\}$ , the transmitted signal  $X = \sum_{k=1}^K \sqrt{p_k} \mathbf{h}_k \mathbf{w}_k x_k$ . Then, let  $n_k$  denotes the noise level of user  $k$ , we get the received signal vector as:

$$y_k = \sqrt{p_k} \mathbf{h}_k \mathbf{w}_k x_k + \sum_{j \neq k, j \in S} \sqrt{p_j} \mathbf{h}_k \mathbf{w}_j x_j + n_k, k \in S. \quad (1)$$

To eliminate the interference from other beamforming frame streams, ZFBF should satisfy the zero-interference condition:  $\mathbf{h}_k \mathbf{w}_j$  for all receivers  $j \in S, j \neq k$ . So that receiver  $k$  only gets its symbol  $x_k$ . Let the channel state matrix  $\mathbf{H} = [\mathbf{h}_1^T, \mathbf{h}_2^T, \dots, \mathbf{h}_K^T]^T$  and the beamforming weight matrix  $\mathbf{W} = [\mathbf{w}_1, \mathbf{w}_2, \dots, \mathbf{w}_K]$ . One optimal choice of  $\mathbf{W}$  that satisfies zero-interference condition is the pseudo-inverse of  $\mathbf{H}$ :

$$\mathbf{W} = \mathbf{H}^+ = \mathbf{H}^*(\mathbf{H}\mathbf{H}^*)^{-1}. \quad (2)$$

Thus, another problem that need to be consider is power allocation. For simplicity, we adopted ZFBF-EP scheme where the transmitter allocates equal power to its users.

## 75 2.2. Impact of User Selection Mechanism

From above section, the performance of ZFBF is highly dependent on the channel vectors from transmitter to receiver. When the channel vectors of different receiver is uncorrelation with each other, it is most likely to improved the network capacity gain. It was proved by the experimental [8] for indoor wireless  
80 network. The network spatial multiplexing gain of ZFBF can be increased by a high number of transmitter antennas, whatever the location of receivers in indoor environment.

Select beamforming group is one of the key issues which is related to the performance of MU-MIMO system. From Eq. (1), the SNR of each receiver  
85 depends on its group member. If one receiver's channel vector is orthogonal to another, it will cause limit interference when transmit together. The research [8] also proved that ZFBF different SNR regions cause different capacity improved, and number of beamforming group is other factor. The optimal size of beamforming group is depends on the link state of member. The state of queue  
90 and other information should be taken into account as well.

## 2.3. Challenges in User Selection

User selection is a complicated process. Although optimal transmit beamforming group can improve the network capacity, but high computational over-

head is unacceptable. Before each downlink transmission, the AP needs to  
 95 obtained the CSI from the users' feedback. During the feedback process, AP  
 sends a training sequence to the target users, users calculate the CSI by the  
 training sequence and feedback the CSI to AP one by one. Due to this mecha-  
 nism, overhead by CSI feedback also increased with number of users. Research  
 [3] present that even with 20 users, the channel time cost of existing schemes  
 100 can be comparable to or even exceed that of actual data transmission.

There are a number of factors which a user selection mechanism should  
 be consider. First, how to determine the size of beamforming group. In a  
 transmission time slot, AP beamforming to send frame to a set of users  $S$  and  
 satisfy  $K \leq M$ . In [8], it proved that maybe  $K = 3$  have a better network  
 105 performance than the case of  $K = 4$ . The authors of [5] proposed a aggregate  
 throughput to select the combination mode. Second is the complexity reduction.  
 Instead of exhaustive search over all possible combination, mostly research adopt  
 the method of local optimal to solve this problem, which performs inefficiently.  
 It is hard to achieve both low complexity and high performance, the tradeoff  
 110 between performance and complexity is essential [9]. Other solution is to reduce  
 the feedback overhead, which is not the way to the underlying problem. The  
 last challenge is how to realize fairness. A simply way to improving the network  
 throughput is just selecting the users which have a high link quality. But it  
 might not be fair for all users [3]. Sometimes, it will caused starvation.

### 115 3. TOUSE DESIGN

#### 3.1. Design Overview

The design inherits the advantages of throughput fairness and low complex-  
 ity in user selection, it also improve the network capacity gain. TOUSE present  
 a new preference metric which aim to make full use of time resource and guar-  
 120 antees fairness. Besides, instead of requires CSI feedback, TOUSE provides a  
 mechanism that AP just obtained effective SNR from users to make decision.  
 This mechanism has limited time overhead compared to the CSI feedback.

Before given the detail of TOUSE, there are some available pre-sounding information to introduce. In MU-MIMO system, AP own the information of system state and queue state before channel sounding or communication. For each transmission, AP knows the hardware configuration, like available number of transmit antennas  $M$ , number of clients' receive antennas. AP also aware of the queue state information for each users, like each user's backlog or queue size. The amount of available data directly affects the data transmission time in each transmission, which used for user selection. By leveraging this information, TOUSE design a performance metric to select optimal beamforming group. The TOUSE works as follows:

1) First, the AP announces its intention for MU-MIMO downlink transmission through the NDP Announcement frame, and it is the time to start the MU-MIMO sounding process for users. AP random select a first user to the optimal beamforming group, which can achieve channel access fairness.

2) Then, each users  $k$  estimates its CSI, independently based on the NDP Announcement frame. AP obtain the effective SNR feedback which is calculated by each client from the CSI. This is the first round of TOUSE user selection.

