Facultad de Ciencias, UNAM Lenguajes de Programación Tarea 7

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- 1. Da la derivación de las siguientes expresiones usando las reglas de semántica operacional para FAE, vistas en clase:
 - a) {- {{fun {x} x} 2 } {+ 3 5}} SOLUCIÓN:

b) {{fun {x} {fun {y}{+ x y}}} 2} 3} SOLUCIÓN:

$$\begin{array}{c|ccccc} A & B & C & & E & F \\ \hline D & & H & G \\ \hline & & T & & \end{array}$$

donde

- A = {fun {x} {fun {y} {+ x y}}}, $\emptyset \Rightarrow \langle x, \{fun \{y\} \{+ x y\}\}, \emptyset \rangle$
- lacksquare B = 2, $arnothing \Rightarrow \hat{2}$
- C = {fun {y} {+ x y}}[x \leftarrow 2] \Rightarrow \langle y, {+ x y}, [x \leftarrow 2] \rangle
- D = {{fun {x} {fun {y} {+ x y}}} 2}, $\varnothing \Rightarrow \langle y, {+ x y}, [x \leftarrow \hat{2}] \rangle$
- E = x, $[x \leftarrow \hat{2}, y \leftarrow \hat{3}] \Rightarrow [x \leftarrow \hat{2}, y \leftarrow \hat{3}](x) = \hat{2}$
- F = y, $[x \leftarrow \hat{2}, y \leftarrow \hat{3}] \Rightarrow [x \leftarrow \hat{2}, y \leftarrow \hat{3}](y) = \hat{3}$
- \blacksquare G = {+ x y}, [x \leftarrow 2̂, y \leftarrow 3̂] \Rightarrow 5̂
- \blacksquare H = 3, $\varnothing\Rightarrow \hat{3}$
- I = {{fun {x} {fun {y} {+ x y}}} 2} 3}, $\varnothing \Rightarrow \hat{5}$
- 2. Realiza el juicio de tipo para cada una de las siguientes expresiones, usa las reglas visitas en clase.
 - $\begin{array}{c} (a) \ \{ \texttt{with} \ \{ \texttt{a} \ : \ \texttt{number} \ 2 \} \\ \\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \end{array}$

(b) {fun {x : number} : number {+ x 2}}

(c) {{fun {x} {+ x 2}} {+ 3 4}}

(d) {with {f : {number -> number} {fun {x : number} : number {+ x 2}}} {f {+ 3 4}}}

$$\begin{array}{c|cccc} A & B & & F & G \\ \hline \underline{C} & E & H \\ \hline & I & \\ \end{array}$$

Donde:

$$A \text{ es } [x \leftarrow number] \vdash x : number$$

$$B \text{ es } [x \leftarrow number] \vdash 2 : number$$

$$C \text{ es } [x \leftarrow number] \vdash \{+x \ 2\} : number$$

$$D \in \mathcal{Q} \vdash \{fun\{x : number\} : number\{+x\ 2\}\} : \{number \rightarrow number\}$$

$$E \text{ es } [f \leftarrow \{number \rightarrow number\}] \vdash f : \{number \rightarrow number\}$$

$$F \text{ es } [f \leftarrow \{number \rightarrow number\}] \vdash 3 : number$$

$$G \text{ es } [f \leftarrow \{number \rightarrow number\}] \vdash 2 : number$$

$$H \text{ es } [f \leftarrow \{number \rightarrow number\}] \vdash \{+34\} : number$$

$$I \text{ es } [f \leftarrow \{number \rightarrow number\}] \vdash \{f\{+34\}\} : number$$

$$J \text{ es } \varnothing \vdash \{with\{f: \{number \rightarrow number\} \{fun \ \{x: number\}: number \ \{+ \ x \ 2\}\}\} \ \{f\{+ \ 3 \ 4\}\}\}: number$$

(e) {with {g {fun {x} {x 4}}} {g {fun {y} {- y 2}}}}

$$\begin{array}{c|c}
A & B \\
\hline
C \\
D
\end{array}
\qquad
\begin{array}{c|c}
E & \hline
H \\
\hline
J
\end{array}$$

