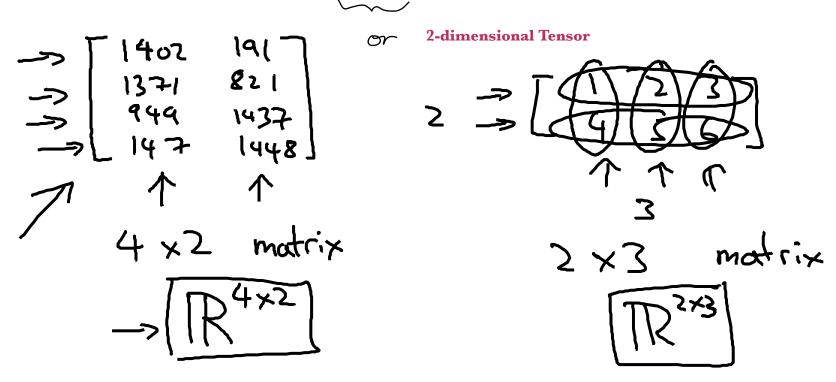


Linear Algebra review (optional)

Matrices and vectors

Matrix: Rectangular array of numbers:



Dimension of matrix: number of rows x number of columns

"i , j entry" in the i^{th} row, j^{th} column.

3x2 matrix

Dimension of matrix:

Vector: An n x 1 matrix.



$$y = \begin{pmatrix} 460 \\ 232 \\ 315 \\ 178 \end{pmatrix}$$

$$y_i = i^{th}$$
 element

1-indexed vs 0-indexed:

$$y = \begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \end{bmatrix}$$

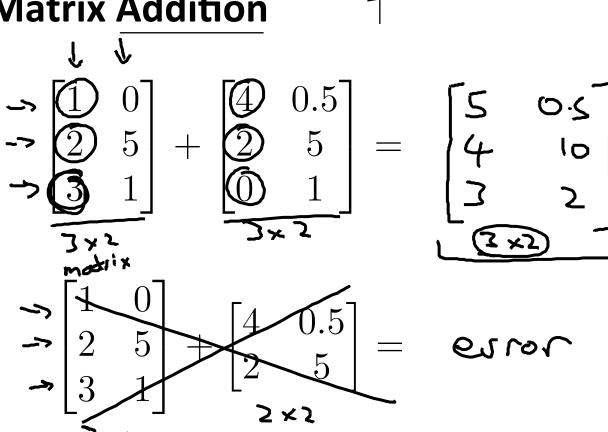
$$y = \begin{bmatrix} y_0 \\ y_1 \\ y_2 \\ y_3 \end{bmatrix} \leftarrow$$



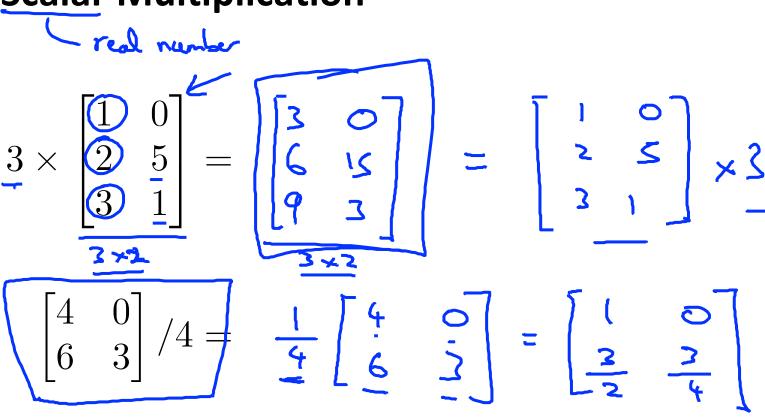
Linear Algebra review (optional)

