

# TOUSE: A Fair User Selection Mechanism Based on Dynamic Time Warping for MU-MIMO Networks

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## Abstract

Multi-user Multiple-Input and Multiple-Output (MU-MIMO) has potential for prominently enhancing the capacity of wireless network by simultaneously transmitting to multiple users. User selection is an unavoidable problem which bottlenecks the gain of MU-MIMO to a great extent. Major state-of-the-art works focus on improving network capacity by using Channel State Information (CSI), however, the overhead of CSI feedback becomes unacceptable when the number of users is large. Some work does well in balancing tradeoff between complexity and achievable capacity but lack of consideration of fairness. Current works universally ignore the rational utilizing of time resource, which lead the improvement of network throughput to a standstill. In this paper, we propose TOUSE, a scalable and fair user selection scheme for MU-MIMO. The core design is dynamic time warping based user selection mechanism for downlink MU-MIMO, which could make full use of concurrent transmitting time. TOUSE also presents a novel data-rate estimation method without any CSI feedback, which provide supports for user selection. Simulation result shows that TOUSE significantly outperforms traditional contention-based user selection schemes in both throughput and fairness in an indoor condition.

*Keywords:* MU-MIMO, user selection, fairness, dynamic time warping

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## 1. Introduction

Multi-user Multiple Input Multiple Output (MU-MIMO) has already attracted a huge amount of attention because it enables better spatial reuse. The network capacity is enhanced by sending frames to multiple single-stream users concurrently. Prior to 802.11ac, traditional 802.11 protocol limited every transmission only sent to a single user, which cannot full utilize spatial resources supported by multiple antennas AP. Multi-user transmission is a new technology within 802.11. By using MU-MIMO [1], AP is equipped with multiple antennas, and could transmit to multiple users at one time. Due to these abilities, MU-MIMO has the potential to change the way in which Wi-Fi networks are built and achieve improved capacity gains.

A MU-MIMO downlink system, in theory, its capacity gains increases linearly with the number of transmitting and receiving antennas. But in practice, the number of antennas is limited by several reasons, and the inter-user interference could not be ignored. These lead to a series of important problems. First, how could an AP select a beamforming group of users and transmit simultaneously. Second, how to determine the size of the beamforming group. Different beamforming group selection leads to variant transmitting rate, then influences the overall network performance. Unwise selecting method may results in a huge waste of space-time at any single transmitted slot, and causes the problems of fairness and complexities. To make an optimal selection, we should choose a metric like sum rate as a criterion to process the feedback information like CSI (Channel State Information) or SNR (Signal-Noise Ratio), design an efficient scheduling scheme based on various data we obtained.

Substantial researches [2] have provided the solving methods to the user selection problem for MU-MIMO. Most solutions select the optimal beamforming group based on understanding the full CSI of all potential users. CSI reflects the characteristics of the channel including fading distribution, average channel gain and spatial correlation, all are important for beamforming group select. However, CSI is calculated by estimating the training sequence from AP, then

users feed it back to the AP. Reducing the CSI overhead becomes an important issue in MU-MIMO since this is a long and complex process [3]. Although numerous optimization schemes of feedback have been proposed, like compression algorithms [4], the overhead of CSI feedback is still huge sometimes and severely  
35 affects the performance of network, since the overhead grows linearly with the number of users. Even worse, infrequent CSI feedback results in outdated, which may leads to the inter-user interference. It is convenient to select beamforming group within CSI, but intolerable for MU-MIMO system with unacceptable feedback overhead.

40 In fact, these challenges have motivated previous works to find better possible solutions for user selection. In [3], the author proposed a distributed contention mechanism that singles out the best user to feed back its CSI. Narendra [5] present pre-sounding user selection algorithm only using available pre-sounding information instead of posting channel sounding information,  
45 and solved the problem of feedback overhead to a certain extent.

In this paper, we propose *Time Optimal User Selection based on Effective SNR* (TOUSE), a scalable and fair user selection scheme for MU-MIMO networks to achieve higher capacity. To sum up, our main contributions are as follows:

- 50 • We design a novel dynamic time warping based user selection mechanism to increasing throughput under the fairness constraints, and propose a algorithm to solve it.
- We adopt a low complexity feedback mechanism to obtain the available channel information and presents a novel data-rate estimation method  
55 base on the information of effective SNR [6] without any CSI feedback.
- TOUSE has abilities to adapt to different network channel qualities, no matter low SNR region or high link qualities. It is also suitable to dynamic network, since it selects users after channel sounding is completed and acquires real-time information.

60 • Finally we experimentally evaluate the performance of TOUSE. Result shows that, on average, the gain of TOUSE is  $1.5\times$  over traditional Random user selection scheme in 3-antennas AP scenarios. Compared with PUMA scheme [5], network capacity gain is similar but TOUSE provides users with fair selection opportunities.

65 The rest of this paper is organized as follows. In Section II, we present background of user selection in MU-MIMO. Section III provides an overview of the components of TOUSE. Section IV evaluates the performance of TOUSE with experimentations. Then we describe related works in Section V and Section VI concludes the paper.

