



Data Mining Project

Clustering Clean Ads

Submitted by: Taniya Dubey

INDEX

1.1	Clustering: Read the data and perform basic analysis such as printing a few rows (head and tail), info, data summary, null values duplicate values, etc.
1.2	Clustering: Treat missing values in CPC, CTR and CPM using the formula given.
1.3	Clustering: Check if there are any outliers. Do you think treating outliers is necessary for K-Means clustering?
1.4	Clustering: Perform z-score scaling and discuss how it affects the speed of the algorithm.
1.5	Clustering: Perform Hierarchical by constructing a Dendrogram using WARD and Euclidean distance.
1.6	Clustering: Make Elbow plot (up to n=10) and identify optimum number of clusters for k-means algorithm.
1.7	Clustering: Print silhouette scores for up to 10 clusters and identify optimum number of clusters.
1.8	Clustering: Profile the ads based on optimum number of clusters using silhouette score and your domain understanding
1.9	Clustering: Conclude the project by providing summary of your learnings.
2.1	PCA: Read the data and perform basic checks like checking head, info, summary, nulls, and duplicates, etc.
2.2	PCA: Perform detailed Exploratory analysis by creating certain questions
2.3	PCA: We choose not to treat outliers for this case. Do you think that treating outliers for this case is necessary?
2.4	PCA: Scale the Data using z-score method. Does scaling have any impact on outliers? Compare boxplots before and after scaling and comment.
2.5	PCA: Perform all the required steps for PCA (use sklearn only) Create the covariance Matrix Get eigen values and eigen vector.
2.6	PCA: Identify the optimum number of PCs (for this project, take at least 90% explained variance). Show Scree plot.
2.7	PCA: Compare PCs with Actual Columns and identify which is explaining most variance. Write inferences about all the principal components in terms of actual variables.
2.8	PCA: Write linear equation for first PC.

List of figures

Fig 1: count plot of variables

Fig2: boxplot with outliers' part 1

Fig3: box plot without outliers part1

Fig4: box plot of scaled data

Fig5: dendrogram

Fig6: scree plot part 1

Fig7:count plot of state and area

Fig8: heatmap of these variables

Fig9: EDA of variables

Fig10: boxplot of five variables

Fig11: pair plot of variables

Fig12: plot of male literacy

Fig13: plot of female literacy

Fig14: plot of literacy

Fig15: plot of illiteracy

Fig16: plot of illiteracy and literacy

Fig17: plot of total working population and female literacy

Fig18: box plot of all variables

Fig19: box plot of all variables

Fig20: heatmap of all variables

Fig21: scree plot & cluster plot

Fig22: compare pcs

Fig23: heatmap of pcs

Fig 24: correlation matrix

Fig25: cluster plot

List of tables

Table 1: Top five rows of the dataset

Table 2: Top five rows of the dataset

Table 3: Basic info about dataset

Table4: value counts of categorical variables

Table5: statistical summary

Table6: statistical summary after null values treatment

Table7: few rows of cleaned data

Table8: datatype of df3

Table9: table of data with kmeans

Table10: table of silhouette score

Table 11: data with silhouette width

Table 12: cluster and kmeans table

Table 13: few top rows of data set

Table14: few last rows of dataset

Table15: info of dataset

Table 16: statistical summary

Table17: table of pcs

Part 1: Clustering: Digital Ads Data:

The ads24x7 is a Digital Marketing company which has now got seed funding of \$10 Million. They are expanding their wings in Marketing Analytics. They collected data from their Marketing Intelligence team and now wants you (their newly appointed data analyst) to segment type of ads based on the features provided. Use Clustering procedure to segment ads into homogeneous groups.

The following three features are commonly used in digital marketing:

$CPM = (\text{Total Campaign Spend} / \text{Number of Impressions}) * 1,000$

$CPC = \text{Total Cost (spend)} / \text{Number of Clicks}$

$CTR = \text{Total Measured Clicks} / \text{Total Measured Ad Impressions} * 100$

1.1 Clustering: Read the data and perform basic analysis such as printing a few rows (head and tail), info, data summary, null values duplicate values, etc.

➤ Dataset has 25857 rows and 19 columns.

Table 1: Top five rows of the dataset

	Timestamp	InventoryType	Ad - Length	Ad- Width	Ad Size	Ad Type	Platform	Device Type	Format	Available_Impressions	Matched_Queries	Impressions	Clicks	Spend	Fee	Revenue	CTR	CPM	CPC
0	2020-9-2-17	Format1	300	250	75000	Inter222	Video	Desktop	Display	1806	325	323	1	0.0	0.35	0.0	0.0031	0.0	0.0
1	2020-9-2-18	Format1	300	250	75000	Inter223	Web	Mobile	Display	1979	384	380	0	0.0	0.35	0.0	0.0000	0.0	NaN
2	2020-9-3-16	Format6	336	250	84000	Inter217	Web	Desktop	Video	1586	298	297	0	0.0	0.35	0.0	0.0000	0.0	NaN
3	2020-9-3-2	Format1	300	250	75000	Inter224	Web	Desktop	Display	643	103	102	0	0.0	0.35	0.0	0.0000	0.0	NaN
4	2020-9-3-13	Format1	300	250	75000	Inter225	Video	Mobile	Display	1550	347	345	0	0.0	0.35	0.0	0.0000	0.0	NaN

Table 2: Top last rows of the dataset

	Timestamp	InventoryType	Ad - Length	Ad- Width	Ad Size	Ad Type	Platform	Device Type	Format	Available_Impressions	Matched_Queries	Impressions	Clicks	Spend	Fee	Revenue	CTR	CPM	CPC
25852	2020-10-1-5	Format5	720	300	218000	Inter222	Video	Desktop	Video	1	1	1	0	0.01	0.35	0.0085	NaN	NaN	NaN
25853	2020-11-18-2	Format4	120	600	72000	Inter230	Video	Mobile	Video	7	1	1	1	0.07	0.35	0.0455	NaN	NaN	NaN
25854	2020-9-14-0	Format5	720	300	218000	Inter221	App	Mobile	Video	2	2	2	1	0.09	0.35	0.0585	NaN	NaN	NaN
25855	2020-9-30-4	Format7	300	600	180000	Inter228	Video	Mobile	Display	1	1	1	0	0.01	0.35	0.0085	NaN	NaN	NaN
25856	2020-10-17-3	Format5	720	300	218000	Inter225	Video	Mobile	Display	1	1	1	0	0.01	0.35	0.0085	NaN	NaN	NaN

Table 3: Basic Information of the dataset

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 25857 entries, 0 to 25856
Data columns (total 19 columns):
#   Column                                Non-Null Count  Dtype
---  -
0   Timestamp                             25857 non-null  object
1   InventoryType                         25857 non-null  object
2   Ad - Length                           25857 non-null  int64
3   Ad- Width                             25857 non-null  int64
4   Ad Size                               25857 non-null  int64
5   Ad Type                               25857 non-null  object
6   Platform                              25857 non-null  object
7   Device Type                           25857 non-null  object
8   Format                                25857 non-null  object
9   Available_Impressions                 25857 non-null  int64
10  Matched_Queries                       25857 non-null  int64
11  Impressions                           25857 non-null  int64
12  Clicks                                25857 non-null  int64
13  Spend                                 25857 non-null  float64
14  Fee                                   25857 non-null  float64
15  Revenue                               25857 non-null  float64
16  CTR                                  19392 non-null  float64
17  CPM                                  19392 non-null  float64
18  CPC                                  18330 non-null  float64
dtypes: float64(6), int64(7), object(6)
memory usage: 3.7+ MB
```

Table 4: Value Counts of the Categorical variables

```
Inventory type
Format4      7218
Format1      5432
Format5      5151
Format3      3542
Format6      1968
Format2      1789
Format7       757
Name: InventoryType, dtype: int64

AD type
Inter217     1849
Inter227     1848
Inter218     1848
Inter219     1848
Inter220     1848
Inter221     1848
Inter222     1847
Inter223     1847
Inter224     1847
inter230     1847
Inter225     1845
Inter226     1845
Inter228     1845
Inter229     1845
Name: Ad Type, dtype: int64
```

```
Platform
Video     11077
Web        9236
App        5544
Name: Platform, dtype: int64

