

Direct integration (or direct inspection)

Examples:

$$\bullet \int 3 \, dx = 3x + C$$

$$\bullet \int \frac{1}{2} \, dx = \frac{x}{2} + C$$

$$\bullet \int -5 \, dx = -5x + C$$

$$\bullet \int 10^3 \, dx = 10^3 x + C$$

Formula

$$\rightarrow \int k \, dx = kx + C$$

k a constant

$$\downarrow$$
$$(Kx + C)' = k$$



• $\int x \, dx = \frac{x^2}{2} + C$

• $\int f' \cdot f^m \, dx = \frac{f^{m+1}}{m+1} + C$

$\left. \begin{array}{l} f(x) = x \\ m = 1 \Rightarrow m+1 = 2 \\ f'(x) = 1 \end{array} \right\}$

• $\int 1 \cdot x^3 \, dx = \frac{x^4}{4} + C$

$\left. \begin{array}{l} f' = 1 \\ f = x^3 \end{array} \right\}$

• $\int 1 \cdot x^{1/2} \, dx = \frac{x^{3/2}}{3/2} + C = \frac{2}{3} x^{3/2} + C$

$\left. \begin{array}{l} f' = 1 \\ f = x^{1/2} \end{array} \right\}$

$m = \frac{1}{2} \Rightarrow m+1 = \frac{3}{2}$

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$$\bullet \int \underbrace{1}_{f'} \cdot \underbrace{(x+1)}_f \overset{(3) \rightarrow m}{dx} = \frac{(x+1)^4}{4} + C$$

$$\bullet \int \underbrace{2x}_{f'} \cdot \underbrace{(x^2+1)}_f \overset{(10) \rightarrow m}{dx} = \frac{(x^2+1)^{11}}{11} + C$$

$m+1 = 10+1 = 11$

$$\bullet \int x^2 \underbrace{(x^3+2)}_f dx = \frac{1}{3} \int \underbrace{3x^2}_{f'} \cdot (x^3+2)^5 dx =$$

$$\Rightarrow f'(x) = 3x^2$$

$$= \frac{1}{3} \cdot \frac{(x^3+2)^6}{6} + C$$

$$= \frac{(x^3+2)^6}{18} + C$$

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