## 70 2. BACKGROUND AND CHALLENGES

### 2.1. MU-MIMO System Model

In a downlink MU-MIMO system, consider a single-cell MIMO with a single base station serving  $N$  users. The base station is equipped with  $M$  antennas and the client with one or more receive antennas. We assume that AP sends frames to a set of selected single antenna users  $S$  called beamforming group at the same time, which satisfies  $K = |S|$ ,  $K \leq M$ . Due to the multi-user interference at the client side, it is essential for AP to precode outgoing signals to minimize interference among simultaneous streams. Owing to its low complexity, AP applies ZFBF (Zero-forcing beamforming) [7]. In ZFBF, user streams are separated by different beamforming directions. Let  $x_k$  denotes the data symbol sending to user  $k$ ,  $\mathbf{w}_k$  be the beamforming weight vector, and  $p_k$  presents the transmit power. Assume  $\mathbf{h}_k$  is the  $1 \times M$  channel state vector between transmission antennas and receiver  $k$ . Define  $\mathbf{W} = [\mathbf{w}_1, \mathbf{w}_2, \dots, \mathbf{w}_K]$ ,  $S = \{s_1, s_2, \dots, s_K\}$ , the transmitted signal  $X = \sum_{k=1}^K \sqrt{p_k} \mathbf{h}_k \mathbf{w}_k x_k$ . Then, let  $n_k$  denotes the noise level of user  $k$ , and the received signal vector is:

$$y_k = \sqrt{p_k} \mathbf{h}_k \mathbf{w}_k x_k + \sum_{j \neq k, j \in S} \sqrt{p_j} \mathbf{h}_k \mathbf{w}_j x_j + n_k, k \in S. \quad (1)$$

To eliminate the interference from other beamforming frame streams, ZFBF should satisfy the zero-interference condition:  $\mathbf{h}_k \mathbf{w}_j$  for all receivers  $j \in S, j \neq k$ . So that receiver  $k$  only gets its symbol  $x_k$ . Let the channel state matrix  $\mathbf{H} = [\mathbf{h}_1^T, \mathbf{h}_2^T, \dots, \mathbf{h}_K^T]^T$  and the beamforming weight matrix  $\mathbf{W} = [\mathbf{w}_1, \mathbf{w}_2, \dots, \mathbf{w}_K]$ . One optimal choice of  $\mathbf{W}$  that satisfies zero-interference condition is the pseudo-inverse of  $\mathbf{H}$ :

$$\mathbf{W} = \mathbf{H}^+ = \mathbf{H}^*(\mathbf{H}\mathbf{H}^*)^{-1}. \quad (2)$$

Thus, another problem that needs to be considered is power allocation. For simplicity, we adopted ZFBF-EP scheme where the transmitter allocates equal power to its users.

## 75 2.2. Impact of User Selection Mechanism

From above section, the performance of ZFBF highly depends on the channel vectors from transmitter to receiver. When the channel vectors of different receivers uncorrelation with each other, it is most likely to improved the network capacity gain. It was proved by the experimental [8] for indoor wireless  
80 network. The network spatial multiplexing gain of ZFBF can be increased by a high number of transmitter antennas, wherever the location of receivers in indoor environment.

Selecting beamforming group is one of the key issues which are related to the performance of MU-MIMO system. From Eq. (1), the SNR of each receivers  
85 depends on its group member. If one receiver's channel vector is orthogonal to another, it will cause limit interference when transmitting together. The research [8] also proved that ZFBF in different SNR regions causes different capacity improved, and the number of beamforming group is other factor. The optimal size of beamforming group depends on the link state of the members.  
90 The state of queue and other information should be taken into account as well.

## 2.3. Challenges in User Selection

User selection is a complicated process. Although optimal transmission beamforming group can improve the network capacity, high computational over-

head is unacceptable. Before each downlink transmit, the AP needs to obtained  
 95 the CSI from the users' feedback. During the feed back process, AP sends a  
 training sequence to the target users, users calculate the CSI by the training  
 sequence and feedback the CSI to AP one by one. Due to this mechanism,  
 overhead by CSI feedback also increased with number of users. Researches [3]  
 present that even with 20 users, the channel time cost of existing schemes can  
 100 be comparable to or even exceed that of actual data transmission.

There are a number of factors which a user selection mechanism should  
 be considered. First, how to determine the size of beamforming group. In a  
 transmission time slot, AP beamforming to send frame to a set of users  $S$  and  
 satisfy  $K \leq M$ . In [8], it proved that maybe  $K = 3$  have a better network  
 105 performance than the case of  $K = 4$ . The authors of [5] proposed a aggregate  
 throughput to select the combination mode. Second is the complexity reduction.  
 Instead of exhaustive search over all possible combination, most researches adopt  
 the method of local optimal to solve this problem, which performs inefficiently.  
 It is hard to achieve both low complexity and high performance. So the tradeoff  
 110 between performance and complexity is essential [9]. Another solution is to  
 reduce the feedback overhead, which is not the way to the underlying problem.  
 The last challenge is how to realize fairness. A simple way to improve the  
 network throughput is just selecting the users which have a high link quality.  
 But it might not be fair for all users [3]. Sometimes, it will caused starvation.

### 115 3. TOUSE DESIGN

#### 3.1. Design Overview

The design inherits the advantages of throughput fairness and low com-  
 plexity in user selection, it also improves the network capacity gain. TOUSE  
 present a new preference metric which aims to make full use of time resource  
 120 and guarantees fairness. Besides, instead of requiring CSI feedback, TOUSE  
 provides a mechanism in which AP just obtained effective SNR from users to

make decision. This mechanism has limited time overhead compared to the CSI feedback.