3) In subsequent round, AP estimates the potential datarate for each competitors based on the effective SNR and current beamforming group. Then calculates time of data transmission for each users combined with the pre-sounding information, and get global time of transmission slot based on selected users and candidate user.

4) Given transmission time of each data transmission and information of selected users. According to the constraint condition (describe in section D), the AP select the best candidate which can optimal total network capacity for this transmission slot.

5) The one who is satisfies the optimal constraint, which means its could be transmit with the member of beamforming group. The AP added it to the beamforming group.

6) Repeat steps (3)-(5) until the size of beamforming group reaches the maximum transmit number  $M$ , or there is none best choice left. Then, AP

would terminate the user selection process.

155      Next, we are going to present TOUSE more detail.

### 3.2. Effective SNR

In order to accurately predict the packet delivery rate, a key point is using effective SNR (ESNR) [6]. It is a simple, easy to deploy, broadly useful, and accurate method. Using effective SNR makes packet delivery predictions for 802.11n MIMO rates, plus choices of transmit power and antennas. During the process, we use CSI as the piece of input, which provides the SNR values to use for each subcarrier. It is a much richer source of information than the RSSI, and provides the opportunity to develop a much more accurate model.

The effective SNR calculate is not simply the average subcarrier SNR. Instead, it is biased towards the weaker subcarrier SNRs because it is these subcarriers that produce most of the errors. We can compute the effective SNR by averaging the subcarrier BERs and then finding the corresponding SNR. That is formulate as follows:

$$\text{BER}_{eff} = \frac{1}{S} \sum \text{BER}(snr_s); \quad (3)$$

$$\text{ESNR} = \text{BER}^{-1}(\text{BER}_{eff}). \quad (4)$$

$\text{BER}^{-1}$  presents the inverse mapping, from BER to SNR, and  $S$  means number of subcarriers. We use the  $\text{BER}_{eff}$  to denote the average BER across subcarriers, and  $snr_s$  is the SNR values of each subcarrier.

### 3.3. MU-MIMO User Datarate Estimate

In TOUSE, the key problem is to predict the per-user packet delivery rate. During this process ESNR evaluate is essential for each transmission. Then the AP obtain data rate for each user from the ESNR by using MCS table. However, There still a problem When AP transmit to multi-receivers at the same time, the inter-user interference is unavoidable. It will influence the total capacity of network.



1) *Traditional Rate Estimation*: One of the classic approach to calculate the aggregate capacity is using channel state matrix. The sum rate ( $R$ ) [7] achieved by following scheme:

$$R = \max_{\mathbf{w}_k, P_k} \sum_{k=1}^K \log \frac{1 + \sum_{j=1}^K P_j |\mathbf{h}_k \mathbf{w}_j|^2}{1 + \sum_{j=1, j \neq k}^K P_j |\mathbf{h}_k \mathbf{w}_j|^2} \quad (5)$$

subject to  $\sum_{k=1}^K \|\mathbf{w}_k\|^2 P_k \leq P.$

This method is accurate but quite complex. It requires channel state matrix as input. As mentioned before, computational overhead is unavoidable by using CSI. Given the significant overhead of CSI feedback, the AP need more reasonably utilization of this information to maximize the network performance. This leads to the system more complexity and hard to implement, which is opposite to what we think.

2) *ESNR based Rate Estimation*: TOUSE's rate estimation method is based on theoretical MU-MIMO system scaling. In order to facilitation and precision, AP obtain the receivers' ESNR which is calculated by users, and estimate the data delivery rate by MCS-SNR table. Besides, we need quantify the influence to SNR by inter-user interference when AP transmitting to multi-users. As mentioned before, in ZF model, user only receives its desired symbol owing to the composite effects of precoding and channel distortion. The main features of ZF is complete interference cancellation with full CSI, but also caused the noise amplified [10].

Many works [11] provide the analysis to network capacity performance impact by ZF-precoded system. But most of methods are not suitable for our purposes because require too much information. By the ZF criterion, there is residual interference because the beamformers are based on imperfect CSI. The SINR for selected user  $k$  is (proposed in [12])

$$\text{SINR}_k = \frac{\text{SNR}_k \|\mathbf{h}_k\|^2 \cos^2(\angle(\mathbf{h}_k, \mathbf{w}_k))}{1 + \text{SNR}_k \|\mathbf{h}_k\|^2 \sum_{j \neq k} \cos^2(\angle(\mathbf{h}_k, \mathbf{w}_j))} \quad (6)$$

and the corresponding sum rate is  $\sum_{k=1}^n \log_2(1 + \text{SINR}_k)$ . Where  $\mathbf{w}_k$  presents the precoding unit-norm beamforming vector for user  $k$  is chosen in the direction

of the projection of  $\mathbf{h}_k$  on the nullspace of  $\mathbf{h}_j$ ,  $j \neq k$ .

