

**TEST PAPER OF JEE(MAIN) EXAMINATION – 2019**  
**(Held On Friday 11<sup>th</sup> JANUARY, 2019) TIME : 02 : 30 PM To 05 : 30 PM**  
**PHYSICS**

1. A paramagnetic substance in the form of a cube with sides 1 cm has a magnetic dipole moment of  $20 \times 10^{-6}$  J/T when a magnetic intensity of  $60 \times 10^3$  A/m is applied. Its magnetic susceptibility is :-

- (1)  $2.3 \times 10^{-2}$                       (2)  $3.3 \times 10^{-2}$   
 (3)  $3.3 \times 10^{-4}$                       (4)  $4.3 \times 10^{-2}$

**Ans. (3)**

**Sol.**  $\chi = \frac{I}{H}$

$$I = \frac{\text{Magnetic moment}}{\text{Volume}}$$

$$I = \frac{20 \times 10^{-6}}{10^{-6}} = 20 \text{ N/m}^2$$

$$\chi = \frac{20}{60 \times 10^3} = \frac{1}{3} \times 10^{-3}$$

$$= 0.33 \times 10^{-3} = 3.3 \times 10^{-4}$$

2. A particle of mass  $m$  is moving in a straight line with momentum  $p$ . Starting at time  $t = 0$ , a force  $F = kt$  acts in the same direction on the moving particle during time interval  $T$  so that its momentum changes from  $p$  to  $3p$ . Here  $k$  is a constant. The value of  $T$  is :-

- (1)  $2\sqrt{\frac{p}{k}}$     (2)  $\sqrt{\frac{2p}{k}}$     (3)  $\sqrt{\frac{2k}{p}}$     (4)  $2\sqrt{\frac{k}{p}}$

**Ans. (1)**

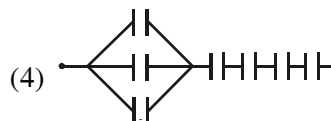
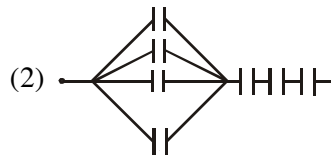
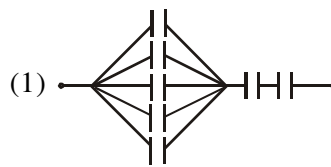
**Sol.**  $\frac{dp}{dt} = F = kt$

$$\int_p^{3p} dP = \int_0^T kt \, dt$$

$$2p = \frac{KT^2}{2}$$

$$T = 2\sqrt{\frac{p}{K}}$$

3. Seven capacitors, each of capacitance  $2 \mu\text{F}$ , are to be connected in a configuration to obtain an effective capacitance of  $\left(\frac{6}{13}\right) \mu\text{F}$ . Which of the combinations, shown in figures below, will achieve the desired value ?



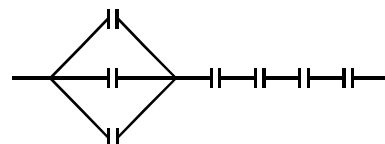
**Ans. (4)**

**Sol.**  $C_{eq} = \frac{6}{13} \mu\text{F}$

Therefore three capacitors must be in parallel to get 6 in

$$\frac{1}{C_{eq}} = \frac{1}{3C} + \frac{1}{C} + \frac{1}{C} + \frac{1}{C} + \frac{1}{C}$$

$$C_{eq} = \frac{3C}{13} = \frac{6}{13} \mu\text{F}$$



4. An electric field of 1000 V/m is applied to an electric dipole at angle of  $45^\circ$ . The value of electric dipole moment is  $10^{-29}$  C.m. What is the potential energy of the electric dipole ?

- (1)  $-9 \times 10^{-20}$  J  
(2)  $-7 \times 10^{-27}$  J  
(3)  $-10 \times 10^{-29}$  J  
(4)  $-20 \times 10^{-18}$  J

**Ans. (2)**

**Sol.**  $U = -\vec{p} \cdot \vec{E}$   
 $= -pE \cos \theta$   
 $= -(10^{-29})(10^3) \cos 45^\circ$   
 $= -0.707 \times 10^{-26}$  J  
 $= -7 \times 10^{-27}$  J.