Device Type
Mobile     16621
Desktop    9236
Name: Device Type, dtype: int64

Format
Display    12929
Video      12928
Name: Format, dtype: int64
```

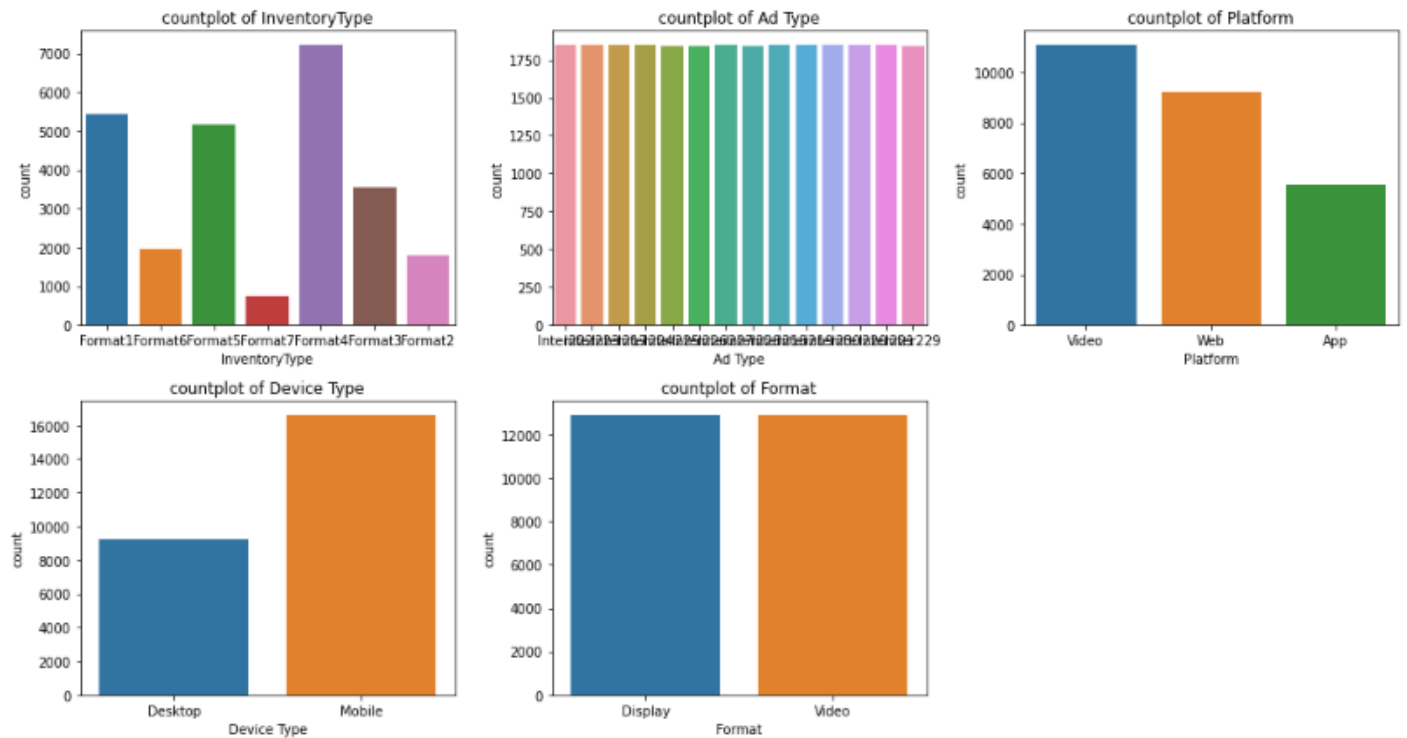


Fig1: count plot of variables

- The info table of dataset tells the following details:
 - Numerical variables: 13
 - Categorical variables: 6
 - Null values: CTR, CPM, CPC
 - Duplicate: 0
- From the count plot of device type we can see that most of the devices are mobile.
- There is no visible difference in count plot of format and ad type.

Table 5: statistical summary

	Ad - Length	Ad - Width	Ad Size	Available_Impressions	Matched_Queries	Impressions	Clicks	Spend	Fee	Revenue	CTR	CPM	CPC
count	25857.000000	25857.000000	25857.000000	2.585700e+04	2.585700e+04	2.585700e+04	25857.000000	25857.000000	25857.000000	25857.000000	25838.000000	25838.000000	2.327100e+04
mean	390.431218	332.182774	99683.278482	2.189821e+08	1.155322e+08	1.107525e+08	9525.881388	2414.473115	0.338729	1716.549955	0.075883	7.588959	inf
std	230.898051	194.260924	62640.885612	4.542680e+08	2.407244e+08	2.326848e+08	18721.888071	3932.835240	0.030540	2993.025498	0.091413	8.938999	NaN
min	120.000000	70.000000	33800.000000	0.000000e+00	0.000000e+00	0.000000e+00	0.000000	0.000000	0.210000	0.000000	0.000000	0.000000	0.000000e+00
25%	120.000000	250.000000	72000.000000	9.133000e+03	5.451000e+03	2.558000e+03	305.000000	38.030000	0.350000	23.420000	0.002400	1.589608	8.998397e-02
50%	300.000000	300.000000	75000.000000	3.309680e+05	1.894490e+05	1.821820e+05	3457.000000	1173.880000	0.350000	782.880000	0.007700	3.333333	1.408485e-01
75%	720.000000	600.000000	84000.000000	2.208484e+08	1.008171e+08	9.496830e+05	10881.000000	2692.280000	0.350000	1749.982000	0.130900	12.491089	5.584425e-01
max	728.000000	600.000000	218000.000000	2.759288e+07	1.470202e+07	1.419477e+07	143049.000000	25931.870000	0.350000	21278.180000	2.000000	715.000000	inf

1.2 Clustering: Treat missing values in CPC, CTR and CPM using the formula given.

➤ Null values

CTR		6465
CPM		6465
CPC	7527	

➤ Handling Null values

Step 1: With the help of formulas given in the question we will make a user define function then make new columns so that most of the null values be replaced with right values in CTR, CPM & CPC.

Step 2: after 1 step we will drop 219 null values from CPC, CPM, CTR as it will impact further analysis

Step 3: after 2 step we will replace null values (Nan) of CPC with 0 and inf values with 0.

Step 4: check nulls in the data

Table 6: statistical summary after null value treatment

	Ad - Length	Ad - Width	Ad Size	Available_Impressions	Matched_Queries	Impressions	Clicks	Spend	Fee	Revenue	CTR	CPM	CPC
count	25638.000000	25638.000000	25638.000000	2.563800e+04	2.563800e+04	2.563800e+04	25638.000000	25638.000000	25638.000000	25638.000000	25638.000000	25638.000000	25638.000000
mean	388.127155	332.155384	98773.479991	2.188154e+06	1.165191e+06	1.116986e+06	9607.251541	2435.097563	0.336616	1731.211730	0.075663	7.588959	0.302902
std	229.832116	194.881782	62055.513861	4.557595e+06	2.415124e+06	2.334302e+06	16769.662367	3943.234023	0.030645	3001.566311	0.091413	8.938999	0.339119
min	120.000000	70.000000	33600.000000	1.000000e+00	1.000000e+00	1.000000e+00	0.000000	0.000000	0.210000	0.000000	0.000000	0.000000	0.000000
25%	120.000000	250.000000	72000.000000	1.053350e+04	6.328500e+03	2.873250e+03	340.000000	40.012500	0.350000	26.007500	0.002400	1.589808	0.078988
50%	300.000000	300.000000	75000.000000	3.469430e+05	1.953880e+05	1.664925e+05	3536.000000	1194.930000	0.350000	776.710000	0.007700	3.333333	0.119888
75%	720.000000	600.000000	84000.000000	2.232121e+06	1.018126e+06	9.616298e+05	10856.250000	2718.142500	0.350000	1786.792875	0.130900	12.491089	0.503213
max	728.000000	600.000000	216000.000000	2.758286e+07	1.470202e+07	1.419477e+07	143049.000000	26931.870000	0.350000	21276.180000	2.000000	715.000000	7.284000

We can see from the statistical summary that now shows data at place of inf and nan values.

Table 7: few rows of cleaned data

	Timestamp	InventoryType	Ad - Length	Ad - Width	Ad Size	Ad Type	Platform	Device Type	Format	Available_Impressions	Matched_Queries	Impressions	Clicks	Spend	Fee	Revenue	CTR	CPM	CPC
0	2020-9-2-17	Format1	300	250	75000	Inter222	Video	Desktop	Display	1806	325	323	1	0.0	0.35	0.0	0.0031	0.0	0.0
1	2020-9-2-18	Format1	300	250	75000	Inter223	Web	Mobile	Display	1979	384	380	0	0.0	0.35	0.0	0.0000	0.0	0.0
2	2020-9-3-16	Format6	336	250	84000	Inter217	Web	Desktop	Video	1566	298	297	0	0.0	0.35	0.0	0.0000	0.0	0.0
3	2020-9-3-2	Format1	300	250	75000	Inter224	Web	Desktop	Display	643	103	102	0	0.0	0.35	0.0	0.0000	0.0	0.0
4	2020-9-3-13	Format1	300	250	75000	Inter225	Video	Mobile	Display	1550	347	345	0	0.0	0.35	0.0	0.0000	0.0	0.0

1.3 - Clustering: Check if there are any outliers. Do you think treating outliers is necessary for K-Means clustering? Based on your judgement decide whether to treat outliers and if yes, which method to employ.

As we know that there are 6 categorical variables which we will drop because for further analysis we will only need numerical variables. The name of new data frame will be df3 which will contain the following columns:

Table 8: datatype of df3 data frame

Ad - Length	int64
Ad- Width	int64
Ad Size	int64
Available_Impressions	int64
Matched_Queries	int64
Impressions	int64
Clicks	int64
Spend	float64
Revenue	float64
CTR	float64
CPM	float64
CPC	float64

Now let's see boxplot for outliers

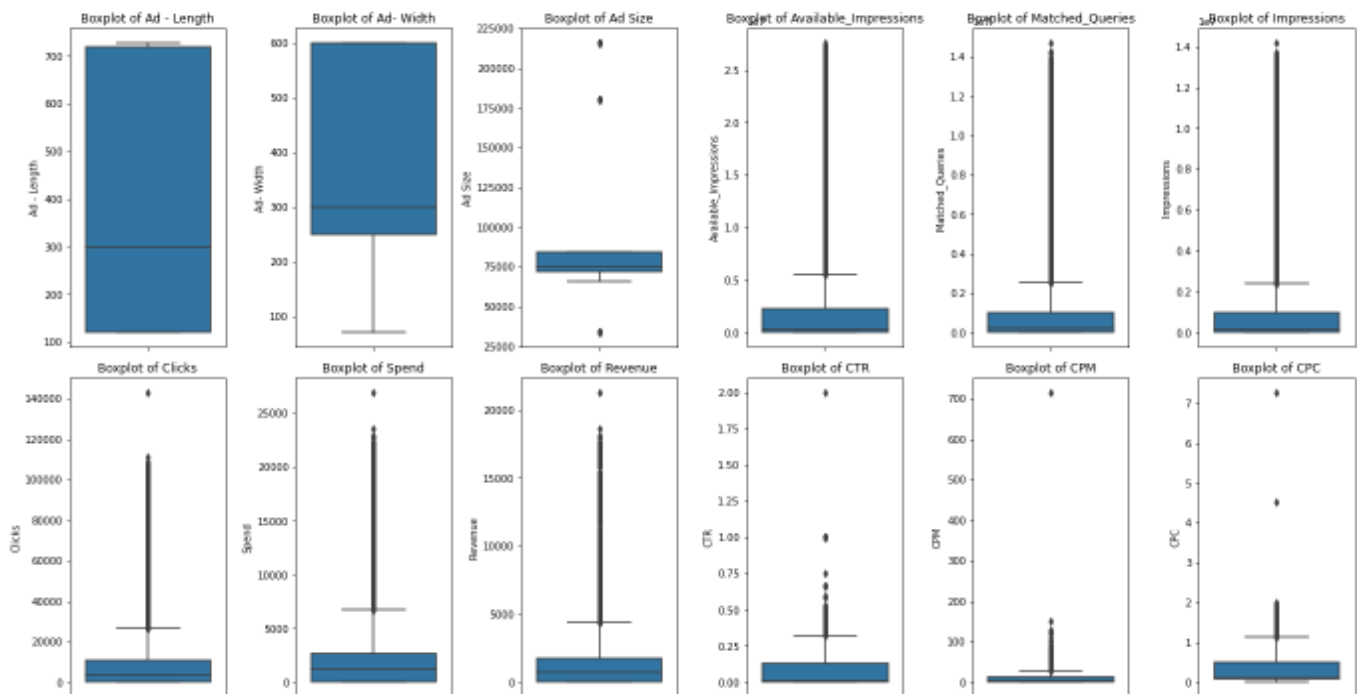


Fig 2: box plot with outliers' part 1

As we can see all the variables except first 2 have outliers

And we know that clustering is very sensitive to outliers and if we don't treat them then it can give rise to errors and then we will not get the most accurate analysis of the data present so we have treated the outliers.

Outliers were treated by using Winsorization, i.e., bringing the larger outliers (Data points above the $Q3 + 1.5 * IQR$ value) to the upper whisker value and bringing the smaller outliers (Data points below the $Q1 - 1.5 * IQR$ value) to the lower whisker.

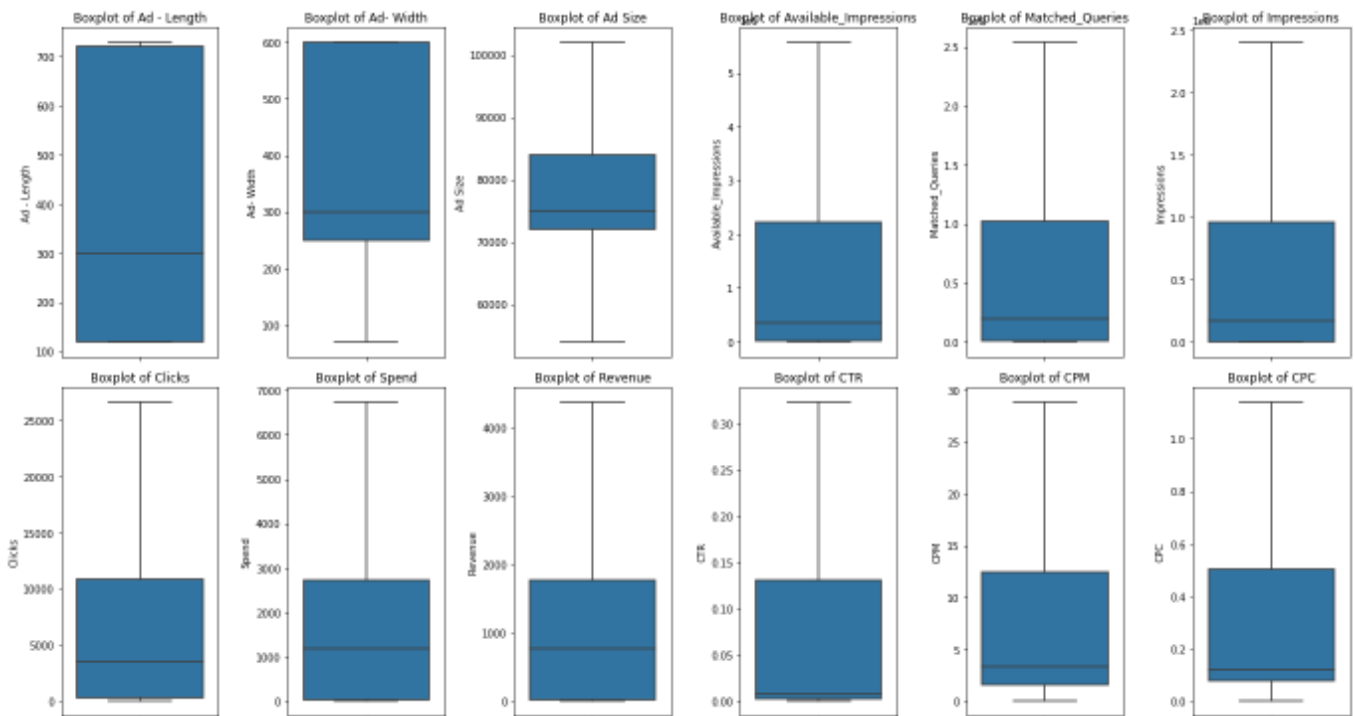


Fig 3: box plot without outliers' part 1

1.4 - Clustering: Perform z-score scaling and discuss how it affects the speed of the algorithm.

We will scale the data with the help of Sklenar preprocessing (standard scaler).

Z-Score scaling consists in transforming each feature subtracting the mean value and dividing by the standard deviation

Z-Score scaling adjusts the numbers to make it easy to compare the values that are out of each other's scope. This **helps increase the accuracy of the models & analysis of the data**. Z-score also increase the speed of further analysis.

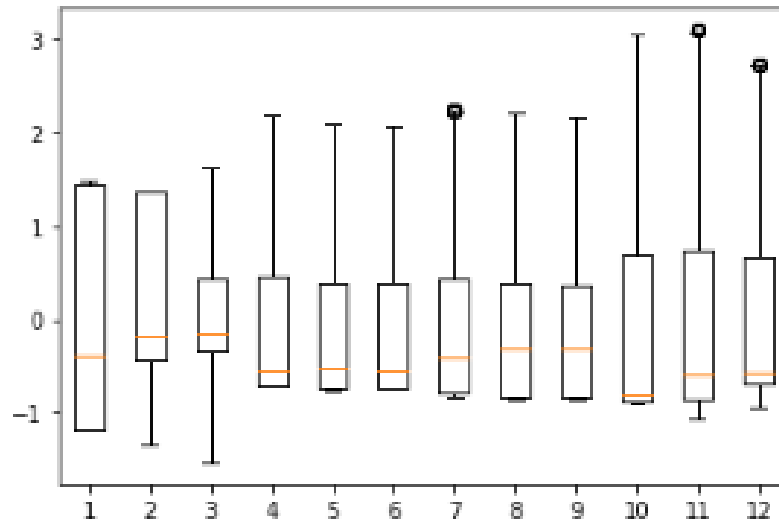


Fig 4: box plot of scaled data

1.5 - Clustering: Perform Hierarchical by constructing a Dendrogram using WARD and Euclidean distance.

We will perform Hierarchical by constructing a Dendrogram using ward with the help of `scipy.cluster.hierarchy`

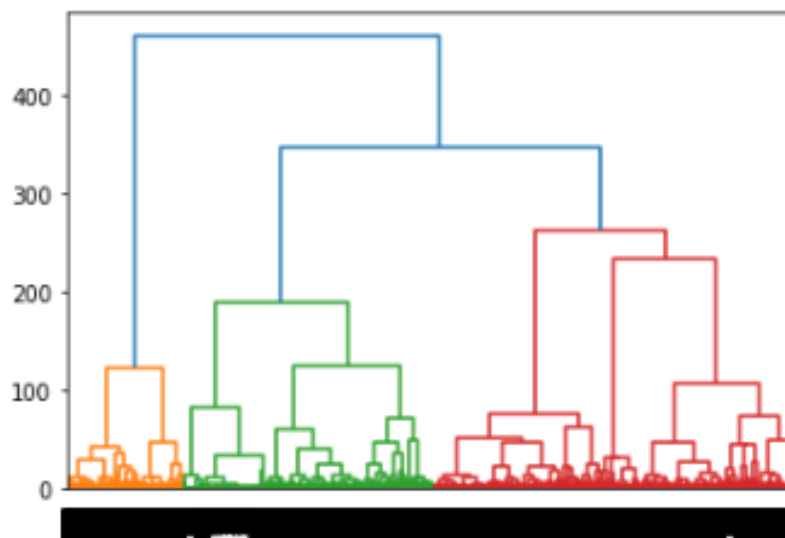


Fig 5: dendrogram

1.6 - Clustering: Make Elbow plot (up to n=10) and identify optimum number of clusters for k-means algorithm.

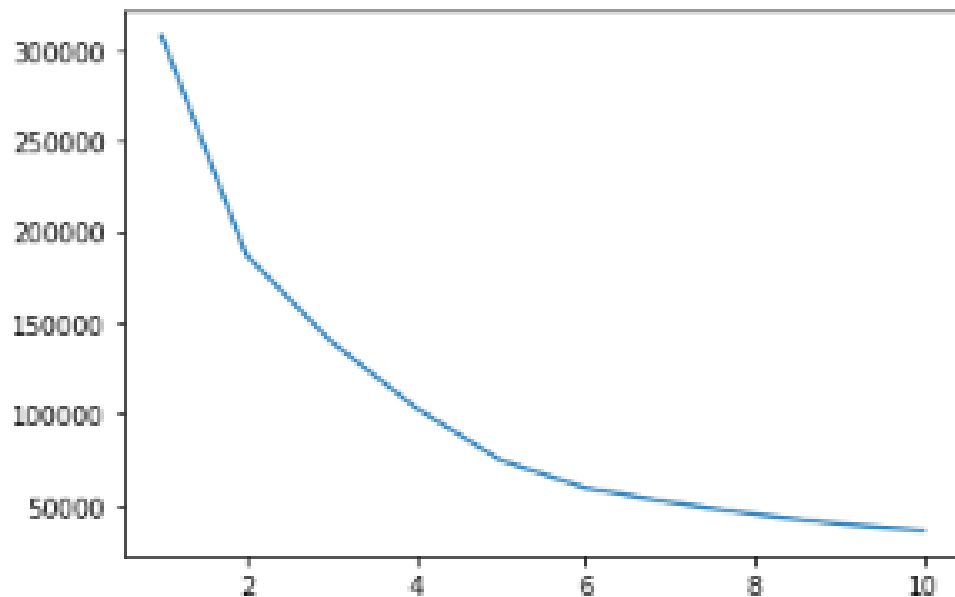


Fig 6: scree plot part 1

As we can see that after 4 the difference is less and less so we will take the 4 of the clusters for k means.

	Ad - Length	Ad- Width	Ad Size	Available_Impressions	Matched_Queries	Impressions	Clicks	Spend	Revenue	CTR	CPM	CPC	kmeans
0	300.0	250.0	75000.0	1806.0	325.0	323.0	1.0	0.0	0.0	0.0031	0.0	0.0	2
1	300.0	250.0	75000.0	1979.0	384.0	380.0	0.0	0.0	0.0	0.0000	0.0	0.0	2
2	336.0	250.0	84000.0	1566.0	298.0	297.0	0.0	0.0	0.0	0.0000	0.0	0.0	2
3	300.0	250.0	75000.0	643.0	103.0	102.0	0.0	0.0	0.0	0.0000	0.0	0.0	2