Donde:

$$A \text{ es } [x \leftarrow number] \vdash x : \{number \rightarrow number\}$$

$$B \text{ es } [x \leftarrow number] \vdash 4 : number$$

$$C \text{ es } [x \leftarrow number] \vdash \{x \ 4\} : number$$

$$D \in \mathcal{Q} \vdash \{fun\{x : number\} : number\{x \ 4\}\} : \{number \rightarrow number\}$$

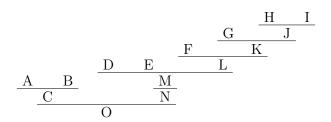
$$E \text{ es } [f \leftarrow \{number \rightarrow number\}] \vdash g : \{number \rightarrow number\}$$

$$F \text{ es } [f \leftarrow \{number \rightarrow number\}, y \leftarrow number] \vdash y : number$$

$$G \text{ es } [f \leftarrow \{number \rightarrow number\}, y \leftarrow number] \vdash 2 : number$$

$$H \text{ es } [f \leftarrow \{number \rightarrow number\}, y \leftarrow number] \vdash \{-y \ 2\} : number$$

```
I \  \, es \  \, [f \leftarrow \{number \rightarrow number\}] \vdash \{fun\{y\}\{-y\ 2\}\} : \{number \rightarrow number\} \\ J \  \, es \  \, [f \leftarrow \{number \rightarrow number\}] \vdash \{g\ \{fun\{y\}\{-y\ 2\}\}\} : number \\ K \  \, es \  \, \varnothing \vdash \{with\{g: \{number \rightarrow number\}\ \{fun\{x: number\}: number\{x\ 4\}\}\} \{g\ \{fun\{y\}\{-y\ 2\}\}\}\} : number \\ \{fun\  \, \{ex: \{number\}\}: number\} \} \\ \{fun\  \, \{ex: \{number\}\}: number \} \} \} \} \\ \{fun\  \, \{ex: \{number\}\}: \{fun\  \, \{ex: \{number\}\}\} \} \} \} \} \}
```



Donde:

```
A \text{ es } [f \leftarrow \{number \rightarrow number\}] \vdash f : \{number \rightarrow number\}
   B \text{ es } [f \leftarrow \{number \rightarrow number\}] \vdash 5 : number
   C \text{ es } [f \leftarrow \{number \rightarrow number\}] \vdash \{f \ 5\} : number
   D \text{ es } [f \leftarrow \{number \rightarrow number\}, \ x \leftarrow number] \vdash x : number
   E \text{ es } [f \leftarrow \{number \rightarrow number\}, \ x \leftarrow number] \vdash 1 : number
   F \text{ es } [f \leftarrow \{number \rightarrow number\}, \ x \leftarrow number] \vdash x : number
   G \text{ es } [f \leftarrow \{number \rightarrow number\}, x \leftarrow number] \vdash f : \{number \rightarrow number\}
  H \text{ es } [f \leftarrow \{number \rightarrow number\}, x \leftarrow number] \vdash n : number
      I \text{ es } [f \leftarrow \{number \rightarrow number\}, \ x \leftarrow number] \vdash \{-n \ 1\} : number
    J \text{ es } [f \leftarrow \{number \rightarrow number\}, \ x \leftarrow number] \vdash 1 : number
  K \text{ es } [f \leftarrow \{number \rightarrow number\}, \ x \leftarrow number] \vdash \{f\{-n \ 1\}\} : number
   L \text{ es } [f \leftarrow \{number \rightarrow number\}, \ x \leftarrow number] \vdash \{*n\{f\{-n \ 1\}\}\} : number\}
M \text{ es } [f \leftarrow \{number \rightarrow number\}, \ x \leftarrow number] \vdash \{if0 \ x \ 1\{* \ n \ \{f\{-n \ 1\}\}\}\}\}: number
 N \text{ es } [f \leftarrow \{number \rightarrow number\}] \vdash \{fun\{x : number\} : number\{if0 \ x \ 1\{* \ n \ \{f\{-n \ 1\}\}\}\}\}\} : number\{if0 \ x \ 1\{* \ n \ \{f\{-n \ 1\}\}\}\}\}\}
                 \{numero \rightarrow numero\}
   O \ \operatorname{es} \varnothing \vdash \{\{\operatorname{rec}\{f: \{\operatorname{number} \to \operatorname{number}\} \mid fun\{x: \operatorname{number}\} : \operatorname{number} \mid fun\{x: \operatorname{number}\} \mid 
                 number
```

3. Para cada una de las siguientes expresiones, realiza su inferencia de tipos generando las restricciones de tipo correspondientes

```
a) (define (potencia a b)
          (if (zero? b)
           1
           (* a (potencia a (sub1 b)))))
```

SOLUCIÓN: Primero, identificamos cada una de nuestras sub-expresiones y las enumeramos.