5. A simple pendulum of length 1 m is oscillating with an angular frequency 10 rad/s. The support of the pendulum starts oscillating up and down with a small angular frequency of 1 rad/s and an amplitude of  $10^{-2}$  m. The relative change in the angular frequency of the pendulum is best given by :-

- (1)  $10^{-3}$  rad/s  
(2)  $10^{-1}$  rad/s  
(3) 1 rad/s  
(4)  $10^{-5}$  rad/s

**Ans. (1)**

**Sol.** Angular frequency of pendulum

$$\omega = \sqrt{\frac{g_{\text{eff}}}{\ell}}$$

$$\therefore \frac{\Delta \omega}{\omega} = \frac{1}{2} \frac{\Delta g_{\text{eff}}}{g_{\text{eff}}}$$

$$\Delta \omega = \frac{1}{2} \frac{\Delta g}{g} \times \omega$$

$[\omega_s = \text{angular frequency of support}]$

$$\Delta \omega = \frac{1}{2} \times \frac{2A\omega_s^2}{100} \times 100$$

$$\Delta \omega = 10^{-3} \text{ rad/sec.}$$

6. Two rods A and B of identical dimensions are at temperature  $30^\circ\text{C}$ . If A is heated upto  $180^\circ\text{C}$  and B upto  $T^\circ\text{C}$ , then the new lengths are the same. If the ratio of the coefficients of linear expansion of A and B is 4 : 3, then the value of T is :-

- (1)  $270^\circ\text{C}$  (2)  $230^\circ\text{C}$   
(3)  $250^\circ\text{C}$  (4)  $200^\circ\text{C}$

**Ans. (2)**

**Sol.**  $\Delta \ell_1 = \Delta \ell_2$

$$\ell \alpha_1 \Delta T_1 = \ell \alpha_2 \Delta T_2$$

$$\frac{\alpha_1}{\alpha_2} = \frac{\Delta T_1}{\Delta T_2}$$

$$\frac{4}{3} = \frac{T - 30}{180 - 30}$$

$$\boxed{T = 230^\circ\text{C}}$$

7. In a double-slit experiment, green light ( $5303 \text{ \AA}$ ) falls on a double slit having a separation of  $19.44 \mu\text{m}$  and a width of  $4.05 \mu\text{m}$ . The number of bright fringes between the first and the second diffraction minima is :-

- (1) 09 (2) 10  
(3) 04 (4) 05

**Ans. (4)**

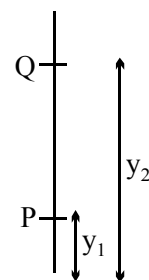
**Sol.** For diffraction

location of 1<sup>st</sup> minime

$$y_1 = \frac{D\lambda}{a} = 0.2469 D\lambda$$

location of 2<sup>nd</sup> minima

$$y_2 = \frac{2D\lambda}{a} = 0.4938 D\lambda$$



Now for interference

Path difference at P.

$$\frac{dy}{D} = 4.8\lambda$$

path difference at Q

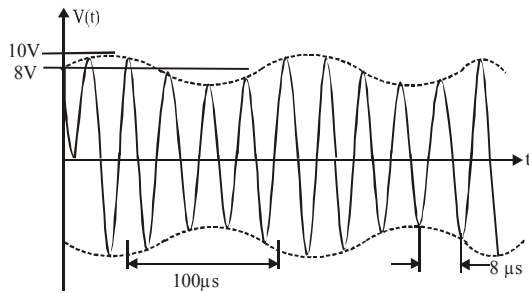
$$\frac{dy}{D} = 9.6\lambda$$

So orders of maxima in between P & Q is

5, 6, 7, 8, 9

So 5 bright fringes all present between P & Q.

8. An amplitude modulated signal is plotted below :-



Which one of the following best describes the above signal ?

- (1)  $(9 + \sin(2.5\pi \times 10^5 t)) \sin(2\pi \times 10^4 t)V$
- (2)  $(9 + \sin(4\pi \times 10^4 t)) \sin(5\pi \times 10^5 t)V$
- (3)  $(1 + 9\sin(2\pi \times 10^4 t)) \sin(2.5\pi \times 10^5 t)V$
- (4)  $(9 + \sin(2\pi \times 10^4 t)) \sin(2.5\pi \times 10^5 t)V$