Addition and scalar multiplication

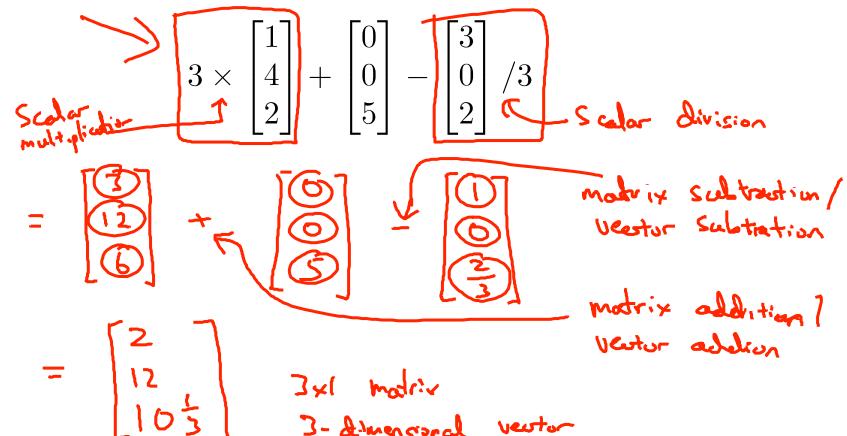
Matrix Addition



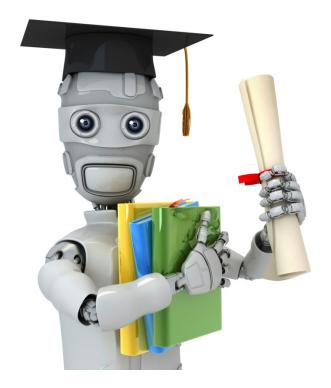
Scalar Multiplication



Combination of Operands



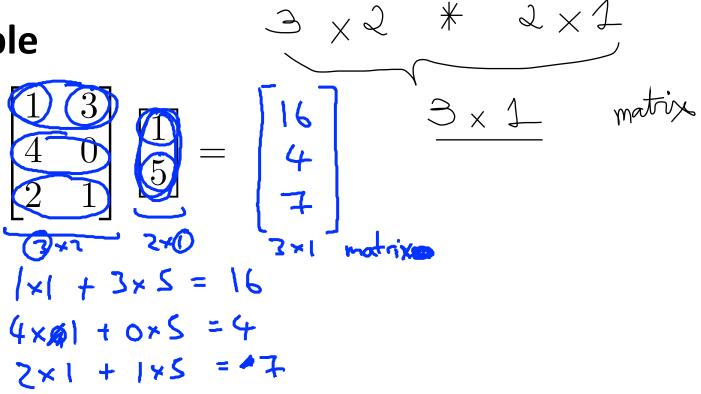
Andrew Ng



Linear Algebra review (optional)

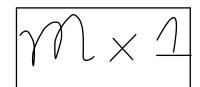
Matrix-vector multiplication

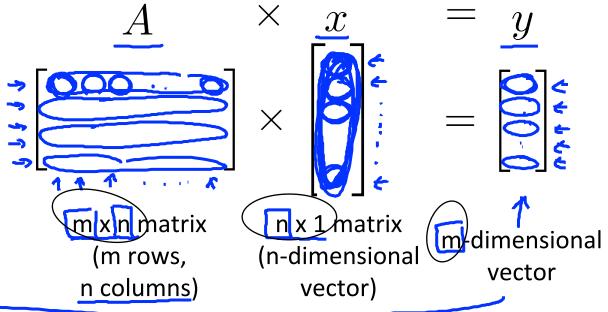
Example



Details:

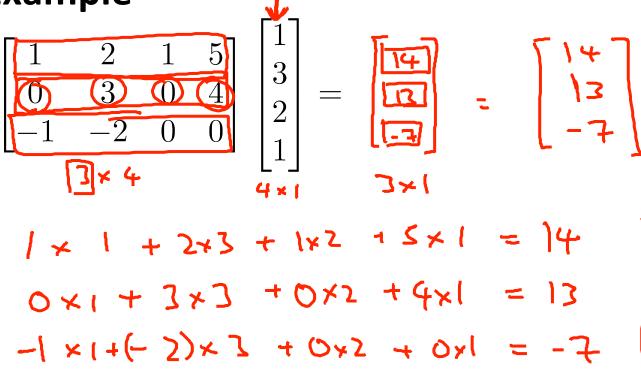
 $m \times n \quad \# \quad n \times 7 =$