Before giving the detail of TOUSE, there are some available pre-sounding  
125 information to introduce. In MU-MIMO system, AP owns the information of  
system state and queue state before channel sounding or communication. For  
each transmission, AP knows the hardware configuration, like available number  
of transmission antennas  $M$ , the number of clients' receiving antennas. AP is  
also aware of the queue state information for each users, like each user's backlog  
130 or queue size. The amount of available data directly affects the data trans-  
mission time in each transmission, which is used for user selection. By leveraging  
this information, TOUSE design a performance metric to select optimal beam-  
forming group. The TOUSE works as follows:

1) First, the AP announces its intention for MU-MIMO downlink transmis-  
135 sion through the NDP Announcement frame, and it is the time to start the  
MU-MIMO sounding process for users. AP randomly selects a first user into  
the optimal beamforming group, which can achieve channel access fairness.

2) Then, each user estimates its own CSI, independently based on the NDP  
Announcement frame. AP obtain the effective SNR feedback which is calculated  
140 by each client from the CSI. This is the first round of TOUSE user selection.

3) In subsequent round, AP estimates the potential datarate for each com-  
petitors based on the effective SNR and current beamforming group. Then cal-  
culate time of data transmission for each users combined with the pre-sounding  
information, and get global time of transmission slot based on selected users  
145 and candidate users.

4) Given transmission time of each data transmission and information of  
selected users. According to the constraint condition (describe in section D),  
the AP selects the best candidate which can optimise total network capacity for  
this transmission slot.

150 5) The one who satisfies the optimal constraint, which means its could trans-  
mit with the member of beamforming group. The AP adds it to the beamform-  
ing group.

6) Repeat steps (3)-(5) until the size of beamforming group reaches the maximum transmission number  $M$ , or there is none best choice left. Then, AP  
155 would terminate the user selection process.

Next, we are going to present TOUSE more detailed.

### 3.2. Effective SNR

In order to accurately predict the packet delivery rate, a key point is using effective SNR (ESNR) [6]. It is a simple, easy to deploy, broadly useful, and accurate method. Using effective SNR makes packet delivery predicted for 802.11n  
160 MIMO rates, plus choices of transmit power and antennas. During the process, CSI was need to be the piece of input, which can provides the SNR values for each subcarrier. It is contain more information than RSSI, and provides the opportunity to design an accurate evaluate model.

The effective SNR calculation is not just the average subcarrier SNR. Instead, it is biased towards the weaker subcarrier SNRs because the subcarriers caused most of the errors. The effective SNR was calculated by averaging the subcarrier BERs and find the corresponding SNR. That is formulated as follows:

$$\text{BER}_{eff} = \frac{1}{S} \sum \text{BER}(snr_s); \quad (3)$$

$$\text{ESNR} = \text{BER}^{-1}(\text{BER}_{eff}). \quad (4)$$

165  $\text{BER}^{-1}$  presents the inverse mapping, from BER to SNR, and  $S$  is number of subcarriers.  $\text{BER}_{eff}$  denote the average BER across subcarriers,  $snr_s$  is the SNR values of each subcarrier.

### 3.3. MU-MIMO User Datarate Estimate

In TOUSE, the key problem is to predict the per-user packet delivery rate. During this process ESNR evaluate is essential for each transmission. Then  
170 the AP obtains data rate for each user from the ESNR by using MCS table. However, There is still a problem When AP transmits to multi-receivers at the



same time, the inter-user interference is unavoidable. It will influence the total capacity of network.

1) *Traditional Rate Estimation*: One of the classical approach to calculate the aggregate capacity is using channel state matrix. The sum rate ( $R$ ) [7] is achieved by following scheme:

$$R = \max_{\mathbf{w}_k, P_k} \sum_{k=1}^K \log \frac{1 + \sum_{j=1}^K P_j |\mathbf{h}_k \mathbf{w}_j|^2}{1 + \sum_{j=1, j \neq k}^K P_j |\mathbf{h}_k \mathbf{w}_j|^2} \quad (5)$$

subject to  $\sum_{k=1}^K \|\mathbf{w}_k\|^2 P_k \leq P.$

175 This method is accurate but quite complexity. It requires channel state matrix as input which is difficult to obtain. Given the significant overhead of CSI feedback, the AP needs more reasonable utilization of this information to maximize the network performance. This leads to the system more complexity and hard to implement, which is opposite to what we think.

180 2) *ESNR based Rate Estimation*: TOUSE's rate estimation method is based on theoretical MU-MIMO system scaling. In order to make sure facilitate and precise, AP obtain the ESNR which is calculated by users, and estimates the data delivery rate by MCS-SNR table. Besides, quantify the influence of inter-user interference when AP transmits to multi-users is also essential. As mentioned  
185 before, in ZF model, user only receives its desired symbol owing to the composite effects of precoding and channel distortion. The main features of ZF is complete interference cancellation with full CSI, but it will amplify the noise [10].