Eq. (6) present SINR variation for each users, but there is the same problem of using information of CSI as input. As Eq. (6) shows that the interference by other receivers in beamforming group is related to per-receiver SNR. Besides, the system state information also has great influence on the SINR, like transmit antennas number  $M$  and the size of current transmit users group  $K$ . It is also necessary to note that this paper focuses on the user equipped with a single antennas. In [13] and [12], it proved that in order to achieve the full multiplexing gain of  $M$ , the transmitter must have perfect channel knowledge in order to choose the zero-forcing beamforming vectors. However due to the imperfection in this knowledge, there inevitably will be some multi-user interference, which leads to performance degradation. Therefore, we proposed a suitable per-receiver SINR estimation method as following.

$$\text{SINR}_k = \frac{\text{ESNR}_k - \text{ESNR}_k \cdot 2^{-B}}{1 + \text{ESNR}_k \cdot 2^{-B}} \quad (7)$$

$$B = ((M - 1)P)/(3(K - 1))$$

Where  $M$  is the number of transmit antennas, present the degree of freedom of MU-MIMO system.  $K$  denote the number of size of beamforming group, which leads an exponential increase in the multi-user interference.

195 In TOUSE, we assume that each transmit antennas have a same transmit power  $P$ . From Eq. (7), we know that the value of per-receiver SINR is inherently less precise than Eq. (5). But it can provides a sufficiently accurate result for TOUSE user selection process as well, and easy to implemnet. Then we can get the transmit data rate  $rate_k$  for user  $k$  based on the SINR for each  
200 receivers from the MCS-Rate (Table 1).

3) *TOUSE Rate Estimation Analyse*: In Eq. (7), the TOUSE's SINR estimation method only requires the system hardware configurations  $M$ , number of users  $K$  and the ESNR calculated by per-user. This estimation scheme can accommodate with the network dynamic by using ESNR, and avoid CSI feedback  
205 overhead at the same times.  $2^{-B}$  presents the multiplexing gain of inter-user in-

interference, and it increased linearly with the transmit power. Thus, MU-MIMO SINR should relatively with  $B$ .

During the rate estimation process, TOUSE first measure the channel state information, and calculate the ESNR by each receivers. We estimate the per-  
 210 receiver SINR based on the size of beamforming group. Then the data delivery rate (for 90% packet reception rate) is obtained by using the MCS-SNR table provided by the standard (as shown in Table 1).

Table 1: Minimum SNR required

MCS	Rate (Mbps)	SNR (dB)
0	6.5	1.1
1	13.0	4.1
2	19.5	6.7
3	26.0	9.6
4	39.0	12.8
5	52.0	17.2
6	58.5	18.4
7	65.0	19.7

### 3.4. User Selection Mechanism

In this section, we present the user selection mechanism to maximum the  
 215 aggregate throughput of network. To achieve this goal, we design two constraint conditions for optimal beamforming group selection. At the same time, we need to improve fairness of channel access for each users.

Previous section give the data rate estimation method. In order to calculate the data transmission time for a transport connection, key point is total delivery data and network overhead (such as channel sounding and ESNR feedback overhead). These pre-sounding information can obtain by AP queue state or network measurement. So we can calculate the total throughput  $R$  for each transmission slot, which is the performance metric to user selection mechanism. It is formula as following,  $L$  denote the total transmission data at a time slot,

$T_s$  is the maximum transmission time of all transmission and  $T_o$  is the network overhead.

$$R = L/(T_s + T_o). \quad (8)$$

In order to achieve the two design goals: throughput increase and fairness ensures. We design a similarity matching algorithm for optimal user group selection based on dynamic time warping [14]. Before present time constraint condition, we would like to give some definition. First,  $S = \{s_1, s_2, \dots, s_k\}$  denote the current selected beamforming group and  $|S|$  is the size of  $S$ ,  $c$  denote a user which is candidate for  $k + 1$  solution from the unselected users, but still waiting for check by constraint condition.  $T(c)$  present the transmission time requirement that AP transmit the queue data to user  $c$ . Here shown the first constraint condition : to maximum the aggregate throughput.

$$\begin{cases} \frac{T(c)}{T(\max(S))} < \frac{1}{(ratio(c)-1)} & T(\max(S)) \leq T(c) \\ \frac{T(\max(S))}{T(c)} < \frac{1}{(ratio(\max(S))-1)} & T(\max(S)) > T(c) \end{cases} \quad (9)$$

Where  $\max(S)$  present the one with maximum data transmission time in select-  
ed group,  $T(\max(S)) = \max(L_i/rate_i)$ ,  $i \in S$ ,  $ratio(c)$  is the ratio between the  
220 datarata of user  $c$  at the mode of  $K = |S|$  and  $K = |S| + 1$ . The size of beam-  
forming group  $K$  has a big impact on the transmitting rate of each user. For  
example, user  $u$  from beamforming group which the size is  $K$ , the transmission  
rate is  $a$ , and rate equals  $b$  in the mode of  $K + 1$ , then  $ratio(u) = a/b$ . Eq.  
(9) is a throughput constraint for network capacity, judgement the benefit from  
225 user  $c$  in this transmit time slot. Then we make choices whether put it into the  
beamforming group or just throw it away. As we talked before, increase the size  
of beamforming group leads to inter-user interference. So we should judge the  
total network throughput when put candidate user  $c$  into beamforming group.

Next we give the other constraint to make full utilization of space-time re-  
source.

$$T(c) \leq \frac{M}{K} \cdot T(\max(S)). \quad (10)$$

Where  $K = |S|$  denote the size of beamforming group which is received transmit  
 230 date from AP concurrently. This restriction allows our algorithm to find an  
 optimal match between given transmission time of selected users. For example,  
 in a transmit slot, AP transmit to *user1* and *user2*, while the transmission  
 time of *user1* is 1s and *user2* is 100s. In this case, compared with *user2*, the  
 transmission time of *user1* is too small, which is not a best choice to bind them  
 235 together for total network.