4	300.0	250.0	75000.0	1550.0	347.0	345.0	0.0	0.0	0.0	0.0000	0.0	0.0	2

Table 9: of data with k means

1.7 - Clustering: Print silhouette scores for up to 10 clusters and identify optimum number of clusters.

For n_clusters = 2 The average silhouette_score is : 0.3790731628519866
 For n_clusters = 3 The average silhouette_score is : 0.3497350804755862
 For n_clusters = 4 The average silhouette_score is : 0.4258753276320477
 For n_clusters = 5 The average silhouette_score is : 0.4839513671813748
 For n_clusters = 6 The average silhouette_score is : 0.4879521917720897
 For n_clusters = 7 The average silhouette_score is : 0.4908768188248661
 For n_clusters = 8 The average silhouette_score is : 0.5127144457099674
 For n_clusters = 9 The average silhouette_score is : 0.5064391516899717
 For n_clusters = 10 The average silhouette_score is : 0.47033918891999843

Table 10: table of silhouette score

4 is the optimum number of clusters which we require.

	Ad - Length	Ad - Width	Ad Size	Available_Impressions	Matched_Queries	Impressions	Clicks	Spend	Revenue	CTR	CPM	CPC	kmeans	sil_width
0	300.0	250.0	75000.0	1806.0	325.0	323.0	1.0	0.0	0.0	0.0031	0.0	0.0	0	0.889424
1	300.0	250.0	75000.0	1979.0	384.0	380.0	0.0	0.0	0.0	0.0000	0.0	0.0	0	0.897774

Table 11: data with silhouette width

Minimum silhouette sample is -0.2566

1.8 - Clustering: Profile the ads based on optimum number of clusters using silhouette score and your domain understanding

Table 12: cluster and kmeans table

Clus_kmeans8	Device Type							
0	Desktop	2739.499379	1878.141205	1225.868135	0.002800	1.888647	0.814333	
	Mobile	2696.674403	1881.736233	1228.186592	0.002742	1.890719	0.817669	
1	Desktop	1621.475632	166.433312	108.181600	0.163459	14.629112	0.101136	
	Mobile	1593.275967	169.120551	109.928303	0.163285	14.947250	0.101228	
2	Desktop	8490.731092	5242.815011	3654.079817	0.002404	1.469917	0.620312	
	Mobile	8347.800242	5182.984304	3603.685739	0.002403	1.478311	0.624004	
3	Desktop	14560.822610	1251.564690	814.951886	0.138678	12.147766	0.089129	
	Mobile	14457.597914	1261.891205	821.717384	0.139819	12.224552	0.090142	
4	Desktop	62108.580699	6658.438802	4764.444965	0.138379	15.597476	0.113041	
	Mobile	62297.969582	6706.956778	4803.094412	0.137512	15.547503	0.113266	
5	Desktop	95.441361	21.279311	13.831562	0.007076	0.996617	0.028351	
	Mobile	144.570525	28.578127	18.575772	0.008241	1.080855	0.029425	
6	Desktop	3848.759684	1348.308055	876.502439	0.004877	1.851673	0.403109	
	Mobile	3840.537549	1332.892653	866.537555	0.004853	1.832937	0.398911	
7	Desktop	15815.355839	14167.534089	10794.622053	0.001796	1.711820	0.975508	
	Mobile	15582.460381	14056.087944	10706.635538	0.001810	1.740815	0.985900	

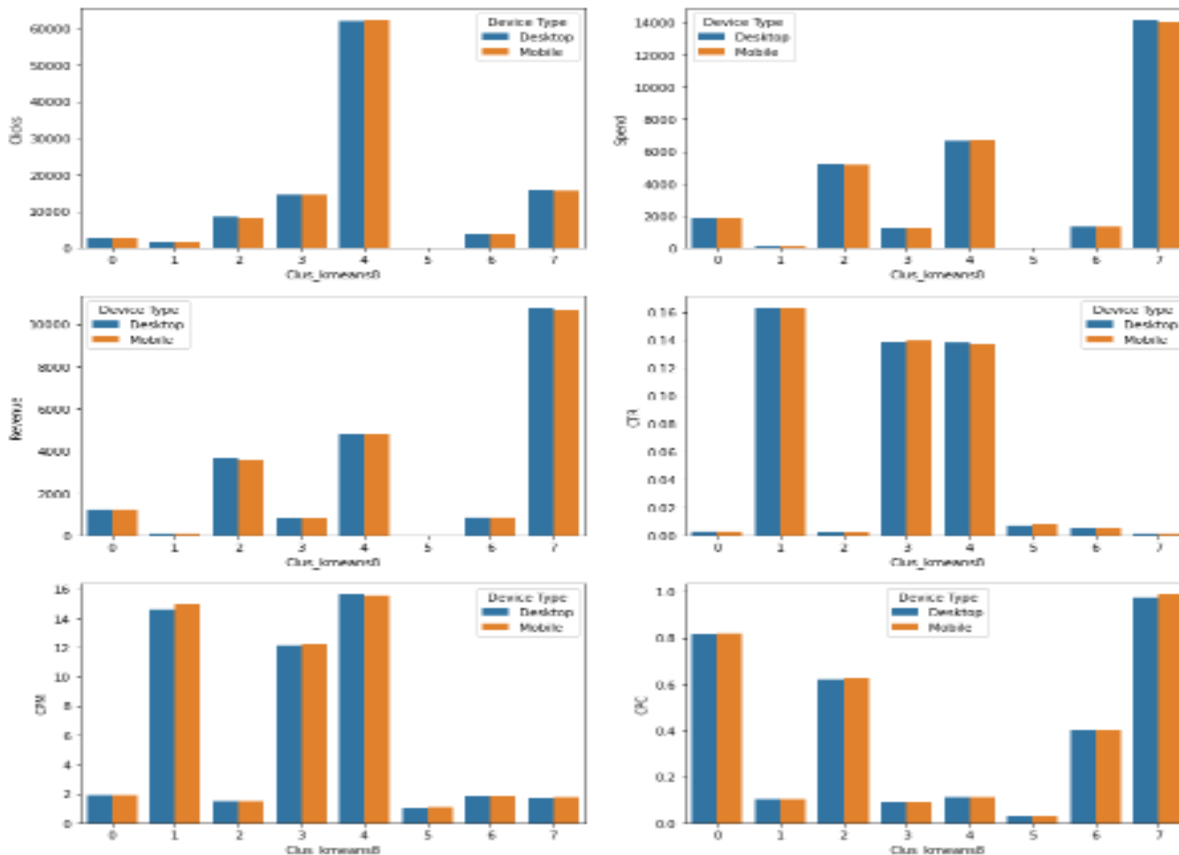


Fig 25: plot of clusters.

1.9 - Clustering: Conclude the project by providing summary of your learnings.

Some recommendation which can be followed by the ads24x7 company are as follows

We can make some conclusion based on above figures and tables.

- **Cluster 0:**

This type of cluster has highest average **CTR** (click through rate) among other clusters. It shows that a greater number of users sees and click these types of ads. The average **CPM** (cost per impression) is more as compare to others which means that the relevance and quality of these are more. The average **CPC** (cost per clicks) is not so high which shows that the user of this type does not purchase the product that much. this type of ads can provide some offers to increase CPC.

Like this every cluster is providing meaning full information which will help the business to grow and expand.

After the whole process we can conclude that the ads having low CTR and CPM value have to improve their quality and relevance of content by spend some amount of money while the ads having low CPC value have to provide some great offers so more number of customers are buying the product. This also results in larger revenue.

Part 2 : PCA

PCA FH (FT): Primary census abstract for female headed households excluding institutional households (India & States/UTs - District Level), Scheduled tribes - 2011 PCA for Female Headed Household Excluding Institutional Household. The Indian Census has the reputation of being one of the best in the world. The first Census in India was conducted in the year 1872. This was conducted at different points of time in different parts of the country. In 1881 a Census was taken for the entire country simultaneously. Since then, Census has been conducted every ten years, without a break. Thus, the Census of India 2011 was the fifteenth in this unbroken series since 1872, the seventh after independence and the second census of the third millennium and twenty first century. The census has been uninterruptedly continued despite of several adversities like wars, epidemics, natural calamities, political unrest, etc. The Census of India is conducted under the provisions of the Census Act 1948 and the Census Rules, 1990. The Primary Census Abstract which is important publication of 2011 Census gives basic information on Area, Total Number of Households, Total Population, Scheduled Castes, Scheduled Tribes Population, Population in the age group 0-6, Literates, Main Workers and Marginal Workers classified by the four broad industrial categories, namely, (i) Cultivators, (ii) Agricultural Laborers, (iii) Household Industry Workers, and (iv) Other Workers and also non-Workers. The characteristics of the Total Population include Scheduled Castes, Scheduled Tribes, Institutional and Houseless Population and are presented by sex and rural-urban residence. Census 2011 covered 35 States/Union Territories, 640 districts, 5,924 sub-districts, 7,935 Towns and 6,40,867 Villages. The data collected has so many variables thus making it difficult to find useful details without using Data Science Techniques. You are tasked to perform detailed EDA and identify Optimum Principal Components that explains the most variance in data.

2.1 - PCA: Read the data and perform basic checks like checking head, info, summary, nulls, and duplicates, etc.

Table 13: few top rows of data set

State Code	Dist.Code	State	Area Name	No_HH	TOT_M	TOT_F	M_06	F_06	M_SC	...	MARG_CL_0_3_M	MARG_CL_0_3_F	MARG_AL_0_3_M	MARG_AL_0_3_F	MARG_HH_0_3_M	MARG_HH_0_3_F	MARG_OT_0_3_M	MARG_OT_0_3_F	NON_WORK_M	NON_WORK_F	
0	1	1	Jammu & Kashmir	Kupwara	7707	23388	29796	5862	6196	3	...	1150	749	180	237	680	252	32	46	258	214
1	1	2	Jammu & Kashmir	Badgam	6218	19585	23102	4482	3733	7	...	525	715	123	229	186	148	76	178	140	160
2	1	3	Jammu & Kashmir	Leh(Ladakh)	4452	6546	10964	1082	1018	3	...	114	188	44	89	3	34	0	4	67	61
3	1	4	Jammu & Kashmir	Kargil	1320	2784	4206	563	677	0	...	194	247	61	128	13	50	4	10	116	59
4	1	5	Jammu & Kashmir	Punch	11654	20591	29981	5157	4587	20	...	874	1928	465	1043	205	302	24	105	180	478

Table 14: few last rows of data set

State Code	Dist.Code	State	Area Name	No_HH	TOT_M	TOT_F	M_06	F_06	M_SC	...	MARG_CL_0_3_M	MARG_CL_0_3_F	MARG_AL_0_3_M	MARG_AL_0_3_F	MARG_HH_0_3_M	MARG_HH_0_3_F	MARG_OT_0_3_M	MARG_OT_0_3_F	NON_WORK_M	NON_WORK_F	
535	34	636	Putucherry	Mahe	3333	8154	11781	1146	1203	21	...	32	47	0	0	0	0	0	0	32	47
536	34	637	Putucherry	Karaikal	10612	12346	21691	1544	1533	2234	...	155	337	3	14	38	130	4	23	110	170
537	35	638	Andaman & Nicobar Island	Nicobars	1275	1549	2630	227	225	0	...	104	134	9	4	2	6	17	47	78	77
538	35	639	Andaman & Nicobar Island	North & Middle Andaman	3762	5200	8012	723	664	0	...	136	172	24	44	11	21	1	4	100	103
539	35	640	Andaman & Nicobar Island	South Andaman	7975	11977	18049	1470	1358	0	...	173	122	6	2	17	17	2	4	148	96

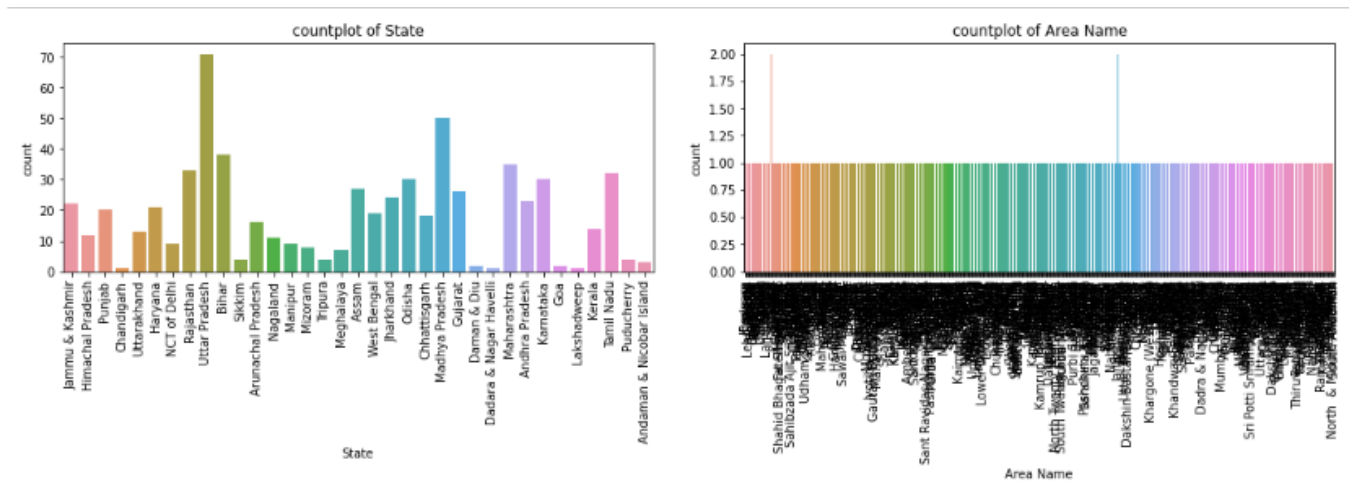


fig 7: count plot of state and area

Table 15: info of data set


