

Integration of Trigonometric (power) Functions — Rules

$$\text{P4.} \quad \int \sin^2(mx) \, dx = \frac{1}{2m} (mx - \sin(mx) \cos(mx)) + C$$

$$\text{P5.} \quad \int \cos^2(mx) \, dx = \frac{1}{2m} (mx + \sin(mx) \cos(mx)) + C$$

$$\text{P6.} \quad \int \sin^n(x) \, dx = -\frac{\sin^{n-1}(x) \cos(x)}{n} + \frac{n-1}{n} \int \sin^{n-2}(x) \, dx$$

$$\text{P7.} \quad \int \cos^n(x) \, dx = \frac{\cos^{n-1}(x) \sin(x)}{n} + \frac{n-1}{n} \int \cos^{n-2}(x) \, dx$$

$$\text{P8.} \quad \int \sin^m(x) \cos^n(x) \, dx = \frac{\sin^{m+1}(x) \cos^{n-1}(x)}{n+m} + \frac{n-1}{n+m} \int \sin^m(x) \cos^{n-2}(x) \, dx, \quad \text{for } m \neq 1 \text{ or } n \neq 1$$

$$\text{P9.} \quad \int \operatorname{tg}^n(x) \, dx = \frac{\operatorname{tg}^{n-1}(x)}{n-1} - \int \operatorname{tg}^{n-2}(x) \, dx, \quad n \neq 1$$

$$\text{P10.} \quad \int \operatorname{cotg}^n(x) \, dx = -\frac{\operatorname{cotg}^{n-1}(x)}{n-1} - \int \operatorname{cotg}^{n-2}(x) \, dx, \quad n \neq 1$$

$$\text{P11.} \quad \int \sec^n(x) \, dx = \frac{\operatorname{tg}(x) \sec^{n-2}(x)}{n-1} + \frac{n-2}{n-1} \int \sec^{n-2}(x) \, dx, \quad n \neq 1$$

$$\text{P12.} \quad \int \operatorname{cosec}^n(x) \, dx = -\frac{\operatorname{cotg}(x) \operatorname{cosec}^{n-2}(x)}{n-1} + \frac{n-2}{n-1} \int \operatorname{cosec}^{n-2}(x) \, dx, \quad n \neq 1$$