Based on the idea of dynamic time warping, we make sure that find an  
 optimal beamforming group which is benefit to the capacity of network by these  
 restrictions. We selected user  $c$  depend on the similarity of transmission time  
 between candidate user  $c$  and current beamforming group. We choose a first  
 240 user in beamforming group at random, then we selected the other member of  
 beamforming group which has similar transmission time with the first one. The  
 selection process will go through the total unselected user until we find a solution  
 or nothing, which means current beamforming group is a optimal solution at a  
 transmitting slot.

TOUSE user selection mechanism based on data transmission time, which  
 245 means the contention is fairness in term of SNR of user. Next section will  
 present the fairness performance of our mechanism. Eq. (8) show that the  
 network overhead limits the performance of a MU-MIMO transmission. Along  
 with the increase of beamforming group size, the amount of total transmit data  
 250  $L$  grows. The larger amount of network overhead is create meanwhile. So it is  
 an important issue to get the trade off between of aggregate data and network  
 overhead.

### 3.5. TOUSE Algorithm

In order to seek an optimal combination to improve the network capacity,  
 255 TOUSE use the two constraints which is mentioned before. Given the set of can-  
 didate receivers  $C = \{c_1, c_2, \dots, c_n\}$  which to contend for the transmission slot.  
 TOUSE select the best combination as beamforming group for AP to simulta-  
 neous downlink transmissions. Here is the TOUSE user selection algorithm.

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**Algorithm 1** TOUSE User Selection

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**Input:**

The set of single antenna users,  $C$ ;

The number of transmit antennas and transmit power,  $M$  and  $P$ ;

**Output:**

The set of solution receivers,  $S$ ;

The size of solution group,  $k = |S|$ ;

**Begin:**

```
1: while  $k \leq M$  and  $C \neq \emptyset$  do
2:   if  $k = 0$  then
3:     Selecting a solution  $s_1 \in C$  at randomly from  $C$ ;
4:      $C = C - s_1$ ,  $S = S + s_1$ ;
5:   else
6:     repeat
7:       Selecting a optimal receiver  $c_k \in C$  matches  $S$ ;
8:       Judging  $c_k$  by two constraint: Eq. (9), Eq. (10);
9:       if  $c_k$  satisfies the two constraint then
10:         $S = S + c_k$ ;  $C = C - c_k$ ;
11:      end if
12:    until Get the solution  $s_k = c_k$  or none of optimal solution  $s_k \notin C$ 
      meets the condition;
13:   end if
14:   if  $s_k \notin C$  then
15:     None of receiver  $c \in C$  matches  $S$ ;
16:     Break, //terminate the process of user selection;
17:   end if
18: end while
```

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The algorithm (1) shows our user selection process. Given the candidate set, TOUES output the solution as the beamforming group  $S$ ,  $|S| \leq M$ . In the first round, we selecting a solution at random from candidate set, which is meet the require of competition fairness. The time constraint condition process is repeated until select a receiver to matching already solution group, or none of optimal solution in candidate receivers, as lines 6-12 in Algorithm 1. During the process of searching solution, we judge from the time closest receiver compared with solution set. This searching method was reduced the complexity of TOUSE and a optimum result was acquired rapidly and exactly.

#### 4. PERFORMANCE EVALUATION

In this section, we further perform simulations to evaluate the performance of TOUSE in indoor environment. The simulations are aiming to answer the following questions:

- How much capacity gain can TOUSE achieve in comparison with existing schemes?
- How does TOUSE perform in terms of fairness compared with existing schemes?
- How much the number of transmit antennas impact on TOUSE?
- Does TOUSE scale?
- Could TOUSE work in different channel quality region?

For performance comparison, we implemented three state-of-the-art user selection schemes: (1) Pre-sounding User and Mode selection Algorithm (PUMA) [5]. PUMA allows MU-MIMO system to efficiently transmit multiple streams by using pre-sounding information. It estimates the throughput of all potential user group combinations. (2) Mixed PUMA algorithm (PUMA-MIX). PUMA employed exhaustively searched to find the optimal user group. We replaced with our iteration method for comparison in simulations. (3) Random User

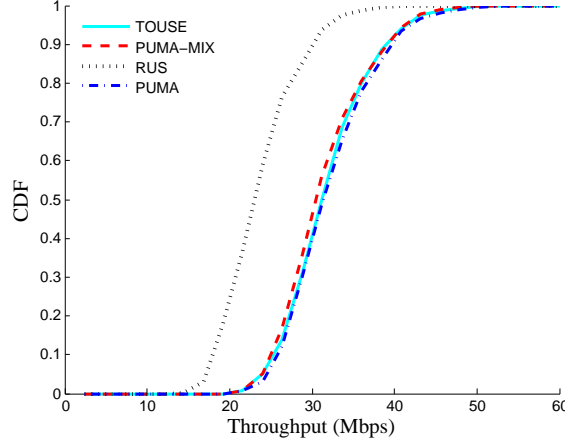


Figure 1: Performance comparison by total throughput

Selection (RUS), essentially the default standard of 802.11ac , which random select users with equal probability.