**Ans. (4)**

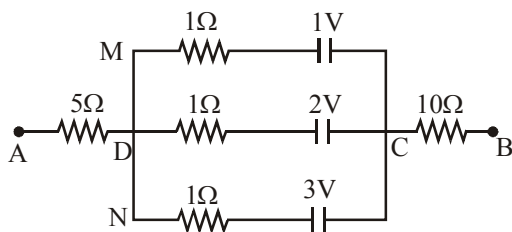
**Sol.** Analysis of graph says

- (1) Amplitude varies as  $8 - 10$  V or  $9 \pm 1$
- (2) Two time period as  
 $100 \mu s$  (signal wave) &  $8 \mu s$  (carrier wave)

$$\text{Hence signal is } \left[ 9 \pm 1 \sin\left(\frac{2\pi t}{T_1}\right) \right] \sin\left(\frac{2\pi t}{T_2}\right)$$

$$= 9 \pm 1 \sin(2\pi \times 10^4 t) \sin 2.5\pi \times 10^5 t$$

9. In the circuit, the potential difference between A and B is :-



- (1) 6 V
- (2) 1 V
- (3) 3 V
- (4) 2 V

**Ans. (4)**

**Sol.** Potential difference across AB will be equal to battery equivalent across CD

$$V_{AB} = V_{CD} = \frac{\frac{E_1}{r_1} + \frac{E_2}{r_2} + \frac{E_3}{r_3}}{\frac{1}{r_1} + \frac{1}{r_2} + \frac{1}{r_3}} = \frac{\frac{1}{1} + \frac{2}{1} + \frac{3}{1}}{\frac{1}{1} + \frac{1}{1} + \frac{1}{1}}$$

$$= \frac{6}{3} = 2V$$

10. A 27 mW laser beam has a cross-sectional area of  $10 \text{ mm}^2$ . The magnitude of the maximum electric field in this electromagnetic wave is given by [Given permittivity of space  $\epsilon_0 = 9 \times 10^{-12} \text{ SI units}$ , Speed of light  $c = 3 \times 10^8 \text{ m/s}$ ]:-

- (1) 1 kV/m
- (2) 2 kV/m
- (3) 1.4 kV/m
- (4) 0.7 kV/m

**Ans. (3)**

**Sol.** Intensity of EM wave is given by

$$I = \frac{\text{Power}}{\text{Area}} = \frac{1}{2} \epsilon_0 E_0^2 C$$

$$= \frac{27 \times 10^{-3}}{10 \times 10^{-6}} = \frac{1}{2} \times 9 \times 10^{-12} \times E^2 \times 3 \times 10^8$$

$$E = \sqrt{2} \times 10^3 \text{ kv/m}$$

$$= 1.4 \text{ kv/m}$$

11. A pendulum is executing simple harmonic motion and its maximum kinetic energy is  $K_1$ . If the length of the pendulum is doubled and it performs simple harmonic motion with the same amplitude as in the first case, its maximum kinetic energy is  $K_2$ . Then :-

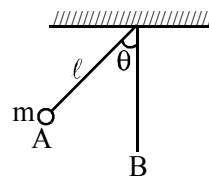
- (1)  $K_2 = \frac{K_1}{4}$
- (2)  $K_2 = \frac{K_1}{2}$
- (3)  $K_2 = 2K_1$
- (4)  $K_2 = K_1$

**Ans. (3)**

**Sol.** Maximum kinetic energy at lowest point B is given by

$$K = mgl(1 - \cos \theta)$$

where  $\theta$  = angular amp.



$$K_1 = mgl(1 - \cos \theta)$$

$$K_2 = mg(2l)(1 - \cos \theta)$$

$$K_2 = 2K_1.$$

12. In a hydrogen like atom, when an electron jumps from the M - shell to the L - shell, the wavelength of emitted radiation is  $\lambda$ . If an electron jumps from N-shell to the L-shell, the wavelength of emitted radiation will be :-

(1)  $\frac{27}{20}\lambda$     (2)  $\frac{16}{25}\lambda$     (3)  $\frac{20}{27}\lambda$     (4)  $\frac{25}{16}\lambda$

**Ans. (3)**

**Sol.** For  $M \rightarrow L$  steel

$$\frac{1}{\lambda} = K \left( \frac{1}{2^2} - \frac{1}{3^2} \right) = \frac{K \times 5}{36}$$

for  $N \rightarrow L$

$$\frac{1}{\lambda'} = K \left( \frac{1}{2^2} - \frac{1}{4^2} \right) = \frac{K \times 3}{16}$$

$$\lambda' = \frac{20}{27}\lambda$$

**13.** If speed (V), acceleration (A) and force (F) are considered as fundamental units, the dimension of Young's modulus will be :-

- (1)  $V^{-2} A^2 F^2$                       (2)  $V^{-4} A^2 F$   
 (3)  $V^{-4} A^{-2} F$                       (4)  $V^{-2} A^2 F^{-2}$