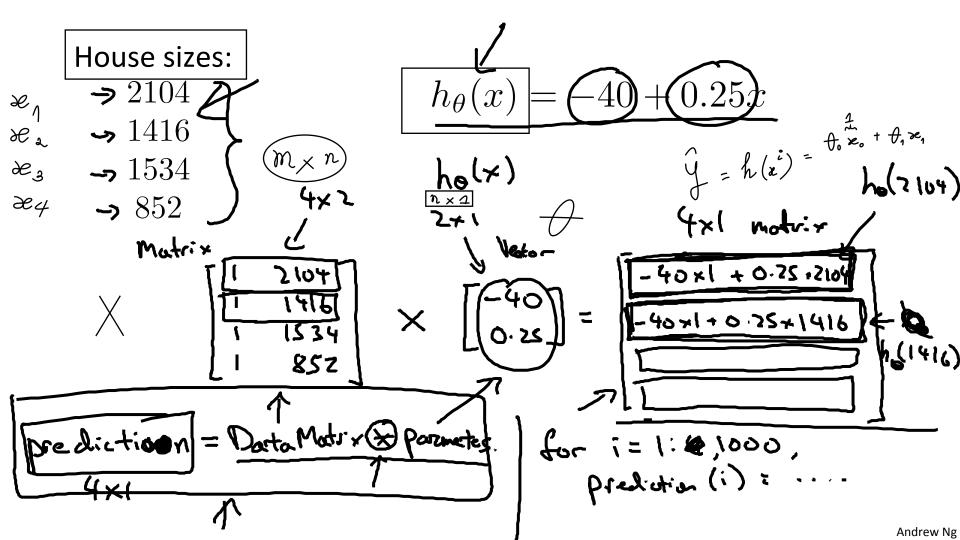




To get y_i , multiply \underline{A} 's i^{th} row with elements of vector x, and add them up.

Example







Linear Algebra review (optional)

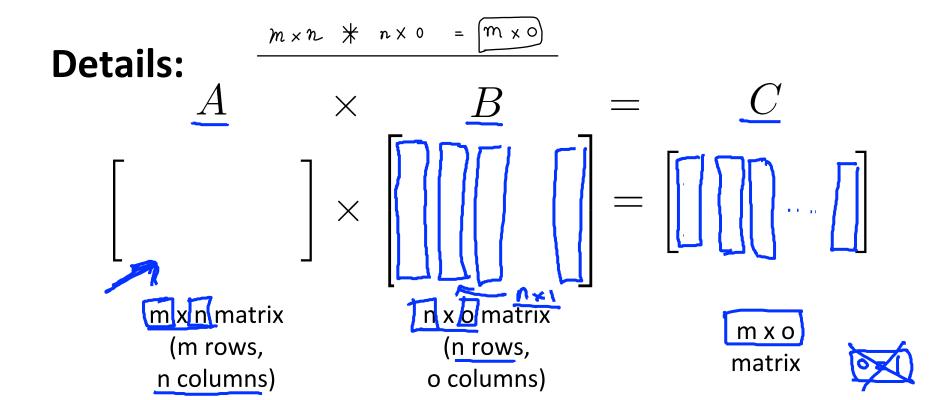
Matrix-matrix multiplication

Example

$$\begin{bmatrix} 1 & 3 & 2 \\ 4 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 3 \\ 0 & 1 \\ 5 & 2 \end{bmatrix} = \begin{bmatrix} 1 & 10 \\ 2 & 14 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 3 & 2 \\ 4 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 \\ 0 \\ 5 \end{bmatrix} = \begin{bmatrix} 1 & 3 \\ 4 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 3 & 2 \\ 4 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 3 \\ 1 \\ 2 \end{bmatrix} = \begin{bmatrix} 10 \\ 14 \end{bmatrix}$$



The $\underline{i^{th}}$ column of the matrix C is obtained by multiplying A with the i^{th} column of B. (for i = 1,2,...,0)

Example

$$\begin{bmatrix} 1 & 3 \\ 2 & 5 \end{bmatrix} \begin{bmatrix} 0 & 1 \\ 3 \end{bmatrix} = \begin{bmatrix} 9 & 7 \\ 15 & 12 \end{bmatrix}$$

$$\begin{bmatrix} 3 & 0 \\ 2 & 5 \end{bmatrix} \begin{bmatrix} 0 \\ 3 \end{bmatrix} = \begin{bmatrix} 1 \times 0 + 3 \times 3 \\ 2 \times 0 + 5 \times 3 \end{bmatrix} = \begin{bmatrix} 9 \\ 15 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 3 \\ 2 & 5 \end{bmatrix} \begin{bmatrix} 1 \\ 2 & 5 \end{bmatrix} = \begin{bmatrix} 1 \times 1 + 3 \times 2 \\ 2 \times 1 + 5 \times 2 \end{bmatrix} = \begin{bmatrix} 7 \\ 12 \end{bmatrix}$$

$$\begin{bmatrix} 5 \times 3 \times 3 \times 2 \\ 5 \times 3 \times 3 \times 3 \end{bmatrix} = \begin{bmatrix} 5 \times 3 \times 2 \times 3 & \text{Errol} \\ 5 \times 3 \times 3 \times 3 & \text{Errol} \\ 5 \times 3 \times 3 \times 3 & \text{Errol} \end{bmatrix}$$