Many works [11] provide the analysis to network capacity performance influenced by ZF-precoded system. But most of methods are not suitable for our purposes because requiring too much information. By the ZF criterion, there is residual interference because the beamformers are based on imperfect CSI. The SINR for selected user  $k$  is (proposed in [12])

$$\text{SINR}_k = \frac{\text{SNR}_k \|\mathbf{h}_k\|^2 \cos^2(\angle(\mathbf{h}_k, \mathbf{w}_k))}{1 + \text{SNR}_k \|\mathbf{h}_k\|^2 \sum_{j \neq k} \cos^2(\angle(\mathbf{h}_k, \mathbf{w}_j))} \quad (6)$$

and the corresponding sum rate is  $\sum_{k=1}^n \log_2(1 + \text{SINR}_k)$ . Where  $\mathbf{w}_k$  presents

190 the precoding unit-norm beamforming vector for user  $k$  is chosen in the direction of the projection of  $\mathbf{h}_k$  on the nullspace of  $\mathbf{h}_j$ ,  $j \neq k$ .

Eq. (6) presents SINR variation for each users, but there is the same problem of using information of CSI as input. As Eq. (6) shows that the interference by other receivers in beamforming group is related to per-receiver SNR. Besides, the system state information also has great influence on the SINR, like transmission antennas number  $M$  and the size of current transmission users group  $K$ . It is also necessary to note that this paper focuses on the users equipped with a single antennas. In [13] and [12], it proved that in order to achieve the full multiplexing gain of  $M$ , the transmitters must have perfect channel knowledge in order to choose the zero-forcing beamforming vectors. However due to the imperfection in this knowledge, there inevitably will be some multi-user interference, which leads to performance degradation. Therefore, we proposed a suitable per-receiver SINR estimation method as following.

$$\text{SINR}_k = \frac{\text{ESNR}_k - \text{ESNR}_k \cdot 2^{-B}}{1 + \text{ESNR}_k \cdot 2^{-B}} \quad (7)$$

$$B = ((M - 1)P)/(3(K - 1))$$

Where  $M$  is the number of transmitting antennas, presents the degree of freedom of MU-MIMO system.  $K$  denotes the number of size of beamforming group, which leads an exponential increase in the multi-user interference.

195 In TOUSE, we assume that each transmission antenna has a same transmitting power  $P$ . From Eq. (7), the value of per-receiver SINR is inherently less precise than Eq. (5). But it can provide a sufficiently accurate result for TOUSE user selection process as well, and easy to implement. then the transmission data rate  $rate_k$  for user  $k$  is calculate from the MCS-Rate (Table 1) by  
200 the SINR.

3) *TOUSE Rate Estimation Analyse:* In Eq. (7), the TOUSE's SINR estimation method only requires the system hardware configurations  $M$ , number of users  $K$  and the ESNR calculated by per-user. This estimation scheme can accommodate with the network dynamically by using ESNR, and avoid CSI

205 feedback overhead at the same time.  $2^{-B}$  presents the multiplexing gain of inter-user interference, and it increased linearly with the transmission power. Thus, the SINR of each user is related to  $B$  in MU-MIMO system.

During the rate estimation process, TOUSE first measures the channel state information, and calculates the ESNR by each receivers. Then the each user's 210 SINR was calculated based on the size of beamforming group. Finally the data delivery rate (for 90% packet reception rate) is obtained by using the MCS-SNR table provided by the standard (as shown in Table 1).

Table 1: Minimum SNR required

MCS	Rate (Mbps)	SNR (dB)
0	6.5	1.1
1	13.0	4.1
2	19.5	6.7
3	26.0	9.6
4	39.0	12.8
5	52.0	17.2
6	58.5	18.4
7	65.0	19.7

### 3.4. User Selection Mechanism

In this section, we present the user selection mechanism to maximum the 215 aggregate throughput of network, and the fairness of channel access for each users is also important. In this subsection, the key point is the two type of limiting condition in the selection process.

Previous sections give the data rate estimation method. In order to calculate the data transmission time for a transport connection, key point is total delivery data and network overhead (such as channel sounding and ESNR feedback overhead). These pre-sounding information can be obtained by AP queue state or network measurement. So the total throughput  $R$  for each transmission slot

can be calculated, which is the performance metric for user selection mechanism. The formula is as following,  $L$  denotes the total transmission data at a time slot,  $T_s$  is the maximum transmission time of all transmission and  $T_o$  is the network overhead.

$$R = L/(T_s + T_o). \quad (8)$$

In order to achieve the two design goals: throughput increment and fairness guarantee. We design a similarity matching algorithm for optimal user group selection based on dynamic time warping [14]. Before present time constraint condition, some definition should be introduce. First,  $S = \{s_1, s_2, \dots, s_k\}$  denote the current selected beamforming group and  $|S|$  is the size of  $S$ ,  $c$  denotes a user which is candidate for  $k + 1$  solution from the unselected users, but still waiting for check by constraint condition.  $T(c)$  present the transmission time requirement that AP transmits the queue data to user  $c$ . Here is the first constraint condition : to maximum the aggregate throughput.

$$\begin{cases} \frac{T(c)}{T(\max(S))} < \frac{1}{(ratio(c)-1)} & T(\max(S)) \leq T(c) \\ \frac{T(\max(S))}{T(c)} < \frac{1}{(ratio(\max(S))-1)} & T(\max(S)) > T(c) \end{cases} \quad (9)$$

Where  $\max(S)$  presents the one with maximum data transmission time in selected group,  $T(\max(S)) = \max(L_i/rate_i)$ ,  $i \in S$ ,  $ratio(c)$  is the ratio between the data rate of user  $c$  at the mode of  $K = |S|$  and  $K = |S| + 1$ . The size of beamforming group  $K$  has a big impact on the transmitting rate of each user. For example, user  $u$  from beamforming group of which the size is  $K$ , the transmission rate is  $a$ , and rate equals  $b$  in the mode of  $K + 1$ , then  $ratio(u) = a/b$ . Eq. (9) is a throughput constraint for network capacity, which can judge the benefits of user  $c$  in this transmit time slot. Then this user will be judge whether put it into the beamforming group or just throw it away. As we have talked before, increasing the size of beamforming group leads to inter-user interference. So the total network capacity performance should be consider when put candidate user  $c$  into beamforming group.