```

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 648 entries, 0 to 639
Data columns (total 61 columns):
#   Column                Non-Null Count  Dtype
---  -
0   State Code            648 non-null    int64
1   Dist.Code            648 non-null    int64
2   State                648 non-null    object
3   Area Name            648 non-null    object
4   No_HH                648 non-null    int64
5   TOT_M                648 non-null    int64
6   TOT_F                648 non-null    int64
7   M_06                 648 non-null    int64
8   F_06                 648 non-null    int64
9   M_SC                 648 non-null    int64
10  F_SC                 648 non-null    int64
11  M_ST                 648 non-null    int64
12  F_ST                 648 non-null    int64
13  M_LIT                648 non-null    int64
14  F_LIT                648 non-null    int64
15  M_ILL                648 non-null    int64
16  F_ILL                648 non-null    int64
17  TOT_WORK_M           648 non-null    int64
18  TOT_WORK_F           648 non-null    int64
19  MAINWORK_M           648 non-null    int64
20  MAINWORK_F           648 non-null    int64
21  MAIN_CL_M            648 non-null    int64
22  MAIN_CL_F            648 non-null    int64
23  MAIN_AL_M            648 non-null    int64
24  MAIN_AL_F            648 non-null    int64
25  MAIN_HH_M            648 non-null    int64
26  MAIN_HH_F            648 non-null    int64
27  MAIN_OT_M            648 non-null    int64
28  MAIN_OT_F            648 non-null    int64
29  MARGWORK_M           648 non-null    int64
30  MARGWORK_F           648 non-null    int64
31  MARG_CL_M            648 non-null    int64
32  MARG_CL_F            648 non-null    int64
33  MARG_AL_M            648 non-null    int64
34  MARG_AL_F            648 non-null    int64
35  MARG_HH_M            648 non-null    int64
36  MARG_HH_F            648 non-null    int64
37  MARG_OT_M            648 non-null    int64
38  MARG_OT_F            648 non-null    int64
39  MARGWORK_3_5_M       648 non-null    int64
40  MARGWORK_3_5_F       648 non-null    int64
41  MARG_CL_3_5_M        648 non-null    int64
42  MARG_CL_3_5_F        648 non-null    int64
43  MARG_AL_3_5_M        648 non-null    int64
44  MARG_AL_3_5_F        648 non-null    int64
45  MARG_HH_3_5_M        648 non-null    int64
46  MARG_HH_3_5_F        648 non-null    int64
47  MARG_OT_3_5_M        648 non-null    int64
48  MARG_OT_3_5_F        648 non-null    int64
49  MARGWORK_0_3_M       648 non-null    int64
50  MARGWORK_0_3_F       648 non-null    int64
51  MARG_CL_0_3_M        648 non-null    int64
52  MARG_CL_0_3_F        648 non-null    int64
53  MARG_AL_0_3_M        648 non-null    int64
54  MARG_AL_0_3_F        648 non-null    int64
55  MARG_HH_0_3_M        648 non-null    int64
56  MARG_HH_0_3_F        648 non-null    int64
57  MARG_OT_0_3_M        648 non-null    int64
58  MARG_OT_0_3_F        648 non-null    int64
59  NON_WORK_M           648 non-null    int64
60  NON_WORK_F           648 non-null    int64
dtypes: int64(59), object(2)
memory usage: 385.1+ KB

```

Table 16: statical summary of data set

	count	mean	std	min	25%	50%	75%	max
State Code	840.0	17.114082	9.428488	1.0	9.00	18.0	24.00	35.0
Dist.Code	840.0	320.500000	184.898367	1.0	180.75	320.5	480.25	640.0
No HH	840.0	51222.871875	48135.405475	350.0	19484.00	35837.0	68892.00	310450.0
IOI M	840.0	79940.578583	73384.511114	391.0	30228.00	58339.0	107918.50	485417.0
IOI F	840.0	122372.084375	113800.717282	898.0	48517.75	87724.5	184251.75	750392.0
M US	840.0	12309.098438	11500.906881	58.0	4733.75	9159.0	18520.25	98223.0
F US	840.0	11942.300000	11328.294987	58.0	4872.25	8863.0	15902.25	95129.0
M SC	840.0	13820.948875	14428.373130	0.0	3486.25	9591.5	19429.75	103307.0
F SC	840.0	20778.392188	21727.887713	0.0	5803.25	13709.0	29180.00	158429.0
M SI	840.0	8191.807813	9912.888948	0.0	293.75	2333.5	7858.00	98785.0
F SI	840.0	10155.840825	15875.701488	0.0	429.50	3834.5	12480.25	130119.0
M LI	840.0	57987.979888	55910.282468	288.0	21298.00	42893.5	77989.50	403281.0
F LI	840.0	68359.585825	75037.880207	371.0	20932.00	43798.5	84799.75	571140.0
M IL	840.0	21972.598875	19825.805288	105.0	8590.00	15787.5	29512.50	105981.0
F IL	840.0	58012.518750	47118.893789	327.0	22387.00	42386.0	78471.00	254180.0
IOI WORK M	840.0	37992.407813	38419.537491	100.0	13753.50	27938.5	50228.75	289422.0
IOI WORK F	840.0	41295.780938	37192.980943	357.0	18097.75	30588.5	53234.25	257848.0
MAINWORK M	840.0	30204.448875	31480.915880	65.0	9787.00	21250.5	40119.00	247911.0
MAINWORK F	840.0	28198.848875	29598.280889	240.0	9502.25	18484.0	35083.25	228188.0
MAIN CL M	840.0	5424.342188	4739.181969	0.0	2023.50	4180.5	7895.00	29113.0
MAIN CL F	840.0	5488.042188	5328.982728	0.0	1920.25	3908.5	7288.25	38193.0
MAIN AL M	840.0	5849.109375	8399.507968	0.0	1070.25	3938.5	8087.25	40843.0
MAIN AL F	840.0	8925.995312	12884.287584	0.0	1408.75	3933.5	10817.50	87945.0
MAIN HH M	840.0	883.893750	1278.842345	0.0	187.50	498.5	1099.25	18429.0
MAIN HH F	840.0	1380.773438	3179.414449	0.0	248.75	540.5	1435.75	45979.0
MAIN DI M	840.0	18047.101982	28088.480888	38.0	3997.50	9598.0	21249.50	240855.0
MAIN DI F	840.0	12408.035938	18972.202389	153.0	3142.50	8380.5	14388.25	209355.0
MAHCWORK M	840.0	7787.980938	7410.791891	35.0	2937.50	5827.0	9800.25	47553.0
MAHCWORK F	840.0	13098.914082	10998.474528	117.0	5424.50	10175.0	18879.25	88915.0
MAHC CL M	840.0	1040.737500	1311.548847	0.0	311.75	808.5	1281.00	13201.0
MAHC CL F	840.0	2307.882813	3584.828095	0.0	630.25	1228.0	2859.25	44324.0
MAHC AL M	840.0	3304.328582	3781.555707	0.0	873.50	2082.0	4300.75	23719.0
MAHC AL F	840.0	6483.281250	8773.878298	0.0	1402.50	4020.5	9089.25	45301.0
MAHC HH M	840.0	318.742188	482.881891	0.0	71.75	188.0	358.50	4298.0
MAHC HH F	840.0	788.828582	1198.718213	0.0	171.75	429.0	982.50	15448.0
MAHC DI M	840.0	3128.154887	3809.391821	7.0	935.50	2038.0	3985.25	24728.0
MAHC DI F	840.0	3539.323438	4115.191314	19.0	1071.75	2349.5	4400.50	38377.0
MAHCWORK 3 S M	840.0	41948.188750	39045.318918	291.0	18208.25	30315.0	57218.75	300937.0
MAHCWORK 3 S F	840.0	81078.323438	82970.406218	341.0	28819.50	58793.0	107924.00	878450.0
MAHC CL 3 S M	840.0	8394.987500	8019.808844	27.0	2372.00	4830.0	8187.00	39108.0

MAIRC	CL	3	B	F	840.0	10339.884083	8487.473429	85.0	435.150	8295.0	15102.00	50665.0
MAIRC	AL	3	B	M	840.0	789.848438	905.839279	0.0	235.50	480.5	988.00	7428.0
MAIRC	AL	3	B	F	840.0	1749.584375	2498.541514	0.0	497.25	985.5	2059.00	27171.0
MAIRC	HH	3	B	M	840.0	2743.835938	3059.588387	0.0	718.75	1714.5	3702.25	19343.0
MAIRC	HH	3	B	F	840.0	5169.850000	5335.840980	0.0	1113.75	3294.0	7502.25	38253.0
MAIRC	CH	3	B	M	840.0	245.382500	358.728587	0.0	58.00	129.5	278.00	3535.0
MAIRC	CH	3	B	F	840.0	585.884375	900.025817	0.0	127.75	320.5	719.25	12094.0
MAIRCWORK	D	3	M		840.0	2818.140825	3038.984381	7.0	755.00	1881.5	3320.25	20848.0
MAIRCWORK	D	3	F		840.0	2834.545312	3327.838932	14.0	833.50	1834.5	3810.50	25844.0
MAIRC	CL	D	3	M	840.0	1392.973438	1489.707052	4.0	489.50	949.0	1714.00	9875.0
MAIRC	CL	D	3	F	840.0	2757.050000	2788.778878	30.0	957.25	1928.0	3599.75	21811.0
MAIRC	AL	D	3	M	840.0	250.889082	453.338594	0.0	47.00	114.5	270.75	5775.0
MAIRC	AL	D	3	F	840.0	558.098438	1117.842748	0.0	109.00	247.5	588.75	17153.0
MAIRC	HH	D	3	M	840.0	580.890825	782.578991	0.0	138.50	308.0	842.00	8118.0
MAIRC	HH	D	3	F	840.0	1293.431250	1585.377938	0.0	298.00	717.0	1710.75	13714.0
MAIRC	CH	D	3	M	840.0	71.379888	107.897827	0.0	14.00	35.0	79.00	895.0
MAIRC	CH	D	3	F	840.0	200.742188	309.740854	0.0	43.00	113.0	240.00	3354.0
NON WORK	M				840.0	510.014083	810.803187	0.0	181.00	326.0	804.50	8458.0
NON WORK	F				840.0	704.778125	910.269225	5.0	220.50	484.5	853.50	10533.0

- Dataset has 640 rows and 61 columns.
- There are no duplicates in the data.
- There are no null values in the data.
- There are two objective type data and others are integers.

2.2 - PCA: Perform detailed Exploratory analysis by creating certain questions

The 5 variables which I have choose are following:

- 1)F_ILL
- 2)M_ILL
- 3)F_LIT
- 4)M_LIT
- 5)TOT_WORK_F

Table 17: statical summary of data set

	count	mean	std	min	25%	50%	75%	max
F_ILL	640.0	58012.518750	47116.893789	327.0	22367.00	42386.0	78471.00	254160.0
M_ILL	640.0	21972.596875	19825.605268	105.0	8590.00	15767.5	29512.50	105961.0
F_LIT	640.0	68359.585625	75037.880207	371.0	20932.00	43796.5	84799.75	571140.0
M_LIT	640.0	57967.979688	55910.282466	286.0	21298.00	42693.5	77989.50	403261.0
TOT_WORK_F	640.0	41295.760938	37192.380943	357.0	16097.75	30588.5	53234.25	257848.0

Fig 8: heatmap of these variables

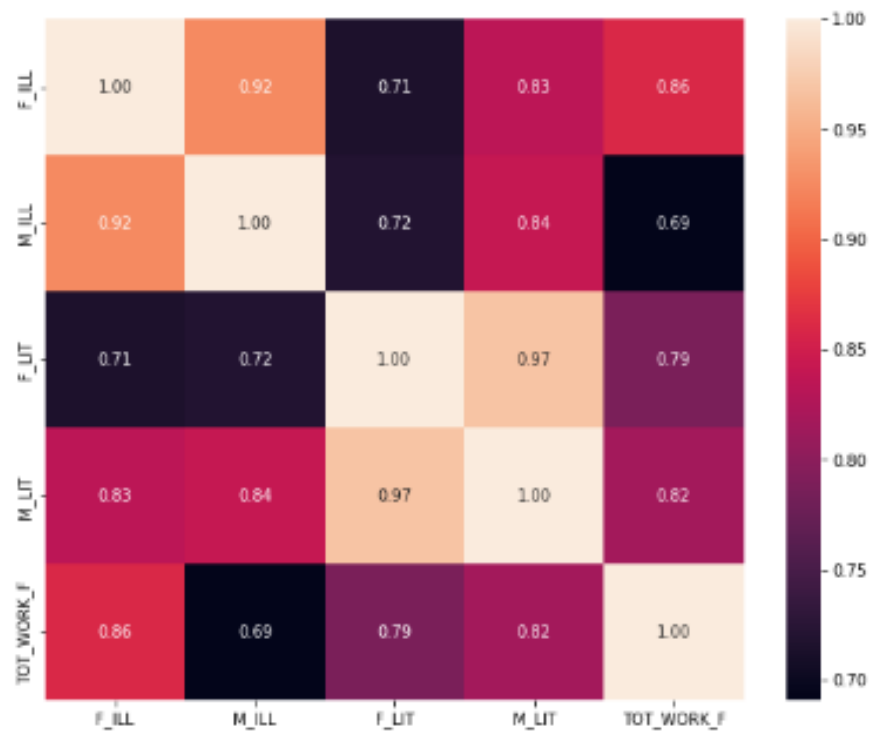
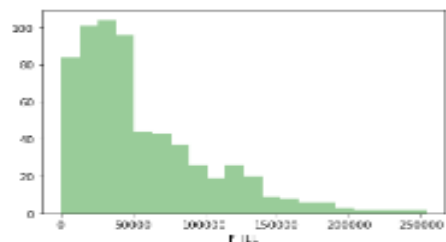


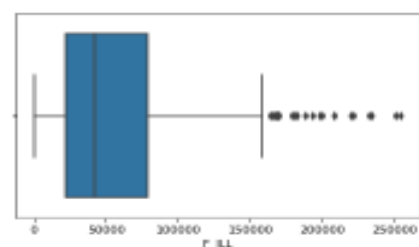
Fig 9: EDA of variables

Description of F_ILL

```
count      648.000000
mean      56812.518750
std       47116.693769
min        327.000000
25%       22367.000000
50%       42386.000000
75%       78471.000000
max       254160.000000
Name: F_ILL, dtype: float64 Distribution of F_ILL
```



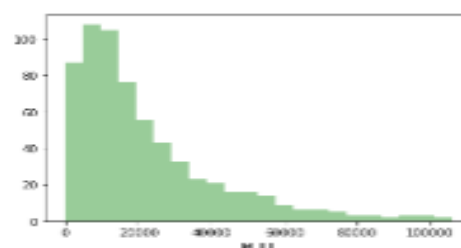
BoxPlot of F_ILL



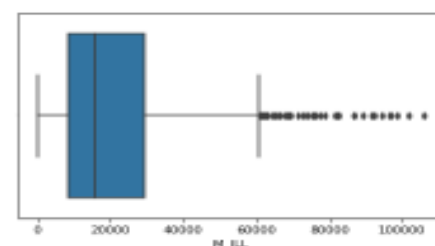
Description of M_ILL

Description of M_ILL

