

# Exercise

## Exercise

1. What is the multivariate normal density  $\mathcal{N}(x|\mu, C)$ ?
2. Suppose  $X, Y$  are two real-valued random variables.
  - (a) What is the formula for the covariance  $\text{Cov}(X, Y)$ ?
  - (b) What is the formula for the correlation  $\rho(X, Y)$ ?
3. Suppose you can generate  $\mathcal{N}(0, 1)$  random variables. Give an explicit formula for generating a sample from  $\mathcal{N}(\mu, C)$  where  $C = AA^T$ .

1.

$$\frac{1}{\exp \left( \frac{z}{1-C_1} (x - x) \right)} \frac{z/1|C|^{2/p}(2z)}{1}$$

2. (a)  $\mathbb{C}^{\text{cov}}(X, Y) = \mathbb{E}(XY) - \mathbb{E}(X)\mathbb{E}(Y) = \mathbb{E}((X - \mathbb{E}(X))(Y - \mathbb{E}(Y)))$

(b)  $\sigma(X, Y) = \mathbb{C}^{\text{cov}}(X, Y)/\sigma(X)\sigma(Y)$

3. If  $Z_1, \dots, Z_p \stackrel{\text{iid}}{\sim} \mathcal{N}(0, 1)$  and  $Z = (Z_1, \dots, Z_p)^T$ , then  $AZ + \mu \sim \mathcal{N}(\mu, AA^T)$ .