- $\boxed{0}$ (define (potencia a b) (if (zero? b) 1 (* a (potencia a (sub1 b)))))
- 1 (if (zero? b) 1 (* a (potencia a (sub1 b))))
- 2 (zero? b)

- **3** 1
- 4 (* a (potencia a (sub1 b)))
- \bullet $\boxed{5}$ (potencia a (sub1 b))
- 6 (sub1 b)

Luego, vamos a analizar el tipo de expresiones que encontramos.

Para la cajita cero,

$$[[\boxed{0}]] = [[a]] \times [[b]] \rightarrow [[\boxed{1}]]$$

Para la primer cajita,

$$[[\boxed{1}]] = [[\text{ (if (zero? b) 1 (* a (potencia a (sub1 b))))}]]$$

$$= [[\text{ (if }\boxed{2}\boxed{3}\boxed{4})]]$$

de donde

- $\bullet \ [[\boxed{1}\]] = [[\boxed{3}\]]$
- $\bullet \ [[\ \boxed{1} \]] = [[\ \boxed{4} \]]$
- $\bullet \ [[\ \boxed{3}\]] = [[\ \boxed{4}\]]$
- \bullet [[2]] = boolean
- Para la segunda cajita,

$$[[\boxed{2}]] = [[(\texttt{zero? b})]]$$

de donde

- [[(zero? b)]] = boolean
- [[b]] = number
- Para la tercer cajita,

$$[[\ \boxed{3}\]] = [[1]] = \mathtt{number}$$

Para la cuarta cajita,

$$[[4]] = [[(* a (potencia a (sub1 b)))]]$$
$$= [[(* a [5]]]$$

de donde

- $\bullet \ [[\, \boxed{4}\,]] = \mathtt{number}$
- $\bullet \ [[\mathtt{a}]] = \mathtt{number}$
- $\bullet \ [[\, \boxed{5}\,]] = \mathtt{number}$
- Para la quinta cajita,

$$[[5]] = [[(potencia a (sub1 b))]]$$
$$= [[(potencia a 6)]]$$

de donde $[[a \rightarrow \boxed{6}]]$

• Para la sexta cajita,

$$[[6]] = [[(sub1 b)]]$$

de donde

- [[(sub1 b)]] = number
- [[b]] = number

Por lo tanto, el tipo de la función potencia es

potencia: number number -> number

donde a y b son ambos number.

Solución: Primero, identificamos cada una de nuestras sub-expresiones y las enumeramos.

- lacksquare 0 (define (suma 1) (if (nempty? 1) 0 (ncons (nfirst 1) (suma (nrest 1)))))
- 1 (if (nempty? 1) 0 (ncons (nfirst 1) (suma (nrest 1))))
- 2 (nempty? 1)
- **3** 0
- 4 (ncons (nfirst 1) (suma (nrest 1)))
- 5 (nfirst 1)
- 6 (suma (nrest 1))
- 7 (nrest 1)

Luego, vamos a analizar el tipo de expresiones que encontramos.

• Para la cajita cero,

$$[[\ \boxed{0} \]] = [[l]] \rightarrow [[\ \boxed{1} \]]$$

• Para la primer cajita,

de donde

- $\bullet \ [[\boxed{1}]] = [[\boxed{3}]]$
- $\bullet \ [[\ \boxed{1}\]] = [[\ \boxed{4}\]]$
- [[3]] = [[4]]
- $\lceil \lceil 2 \rceil \rceil = \texttt{boolean}$
- Para la segunda cajita,