The second constraint aim to make full utilization of space-time resource.

$$T(c) \leq \frac{M}{K} \cdot T(\max(S)). \quad (10)$$

230 Where  $K = |S|$  denotes the size of beamforming group which is received transmit  
date from AP concurrently. This restriction allows our algorithm to find an  
optimal match between given transmission time of selected users. For example,  
in a transmit slot, AP transmits to *user1* and *user2*, while the transmission  
time of *user1* is 1s and *user2* is 100s. In this case, compared with *user2*, the  
235 transmission time of *user1* is too small, which is not a best choose to bind them  
together for total network.

Based on the idea of dynamic time warping, in order to find an optimal  
beamforming group which can improved the network capacity. The AP selected  
by the correlation of transmission time between candidate user  $c$  and current  
240 beamforming group. In the process of user selection, AP selected first user  
into beamforming group at random, then the other member of beamforming  
group was selected by correlation with the set of selected user. This process will  
go through the total unselected user until nothing find, which means current  
beamforming group is am optimal solution at a transmitting slot.

245 TOUSE user selection mechanism based on data transmission time, which  
means the contention is fairness in term of SNR of user. Next section will  
present the fairness performance of our mechanism. Eq. (8) shows that the  
network overhead limits the performance of a MU-MIMO transmission. Along  
with the increasing of beamforming group size, the amount of total transmit  
250 data  $L$  grows. The larger amount of network overhead is created meanwhile. So  
it is an important issue to get the trade off between aggregate data and network  
overhead.

### 3.5. TOUSE Algorithm

In order to seek an optimal combination to improve the network capacity,  
255 TOUSE using two constraints which have been mentioned before. Given the  
set of candidate receivers  $C = \{c_1, c_2, \dots, c_n\}$  which is the total candidate users

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**Algorithm 1** TOUSE User Selection

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**Input:**

The set of single antenna users,  $C$ ;

The number of transmit antennas and transmit power,  $M$  and  $P$ ;

**Output:**

The set of solution receivers,  $S$ ;

The size of solution group,  $k = |S|$ ;

