Funktionalanalysis Notizen

Jun Wei Tan*

Julius-Maximilians-Universität Würzburg

(Dated: November 18, 2024)

I. BAIRE SPACES

Definition 1 (Baire Spaces)
Theorem 2 (Baire I)
Theorem 3 (Baire II)

II. TOPOLOGICAL VECTOR SPACES

Definition 4. A topological vector space is a vector space with a topology such that addition and scalar multiplication are continuous.

Theorem 5. Translation $T_v: x \mapsto x + v$ and multiplication $\lambda: x \mapsto \lambda x$ with $\lambda \neq 0$ are continuous.

Proof. They are invertible with inverse T_{-v} and $\frac{1}{\lambda}$ respectively

Definition 6 (Uniform Continuity).

Theorem 7 (Equivalence of Completeness Conditions).

 $^{^{\}ast}$ jun-wei.tan@stud-mail.uni-wuerzburg.de

Definition 8. content...

III. BANACH SPACES