In our simulation, we randomly distribute the users around the AP. The channels are generated according to the rayleigh fading channel model, and we  
 290 assume the transmit power of each antennas is 15W. The default number of users is set to 10, packet size is set to 1500 bytes and the number of transmit antennas is 3. The detailed setting will be specified in each simulation.

#### 4.1. Performance Comparison for Continuous Traffic

We evaluate the performance by comparing with other user selection schemes  
 295 in terms of throughput gain. We set up a AP with 3 antennas and deploy 10 single-antenna users with randomly assignment of locations. Each of ten users have a different channel quality, and always have packets to receive. Before the transmission, AP obtain the queue information which is total transmit data to each candidate users. Then AP estimate the bit-rate of each concurrent packet  
 300 based on the effective SNR which is calculated by each user.

Fig. 1 plot the CDF of the total throughput in 3 antennas scenarios, and show the performance compared with other user selection schemes. The result shows that the traditional scheme, RUS, selecting users with an equal probab-



ity, without considering the channel characteristics and other criterion. Compared to RUS, the average throughput gain from enabling concurrent transmissions with TOUSE's user selection is about 50% in three antennas scenarios. This improvement mainly benefits from the following contributions: First, accurate rate prediction mechanism ensures the high packet reception rate, and reduce the time overhead without CSI feedback. Second, full utilize concurrent transmission time by overhead time matches based mechanism. The figure also shows that the PUMA-MIX and PUMA produce a throughput comparable to or even slightly higher than our user selection scheme. The performance of PUMA-MIX is similar to TOUSE's because we replace its greedy selection with our scheduling algorithm. Although the PUMA perform slightly better than TOUSE and PUMA-MIX, it caused  $10\times$  time overhead in the process of user selection than other two schemes. Besides, this time overhead is growing with the number of users. Next we will show that these scheme result in unfair resource sharing.

#### 4.2. Throughput Fairness Analysis

In this section, we analyse the fairness of user selection opportunities in a three antenna AP scenario. In order to analyse the fairness of TOUSE, we need to compare the probability to be selected for each users, which have different throughput. we set that each users are located at a specific region, where has different channel quality. By such method, we deployed only five different throughput single-antenna user around the AP, and each user have packets to receive from AP. In the simulation, we set *user1*, *user4* with worst and best channel quality, respectively. We also have control group, *user5* is random distributed around AP.

During the user selection process, the user group for downlink transmission was selected one after another. In the first round of simulation, TOUSE choose a lucky user randomly, which means that TOUSE enables all clients to get almost an equal probability to be selected first. In order to present more convincing result, we plot in Fig. 2 the number of the second selection oppor-

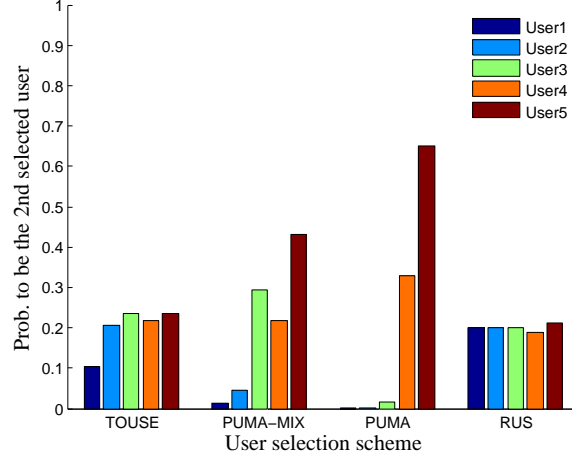


Figure 2: Fairness comparison in a 3-antenna AP scenario

tunities obtained by each user over the total number of selection, which is the metric used to evaluate fairness. The figure show that both the RUS scheme and our TOUSE enable all users to get almost an equal probability to be the second selected user. This implies that TOUSE enables users to achieving a similar level of fairness compared with fair contention mechanism. The probability of *user1* in TOUSE is slightly lower than other users. Because *user1* located in a region with worst channel quality, lead to the lowest throughput. In PUMA and PUMA-MIX, it gave little chance to low-throughput users. The user who has higher value of SNR get more opportunities to be selected. Because these schemes selected concurrent transmit group just depend on throughput of each user.

In order to display the performance of TOUSE more clear, we give one of the most relevant fairness indicators called Jain's fairness index (JFI) [15]. The defined as following.

$$JFI = \frac{[\sum_{u=1}^{N_u} X_u]^2}{N_u \sum_{u=1}^{N_u} [X_u]^2}. \quad (11)$$

Where  $N_u$  present the total number of users complete for channel,  $X_u$  denote channel access times of user  $u$  at some time.  $JFI$  ranges from  $1/N_u$  (only one user is served) to 1 (all users are served at the same chance). Fig. 3 plots the

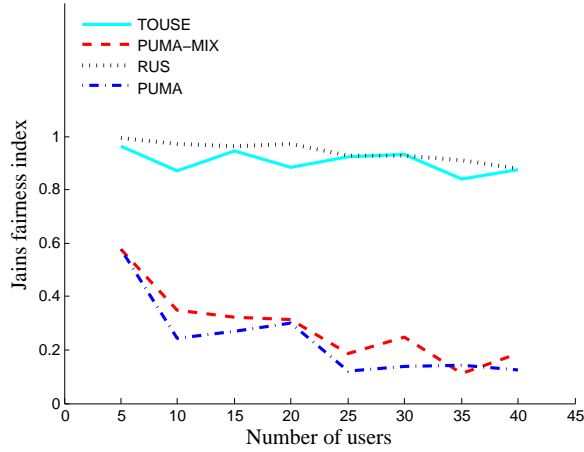


Figure 3: Jain's fairness index versus the number of users for different user selection mechanism

Jain's fairness index for TOUSE, PUMA-MIX, PUMA and RUS as a function of the number of users in a 3-antenna AP scenario. It is shown that the fairness performance of the proposed TOUSE clearly outperforms PUMA and almost close to the ideal case.