**Ans. (2)**

**Sol.**  $\frac{F}{A} = y \cdot \frac{\Delta \ell}{\ell}$

$$[Y] = \frac{F}{A}$$

Now from dimension

$$F = \frac{ML}{T^2}$$

$$L = \frac{F}{M} \cdot T^2$$

$$L^2 = \frac{F^2}{M^2} \left( \frac{V}{A} \right)^4 \therefore T = \frac{V}{A}$$

$$L^2 = \frac{F^2}{M^2 A^2} \frac{V^4}{A^2} \quad F = MA$$

$$L^2 = \frac{V^4}{A^2}$$

$$[Y] = \frac{[F]}{[A]} = F^1 V^{-4} A^2$$

**14.** A particle moves from the point  $(2.0\hat{i} + 4.0\hat{j})$  m, at  $t = 0$ , with an initial velocity  $(5.0\hat{i} + 4.0\hat{j}) \text{ ms}^{-1}$ . It is acted upon by a constant force which produces a constant acceleration  $(4.0\hat{i} + 4.0\hat{j}) \text{ ms}^{-2}$ . What is the distance of the particle from the origin at time 2 s ?

- (1)  $20\sqrt{2}$  m                      (2)  $10\sqrt{2}$  m  
 (3) 5 m                              (4) 15 m

**Ans. (1)**

**Sol.**  $\vec{S} = (5\hat{i} + 4\hat{j})2 + \frac{1}{2}(4\hat{i} + 4\hat{j})4$

$$= 10\hat{i} + 8\hat{j} + 8\hat{i} + 8\hat{j}$$

$$\vec{r}_f - \vec{r}_i = 18\hat{i} + 16\hat{j}$$

$$\vec{r}_f = 20\hat{i} + 20\hat{j}$$

$$|\vec{r}_f| = 20\sqrt{2}$$

**15.** A monochromatic light is incident at a certain angle on an equilateral triangular prism and suffers minimum deviation. If the refractive index of the material of the prism is  $\sqrt{3}$ , then the angle of incidence is :-

- (1)  $30^\circ$                               (2)  $45^\circ$   
 (3)  $90^\circ$                               (4)  $60^\circ$

**Ans. (4)**

**Sol.**  $i = e$

$$r_1 = r_2 = \frac{A}{2} = 30^\circ$$

by Snell's law

$$1 \times \sin i = \sqrt{3} \times \frac{1}{2} = \frac{\sqrt{3}}{2}$$

$$i = 60$$

**16.** A galvanometer having a resistance of  $20 \Omega$  and 30 divisions on both sides has figure of merit 0.005 ampere/division. The resistance that should be connected in series such that it can be used as a voltmeter upto 15 volt, is :-

- (1)  $80 \Omega$                               (2)  $120 \Omega$   
 (3)  $125 \Omega$                               (4)  $100 \Omega$

**Ans. (1)**

**Sol.**  $R_g = 20\Omega$

$$N_L = N_R = N = 30$$

$$\text{FOM} = \frac{I}{\phi} = 0.005 \text{ A/Div.}$$

$$\text{Current sensitivity} = \text{CS} = \left( \frac{1}{0.005} \right) = \frac{\phi}{I}$$

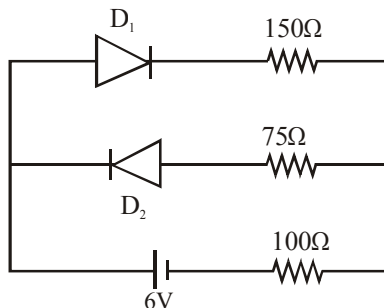
$$I_{g_{\max}} = 0.005 \times 30 \\ = 15 \times 10^{-2} = 0.15$$

$$15 = 0.15 [20 + R]$$

$$100 = 20 + R$$

$$R = 80$$

- 17.** The circuit shown below contains two ideal diodes, each with a forward resistance of  $50\Omega$ . If the battery voltage is 6 V, the current through the  $100\Omega$  resistance (in Amperes) is :-



- (1) 0.027                      (2) 0.020  
(3) 0.030                      (4) 0.036

**Ans. (2)**

**Sol.**  $I = \frac{6}{300} = 0.002$  ( $D_2$  is in reverse bias)

- 18.** When 100 g of a liquid A at  $100^\circ\text{C}$  is added to 50 g of a liquid B at temperature  $75^\circ\text{C}$ , the temperature of the mixture becomes  $90^\circ\text{C}$ . The temperature of the mixture, if 100 g of liquid A at  $100^\circ\text{C}$  is added to 50 g of liquid B at  $50^\circ\text{C}$ , will be :-