**Begin:**

```
1: while  $k \leq M$  and  $C \neq \emptyset$  do
2:   if  $k = 0$  then
3:     Selecting a solution  $s_1 \in C$  at randomly from  $C$ ;
4:      $C = C - s_1$ ,  $S = S + s_1$ ;
5:   else
6:     repeat
7:       Selecting a optimal receiver  $c_k \in C$  matches  $S$ ;
8:       Judging  $c_k$  by two constraint: Eq. (9), Eq. (10);
9:       if  $c_k$  satisfies the two constraint then
10:         $S = S + c_k$ ;  $C = C - c_k$ ;
11:      end if
12:    until Get the solution  $s_k = c_k$  or none of optimal solution  $s_k \notin C$ 
      meets the condition;
13:   end if
14:   if  $s_k \notin C$  then
15:     None of receiver  $c \in C$  matches  $S$ ;
16:     Break, //terminate the process of user selection;
17:   end if
18: end while
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in one transmission slot. TOUSE selects the best combination as beamforming group for AP to simultaneous downlink transmissions. Here is the TOUSE user selection algorithm.

260 The algorithm (1) shows the user selection process of TOUSE's. The inputs of this algorithm is a candidate set of users, and the outputs is the beamforming group  $S$ ,  $|S| \leq M$ . In the first round, AP select a solution randomly from candidate set, which met the requirements of competition fairness. The time constraint condition process is repeated until select a receiver to match the  
 265 existing solution group, or none of optimal solutions exist in candidate receivers, as lines 6-12 in Algorithm 1. During the process of searching solution, each selected user was the best one when group with the concurrent beamforming group. This searching method can reduced the complexity of TOUSE and an optimum result was acquired rapidly and exactly.

#### 270 4. PERFORMANCE EVALUATION

In this section, we further perform simulations to evaluate the performance of TOUSE in indoor environment. The simulations aims to answer the following questions:

- How much capacity gain can TOUSE achieve in comparison with existing  
 275 schemes?
- How does TOUSE perform in terms of fairness compared with existing schemes?
- How much the number of transmit antennas impact on TOUSE?
- Does TOUSE scale?
- 280 • Could TOUSE work in different channel quality region?

For performance comparison, we implemented three state-of-the-art user selection schemes: (1) Pre-sounding User and Mode selection Algorithm (PUMA) [5]. PUMA allows MU-MIMO system to efficiently transmit multiple streams

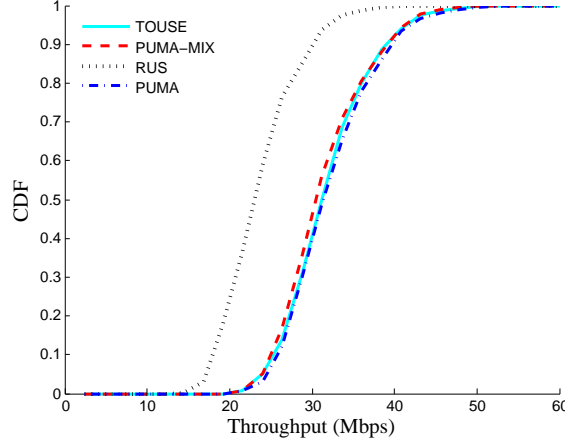


Figure 1: Performance comparison by total throughput

by using pre-sounding information. It estimates the throughput of all potential user group combinations. (2) Mixed PUMA algorithm (PUMA-MIX). PUMA employed exhaustively searching method to find the optimal user group. We replaced with iteration method using for comparison in simulations. (3) Random User Selection (RUS), essentially the default standard of 802.11ac , which randomly selects users with equal probability.

In our simulation, we randomly distribute the users around the AP. The channels are generated according to the rayleigh fading channel model, and the transmit power of each antennas is 15W. The default number of users is set to 10, packet size is set to 1500 bytes and the number of transmit antennas is 3. The detailed setting will be specified in each simulation.

#### 4.1. Performance Comparison for Continuous Traffic

We evaluate the performance by comparing with other user selection schemes in terms of throughput gain. We set up an AP with 3 antennas and deploy 10 single-antenna users with randomly assignments of locations. Each of ten users have a different channel quality, and always have packets to receive. Before the transmission, AP obtains the queue information which is totally transmit data to each candidate users. Then AP estimates the bit-rate of each concurrent



packet based on the effective SNR which is calculated by each user.

Fig. 1 plots the CDF of the total throughput in 3 antennas scenarios, and shows the performance compared with other user selection schemes. The result shows that the traditional scheme, RUS, selecting users with an equal probability, without considering the channel characteristics and other criteria. Compared to RUS, the average throughput gain from enabling concurrent transmissions with TOUSE's user selection is about 50% in three antennas scenarios. This improvement mainly benefits from the following contributions: First, accurate rate prediction mechanism ensures the high packet reception rate, and reduce the time overhead without CSI feedback. Second, fully utilizing concurrent transmission time by overhead time matches based mechanism. The figure also shows that the PUMA-MIX and PUMA produce a throughput comparable to or even slightly higher than our user selection scheme. The performance of PUMA-MIX is similar to TOUSE's because the same kind of scheduling algorithm. Although the PUMA performs slightly better than TOUSE and PUMA-MIX, it caused  $10\times$  time overhead in the process of user selection than other two schemes. Besides, this time overhead is growing with the number of users.