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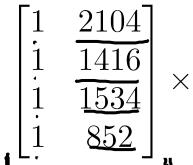
House sizes:

$$h_{\theta}(x) = -40 + 0.25x$$

2.
$$h_{\theta}(x) = 200 + 0.1x$$

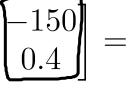
3.
$$h_{\theta}(x) = (150 + 0.4)$$

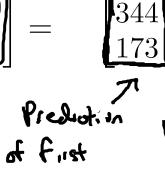
Matrix

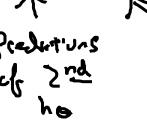


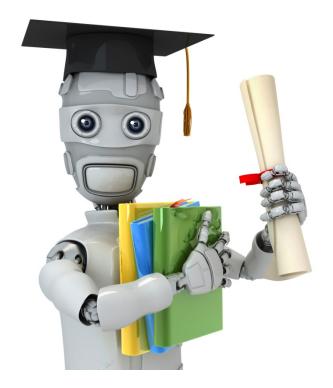












Linear Algebra review (optional)

Matrix multiplication properties

Let A and B be matrices. Then in general, $A \times B \neq B \times A$. (not commutative.)

E.g.
$$\begin{bmatrix} 1 & 1 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} 0 & 0 \\ 2 & 0 \end{bmatrix} = \begin{bmatrix} 2 & 0 \\ 0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 0 \\ 2 & 0 \end{bmatrix} \begin{bmatrix} 1 & 1 \\ 0 & 0 \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ 2 & 2 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 0 \\ 2 & 2 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 0 \\ 2 & 2 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 0 \\ 2 & 2 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 0 \\ 2 & 2 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 0 \\ 2 & 2 \end{bmatrix}$$

$$3 \times 5 \times 2$$
 $3 \times (5 \times 2) = (3 \times 5) \times 2$

$$3 \times 10 = 30 = 15 \times 2$$

$$A \times (0 \times c) \leftarrow \uparrow$$

$$(A \times B) \times C \leftarrow$$

$$A \times B \times C$$
.

Let
$$\underline{D} = B \times C$$
. Compute $A \times D$.

Let $\underline{E} = A \times B$. Compute $E \times C$.

A \times ($\mathbb{C} \times \mathbb{C}$)

Some

Identity Matrix

Denoted \underline{I} (or $I_{n \times n}$).

Examples of identity matrices:

$$\begin{bmatrix}
0 & 0 \\
0 & 1
\end{bmatrix}$$

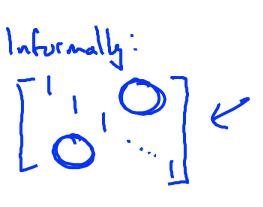
$$\begin{bmatrix}
0 & 0 \\
0 & 0
\end{bmatrix}$$

$$\begin{bmatrix}
0 & 0 \\
0 & 0
\end{bmatrix}$$

$$\begin{bmatrix}
0 & 0 \\
0 & 0
\end{bmatrix}$$

$$3 \times 3$$





For any matrix A, $A \cdot I = I$, A

Note: AB + BA in general AI = BA IA



Linear Algebra review (optional)

Inverse and transpose

Not all numbers have an inverse.

Matrix inverse:

If A is an m x m matrix, and if it has an inverse,

$$A^{-1} = A^{-1}A = I.$$

Eg. [3 4]

[0.4 -0.1]

[-0.05 0.075]

[1.2 x2

Matrices that don't have an inverse are "singular" or "degenerate"

12 > (12-1) = 1

Matrix Transpose

Example:
$$\underline{\underline{A}} = \underbrace{\frac{1}{2} \underbrace{\frac{2}{3} \underbrace{5}}_{2 \times 3} \underbrace{0}_{2}$$

$$\mathbf{B} = \underline{A^T} = \begin{bmatrix} 1 \\ 2 \\ 5 \\ 0 \end{bmatrix} \underbrace{5}_{5}$$

Let A be an $\underline{\mathbf{m}}$ $\underline{\mathbf{x}}$ $\underline{\mathbf{n}}$ matrix, and let $B = A^T$. Then B is an $\underline{\mathbf{n}}$ $\underline{\mathbf{x}}$ $\underline{\mathbf{m}}$ matrix, and

$$B_{\underline{i}\underline{j}} = A_{\underline{j}\underline{i}}.$$

$$B_{12} = A_{21} = 2$$

$$B_{32} = 9$$

$$A_{23} = 9$$