```
count      648.000000
mean      21972.596875
std       19825.685268
min        105.000000
25%       8590.000000
50%       15767.500000
75%       29512.500000
max       185961.000000
Name: M_ILL, dtype: float64 Distribution of M_ILL
```



BoxPlot of M_ILL

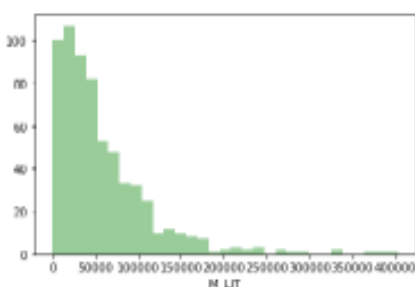


Description of M_LIT

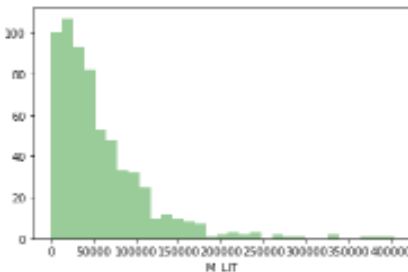
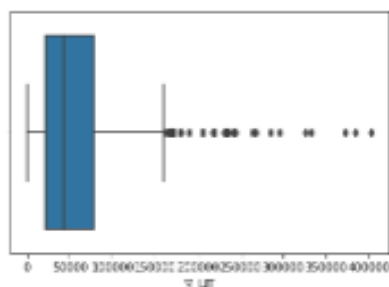
Description of M_LIT

```
count      648.000000
mean      57967.979688
std       55910.282466
min        286.000000
25%       21298.000000
50%       42693.500000
75%       77989.500000
max       483261.000000
Name: M_LIT, dtype: float64 Distribution of M_LIT
```

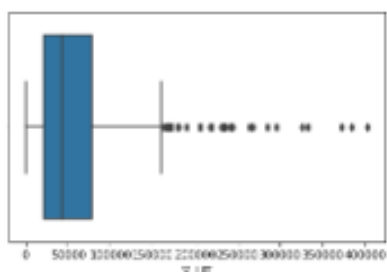
```
count      648.000000
mean      57967.979688
std       55910.282466
min        286.000000
25%       21298.000000
50%       42693.500000
75%       77989.500000
max       483261.000000
Name: M_LIT, dtype: float64 Distribution of M_LIT
```



BoxPlot of M_LIT



BoxPlot of M_LIT

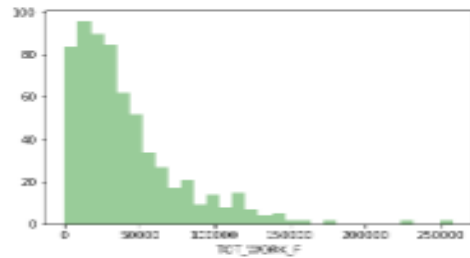


Description of TOT_WORK_F

```

count      648.000000
mean       41295.760938
std        37192.360943
min         357.000000
25%        16097.750000
50%        30588.500000
75%        53234.250000
max       257848.000000
Name: TOT_WORK_F, dtype: float64
Distribution of TOT_WORK_F

```



BoxPlot of TOT_WORK_F

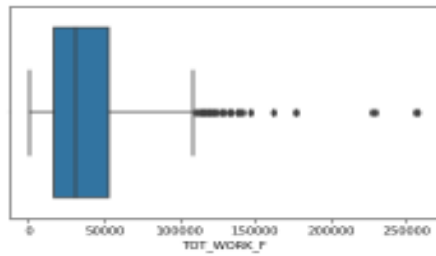
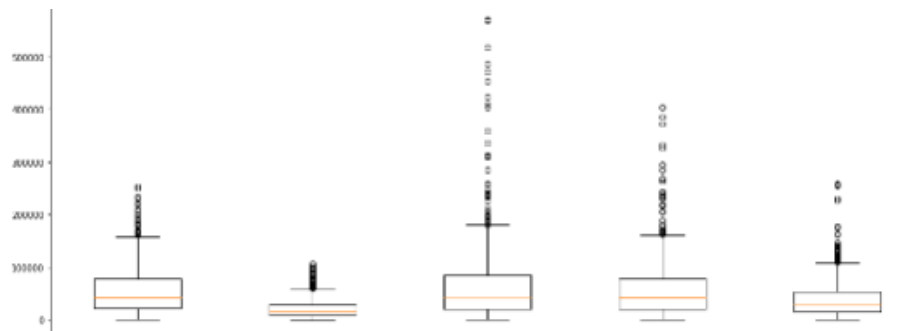


Fig 10: boxplot of five variables



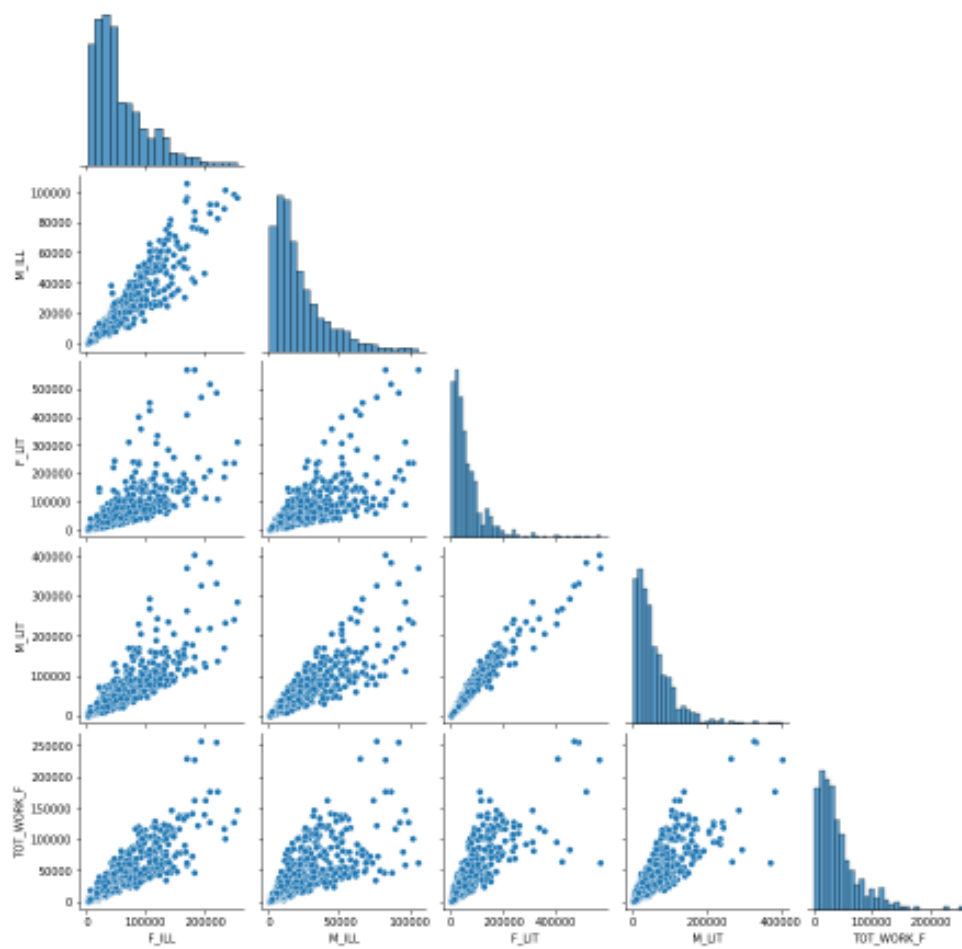


Fig 11: pair plot of variables

Q1 Is most of the male population is literate or illiterate ?

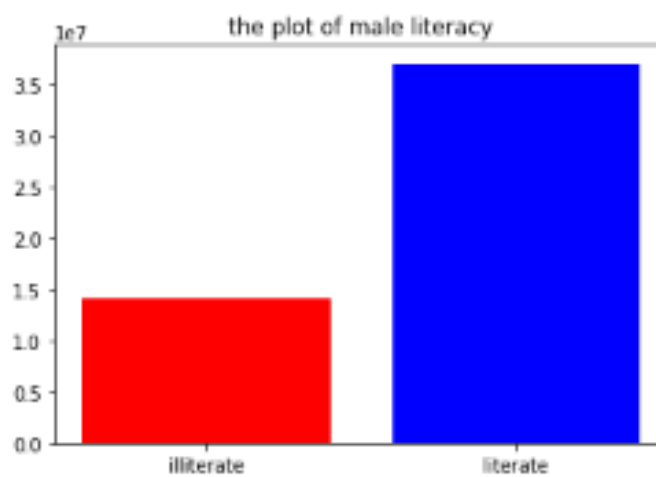


Fig 12: plot of male literacy

We can clearly see from the plot that most of the male population is literate.

Q2 Is most of the female population is literate or illiterate?



Fig 13: plot of female literacy

We can clearly see from the plot that most of the female population is literate

Q3 Which gender has more number of literate population ?

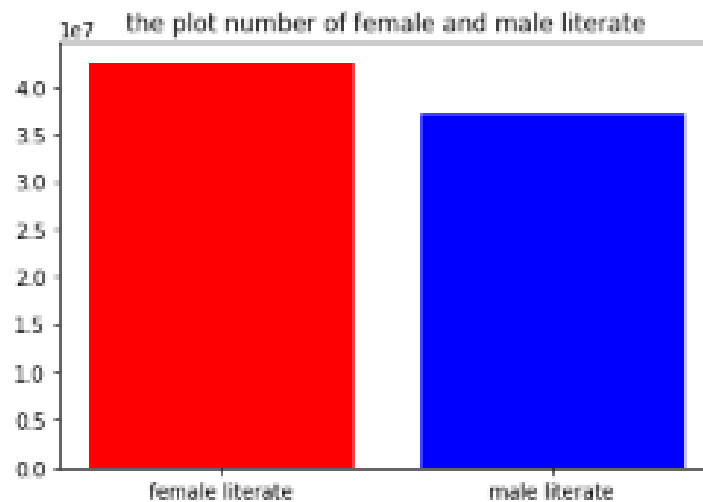


Fig 14: plot of literacy

We can clearly see from the plot that most of the female population is literate

Q4 which gender has more number of illiterate population ?

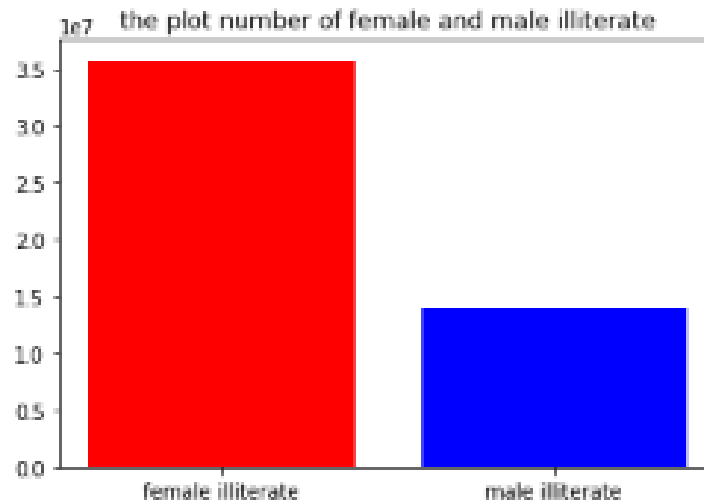


Fig 15: plot of illiteracy

We can clearly see from the plot that most of the female population is literate

Q5 which gender has most literate and illiterate population

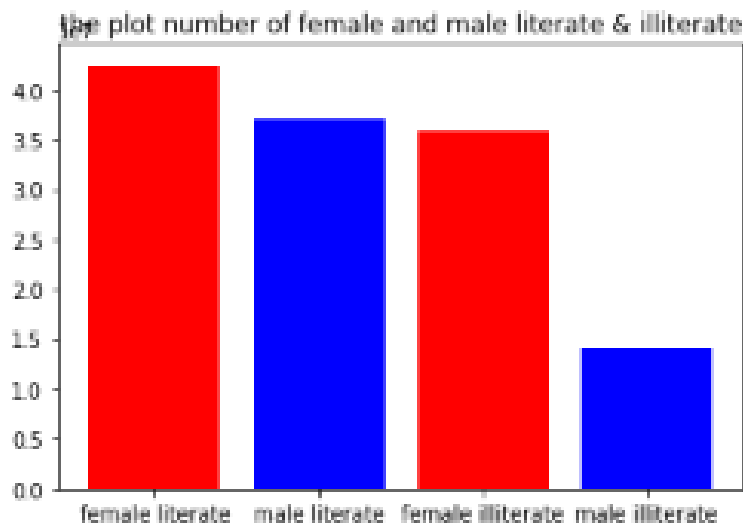


Fig 16: plot of illiteracy and literacy

We can clearly see from the plot that most of the female population is literate

And males have the least illiterate population

Q6 how much total working population of females is literate

the plot number of total working population of female is literate

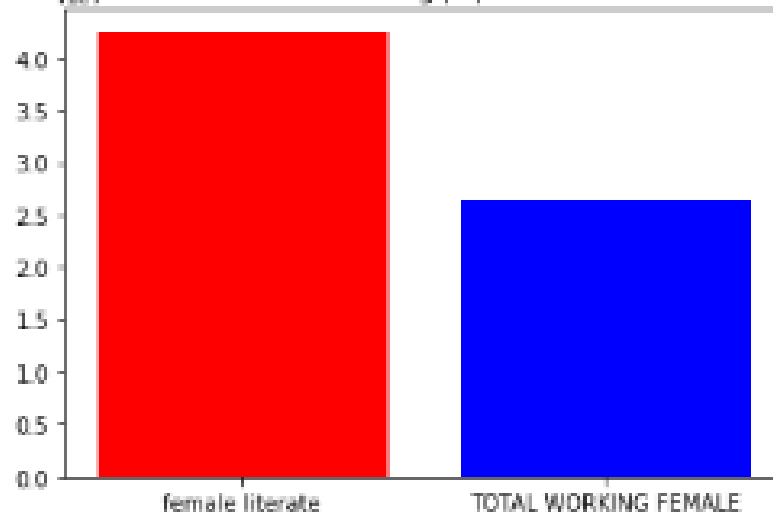


Fig 17: plot of total working population and female literate

We can clearly see from the plot that most of the female population is literate but only 50-60% of them are working.

2.3 - PCA: We choose not to treat outliers for this case. Do you think that treating outliers for this case is necessary?

Yes, treating outliers are necessary to treat outliers as it helps in getting the accurate data analysis results and helps in reducing errors.

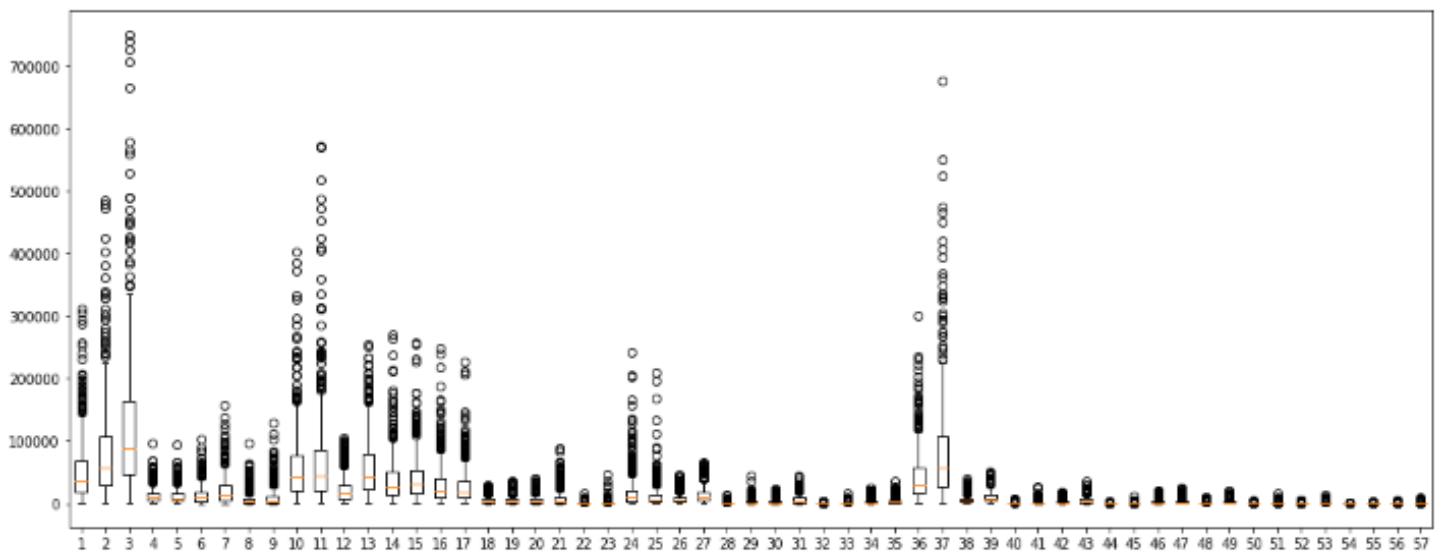


Fig 18: box plot of all variables

2.4 - PCA: Scale the Data using z-score method. Does scaling have any impact on outliers?

I have scaled the data with SciPy stat but we can also do scaling of the with sklearn.preprocessing.

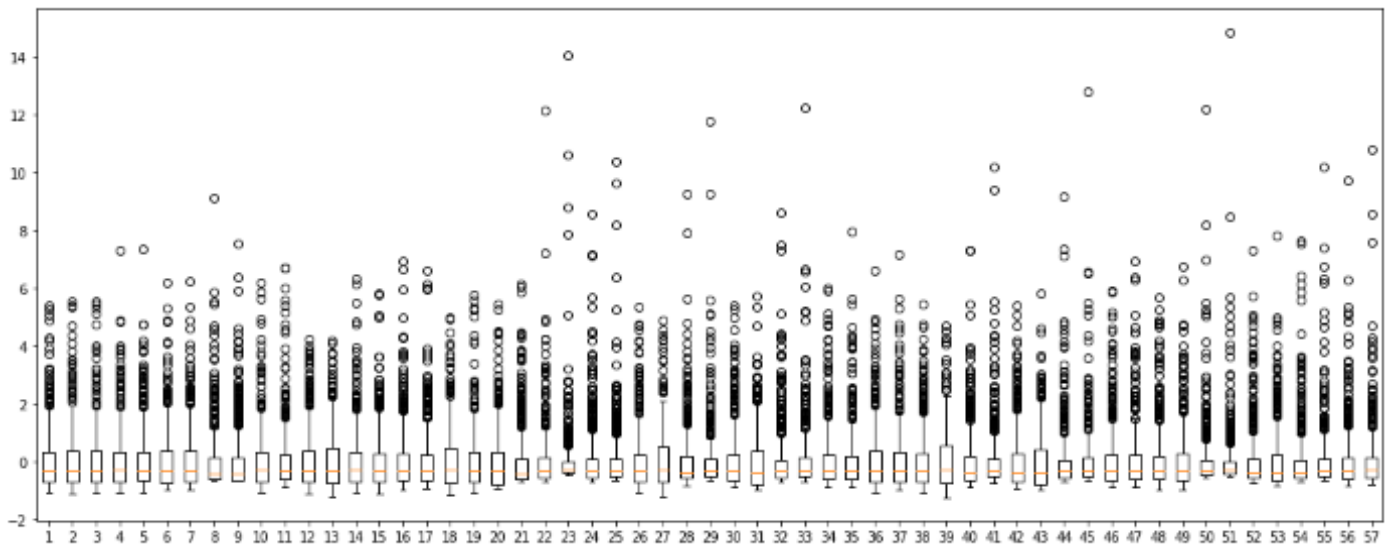


Fig 19: box plot of all variables

With help of NumPy we get covariance matrix:

```
array ([[2.65384958, 2.71559682, 3.0810424, ..., 3.32705346, 3.26012156,
3.09943089],
[2.71559682, 2.95818195, 3.21927718, ..., 3.52898196, 3.42192001,
3.25382599],
[3.0810424, 3.21927718, 3.85909673, ..., 4.05405594, 3.96445766,
3.77161732],
...,
[3.32705346, 3.52898196, 4.05405594, ..., 4.36443144, 4.25265838,
4.05275828],
[3.26012156, 3.42192001, 3.96445766, ..., 4.25265838, 4.15880459,
3.96567682],
[3.09943089, 3.25382599, 3.77161732, ..., 4.05275828, 3.96567682,
3.79502824]])
```

With the help of Sklenar function we got eigen values: array ([31.81356474, 7.86942415, 4.15340812, 3.66879058, 2.20652588, 1.93827502, 1.17617374, 0.75115909, 0.61705374, 0.52830088])

And eigen vectors are array ([[1.56020579e-01, 1.67117635e-01, 1.65553179e-01, 1.62192948e-01, 1.62566396e-01, 1.51357849e-01, 1.51566500e-01, 2.72341946e-02, 2.81833150e-02, 1.61992837e-01, 1.46872680e-01, 1.61749445e-01, 1.65248187e-01, 1.59871988e-01, 1.45935804e-01, 1.46200730e-01, 1.23970284e-01, 1.03127159e-01, 7.45397856e-02, 1.13355712e-01, 7.38821590e-02, 1.31572584e-01, 8.33826397e-02, 1.23526242e-01, 1.11021264e-01, 1.64615479e-01, 1.55395618e-01, 8.23885414e-02, 4.91953957e-02, 1.28598563e-01, 1.14305073e-01, 1.40853227e-01, 1.27669598e-01, 1.55262872e-01, 1.47286584e-01, 1.64971950e-01, 1.61253433e-01, 1.65501611e-01, 1.55647049e-01, 9.30142064e-02, 5.15358640e-02, 1.28576116e-01, 1.10645843e-01, 1.39592763e-01, 1.24545909e-01, 1.54293786e-01, 1.46285654e-01, 1.50125706e-01, 1.40157047e-01, 5.25417829e-02, 4.17859530e-02, 1.21840354e-01, 1.16011410e-01, 1.39868774e-01, 1.32192245e-01, 1.50375578e-01, 1.31066203e-01], [-1.26346525e-01, -8.96765481e-02, -1.04912371e-01, -2.20945086e-02, -2.02705495e-02, -4.51109032e-02, -5.19237543e-02, 2.76790387e-02, 3.02225550e-02, -1.15354767e-01, -6.62537318e-03, -9.10743682e-03, -1.33529221e-01, -8.50869689e-02, -1.76368057e-01, -1.51412544e-01, 6.24149874e-02,

8.64767269e-02,	-3.10403498e-02,	-5.86880214e-02,
-7.60210677e-02,	-8.24766375e-02,	-2.12984254e-01,
-2.10071166e-01,	9.29935012e-02,	1.25269967e-01,
2.69449716e-01,	2.46546811e-01,	1.65830750e-01,
1.40957749e-01,	6.80679428e-02,	2.42164125e-02,
-8.94419720e-02,	-1.17899307e-01,	-4.39949601e-02,
-1.05501898e-01,	7.71926975e-02,	1.03173976e-01,
2.64409408e-01,	2.44261317e-01,	1.58782773e-01,
1.25286970e-01,	6.22623250e-02,	1.47659019e-02,
-9.31585894e-02,	-1.25595577e-01,	1.50680869e-01,
1.80690375e-01,	2.51328442e-01,	2.40719745e-01,
1.85277342e-01,	1.80615650e-01,	8.48690452e-02,
5.08133220e-02,	-6.53645529e-02,	-7.38474208e-02],
[-2.69025027e-03,	5.66976190e-02,	3.87494746e-02,
5.77881518e-02,	5.01255677e-02,	2.56890397e-03,
-2.51008795e-02,	-1.23504453e-01,	-1.39768833e-01,
8.21676677e-02,	1.17097683e-01,	-2.18550935e-02,
-9.30623763e-02,	4.51763691e-02,	-5.94495457e-02,
5.42945289e-02,	-5.56090961e-02,	-6.73992944e-02,
-9.23808946e-03,	-2.47917055e-01,	-2.51932296e-01,
2.65689386e-02,	-6.05232993e-02,	1.37377881e-01,
9.56339841e-02,	-8.62782527e-03,	-4.93697036e-02,
1.98754143e-01,	2.68786906e-01,	-1.89867566e-01,
-2.67767729e-01,	-2.12567389e-02,	-8.25040484e-02,
1.11712747e-01,	1.00045670e-01,	6.44232083e-02,
7.97035639e-02,	-2.42054166e-02,	-7.20134423e-02,
1.53517557e-01,	2.56212918e-01,	-2.00118572e-01,
-2.79866018e-01,	-2.06182531e-02,	-8.27935649e-02,
1.10285441e-01,	9.56665986e-02,	5.48919412e-02,
2.39815623e-02,	2.68330072e-01,	2.84955665e-01,
-1.38627894e-01,	-2.02198401e-01,	-2.25985196e-02,
-7.87198692e-02,	1.11827318e-01,	1.02552501e-01],
[-1.25293371e-01,	-1.99415702e-02,	-7.08726202e-02,
1.19171726e-02,	1.48442005e-02,	1.24850957e-02,
-2.98925083e-02,	-2.22247412e-01,	-2.29754420e-01,
-3.51625572e-02,	-5.95594178e-02,	2.53483370e-02,
-7.60233569e-02,	-4.01544117e-02,	-2.25160033e-01,
-6.83507465e-02,	-2.46639865e-01,	-8.97686819e-02,
-2.88964883e-01,	-1.36082339e-01,	-2.90042169e-01,
1.52366335e-01,	4.89504702e-02,	-4.02891831e-02,
-1.20391064e-01,	9.30182650e-02,	-8.87071351e-02,
-6.27609058e-02,	-1.68401590e-01,	9.17874509e-02,
-1.06365430e-01,	2.37984720e-01,	1.96320743e-01,
8.71191186e-02,	2.67292472e-02,	-2.55415177e-05,
3.89358966e-03,	9.28748901e-02,	-1.07860188e-01,
-3.84875762e-02,	-1.79691340e-01,	8.04108514e-02,
-1.36240262e-01,	2.37744957e-01,	1.90510604e-01,
8.64794098e-02,	2.72754576e-02,	8.74333682e-02,

-2.22902303e-02,	-1.04686028e-01,	-1.35715829e-01,
1.32544187e-01,	4.05131037e-03,	2.30037988e-01,
2.06200724e-01,	8.48540392e-02,	2.11244736e-02],
[-7.02208326e-03,	-3.30261797e-02,	-1.28467033e-02,
-5.02475101e-02,	-4.38479670e-02,	-1.73006734e-01,
-1.59803417e-01,	4.33163419e-01,	4.38791921e-01,
-9.10133039e-03,	5.58437008e-02,	-9.65797550e-02,
-1.19910504e-01,	-1.95528839e-02,	-4.04373671e-02,
-3.68019626e-02,	-8.28338587e-02,	-2.86039079e-01,
-2.41936366e-01,	-2.05723504e-01,	-1.77604766e-01,
-1.34088831e-01,	-1.39440884e-01,	6.46377099e-02,
8.07427680e-02,	6.02435623e-02,	8.92022890e-02,
-2.22632349e-02,	-5.92051969e-02,	1.94217749e-02,
8.05270982e-02,	-5.99705215e-02,	-3.36016572e-02,
1.19120710e-01,	1.66882498e-01,	-4.38337603e-02,
5.37136660e-04,	5.40731673e-02,	7.30497551e-02,
-7.78921571e-03,	-6.13026163e-02,	8.45700429e-03,
6.41091701e-02,	-6.64002513e-02,	-4.48097937e-02,
1.08828726e-01,	1.41190165e-01,	8.11854109e-02,
1.29936485e-01,	-4.88490365e-02,	-5.18948148e-02,
6.23798835e-02,	1.28308262e-01,	-3.63901233e-02,
1.64823759e-04,	1.62862488e-01,	2.38291984e-01],
[4.08281236e-03,	-7.33892582e-02,	-4.36468776e-02,
-1.57956741e-01,	-1.54435838e-01,	-6.42950849e-02,
-4.05178242e-02,	2.22590756e-01,	2.25530984e-01,
-5.54647180e-02,	-4.80207140e-02,	-1.15234150e-01,
-2.87572169e-02,	-1.80069366e-03,	1.05162304e-01,
1.92826056e-02,	1.23832265e-01,	-6.16981242e-03,
1.02951208e-01,	-3.10678194e-02,	1.92397157e-02,
1.74465381e-01,	4.22309325e-01,	2.34771546e-02,
8.30792178e-02,	-9.07614920e-02,	1.78676850e-02,
3.19145578e-02,	9.20857153e-02,	-1.41604662e-01,
-8.51201684e-02,	8.95332953e-02,	3.65111795e-01,
-6.10655989e-02,	1.73934355e-03,	-1.36253329e-01,
-1.06900175e-01,	-9.67084917e-02,	2.37730742e-02,
1.34769857e-02,	9.39927460e-02,	-1.44060823e-01,
-7.67084401e-02,	9.70574753e-02,	3.84552143e-01,
-6.20430271e-02,	8.96165312e-03,	-6.07153533e-02,
-1.72704069e-03,	6.54086839e-02,	8.37426375e-02,
-1.24209277e-01,	-1.05529913e-01,	6.12279896e-02,
2.95599696e-01,	-5.23862474e-02,	-2.49010756e-02],
[-1.18110420e-01,	8.95543279e-02,	-2.12425804e-03,
1.65066693e-01,	1.69082313e-01,	-1.56616120e-03,
-8.46576325e-02,	4.05505171e-01,	3.57799733e-01,
4.59340904e-02,	-2.10641811e-02,	2.01946551e-01,
2.84250386e-02,	4.50530285e-02,	-1.19423828e-01,
4.73668824e-02,	-9.04307518e-02,	3.85792299e-01,
2.07881596e-01,	-1.30773481e-02,	-1.58333973e-01,

1.19824865e-01,	-1.39294074e-01,	-1.56013662e-02,
-7.06449807e-02,	2.01945537e-02,	-1.57222087e-01,
2.90721618e-02,	-4.58837977e-02,	2.02976379e-02,
-1.50711850e-01,	1.08603621e-01,	-4.94715251e-02,
-4.28750247e-03,	-1.17886196e-01,	1.26291461e-01,
5.06245188e-02,	2.66713701e-02,	-1.38020671e-01,
6.32740099e-02,	-1.92212141e-02,	2.14514915e-02,
-1.46120967e-01,	1.15067653e-01,	-4.22393179e-02,
-1.20438787e-03,	-9.10604465e-02,	-7.31610967e-03,
-2.00877437e-01,	-4.22951220e-02,	-1.03406947e-01,
1.45872850e-02,	-1.52174700e-01,	8.31223341e-02,
-6.87217760e-02,	-1.93539659e-02,	-2.00052834e-01],
[5.72389403e-02,	1.11431209e-01,	8.83553113e-02,
1.69594884e-01,	1.69458172e-01,	-1.29301290e-01,
-1.44352081e-01,	2.19818496e-02,	1.48736254e-02,
9.94228857e-02,	1.10359861e-01,	1.32079860e-01,
3.72704185e-02,	7.68689545e-02,	-4.12544522e-02,
8.79616816e-02,	-1.80367069e-02,	-2.31343705e-01,
-2.99574045e-01,	5.17576329e-02,	-1.13997037e-01,
-1.35092829e-01,	3.77112324e-01,	1.42202440e-01,
6.96842900e-02,	4.10448554e-03,	-9.03271864e-02,
7.38189176e-02,	4.89339728e-03,	1.41822624e-01,
-2.51860324e-02,	-2.06463038e-01,	7.49567994e-02,
-1.40518702e-01,	-2.25984329e-01,	1.37732088e-01,
1.39466320e-01,	-2.69871622e-03,	-1.17627847e-01,
6.80031882e-02,	-1.94446250e-02,	1.40602227e-01,
-5.20077614e-02,	-2.13660011e-01,	8.44478387e-02,
-1.42040131e-01,	-2.24162681e-01,	3.13237674e-02,
9.78947498e-04,	7.77140227e-02,	5.90416261e-02,
1.39166557e-01,	6.74209419e-02,	-1.74949447e-01,
4.47046152e-02,	-1.24166132e-01,	-2.02142424e-01],
[4.26426297e-03,	1.88718994e-02,	1.49110483e-02,
-5.67729534e-02,	-5.93231092e-02,	3.74800933e-02,
4.12320246e-02,	1.86322807e-02,	4.38659393e-02,
4.51935138e-02,	2.19962970e-02,	-5.75960731e-02,
9.20071457e-04,	4.52565826e-02,	1.14253939e-01,
6.20674638e-02,	1.43678886e-01,	-3.64574761e-01,
-1.13373697e-01,	-1.79033216e-01,	2.49005270e-02,
3.83824269e-01,	-2.14204450e-01,	1.66356835e-01,
2.78022734e-01,	-4.12529185e-02,	-5.52388166e-03,
1.56551464e-02,	2.37227547e-02,	-1.13496935e-02,