$$[[2]] = [[(nempty? 1)]]$$

de donde

- [[(nempty? 1)]] = boolean
- [[b]] = nlist
- Para la tercer cajita,

$$[[\,\boxed{3}\,]] = [[\mathbf{0}]] = \mathtt{number}$$

Para la cuarta cajita,

$$[[4]] = [[(ncons (nfirst 1) (suma (nrest 1)))]]$$
$$= [[(ncons [5] [6])]]$$

de donde

- [[4]] = nlist
- [[5]] = [[(nfirst 1)]] = number
- $[[\lfloor 6 \rfloor]] = [[(suma (nrest 1))]]$ • $[[suma]] = [[(nrest 1)]] \rightarrow [[\lceil 6 \rceil]] = [[\lceil 7 \rceil]] \rightarrow [[\lceil 6 \rceil]] = nlist$

Sin embargo, por el análisis de la primer cajita tenemos que [[3]] = [[4]], pero

$$[[\ \boxed{3}\]] = \mathtt{number} \neq \mathtt{nlist} = [[\ \boxed{4}\]]$$

Por lo tanto, obtenemos una contradicción.

c) (define (nfilter p 1)

(cond

[(nempty? 1) nempty]
[(p (nfirst 1)) (ncons (nfirst 1) (nfilter p (nrest 1)))]
[else (nfilter p (nrest 1))]))

Solución: Primero, identificamos cada una de nuestras sub-expresiones y las enumeramos.

- 0 (define (nfilter p 1) (cond [(nempty? 1) nempty] [(p (nfirst 1)) (ncons (nfirst 1) (nfilter p (nrest 1)))] [else (nfilter p (nrest 1))]))
- 1 (cond [(nempty? 1) nempty] [(p (nfirst 1)) (ncons (nfirst 1) (nfilter p (nrest 1)))] [else (nfilter p (nrest 1))])
- 2 (nempty? 1)
- 3 nempty
- 4 (p (nfirst 1))
- 5 (nfirst 1)
- 6 (ncons (nfirst 1) (nfilter p (nrest 1)))
- 7 (nfirst 1)
- 8 (nfilter p (nrest 1))
- 9 (nrest 1)
- 10 else
- 11 (nfilter p (nrest 1))
- 12 (nrest 1)

Luego, vamos a analizar el tipo de expresiones que encontramos.

Para la cajita cero,

$$[[\ \boxed{0}\]] = [[p]] \times [[l]] \rightarrow [[\ \boxed{1}\]]$$

• Para la primer cajita,

$$\begin{split} [[\hspace{.08cm} \boxed{1}\hspace{.08cm}]] &= [[\hspace{.08cm} (\text{cond} \hspace{.08cm} \boxed{2} \hspace{.08cm} \boxed{3} \hspace{.08cm} \boxed{4} \hspace{.08cm} \boxed{6} \hspace{.08cm}] \hspace{.08cm} [\hspace{.08cm} \boxed{10} \hspace{.08cm} \boxed{11} \hspace{.08cm}])] \\ &= [[\hspace{.08cm} \boxed{2}\hspace{.08cm}]] \rightarrow [[\hspace{.08cm} \boxed{3}\hspace{.08cm}]] \text{or} [[\hspace{.08cm} \boxed{4}\hspace{.08cm}]] \rightarrow [[\hspace{.08cm} \boxed{6}\hspace{.08cm}]] \text{or} [[\hspace{.08cm} \boxed{10}\hspace{.08cm}]] \rightarrow [[\hspace{.08cm} \boxed{11}\hspace{.08cm}]] \end{aligned}$$

de donde

- \bullet $[[\boxed{2}]] = \mathtt{boolean}$
- $\lceil \lceil 4 \rceil \rceil = boolean$
- [[3]] = [[6]] = [[11]]
- Para la segunda cajita,