#### 4.2. Throughput Fairness Analysis

In this section, we analyse the opportunities of user selection in a three antenna AP scenario, which is better to show the performance. In order to analyse the fairness of TOUSE, user should put into different scenario and evaluate the influence. There are five specific region, where has different channel quality and each region have one user to communicate with AP. In the simulation, *user1*, *user4* located in the region with worst and best channel quality, about  $5dB$  and  $20dB$  respectively. The quality of region *user2* is better than *user1*, but worse than *user3*, and *user5* is control group with randomly case.

During the user selection process, the user group for downlink transmission was selected one after another. In the first round of simulation, TOUSE chooses a lucky user randomly, which means that TOUSE enables all clients to get al-

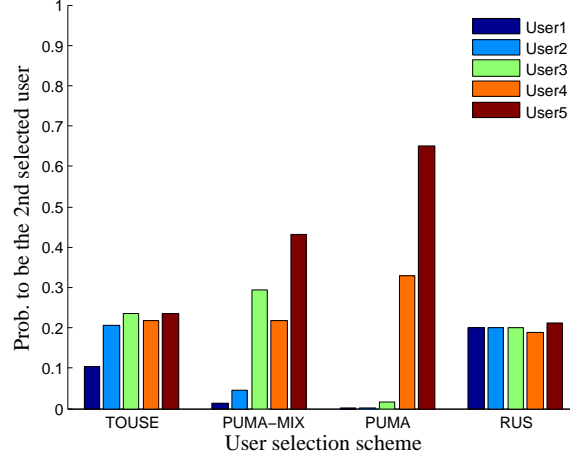


Figure 2: Fairness comparison in a 3-antenna AP scenario

most an equal probability to be selected first. In order to shows more convincing result, we plot in Fig. 2. The opportunities to be second selected for each user in total selection process, which is the metric using for evaluate fairness. The figure show that both the RUS scheme and our TOUSE enable all users to get almost an equal probability to be the second selected user. This implies that TOUSE enables users to achieve a similar level of fairness compared with fair contention mechanism. The probability of *user1* in TOUSE is slightly lower than other users. Because *user1* located in a region with the worst channel quality, leading to the lowest throughput. In PUMA and PUMA-MIX, it gave little chance to low-throughput users. The user who has higher value of SNR get more opportunities to be selected. Because these schemes selected concurrent transmit group just depend on throughput of each user.

In order to display the performance of TOUSE more clear, we give one of the most relevant fairness indicators called Jain's fairness index (JFI) [15]. The definition as following.

$$JFI = \frac{[\sum_{u=1}^{N_u} X_u]^2}{N_u \sum_{u=1}^{N_u} [X_u]^2}. \quad (11)$$

Where  $N_u$  presents the total number of users competing for channel,  $X_u$  denotes

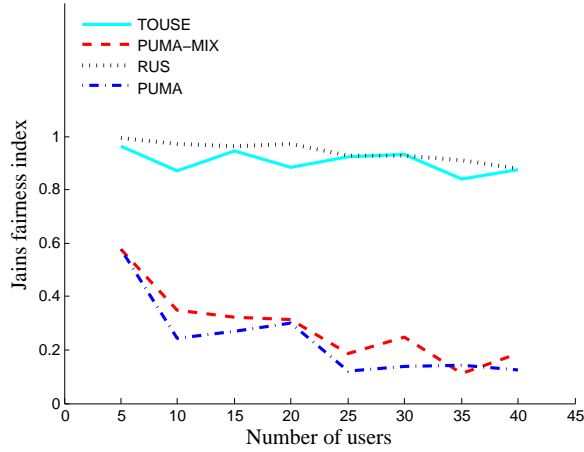


Figure 3: Jain's fairness index versus the number of users for different user selection mechanism

channel access times of user  $u$  at some time.  $JFI$  ranges from  $1/N_u$  (only one user is served) to 1 (all users are served at the same chance). Fig. 3 plots the Jain's fairness index for TOUSE, PUMA-MIX, PUMA and RUS as a function of the number of users in a 3-antenna AP scenario. It shows that the fairness performance of the proposed TOUSE clearly outperforms PUMA and almost close to the ideal case.

#### 4.3. Effect of Number of Transmit Antennas

Here we present the performance by showing the impact of number of transmit antennas on the throughput. In the simulation, we set that the number of transmitting antennas at the AP varies from 2 to 8, and 30 users which randomly distributed around AP competing for the channel. Fig. 4 plots the performance of throughput. It shows that user selection is also important even for small scale MU-MIMO system, but it is more necessary for large scale system. Compared with these user selection schemes, all achieve a similar capacity gain, when the number of antennas increases. The ceiling of throughput is reached with the antennas number growing, due to a large amount of interference between with the inter-user. Besides, the result implies that increasing the number of paralld streams is not always the most efficient transmission scheme. We will prove that

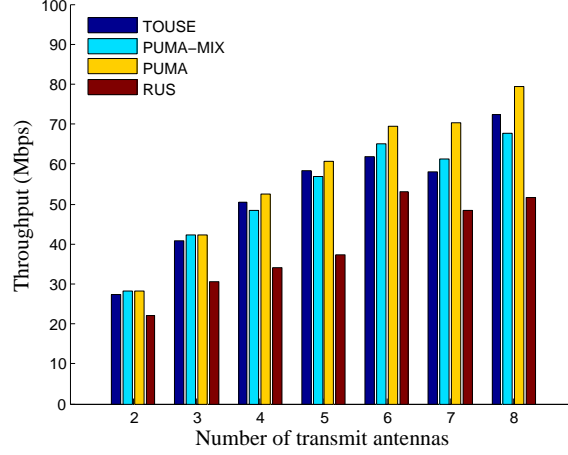


Figure 4: Performance in different AP scenario

whether the TOUSE can perform scalability.

#### 4.4. Impact of Number of Users

365 Here we evaluate the performance of TOUSE when the number of users varies from 5 to 50. We check the total network throughput gain increased by TOUSE when each users just have limited packet to receive. In each simulation, the AP transmits concurrent queue packets to the matches user, and thereby the throughput is calculated based on the process of transmission.

370 We plot the Fig. 5 to shows the performance of scalable. The effect of increasing the number of user on TOUSE, PUMA and PUMA-MIX is relatively small, implies that the TOUSE is performing well even when the network scales up. Since the RUS does not consider the channel characteristics and packet queueing status of users, its total network capacity is poor. But its performance is also independent of the number of users. During this simulation, PUMA 375 get higher throughput whatever the network scales up due to the exhaustively research compared with other schemes. But the total throughput of PUMA-MIX is similar to TOUSE, which means that our user selection have similar level of throughput with a throughput first contention mechanism.

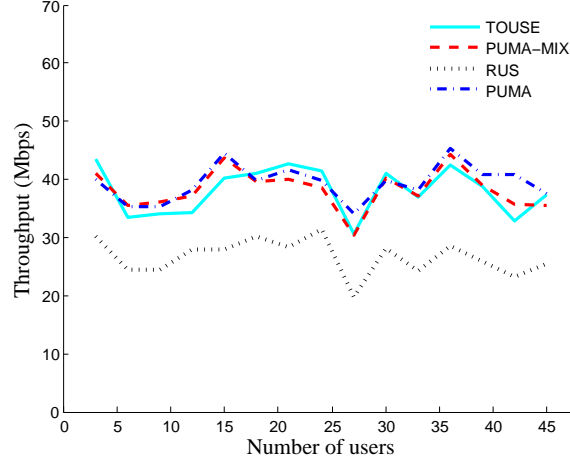


Figure 5: Performance impact by number of users