#### 4.3. Effect of Number of Transmit Antennas

Here we present the performance by the impact of number of transmit antennas on the throughput. In the simulation, we set that the number of transmit antennas at the AP varies from 2 to 8, and 30 users which randomly distributed around AP competed for the channel. Fig. 4 plots the performance of throughput. It shows that user selection is also important even for small scale MU-MIMO system, but it is more necessary for large scale system. Compared with these user selection schemes, all achieve a similar capacity gain, when the number of antennas increases. The ceiling of throughput is reached with the antennas number growing, due to a large amount of interference between with the inter-user. Besides, the result implies that increasing the number of paralld streams is not always the most efficient transmission scheme. We will prove that whether the TOUSE perform scalability.

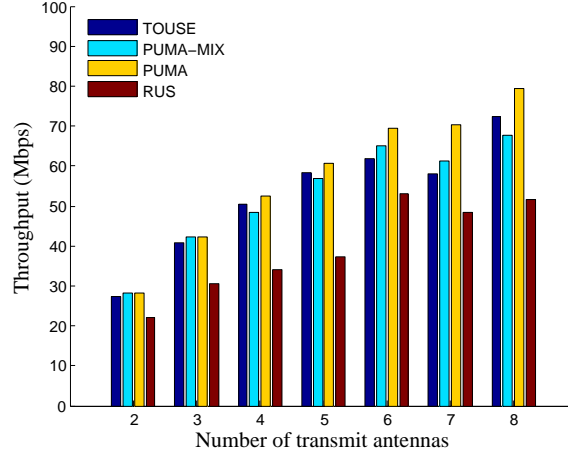


Figure 4: Performance in different AP scenario

#### 365 4.4. Impact of Number of Users

Here we evaluate the performance of TOUSE when the number of users varies from 5 to 50. We check the total network throughput gain increased by TOUSE when each users just have limited packet to received. In each simulation, the AP transmits concurrent queue packets to the matches user, and thereby the throughput is calculated based on the process of transmission.

We plot the Fig. 5 to presents the performance of scalable. The effect of increasing the number of user on TOUSE, PUMA and PUMA-MIX is relatively small, implies that the TOUSE is performance well even when the network scales up. Since the RUS does not consider the channel characteristics and packet queueing status of users, its total network capacity is poor. But its performance is also independent of the number of users. During this simulation, PUMA get higher throughput whatever the network scales up due to the exhaustively research compared with other schemes. But the total throughput of PUMA-MIX is similar to TOUSE, which means that our user selection have similar level of throughput with a throughput first contention mechanism.

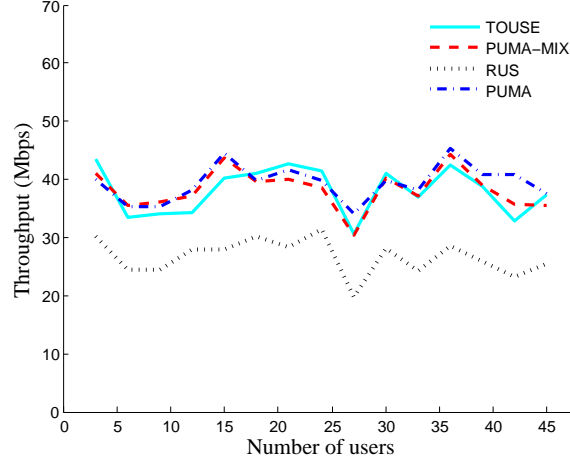


Figure 5: Performance impact by number of users

#### 4.5. Performance in Different Channel Quality Region

In order to evaluate could TOUSE performs where the network has worst channel quality. We make several simulation which has different channel quality. In a low SNR region, the value of SNR just varies from 0 to 5dB, and varies from 15 to 20dB in a highest region. We set that the 10 users locate in a region with similar channel quality. Fig. 6 reveals that user selection mechanism is not so significant for MU-MIMO in a low SNR region. Because the interference is large enough to each users no matter what the combination of beamforming group. However, with higher link qualities, these user selection scheme which consider the channel characteristics of users performs obviously better than RUS. Figure also shows that the TOUSE causes a capacity improvement over RUS even in a low SNR region. Compared with PUMA and PUMA-MIX, TOUSE performs same level or slightly poor in mostly scenario. But TOUSE achieve a similar capacity gain with going better of the channel quality. Obviously, TOUSE can performance better in different channel quality regions.

