

VIETNAM NATIONAL UNIVERSITY, HANOI  
UNIVERSITY OF ENGINEERING AND TECHNOLOGY



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# OPTIMIZE CNF ENCODING FOR ITEMSET MINING TASKS

Major: Computer Science

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Supervisor: Dr. To Van Khanh

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# ABSTRACT

**Summary:** In this thesis, we apply the "Sequential Encounter Encoding" method to optimize itemset mining tasks. This method has been proven effective in optimizing the search process for itemsets in data. By utilizing "Sequential Encounter Encoding" we aim to enhance the performance of itemset mining algorithms while minimizing processing time.

We conduct a series of experiments on real-world datasets to evaluate the performance of the applied method. Experimental results demonstrate a significant improvement in accuracy and efficiency compared to traditional methods. The application of this method not only enhances the performance of data mining processes but also opens up potential applications for similar problems in the field of data science and information retrieval.

**Keywords:** *SAT, SAT Encoding, Sequential Encounter Encoding, Itemset Mining Tasks*

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Thank you sincerely!

Le Tuan Anh

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## AUTHORSHIP

I hereby declare that the thesis "OPTIMIZE CNF ENCODING FOR ITEMSET MINING TASKS" is done by me and has never been submitted as a report for Graduation Thesis at University of Engineering and Technology - Vietnam National University, Hanoi, or any other university. All content in this thesis is written by me and has not been copied from any source, nor is the work of others used without specific citation. I also warrant that the source code is my development and does not copy the source code of any other person. If wrong, I would like to take full responsibility according to the regulations of University of Engineering and Technology - Vietnam National University, Hanoi.

Ha Noi, May 26 2024

Student

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## SUPERVISOR'S APPROVAL

I hereby approve that the thesis in its current form is ready for committee examination as a requirement for the Bachelor of Computer Science degree at the University of Engineering and Technology.

Ha Noi, May 26 2024

Supervisor

Dr. To Van Khanh

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## Introduction

This chapter will focus on introducing the itemset mining tasks and SAT encoding, encompassing their concepts, related terms, and applications.

### 1.1 Itemset Mining Tasks

#### 1.1.1 Overview

Frequent item sets are a key technique in the realm of data mining, specifically aimed at uncovering relationships among different items within a dataset. The essence of association rule mining lies in identifying those item relationships that occur frequently together in the dataset.

In simpler terms, a frequent item set refers to a collection of items that commonly appear together in the dataset. We measure the frequency of an item set using what's known as the support count. This count tells us how many times the particular set of items crops up together in transactions or records within the dataset. In practice, the goal is to find item sets with a minimum support, indicating how frequently they occur in transactions or records within the dataset.

For example, with a dataset of transactions from a retail store

Tid	Itemsets
1	apple, banana, cherry
2	apple, mango
3	apple, cherry
4	mango, cherry
5	apple, mango, cherry

**Table 1.1:** Example of a dataset of transactions

With minimum support is 3, we need to find all itemsets appearing in at least 3 transactions and return the following result:

- Itemset 1: {apple, cherry} in transactions [1, 3, 5]
- Itemset 2: {apple} in transactions [1, 2, 3, 5]

### 1.1.2 Technical background

Firstly, we establish several symbols to represent the itemset mining problem. These symbols aid in formalizing the problem and defining key concepts. For instance, we denote:

- $\Omega$ : a set of all items
- $I$ : an itemset in  $\Omega$ , where  $I \subseteq \Omega$
- $T_i$ : a transaction identifier. For  $T_i = (i, I)$
- $D$ : a transaction database, where  $D$  contains a set of transactions,  $D = \{T_1, T_2, \dots, T_n\}$
- $Supp(I, D)$ : the support of itemset  $I$  in database  $D$ , where  $Supp(I, D)$  is the number of transactions in  $D$  that contain  $I$

For example, in table 1.1, we have:

- $\Omega$  is {apple, banana, cherry, mango}
- $I$  can be {apple}, {apple, mango}, {apple, mango, cherry}, ...
- $D = \{(1, \{\text{apple, banana, cherry}\}), (2, \{\text{apple, mango}\}), (3, \{\text{apple, cherry}\}), (4, \{\text{mango, cherry}\}), (5, \{\text{apple, mango, cherry}\})\}$
- $T_1 = (1, \{\text{apple, banana, cherry}\}), T_2 = (2, \{\text{apple, mango}\}), T_3 = (3, \{\text{apple, cherry}\}), \dots$
- $Supp(\{\text{apple, cherry}\}, D) = 3, Supp(\{\text{apple}\}, D) = 4, \dots$

Let  $\lambda$  be the minimum support threshold, the frequent itemset mining problem is to find all itemsets  $I$  such that  $Supp(I, D) \geq minsup$ . In general, it can present by:

$$FIM(D, \lambda) = \{I \subseteq \Omega \mid Supp(I, D) \geq \lambda\}$$

## **1.2 SAT Encoding**

### **1.2.1 Concept**

### **1.2.2 SAT Solvers**

### **1.2.3 Applications**

## SAT-based Encoding of Itemset Mining

In this chapter, we present how to encode the itemset mining problem into a SAT problem. And we will discuss the limitation of the standard method.

### 2.1 Constraint Encoding

To resolve the itemset mining problem, we using the SAT encoding approach. In essence, SAT encoding involves the creation of variables and the imposition of constraints to represent the itemset mining problem. These variables serve to denote the presence or absence of items within a candidate itemset and are subjected to linear inequalities to ensure the itemset's support.

In the context of a transaction database  $D = (1, T_1), \dots, (m, T_m)$  and a minimum support threshold  $\lambda$ , each item in the candidate itemset  $X$ , we denote:

- $p_a$ : is *true* if the item  $a$  is in the itemset  $X$ , otherwise  $p_a = false$
- $q_i$ : is *true* if the transaction  $T_i$  contains the itemset  $X$ , otherwise  $q_i = false$

Alongside, a set of constraints is imposed on these variables to establish a one-to-one correspondence between the models of the resulting CNF formula and the set of itemsets.

Firstly, to capture all the transactions where the candidate itemset does not appear, we use following constraint:

$$\bigwedge_{i=1}^m (q_i \leftrightarrow \bigwedge_{a \notin T_i} \neg p_a) \quad (2.1)$$

This constraint guarantees that  $q_i$  is true if and only if either all items not in  $T_i$  are also not in the itemset  $X$ , or transaction  $T_i$  contains the itemset  $X$ .

Constraint 2.1 can be rewritten as follows:

$$\bigwedge_{a \in \Omega} \bigwedge_{a \notin T_i} (\neg p_a \vee \neg q_i) \quad (2.2)$$

$$\bigwedge_{T_i \in D} ((\bigvee_{a \notin T_i} p_a) \vee q_i) \quad (2.3)$$

Finally, the frequency constraint, can be simply expressed as follows:

$$\sum_{i=1}^m q_i \geq \lambda \quad (2.4)$$

For example, with a dataset of transactions from a retail store in table 1.1, we mark: a = apple, b = banana, c = cherry, d = mango. Then we have database transactions

Tid	a	b	c	d
1	1	1	1	0
2	1	0	0	1
3	1	0	1	0
4	0	0	1	1
5	1	0	1	1

**Table 2.1:** Example of a dataset of transactions after convert

The itemset mining problem will be defined as:

$$\begin{aligned}
q_1 &\leftrightarrow (\neg p_d) \\
q_2 &\leftrightarrow (\neg p_b \wedge \neg p_c) \\
q_3 &\leftrightarrow (\neg p_b \wedge \neg p_d) \\
q_4 &\leftrightarrow (\neg p_a \wedge \neg p_d) \\
q_5 &\leftrightarrow (\neg p_b) \\
q_1 + q_2 + q_3 + q_4 + q_5 &\geq \lambda
\end{aligned}$$

## 2.2 Standard Method in Itemset Mining

## 2.3 Limitation of Standard Method

## Sequential Encounter Encoding for Optimization

### 3.1 Sequential Encounter Encoding

### 3.2 Optimization CNF Encoding using Sequential Encounter Encoding

## Experiments

### 4.1 Experimental Setup and Datasets

### 4.2 Results and Analysis



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## Conclusions