- (1)  $80^\circ\text{C}$                       (2)  $60^\circ\text{C}$   
(3)  $70^\circ\text{C}$                       (4)  $85^\circ\text{C}$

**Ans. (1)**

**Sol.**  $100 \times S_A \times [100 - 90] = 50 \times S_B \times (90 - 75)$   
 $2S_A = 1.5 S_B$

$$S_A = \frac{3}{4} S_B$$

$$\text{Now, } 100 \times S_A \times [100 - T] = 50 \times S_B (T - 50)$$

$$2 \times \left( \frac{3}{4} \right) (100 - T) = (T - 50)$$

$$300 - 3T = 2T - 100$$

$$400 = 5T$$

$$T = 80$$

- 19.** The mass and the diameter of a planet are three times the respective values for the Earth. The period of oscillation of a simple pendulum on the Earth is 2s. The period of oscillation of the same pendulum on the planet would be :-

- (1)  $\frac{2}{\sqrt{3}} \text{ s}$                       (2)  $2\sqrt{3} \text{ s}$   
(3)  $\frac{\sqrt{3}}{2} \text{ s}$                       (4)  $\frac{3}{2} \text{ s}$

**Ans. (2)**

**Sol.**  $\because g = \frac{GM}{R^2}$

$$\frac{g_p}{g_e} = \frac{M_e}{M_p} \left( \frac{R_e}{R_p} \right)^2 = 3 \left( \frac{1}{3} \right)^2 = \frac{1}{3}$$

$$\text{Also } T \propto \frac{1}{\sqrt{g}}$$

$$\Rightarrow \frac{T_p}{T_e} = \sqrt{\frac{g_e}{g_p}} = \sqrt{3}$$

$$\Rightarrow T_p = 2\sqrt{3} \text{ s}$$

- 20.** The region between  $y = 0$  and  $y = d$  contains a magnetic field  $\vec{B} = B\hat{z}$ . A particle of mass  $m$  and charge  $q$  enters the region with a velocity

$$\vec{v} = v\hat{i}. \text{ If } d = \frac{mv}{2qB}, \text{ the acceleration of the}$$

charged particle at the point of its emergence at the other side is :-

$$(1) \frac{qvB}{m} \left( \frac{\hat{i} + \hat{j}}{\sqrt{2}} \right)$$

$$(2) \frac{qvB}{m} \left( \frac{1}{2}\hat{i} - \frac{\sqrt{3}}{\sqrt{2}}\hat{j} \right)$$

$$(3) \frac{qvB}{m} \left( \frac{-\hat{j} + \hat{i}}{\sqrt{2}} \right)$$

$$(4) \frac{qvB}{m} \left( \frac{\sqrt{3}}{2}\hat{i} + \frac{1}{2}\hat{j} \right)$$

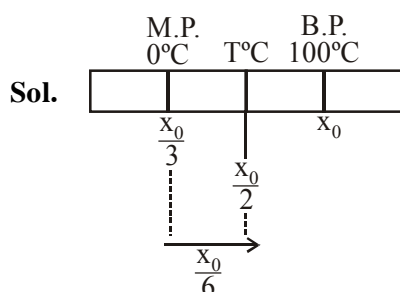
**Ans. (BONUS)**

- 21.** A thermometer graduated according to a linear scale reads a value  $x_0$  when in contact with boiling water, and  $x_0/3$  when in contact with ice.

What is the temperature of an object in  $0^\circ\text{C}$ , if this thermometer in the contact with the object reads  $x_0/2$  ?

- (1) 35 (2) 25  
(3) 60 (4) 40

**Ans. (2)**

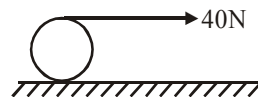


$$\Rightarrow T^\circ\text{C} = \frac{x_0}{6} \quad \& \quad \left( x_0 - \frac{x_0}{3} \right) = (100 - 0^\circ\text{C})$$

$$x_0 = \frac{300}{2}$$

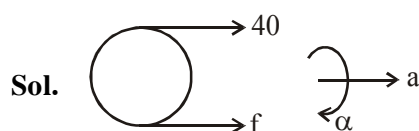
$$\Rightarrow T^\circ\text{C} = \frac{150}{6} = 25^\circ\text{C}$$