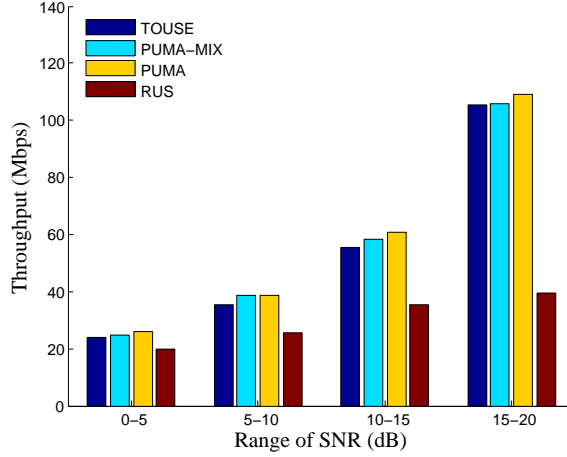


Figure 6: Performance in different channel quality region

## 5. RELATED WORK

Wireless standards like 802.11ac [16], LTE [17] have recently pushed toward the use of MU-MIMO for obtaining high-speed and high-throughput wireless communication. The work [10] present a study to random access based MAC mechanisms for MU-MIMO, and gives a survey and categorize to the most relevant MU-MIMO MAC proposals. It also identify key requirements for designing efficient MU-MIMO MAC protocols including de/pre-coding [1] and scheduling schemes. The potential of MU-MIMO has been investigated both theoretically [18] and empirically [8], which studied pre-coding techniques, scheduling schemes and practical gain of MU-MIMO in various environments.

Substantial theoretical works [19] assumed that CSI is available and paid much attention on implementing low-complexity algorithms to approach the maximum throughput. Xie *et al.*, [3] present scalable and adaptive user selection which requires several rounds of CSI feedback instead of gathering from all users. However, in reality, the vulnerabilities of CSI [20] still exists due to its estimation methods, like time overhead. To avoid overwhelm the actual channel time spent on transmission, the schemes of user selection without CSI feedback was be proposed. The authors of [21] design an orthogonality evaluation mechanism

which enables each user using its own CSI to speculate. But it is only applies  
415 to uplink MU-MIMO. In [5], it proposed a method of user selection prior to  
channel sounding and exploits theoretical properties of MU-MIMO system to  
estimate data rate. PUMA achieves better performance in throughput, however,  
does not do well in respect of fairness.

Some other works focus on the scheduling scheme of user selection [22]. Most-  
420 ly [23] either iteratively select a user that minimizes the interference, reduce the  
complexity or maximizes the aggregate throughput. In [9], a novel search and  
update strategy was proposed for user selection. It design a knob to controls  
tradeoff between aggregate capacity and computational complexity. The work  
[24] present a low complexity scheduling scheme using block diagonalization  
425 with chordal distance.

In addition, some experimental studies emerged, like [25]. Authors realizes  
netMIMO downlink transmission for large-scale wireless network. By organiz-  
ing a network into clusters, it could manages interference with a decentralized  
channel-access algorithm, but environment is limited in static network since  
430 time-averaged CSI is used as input. In [26], Shen *et al.*, introduce TurboRate,  
client annotates its packets with single SNR and direction at the AP to obtain  
the optimal bit rate and could transmit concurrently. Now there are more con-  
ditions are considered, like mobility [27] or channel control [28]. The exciting  
thing is that the team of Xinyu Zhang [29] optimize MU-MIMO performance in  
435 802.11ac commodity devices.

So far, there are three key point in MU-MIMO MAC protocol design: through-  
put, complexity and fairness [30]. But most research only consider two or one  
of these point. TOUSE design a novel metric without CSI feedback benefit  
from [12], and present a fair user selection mechanism based on overhead time  
440 matches.

## 6. CONCLUSION

In this paper, we have presented TOUSE, a scalable and fairness user selection scheme for downlink MU-MIMO. TOUSE is a proportional fair scheduler usually considers both network capacity and fairness. In order to reducing time  
445 overhead, we adopts a novel per-user data-rate estimation method without any CSI feedback. TOUSE selected optimal beamforming group by dynamic time warping based mechanism, which make full use of concurrent transmitting time and achieve equal opportunity of channel contention. We have simulated TOUSE along with three other user selection schemes. Simulation shows that TOUSE  
450 achieve a  $1.5\times$  throughput gain over traditional scheme in three antennas AP scenarios. and the similar level of fairness compared with fair contention mechanism. We also proved that TOUSE can always achieve similar performance of throughput compared with throughput contention schemes. More detail of QoS will be consider in our future work.

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## References

- [1] L.-U. Choi, R. D. Murch, A transmit preprocessing technique for multiuser MIMO systems using a decomposition approach, *IEEE Transactions on Wireless Communications* 3 (1) (2004) 20–24.
- 465 [2] J. Gross, Scheduling with outdated CSI: effective service capacities of optimistic vs. pessimistic policies, in: *Proc. IEEE International Workshop on Quality of Service (IWQoS)*, 2012.