$$\lceil \lceil 2 \rceil \rceil = (nempty? 1)$$

de donde

- [[(nempty? 1)]] = boolean
- [[b]] = nlist

• Para la tercer cajita,

$$[\lceil \boxed{3} \rceil] = \mathtt{nempty} = \mathtt{nlist}$$

■ Para la cuarta cajita,

$$[[4]] = (p (nfirst 1))$$
$$= (p 5)$$

 $\mathrm{donde}\ [[\mathtt{p}]] = [[\ \boxed{5}\]] \to [[\ \boxed{4}\]]$

• Para la quinta cajita,

$$[\lceil 5 \rceil] = (nfirst 1)$$

de donde

- [[((nfirst 1))]] = number
- \bullet [[1]] = nlist
- Para la sexta cajita,

$$[[6]] = [[(ncons (nfirst 1) (nfilter p (nrest 1)))]]$$
$$= [[(ncons 7 8)]]$$

de donde

- $[\lceil \boxed{6} \rceil] = \texttt{nlist}$
- [[7]] = [[5]] = number
- [[8]] = (nfilter p (nrest 1)) = (nfilter p 9)• $[[nfilter]] = [[p]][[9]] \rightarrow [[8]] = nlist$
- Para la novena cajta,

$$[\lceil \boxed{9} \rceil] = (\text{nrest 1})$$

de donde

- [[(nrest 1)]] = nlist
- [[1]] = nlist
- Para la décima cajita,

$$\lceil\lceil \boxed{10}\rceil\rceil = \lceil [\mathtt{else}] = \lceil [\mathtt{true}] \rceil = \mathtt{boolean}$$

• Para la undécima cajita,

$$[\lceil \boxed{11} \rceil] = [\lceil \boxed{8} \rceil] = \mathtt{nlist}$$

Para la duodécima cajita,

$$[[\boxed{12}]] = [[\boxed{9}]] = \mathtt{nlist}$$

Por lo tanto, el tipo de la función nfilter es

donde p es una función del tipo (number -> boolean) y l es del tipo nlist.

- 4. Usando el algoritmo de unificación, muestra la inferencia de tipos de las siguientes expresiones:
 - $(\lambda$ (x) (x 2 3)) Con $1(2\lambda(x)(4x323))$:

Action	Stack	Substitution

	l cell ha cell ha cell ha	
Initialize	$ \begin{bmatrix} \begin{bmatrix} 1 \end{bmatrix} \end{bmatrix} = \begin{bmatrix} \begin{bmatrix} 2 \end{bmatrix} \end{bmatrix} \rightarrow \begin{bmatrix} \begin{bmatrix} 3 \end{bmatrix} \end{bmatrix} $ $ \begin{bmatrix} \begin{bmatrix} 2 \end{bmatrix} \end{bmatrix} = \begin{bmatrix} \begin{bmatrix} 4 \end{bmatrix} \end{bmatrix} $ $ \begin{bmatrix} \begin{bmatrix} 4 \end{bmatrix} \end{bmatrix} = \begin{bmatrix} \begin{bmatrix} 5 \end{bmatrix} \end{bmatrix} = number $ $ \begin{bmatrix} \begin{bmatrix} 6 \end{bmatrix} \end{bmatrix} = number $	empty
step2	$ \begin{bmatrix} $	$[\llbracket 1 \rrbracket] \to [\llbracket 2 \rrbracket] \to [\llbracket 3 \rrbracket]$
		ווו וווי וווי וווי וווי וווי וווי וווי
		$\left[\left[\begin{array}{c} 1 \\ \end{array} \right] \rightarrow \left[\left[\begin{array}{c} 2 \\ \end{array} \right] \rightarrow \left[\left[\begin{array}{c} 3 \\ \end{array} \right] \right]$
step2	$[[\underline{5}]] = number$	$[2] \rightarrow [4]$
	[[[6]]] = number	
	[[5]] = number	$[\hspace{-0.6em} [\hspace{-0.6em} 1\hspace{-0.6em}]\hspace{-0.6em}] \rightarrow [\hspace{-0.6em} [\hspace{-0.6em} 3\hspace{-0.6em}]\hspace{-0.6em}] \rightarrow [\hspace{-0.6em} [\hspace{-0.6em} 3\hspace{-0.6em}]\hspace{-0.6em}] \rightarrow [\hspace{-0.6em} [\hspace{-0.6em} 3\hspace{-0.6em}]\hspace{-0.6em}]$
step2	$[\overline{6}] = number$	
		$[\boxed{4}] \rightarrow [\boxed{5}] \times [\boxed{6}] \rightarrow [\boxed{3}]]$
	[[6]] = number	$[\hspace{-0.5em} [\hspace{-0.5em} 1\hspace{-0.5em}]\hspace{-0.5em}] \rightarrow (number \times [\hspace{-0.5em} [\hspace{-0.5em} 6\hspace{-0.5em}]\hspace{-0.5em}] \rightarrow [\hspace{-0.5em} [\hspace{-0.5em} 3\hspace{-0.5em}]\hspace{-0.5em}]) \rightarrow [\hspace{-0.5em} [\hspace{-0.5em} 3\hspace{-0.5em}]\hspace{-0.5em}]$
stape2		$[2] \rightarrow number \times [6] \rightarrow [3]$
btape2		$[\boxed{4}] \rightarrow number \times [\boxed{6}] \rightarrow [\boxed{3}]]$
		$[[\![\underline{5}]\!]] \rightarrow number$
		$\boxed{ [\llbracket 1 \rrbracket] \rightarrow (number \times number \rightarrow [\llbracket 3 \rrbracket]) \rightarrow [\llbracket 3 \rrbracket] }$
		$[\llbracket 2 \rrbracket] \rightarrow number \times number \rightarrow [\llbracket 3 \rrbracket]$
step2	empty	$[\llbracket \boxed{4} \rrbracket] \rightarrow number \times number \rightarrow [\llbracket \boxed{3} \rrbracket]$
		$[[5]] \rightarrow number$
		$[[\overline{6}]] \rightarrow number$
		[[[]]]

