

## **Example 2 (Complementary events, reunion, intersection)**

Consider A and B, two events from a sample space S.

Knowing that P(A) = 0.5,  $P(\bar{A} \cap \bar{B}) = 0.1$  and  $P(A \cap B) = P(B \cap \bar{A})$ , calculate P(B).

## **Answer:**

If 
$$P(\bar{A} \cap \bar{B}) = 0.1$$
, then  $P(A \cup B) = 1 - P(\bar{A} \cap \bar{B}) = 1 - 0.1 = 0.9$ 

For any two events A and B,  $P(A \cup B) = P(A) + P(B) - P(A \cap B)$ 

This means that  $P(B) - P(A \cap B) = 0.4$ 

As 
$$P(B) - P(A \cap B) = P(B \cap \overline{A})$$
, then  $P(B \cap \overline{A}) = 0.4$ 

Hence,  $P(A \cap B) = 0.4$  and P(B) = 0.8