- [3] X. Xie, X. Zhang, Scalable user selection for MU-MIMO networks, in: Proc. IEEE International Conference on Computer Communications (INFOCOM), 2014.
- [4] X. Xie, X. Zhang, K. Sundaresan, Adaptive feedback compression for MIMO networks, in: Proc. ACM International Conference on Mobile Computing and Networking (MobiCom), 2013.
- [5] N. Anand, J. Lee, S.-J. Lee, E. W. Knightly, Mode and user selection for multi-user MIMO w lans without CSI, in: Proc. IEEE International Conference on Computer Communications (INFOCOM), 2015.
- [6] D. Halperin, W. Hu, A. Sheth, D. Wetherall, Predictable 802.11 packet delivery from wireless channel measurements, ACM SIGCOMM Computer Communication Review 41 (4) (2011) 159–170.
- [7] T. Yoo, A. Goldsmith, On the optimality of multiantenna broadcast scheduling using zero-forcing beamforming, IEEE Journal on Selected Areas in Communications 24 (3) (2006) 528–541.
- [8] E. Aryafar, N. Anand, T. Salonidis, E. W. Knightly, Design and experimental evaluation of multi-user beamforming in wireless LANs, in: Proc. ACM International Conference on Mobile Computing and Networking (MobiCom), 2010.
- [9] W.-L. Shen, K. C.-J. Lin, M.-S. Chen, K. Tan, Sieve: Scalable user grouping for large MU-MIMO systems, in: Proc. IEEE International Conference on Computer Communications (INFOCOM), 2015.
- [10] R. Liao, B. Bellalta, M. Oliver, Z. Niu, Mu-mimo mac protocols for wireless local area networks: A survey, IEEE Communications Surveys and Tutorials 18 (1) (2014) 162–183.
- [11] H. Yang, T. L. Marzetta, Performance of conjugate and zero-forcing beamforming in large-scale antenna systems, IEEE.

- 495 [12] N. Ravindran, N. Jindal, Multi-user diversity vs. accurate channel state information in MIMO downlink channels, *IEEE Transactions on Wireless Communications* 11 (9) (2012) 3037–3046.
- [13] N. Jindal, MIMO broadcast channels with finite-rate feedback, *IEEE Transactions on Information Theory* 52 (11) (2006) 5045–5060.
- 500 [14] M. Müller, *Dynamic time warping*, Springer Information retrieval for music and motion (2007) 69–84.
- [15] R. Jain, D.-M. Chiu, W. R. Hawe, A quantitative measure of fairness and discrimination for resource allocation in shared computer system, Vol. 38, Eastern Research Laboratory, Digital Equipment Corporation Hudson, MA, 1984.
- 505 [16] M. S. Gong M X, Hart B, Advanced wireless lan technologies: IEEE 802.11 ac and beyond, *ACM GetMobile: Mobile Computing and Communications* 18 (2015) 48–52.
- [17] S. Deng, R. Netravali, A. Sivaraman, H. Balakrishnan, WiFi, LTE, or both?: measuring multi-homed wireless internet performance, in: *Proc. ACM Internet Measurement Conference (IMC)*, 2014.
- 510 [18] D. Lee, Performance analysis of zf-precoded scheduling system for MU-MIMO with generalized selection criterion, *IEEE Transactions on Wireless Communications* 12 (4) (2013) 1812–1818.
- 515 [19] W. Lim, G. Kim, J. Kim, H. Park, K. Lee, H. Jang, Performance of linear precoding and user selection in IEEE 802.11 ac downlink MU-MIMO system, in: *Proc. IEEE Wireless Communications and Networking Conference (WCNC)*, 2014.
- 520 [20] R. Miller, W. Trappe, On the vulnerabilities of CSI in MIMO wireless communication systems, *IEEE Transactions on Mobile Computing* 11 (8) (2012) 1386–1398.

- [21] A. Zhou, T. Wei, X. Zhang, M. Liu, Z. Li, Signpost: Scalable MU-MIMO signaling with zero CSI feedback, in: Proc. ACM International Symposium on Mobile Ad Hoc Networking and Computing (MobiHoc), 2015.
- 525 [22] T.-W. Kuo, K.-C. Lee, K. C.-J. Lin, M.-J. Tsai, Leader-contention-based user matching for 802.11 multiuser MIMO networks, IEEE Transactions on Wireless Communications 13 (8) (2014) 4389–4400.
- [23] S. Huang, H. Yin, J. Wu, V. Leung, User selection for multiuser MIMO downlink with zero-forcing beamforming, IEEE Transactions on Vehicular  
530 Technology 62 (7) (2013) 3084–3097.
- [24] K. Ko, J. Lee, Multiuser MIMO user selection based on chordal distance, IEEE Transactions on Communications 60 (3) (2012) 649–654.
- [25] X. Zhang, K. Sundaresan, M. A. A. Khojastepour, S. Rangarajan, K. G. Shin, NEMOx: scalable network MIMO for wireless networks, in: Proc.  
535 ACM International Conference on Mobile Computing and Networking (MobiCom), 2013.
- [26] W.-L. Shen, K. C.-J. Lin, S. Gollakota, M.-S. Chen, Rate adaptation for 802.11 multiuser MIMO networks, IEEE Transactions on Mobile Computing 13 (1) (2014) 35–47.
- 540 [27] O. Bejarano, R. P. F. Hoefel, E. W. Knightly, Resilient multi-user beamforming w lans: Mobility, interference, and imperfect CSI, in: Proc. IEEE International Conference on Computer Communications (INFOCOM), 2016.
- [28] Z. L. Shepard C, Javed A, Control channel design for many-antenna MU-MIMO, in: Proc. ACM International Conference on Mobile Computing and  
545 Networking (MobiCom), 2015.
- [29] Z. X. e. a. Sur S, Pefkianakis I, Practical mu-mimo user selection on 802.11 ac commodity networks, in: Proc. ACM International Conference on Mobile Computing and Networking (MobiCom), 2016.

- <sup>550</sup> [30] M. Esslaoui, F. Riera-Palou, G. Femenias, A fair MU-MIMO scheme for IEEE 802.11 ac, in: IEEE International Symposium on Wireless Communication Systems (ISWCS), 2012.