

# QCD AND YANG MILLS LAGRANGIAN

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$$\begin{aligned}
 1 \cdot L_{qcd} = & -\frac{1}{2}\partial_\nu g_\mu^a \partial_\nu g_\mu^a - g_s f^{abc} \partial_\mu g_\nu^a g_\mu^b g_\nu^c - \frac{1}{4}g_s^2 f^{abs} f^{adc} g_\mu^b g_\nu^c g_\mu^d g_\nu^e - \partial_\mu W_\mu^+ \\
 & - \frac{1}{4}g_s^2 f^{abs} f^{adc} g_\mu^b g_\nu^c g_\mu^d g_\nu^e - \partial_\mu W_\mu^+ - M^2 W_\mu^+ W_\mu^- - \frac{1}{2}\partial_\mu Z_\mu^0 \partial_\mu Z_\mu^0 - M^2 W_\mu^+ W_\mu^- - \frac{1}{2}\partial_\mu Z_\mu^0 \partial_\mu Z_\mu^0 \\
 & - M^2 W_\mu^+ W_\mu^- - \frac{1}{2}\partial_\mu Z_\mu^0 \partial_\mu Z_\mu^0 - \frac{1}{2c^2}M^2 Z_\mu^0 Z_\nu^0 - \frac{1}{2}\partial_\mu Z_\mu^0 \partial_\mu Z_\mu^0 - \frac{1}{2c^2}M^2 Z_\mu^0 Z_\nu^0 - \\
 & - \frac{1}{2c^2}M^2 Z_\mu^0 Z_\nu^0 - \frac{1}{2}\partial_\mu A_\nu \partial_\mu A_\nu - igC_w \partial_\nu Z_\mu^0 (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) \\
 & - 2M^2 \alpha_h H^2 - \partial_\mu \phi^+ \partial_\mu \phi^- - \frac{1}{2}\partial_\nu \phi^0 \partial_\mu \phi^0 - \beta_+ \left( \frac{2M^2}{g^2} + \frac{2M}{g}H + \frac{1}{2}(H^2 + \phi^0 \phi^\theta + 2\phi^+ \phi^-) \right) \\
 & - \frac{ig}{2M\sqrt{2}} W_\mu^- ((e^- \lambda U_{k\lambda}^{iep\dagger} \gamma^\mu (1 + \gamma^\mu) v^\lambda + (\lambda_j^k e_+^\dagger \gamma^\mu)) + \frac{g}{2} \frac{m_\lambda^e}{M} [-\phi^+ (v^\lambda (1 - \gamma^5))] \\
 & - X^+ (\partial^2 - M^2) X^+ + X^0 (\partial^2 - \frac{M^2}{c_w^2}) X^0 + Y \partial^2 Y + igc_w W_\mu^+ (\partial_\mu X^0 X^- - \partial_\mu X^0 X^+) \\
 & + igs_w W_\mu^+ (\partial_\mu Y X^- - \partial_\mu Y X^+) + igs_w W_\mu^- (\partial_\mu X^- Y^- - \partial_\mu X^+ X^-) \\
 & + \frac{1}{2}gM[X^+ X^+ H + X^- X^- H + \frac{1}{c^2}X^0 X^0 H] + \frac{1-2c_w^2}{2c_w} igM[X + X^0 \phi^+ - X^- X^0 \phi^-] \\
 & + igMS_w[X^0 X^- \phi^+ - X^0 X^+ \phi^-] + \frac{1}{2}igM[X^+ X^+ \phi^0 - X^- X^- \phi^0]
 \end{aligned}$$

$$2 \cdot Z[[j, \epsilon]] = e^{-ig \int d^4x \frac{\delta}{ig\epsilon^a(x)} f^{abc} \partial_\mu \frac{i\delta}{\delta j_\mu^b(x)} \frac{i\delta}{\delta \epsilon^c(x)}} \cdot e^{-ig \int d^4x f^{abc} \partial_\mu \frac{i\delta}{\delta j_\nu^a(x)} \frac{i\delta}{\delta j_\nu^b(x)}} \cdot e^{-i\frac{g^2}{4} \int d^4x f^{abc} f^{ars} \frac{i\delta}{\delta j_\mu^b} \frac{i\delta}{\delta j_\nu^c(x)} \frac{i\delta}{\delta j^{\nu\mu}} \frac{i\delta}{\delta j^\nu}}$$

$$\Gamma_{\mu\nu}^\lambda = \frac{\partial x^\lambda}{\partial x^\alpha} \cdot \frac{\partial^2 x^\lambda}{\partial x^\mu \partial x^\nu}$$