#### 4.5. Performance in Different Channel Quality Regions

In order to evaluate how TOUSE performs where the network has the worst channel quality, we make several simulations which have different channel qualities. In a low SNR region, the value of SNR just varies from 0 to 5dB, and varies from 15 to 20dB in a highest region. We set that the 10 users locate in a region with similar channel quality. Fig. 6 reveals that user selection mechanism is not so significant for MU-MIMO in a low SNR region. Because the interference is large enough to each users no matter what the combination of beamforming group. However, with higher link qualities, these user selection scheme which consider the channel characteristics of users performs obviously better than RUS. Figure also shows that the TOUSE causes a capacity improvement over RUS even in a low SNR region. Compared with PUMA and PUMA-MIX, TOUSE performs same level or slightly poor in mostly scenario. But TOUSE achieve a similar capacity gain with going better of the channel quality. Obviously, TOUSE can performance better in different channel quality regions.

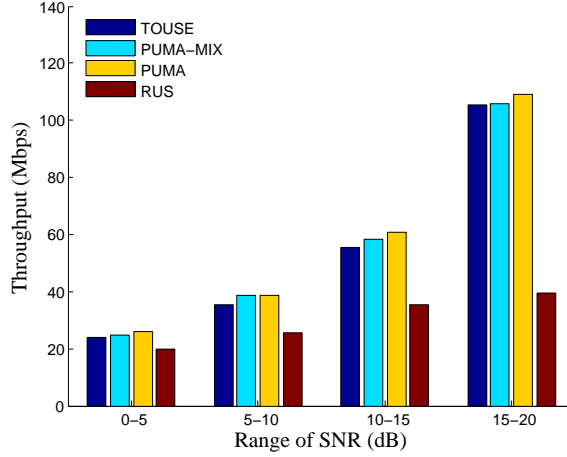


Figure 6: Performance in different channel quality region

## 5. RELATED WORK

Wireless standards like 802.11ac [16], LTE [17] have recently pushed toward the use of MU-MIMO for obtaining high-speed and high-throughput wireless communication. The work [10] presented a study to random access based on  
400 MAC mechanisms for MU-MIMO, and gives a survey and categorize to the most relevant MU-MIMO MAC proposals. It also identified key requirements for designing efficient MU-MIMO MAC protocols including de/pre-coding [1] and scheduling schemes. The potential of MU-MIMO has been investigated both theoretically [18] and empirically [8], which studied pre-coding techniques,  
405 scheduling schemes and practical gain of MU-MIMO in various environments.

Substantial theoretical works [19] assumed that CSI is available and paid much attention on implementing low-complexity algorithms to approach the maximum throughput. Xie *et al.*, [3] presented scalable and adaptive user selection which requires several rounds of CSI feedback instead of gathering from  
410 all users. However, in reality, the vulnerabilities of CSI [20] still exists due to its estimation methods, like time overhead. To avoid overwhelming the actual channel time spent on transmission, the schemes of user selection without CSI feedback was proposed. The authors of [21] design an orthogonality evalua-

tion mechanism which enables each user using its own CSI to speculate. But  
415 it can only be applied to uplink MU-MIMO. In [5], it proposed a method of  
user selection prior to channel sounding and exploits theoretical properties of  
MU-MIMO system to estimate data rate. PUMA achieves better performance  
in throughput, however, does not do well in respect of fairness.

Some other works focus on the scheduling scheme of user selection [22]. Most-  
420 ly [23] either iteratively select a user that minimizes the interference, reduce the  
complexity or maximizes the aggregate throughput. In [9], a novel search and  
update strategy was proposed for user selection. It designed a knob to control  
tradeoff between aggregate capacity and computational complexity. The work  
[24] present a low complexity scheduling scheme using block diagonalization  
425 with chordal distance.

In addition, some experimental studies emerged, like [25]. Authors realizes  
netMIMO downlink transmission for large-scale wireless network. By organiz-  
ing a network into clusters, it could manage interference with a decentralized  
channel-access algorithm, but environment is limited in static network since  
430 time-averaged CSI is used as input. In [26], Shen *et al.*, introduced Turbo-  
Rate, client annotates its packets with single SNR and direction at the AP to  
obtain the optimal bit rate and could transmit concurrently. Now there are  
more conditions are considered, like mobility [27] or channel control [28]. The  
exciting thing is that the team of Xinyu Zhang [29] has optimized MU-MIMO  
435 performance in 802.11ac commodity devices.

So far, there are three key points in MU-MIMO MAC protocol design:  
throughput, complexity and fairness [30]. But most researches only consider  
two or one of these points. TOUSE designs a novel metric without CSI feed-  
back benefiting from [12], and present a fair user selection mechanism based on  
440 overhead time matches.

## 6. CONCLUSION

In this paper, we have presented TOUSE, a scalable and fairness user selection scheme for downlink MU-MIMO. TOUSE is a proportional fair scheduler usually considers both network capacity and fairness. In order to reduce time  
445 overhead, we adopt a novel per-user data-rate estimation method without any CSI feedback. TOUSE selects optimal beamforming group by dynamic time warping based on mechanism, which makes full use of concurrent transmitting time and achieves equal opportunity of channel contention. We have simulated TOUSE along with three other user selection schemes. Simulation shows  
450 that TOUSE achieves a  $1.5\times$  throughput gain over traditional scheme in three antennas AP scenarios. and the similar level of fairness compared with fair contention mechanism. We also proved that TOUSE can always achieve similar performance of throughput compared with throughput contention schemes. More details of QoS will be considered in our future work.

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