

Ques Merge 2 sorted arrays

1	3	7	11	13
---	---	---	----	----

$n_1$

2	4	5	6	8	14	15
---	---	---	---	---	----	----

$n_2$

Res

1	2	3	4	5	6	7	8	11	13	14	15
---	---	---	---	---	---	---	---	----	----	----	----

$n_1 + n_2 = n$

Create new array ( $n_1 + n_2$ )

Copy both the array ( $n_1 + n_2$ )  $\Rightarrow O(n)$

Sort the resultant array  $\Rightarrow n \log n$

TC  $\Rightarrow n + n \log(n) \Rightarrow O(n \log n)$

$i$

$\angle =$

1	3	7	11	13
---	---	---	----	----

$j$

2	4	5	6	8	14	15
---	---	---	---	---	----	----

Res

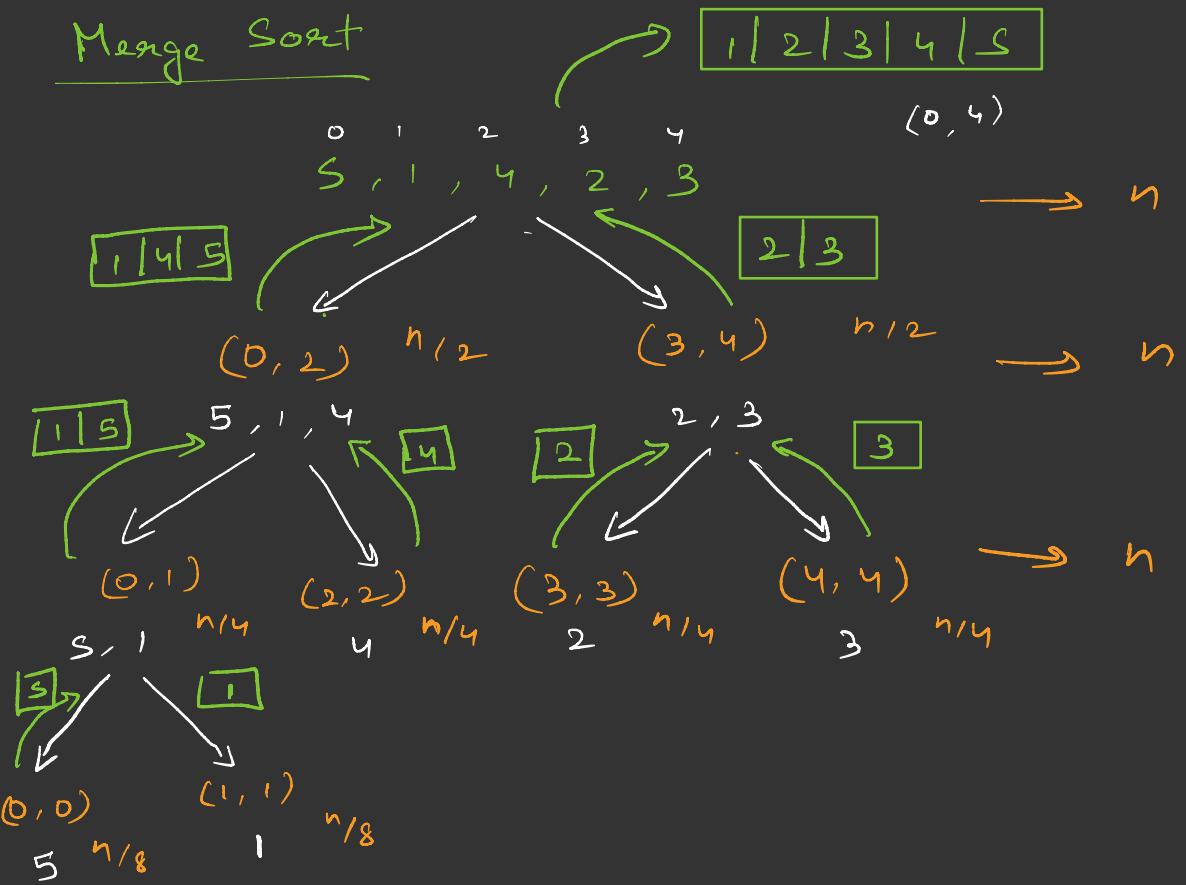
$k$

1	2	3	4	5	6	7	8	11	13	14	15
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TC  $\Rightarrow O(n)$

$n = n_1 + n_2$

# Merge Sort



$$\frac{n}{2^k} = 1$$

$$k \Rightarrow \log_2(n)$$

TC  $\Rightarrow$  no of operations per level  $\times$  no of levels

$$n \times \log_2 n$$

$$TC \Rightarrow O(n \log n)$$



Ques Partition your array

4

5 | 1 | 2 | 4 | 7 | 3 | 6

$\leq$

all elements on left of pivot  
should be smaller or equal to pivot

all elements on right of pivot  
should be greater than pivot

3 | 1 | 2 | 4 | 7 | 5 | 6

pivot = 4

1	2	4	3	7	5	6	
0	1	2	3	4	5	6	

① 0 to  $j-1 \leq \text{pivot}$

②  $j$  to  $i-1 > \text{pivot}$

③  $i$  to end unknown

$j$

$i$

①  
swap  $(i, j)$   
 $i++$   
 $j++$

②  
 $i++$

③

0 1 4 3 0 0 1 3 1 0

0 0 0 0 1 3 4 3 1 1 1

Ques Sort 0, 1

partition odd even

Ques

0 1 3 1 4 2 1 0 <sup>i</sup>

j

$== 0 \quad 0 \rightarrow j-1$

$!= 0 \quad j \rightarrow i-1$

unknown  $i \rightarrow \text{end}$

①

swap(i, j)

i++

j++

②

i++

|



i = 3

j = 2

# 3 way Partitioning

Sort 0, 1, 2

Quers  
Partition

$p=4$

pivot=4

< pivot 0 to  $q-1$  (1)  
 = pivot  $q$  to  $m-1$  (2)  
 Unknown  $m$  to  $r$   
 > pivot  $r+1$  end (3)

		$q$ $r$					
<del>3</del>	<del>1</del>	<del>2</del>	4	<del>6</del>	<del>3</del>	<del>7</del>	<del>5</del>
1	2	3	4	$m$			

1 2

4

\_\_\_\_\_

5

(1)  
 swap( $m, r$ )  
 $m++$   
 $q++$

(2)  
 $m++$

(3)  
 swap( $m, r$ )  
 $r--;$