• ((λ (x) (* x 2)) (+ 2 3)) Con: (($2\lambda(x)$ 4(* x 2)) 3(+ 2 3)):

Action	Stack	Substitution
Initialize	$ \begin{bmatrix} 2 \end{bmatrix} = \begin{bmatrix} 3 \end{bmatrix} \rightarrow \begin{bmatrix} 1 \end{bmatrix} \\ \begin{bmatrix} 2 \end{bmatrix} = \begin{bmatrix} [x] \end{bmatrix} \rightarrow \begin{bmatrix} 4 \end{bmatrix} $	empty
	[[3]] = number	
step2	[3] = number	נעט י נעט י נעט
	$[[\underline{[4]}]] = number$	
	[[3]] = [[x]]	$[\hspace{-0.3em}\lfloor 2\hspace{-0.3em}\rfloor] \to [\hspace{-0.3em}\lfloor 3\hspace{-0.3em}\rfloor] \to [\hspace{-0.3em}\lfloor 1\hspace{-0.3em}\rfloor]$
step4		
	[[3]] = number	
	$[[\![4]\!]] = number$	
	$[\llbracket 1 \rrbracket] = [\llbracket 4 \rrbracket]$	$[[\underline{2}]] [[x]] \rightarrow [[\underline{1}]]$
step2	$[\underline{[x]}] = number$	$[\llbracket 3 \rrbracket] \to [[x]]$
	$[[\![4]\!]] = number$	
	[[x]] = number	$[\llbracket 2 \rrbracket] \to [\llbracket x \rrbracket] \to [\llbracket 4 \rrbracket]$
step2	$[[\boxed{4}]] = number$	$[[3]] \rightarrow [[x]]$
		$[\llbracket 1 \rrbracket] \to [\llbracket 4 \rrbracket]$

step2	$[\llbracket 4 \rrbracket] = number$	
step2	empty	

5. Indica si el sistema de Macros de RACKET y C es *higiénico* o no. Justifica con un pequeño programa que haga uso de macros.

El sistema de Macros de RACKET es higiénico:

Esto debido a que, se define una variable x fuera de la macro mac; otra variable se define por dentro. El (println x) generado por la macro se refiere a la x definida por la macro. El (println x) fuera de la macro se refiere a la x definida fuera de la macro. Entonces terminamos con dos identificadores llamados x con diferentes valores (pues viven en contextos léxicos diferentes).

El sistema de Macros de C es no higiénico

```
#define INCI(i) do { int INCIa = 0; ++i; } while (0)
int main(void)
{
   int x = 5, y = 7;
   INCI(x);
   INCI(y);
   printf("x es ahora %d, y es ahora %d\n", x, y);
   return 0;
}
x es ahora 6, y es ahora 8
```

Esto debido a que, no terminamos con dos identificadores y siempre se refiere a la mismas variables x e y haciendo que estas cambien de valor cada que utilicemos la macro.