9.19244295e-02,	2.38752017e-01,	-1.47744801e-01,
-1.09101817e-01,	-1.43586594e-01,	-6.74392520e-03,
-3.07997521e-02,	-4.78759050e-02,	4.34856707e-03,
6.04167971e-03,	1.23446283e-02,	-2.77157875e-02,
7.99587767e-02,	2.42022448e-01,	-1.69232875e-01,
-9.73659075e-02,	-8.06274087e-02,	-1.17560663e-02,
-3.49847304e-02,	3.32222805e-02,	4.80868090e-02,

	No	MH	IQ1 M	M	M2	P2 M	M3	M5	M1	P1	M11	M13	M15	M17	M19	M21	M23	M25	M27	M29	M31	M33	M35	M37	M39	M41	M43	M45	M47	M49	M51	M53	M55	M57	M59	M61	M63	M65	M67	M69	M71	M73	M75	M77	M79	M81	M83	M85	M87	M89	M91	M93	M95	M97	M99	M101	M103	M105	M107	M109	M111	M113	M115	M117	M119	M121	M123	M125	M127	M129	M131	M133	M135	M137	M139	M141	M143	M145	M147	M149	M151	M153	M155	M157	M159	M161	M163	M165	M167	M169	M171	M173	M175	M177	M179	M181	M183	M185	M187	M189	M191	M193	M195	M197	M199	M201	M203	M205	M207	M209	M211	M213	M215	M217	M219	M221	M223	M225	M227	M229	M231	M233	M235	M237	M239	M241	M243	M245	M247	M249	M251	M253	M255	M257	M259	M261	M263	M265	M267	M269	M271	M273	M275	M277	M279	M281	M283	M285	M287	M289	M291	M293	M295	M297	M299	M301	M303	M305	M307	M309	M311	M313	M315	M317	M319	M321	M323	M325	M327	M329	M331	M333	M335	M337	M339	M341	M343	M345	M347	M349	M351	M353	M355	M357	M359	M361	M363	M365	M367	M369	M371	M373	M375	M377	M379	M381	M383	M385	M387	M389	M391	M393	M395	M397	M399	M401	M403	M405	M407	M409	M411	M413	M415	M417	M419	M421	M423	M425	M427	M429	M431	M433	M435	M437	M439	M441	M443	M445	M447	M449	M451	M453	M455	M457	M459	M461	M463	M465	M467	M469	M471	M473	M475	M477	M479	M481	M483	M485	M487	M489	M491	M493	M495	M497	M499	M501	M503	M505	M507	M509	M511	M513	M515	M517	M519	M521	M523	M525	M527	M529	M531	M533	M535	M537	M539	M541	M543	M545	M547	M549	M551	M553	M555	M557	M559	M561	M563	M565	M567	M569	M571	M573	M575	M577	M579	M581	M583	M585	M587	M589	M591	M593	M595	M597	M599	M601	M603	M605	M607	M609	M611	M613	M615	M617	M619	M621	M623	M625	M627	M629	M631	M633	M635	M637	M639	M641	M643	M645	M647	M649	M651	M653	M655	M657	M659	M661	M663	M665	M667	M669	M671	M673	M675	M677	M679	M681	M683	M685	M687	M689	M691	M693	M695	M697	M699	M701	M703	M705	M707	M709	M711	M713	M715	M717	M719	M721	M723	M725	M727	M729	M731	M733	M735	M737	M739	M741	M743	M745	M747	M749	M751	M753	M755	M757	M759	M761	M763	M765	M767	M769	M771	M773	M775	M777	M779	M781	M783	M785	M787	M789	M791	M793	M795	M797	M799	M801	M803	M805	M807	M809	M811	M813	M815	M817	M819	M821	M823	M825	M827	M829	M831	M833	M835	M837	M839	M841	M843	M845	M847	M849	M851	M853	M855	M857	M859	M861	M863	M865	M867	M869	M871	M873	M875	M877	M879	M881	M883	M885	M887	M889	M891	M893	M895	M897	M899	M901	M903	M905	M907	M909	M911	M913	M915	M917	M919	M921	M923	M925	M927	M929	M931	M933	M935	M937	M939	M941	M943	M945	M947	M949	M951	M953	M955	M957	M959	M961	M963	M965	M967	M969	M971	M973	M975	M977	M979	M981	M983	M985	M987	M989	M991	M993	M995	M997	M999	M1001	M1003	M1005	M1007	M1009	M1011	M1013	M1015	M1017	M1019	M1021	M1023	M1025	M1027	M1029	M1031	M1033	M1035	M1037	M1039	M1041	M1043	M1045	M1047	M1049	M1051	M1053	M1055	M1057	M1059	M1061	M1063	M1065	M1067	M1069	M1071	M1073	M1075	M1077	M1079	M1081	M1083	M1085	M1087	M1089	M1091	M1093	M1095	M1097	M1099	M1101	M1103	M1105	M1107	M1109	M1111	M1113	M1115	M1117	M1119	M1121	M1123	M1125	M1127	M1129	M1131	M1133	M1135	M1137	M1139	M1141	M1143	M1145	M1147	M1149	M1151	M1153	M1155	M1157	M1159	M1161	M1163	M1165	M1167	M1169	M1171	M1173	M1175	M1177	M1179	M1181	M1183	M1185	M1187	M1189	M1191	M1193	M1195	M1197	M1199	M1201	M1203	M1205	M1207	M1209	M1211	M1213	M1215	M1217	M1219	M1221	M1223	M1225	M1227	M1229	M1231	M1233	M1235	M1237	M1239	M1241	M1243	M1245	M1247	M1249	M1251	M1253	M1255	M1257	M1259	M1261	M1263	M1265	M1267	M1269	M1271	M1273	M1275	M1277	M1279	M1281	M1283	M1285	M1287	M1289	M1291	M1293	M1295	M1297	M1299	M1301	M1303	M1305	M1307	M1309	M1311	M1313	M1315	M1317	M1319	M1321	M1323	M1325	M1327	M1329	M1331	M1333	M1335	M1337	M1339	M1341	M1343	M1345	M1347	M1349	M1351	M1353	M1355	M1357	M1359	M1361	M1363	M1365	M1367	M1369	M1371	M1373	M1375	M1377	M1379	M1381	M1383	M1385	M1387	M1389	M1391	M1393	M1395	M1397	M1399	M1401	M1403	M1405	M1407	M1409	M1411	M1413	M1415	M1417	M1419	M1421	M1423	M1425	M1427	M1429	M1431	M1433	M1435	M1437	M1439	M1441	M1443	M1445	M1447	M1449	M1451	M1453	M1455	M1457	M1459	M1461	M1463	M1465	M1467	M1469	M1471	M1473	M1475	M1477	M1479	M1481	M1483	M1485	M1487	M1489	M1491	M1493	M1495	M1497	M1499	M1501	M1503	M1505	M1507	M1509	M1511	M1513	M1515	M1517	M1519	M1521	M1523	M1525	M1527	M1529	M1531	M1533	M1535	M1537	M1539	M1541	M1543	M1545	M1547	M1549	M1551	M1553	M1555	M1557	M1559	M1561	M1563	M1565	M1567	M1569	M1571	M1573	M1575	M1577	M1579	M1581	M1583	M1585	M1587	M1589	M1591	M1593	M1595	M1597	M1599	M1601	M1603	M1605	M1607	M1609	M1611	M1613	M1615	M1617	M1619	M1621	M1623	M1625	M1627	M1629	M1631	M1633	M1635	M1637	M1639	M1641	M1643	M1645	M1647	M1649	M1651	M1653	M1655	M1657	M1659	M1661	M1663	M1665	M1667	M1669	M1671	M1673	M1675	M1677	M1679	M1681	M1683	M1685	M1687	M1689	M1691	M1693	M1695	M1697	M1699	M1701	M1703	M1705	M1707	M1709	M1711	M1713	M1715	M1717	M1719	M1721	M1723	M1725	M1727	M1729	M1731	M1733	M1735	M1737	M1739	M1741	M1743	M1745	M1747	M1749	M1751	M1753	M1755	M1757	M1759	M1761	M1763	M1765	M1767	M1769	M1771	M1773	M1775	M1777	M1779	M1781	M1783	M1785	M1787	M1789	M1791	M1793	M1795	M1797	M1799	M1801	M1803	M1805	M1807	M1809	M1811	M1813	M1815	M1817	M1819	M1821	M1823	M1825	M1827	M1829	M1831	M1833	M1835	M1837	M1839	M1841	M1843	M1845	M1847	M1849	M1851	M1853	M1855	M1857	M1859	M1861	M1863	M1865	M1867	M1869	M1871	M1873	M1875	M1877	M1879	M1881	M1883	M1885	M1887	M1889	M1891	M1893	M1895	M1897	M1899	M1901	M1903	M1905	M1907	M1909	M1911	M1913	M1915	M1917	M1919	M1921	M1923	M1925	M1927	M1929	M1931	M1933	M1935	M1937	M1939	M1941	M1943	M1945	M1947	M1949	M1951	M1953	M1955	M1957	M1959	M1961	M1963	M1965	M1967	M1969	M1971	M1973	M1975	M1977	M1979	M1981	M1983	M1985	M1987	M1989	M1991	M1993	M1995	M1997	M1999	M2001	M2003	M2005	M2007	M2009	M2011	M2013	M2015	M2017	M2019	M2021	M2023	M2025	M2027	M2029	M2031	M2033	M2035	M2037	M2039	M2041	M2043	M2045	M2047	M2049	M2051	M2053	M2055	M2057	M2059	M2061	M2063	M2065	M2067	M2069	M2071	M2073	M2075	M2077	M2079	M2081	M2083	M2085	M2087	M2089	M2091	M2093	M2095	M2097	M2099	M2101	M2103	M2105	M2107	M2109	M2111	M2113	M2115	M2117	M2119	M2121	M2123	M2125	M2127	M2129	M2131	M2133	M2135	M2137	M2139	M2141	M2143	M2145	M2147	M2149	M2151	M2153	M2155	M2157	M2159	M2161	M2163	M2165	M2167	M2169	M2171	M2173	M2175	M2177	M2179	M2181	M2183	M2185	M2187	M2189	M2191	M2193	M2195	M2197	M2199	M2201	M2203	M2205	M2207	M2209	M2211	M2213	M2215	M2217	M2219	M2221	M2223	M2225	M2227	M2229	M2231	M2233	M2235	M2237	M2239	M2241	M2243	M2245	M2247	M2249	M2251	M2253	M2255	M2257	M2259	M2261	M2263	M2265	M2267	M2269	M2271	M2273	M2275	M2277	M2279	M2281	M2283	M2285	M2287	M2289	M2291	M2293	M2295	M2297	M2299	M2301	M2303	M2305	M2307	M2309	M2311	M2313	M2315	M2317	M2319	M2321	M2323	M2325	M2327	M2329	M2331	M2333	M2335	M2337	M2339	M2341	M2343	M2345	M2347	M2349	M2351	M2353	M2355	M2357	M2359	M2361	M2363	M2365	M2367	M2369	M2371	M2373	M2375	M2377	M2379	M2381	M2383	M2385	M2387	M2389	M2391	M2393	M2395	M2397	M2399	M2401	M2403	M2405	M2407	M2409	M2411	M2413	M2415	M2417	M2419	M2421	M2423	M2425	M2427	M2429	M2431	M2433	M2435	M2437	M2439	M2441	M2443	M2445	M2447	M2449	M2451	M2453	M2455	M2457	M2459	M2461	M2463	M2465	M2467	M2469	M2471	M2473	M2475	M2477	M2479	M2481	M2483	M2485	M2487	M2489	M2491	M2493	M2495	M2497	M2499	M2501	M2503	M2505	M2507	M2509	M2511	M2513	M2515	M2517	M2519	M2521	M2523	M2525	M2527	M2529	M2531	M2533	M2535	M2537	M2539	M2541	M2543	M2545	M2547	M2549	M2551	M2553	M2555	M2557	M2559	M2561	M2563	M2565	M2567	M2569	M2571	M2573	M2575	M2577	M2579	M2581	M2583	M2585	M2587	M2589	M2591	M2593	M2595	M2597	M2599	M2601	M2603	M2605	M2607	M2609	M2611	M2613	M2615	M2617	M2619	M2621	M2623	M2625	M2627	M2629	M2631	M2633	M2635	M2637	M2639	M2641	M2643	M2645	M2647	M2649	M2651	M2653	M2655	M2657	M2659	M2661	M2663	M2665	M2667	M2669	M2671	M2673	M2675	M2677	M2679	M2681	M2683	M2685	M2687	M2689	M2691	M2693	M2695	M2697	M2699	M2701	M2703	M2705	M2707	M2709	M2711	M2713	M2715	M2717	M2719	M2721	M2723	M2725	M2727	M2729	M2731	M2733	M2735	M2737	M2739	M2741	M2743	M2745	M2747	M2749	M2751	M2753	M2755	M2757	M2759	M2761	M2763	M2765	M2767	M2769	M2771	M2773	M2775	M2777	M2779	M2781	M2783	M2785	M2787	M2789	M2791	M2793	M2795	M2797	M2799	M2801	M2803	M2805	M2807	M2809	M2811	M2813	M2815	M2817	M2819	M2821	M2823	M2825	M2827	M2829	M2831	M2833	M2835	M2837	M2839	M2841	M2843	M2845	M2847	M2849	M2851	M2853	M2855	M2857	M2859	M2861	M2863	M2865	M2
--	----	----	-------	---	----	------	----	----	----	----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	----

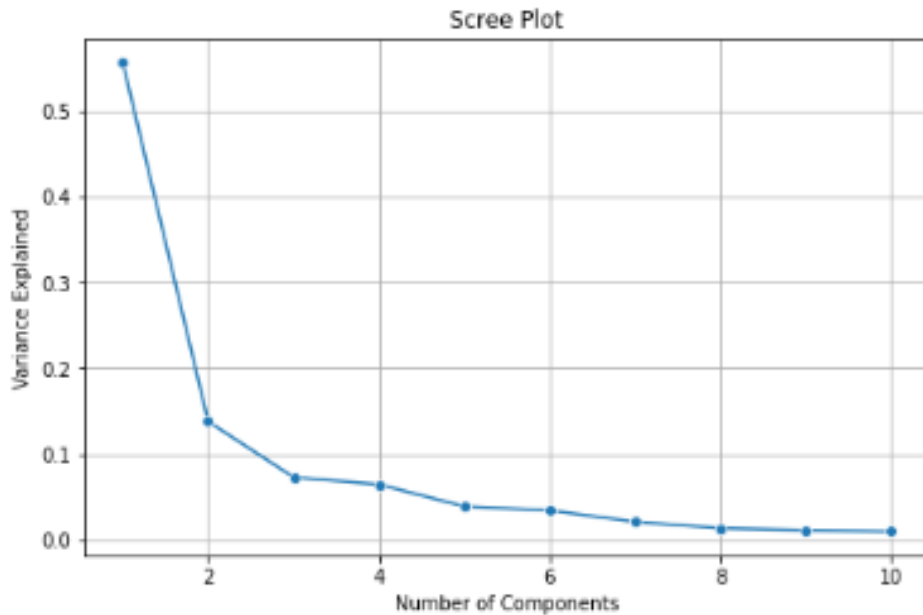


Fig21: scree plot

We will check the cumulative explained variance ratio to find a cut off for selecting the number of PCs (cut off is 90%)

