

Assignment 4

Tanmay Goyal - AI20BTECH11021

Download all python codes from

<https://github.com/tanmaygoyal258/EE3900-Linear-Systems-and-Signal-processing/blob/main/Assignment4/code.py>

Download all latex codes from

<https://github.com/tanmaygoyal258/EE3900-Linear-Systems-and-Signal-processing/blob/main/Assignment4/main.tex>

On further simplification, we get:

$$\begin{pmatrix} 18 & 12 \end{pmatrix} \mathbf{x} = -11 \quad (2.0.7)$$

$$\begin{pmatrix} 3 & 2 \end{pmatrix} \mathbf{x} = \frac{-11}{6} \quad (2.0.8)$$

Thus, we can say that the moving path of the point \mathbf{x} , and hence, the equidistant line is given by

$$\begin{pmatrix} 3 & 2 \end{pmatrix} \mathbf{x} = \frac{-11}{6} \quad (2.0.9)$$

1 PROBLEM

(Linear_Forms/Q.2.15) Find the equation of the line equidistant from parallel lines

$$\begin{pmatrix} 9 & 6 \end{pmatrix} \mathbf{x} = 7 \quad (1.0.1)$$

$$\begin{pmatrix} 3 & 2 \end{pmatrix} \mathbf{x} = -6 \quad (1.0.2)$$

2 SOLUTION

The distance between a point \mathbf{A} and a line $L = \mathbf{n}^T \mathbf{x} - c$ is given by:

$$\|\mathbf{P} - \mathbf{A}\| = \frac{|\mathbf{n}^T \mathbf{A} - c|}{\|\mathbf{n}\|} \quad (2.0.1)$$

where \mathbf{P} is the foot of perpendicular from \mathbf{A} onto L .

The two given parallel lines can be written as:

$$\begin{pmatrix} 9 & 6 \end{pmatrix} \mathbf{x} - 7 = 0 \quad (2.0.2)$$

$$\begin{pmatrix} 3 & 2 \end{pmatrix} \mathbf{x} + 6 = 0 \quad (2.0.3)$$

Since \mathbf{x} is equidistant from both lines, we can write:

$$\frac{|\begin{pmatrix} 9 & 6 \end{pmatrix} \mathbf{x} - 7|}{\left\| \begin{pmatrix} 9 \\ 6 \end{pmatrix} \right\|} = \frac{|\begin{pmatrix} 3 & 2 \end{pmatrix} \mathbf{x} + 6|}{\left\| \begin{pmatrix} 3 \\ 2 \end{pmatrix} \right\|} \quad (2.0.4)$$

$$\frac{|\begin{pmatrix} 9 & 6 \end{pmatrix} \mathbf{x} - 7|}{3} = |\begin{pmatrix} 3 & 2 \end{pmatrix} \mathbf{x} + 6| \quad (2.0.5)$$

$$|\begin{pmatrix} 9 & 6 \end{pmatrix} \mathbf{x} - 7| = |\begin{pmatrix} 9 & 6 \end{pmatrix} \mathbf{x} + 18| \quad (2.0.6)$$

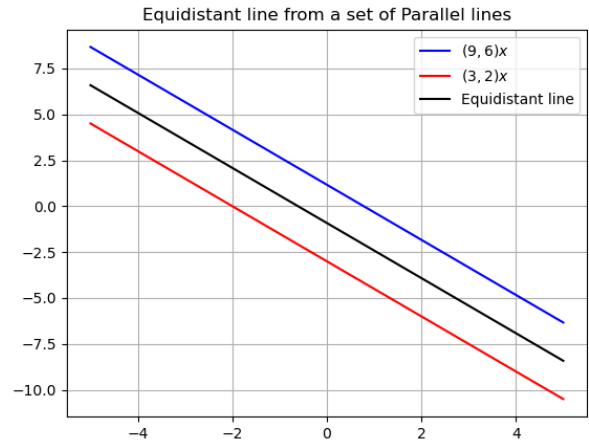


Fig. 0: The equidistant line