```
array ([0.55726063, 0.69510499, 0.76785794, 0.83212212, 0.87077261,
0.9047243, 0.92532669, 0.93848433, 0.94929292, 0.95854687])
```

From the scree plot and from cumulative explained variance we can see that for 90% cutoff we will require 6 PCs as after which there is not much difference in the data.

Df_selected is the data frame with selected 6 PCs.

2.7 - PCA: Compare PCs with Actual Columns and identify which is explaining most variance. Write inferences about all the principal components in terms of actual variables.

Fig 22: compare pcs

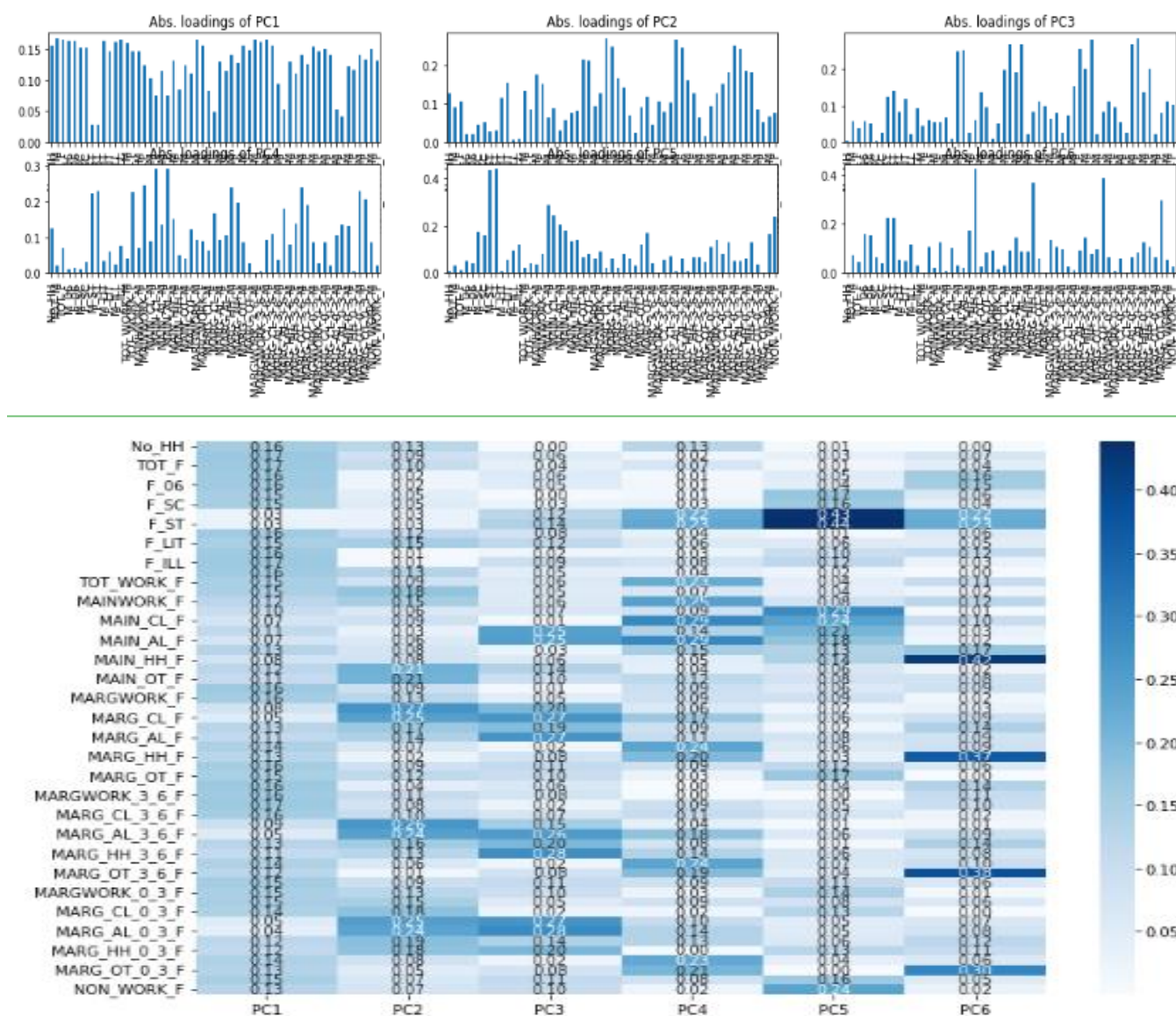


Fig 23: heatmap of pcs

we will extract the required number of PCs which is 6.

we will create a data frame out of fit_transformed scaled data above.

PC 1 explain most of the variance as we can see .

PC1 has captures most of the data.

Table 19: table of pcs

	PC1	PC2	PC3	PC4	PC5	PC6
0	-4.617263	0.138116	0.328545	1.543897	0.353736	-0.420948
1	-4.771662	-0.105885	0.244449	1.963215	-0.153884	0.417308
2	-5.964836	-0.294347	0.367394	0.619543	0.478199	0.276581
3	-6.280796	-0.500384	0.212701	1.074515	0.300799	0.051157
4	-4.478566	0.894154	1.078277	0.535557	0.804085	0.341678
5	-3.319963	2.823865	3.058460	-0.447904	0.742445	0.634676
6	-5.021393	-0.348359	0.650378	0.981072	-0.059778	-0.246957
7	-4.608709	0.022370	0.398755	1.576995	0.171316	-0.139444
8	-5.186703	-0.059097	0.184397	1.735440	0.169174	0.455039
9	-4.226190	-1.335080	0.697838	1.470509	0.269146	-0.002576

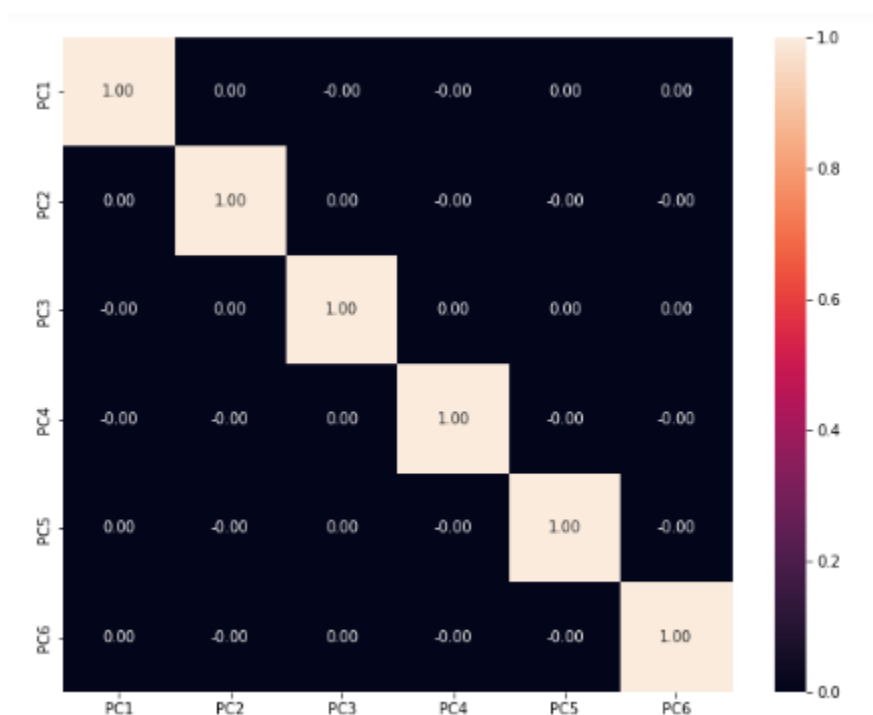


Fig 24: correlation matrix

2.8 - PCA: Write linear equation for first PC.

linear equation formula: $PC1 = a1x1 + a2x2 + a3x3 + a4x4 + \dots + a57x57$

$a1, a2, a3, \dots$ = Coefficients of PC1

array([0.15602058, 0.16711763, 0.16555318, 0.16219295, 0.1625664, 0.15135785, 0.1515665, 0.02723419, 0.02818332, 0.16199284,

0.14687268,	0.16174944,	0.16524819,	0.15987199,	0.1459358
0.14620073,	0.12397028,	0.10312716,	0.07453979,	0.11335571,
0.07388216,	0.13157258,	0.08338264,	0.12352624,	0.11102126,
0.16461548,	0.15539562,	0.08238854,	0.0491954	0.12859856,
0.11430507,	0.14085323,	0.1276696	, 0.15526287,	0.14728658,
0.16497195,	0.16125343,	0.16550161,	0.15564705,	0.09301421,
0.05153586,	0.12857612,	0.11064584,	0.13959276,	0.12454591,
0.15429379,	0.14628565,	0.15012571,	0.14015705,	0.05254178,
0.04178595,	0.12184035,	0.11601141,	0.13986877,	0.13219224,
0.15037558,	0.1310662]		

x1,x2,x3..= Variables of PC1

No_HH	-0.904738
TOT_M	-0.771236
TOT_F	-0.815563
M_06	-0.561012
F_06	-0.507738
M_SC	-0.958575
F_SC	-0.957049
M_ST	-0.423306
F_ST	-0.476423
M_LIT	-0.798097
F_LIT	-0.733477
M_ILL	-0.604015
F_ILL	-0.798229
TOT_WORK_M	-0.859260
TOT_WORK_F	-1.010238
MAINWORK_M	-0.872367
MAINWORK_F	-0.898216
MAIN_CL_M	-1.042844
MAIN_CL_F	-0.986630
MAIN_AL_M	-0.851060
MAIN_AL_F	-0.683276
MAIN_HH_M	-0.630766
MAIN_HH_F	-0.407555
MAIN_OT_M	-0.624042
MAIN_OT_F	-0.611637
MARGWORK_M	-0.516943
MARGWORK_F	-0.966512
MARG_CL_M	-0.321809
MARG_CL_F	-0.485053
MARG_AL_M	-0.331426
MARG_AL_F	-0.860192
MARG_HH_M	-0.377984
MARG_HH_F	-0.453026
MARG_OT_M	-0.548764
MARG_OT_F	-0.614625

MARGWORK_3_6_M	-0.648040
MARGWORK_3_6_F	-0.663795
MARG_CL_3_6_M	-0.595998
MARG_CL_3_6_F	-1.017848
MARG_AL_3_6_M	-0.387707
MARG_AL_3_6_F	-0.563854
MARG_HH_3_6_M	-0.448658
MARG_HH_3_6_F	-0.896723
MARG_OT_3_6_M	-0.377635
MARG_OT_3_6_F	-0.431307
MARGWORK_0_3_M	-0.569151
MARGWORK_0_3_F	-0.612451
MARG_CL_0_3_M	-0.163229
MARG_CL_0_3_F	-0.720610
MARG_AL_0_3_M	-0.156494
MARG_AL_0_3_F	-0.287524
MARG_HH_0_3_M	0.156577
MARG_HH_0_3_F	-0.657412
MARG_OT_0_3_M	-0.365258
MARG_OT_0_3_F	-0.499977
NON_WORK_M	-0.413053
NON_WORK_F	-0.539614

Linear equation of pc1= Coefficients PC1 * Variables

So, the sum after Coefficients of PC1 * Variables is -4.617263481554375.

Now if we compare our PC1 score with original value i.e in our pca_final_df data frame both values are same (-4.617263481554375).