- 22.** A string is wound around a hollow cylinder of mass 5 kg and radius 0.5 m. If the string is now pulled with a horizontal force of 40 N, and the cylinder is rolling without slipping on a horizontal surface (see figure), then the angular acceleration of the cylinder will be (Neglect the mass and thickness of the string) :-



- (1)  $12 \text{ rad/s}^2$  (2)  $16 \text{ rad/s}^2$   
(3)  $10 \text{ rad/s}^2$  (4)  $20 \text{ rad/s}^2$

**Ans. (2)**



$$40 + f = m(R\alpha) \dots\dots(i)$$

$$40 \times R - f \times R = mR^2\alpha$$

$$40 - f = mR\alpha \dots\dots(ii)$$

From (i) and (ii)

$$\alpha = \frac{40}{mR} = 16$$

- 23.** In a process, temperature and volume of one mole of an ideal monoatomic gas are varied according to the relation  $VT = K$ , where K is a constant. In this process the temperature of the gas is increased by  $\Delta T$ . The amount of heat absorbed by gas is (R is gas constant) :

- (1)  $\frac{1}{2}R\Delta T$  (2)  $\frac{3}{2}R\Delta T$   
(3)  $\frac{1}{2}KR\Delta T$  (4)  $\frac{2K}{3}\Delta T$

**Ans. (1)**

**Sol.**  $VT = K$

$$\Rightarrow V \left( \frac{PV}{nR} \right) = k \Rightarrow PV^2 = K$$

$$\therefore C = \frac{R}{1-x} + C_v \quad (\text{For polytropic process})$$

$$C = \frac{R}{1-2} + \frac{3R}{2} = \frac{R}{2}$$

$$\therefore \Delta Q = nC \Delta T$$

$$= \frac{R}{2} \times \Delta T$$

- 24.** In a photoelectric experiment, the wavelength of the light incident on a metal is changed from 300 nm to 400 nm. The decrease in the stopping

potential is close to :  $\left( \frac{hc}{e} = 1240 \text{ nm} \cdot \text{V} \right)$

- (1) 0.5 V                                      (2) 1.0 V  
(3) 2.0 V                                      (4) 1.5 V

**Ans. (2)**

**Sol.**  $\frac{hc}{\lambda_1} = \phi + eV_1$  ..... (i)

$\frac{hc}{\lambda_2} = \phi + eV_2$  ..... (ii)

(i) – (ii)

$$hc \left( \frac{1}{\lambda_1} - \frac{1}{\lambda_2} \right) = e(V_1 - V_2)$$

$$\Rightarrow V_1 - V_2 = \frac{hc}{e} \left( \frac{\lambda_2 - \lambda_1}{\lambda_1 \lambda_2} \right)$$

$$= (1240 \text{ nm} \cdot \text{V}) \frac{100 \text{ nm}}{300 \text{ nm} \times 400 \text{ nm}}$$

$$= 1 \text{ V}$$

- 25.** A metal ball of mass 0.1 kg is heated upto 500°C and dropped into a vessel of heat capacity 800 JK<sup>-1</sup> and containing 0.5 kg water. The initial temperature of water and vessel is 30°C. What is the approximate percentage increment in the temperature of the water ? [Specific Heat Capacities of water and metal are, respectively, 4200 Jkg<sup>-1</sup>K<sup>-1</sup> and 400 Jkg<sup>-1</sup>K<sup>-1</sup>]

- (1) 30%                                      (2) 20%  
(3) 25%                                      (4) 15%

**Ans. (2)**

**Sol.**  $0.1 \times 400 \times (500 - T) = 0.5 \times 4200 \times (T - 30) + 800 (T - 30)$

$$\Rightarrow 40(500 - T) = (T - 30) (2100 + 800)$$

$$\Rightarrow 20000 - 40T = 2900 T - 30 \times 2900$$

$$\Rightarrow 20000 + 30 \times 2900 = T(2940)$$

$$T = 30.4^\circ\text{C}$$

$$\frac{\Delta T}{T} \times 100 = \frac{6.4}{30} \times 100$$

$$\approx 20\%$$

- 26.** The magnitude of torque on a particle of mass 1kg is 2.5 Nm about the origin. If the force acting on it is 1 N, and the distance of the particle from the origin is 5m, the angle between the force and the position vector is (in radians) :-

- (1)  $\frac{\pi}{8}$                       (2)  $\frac{\pi}{6}$                       (3)  $\frac{\pi}{4}$                       (4)  $\frac{\pi}{3}$

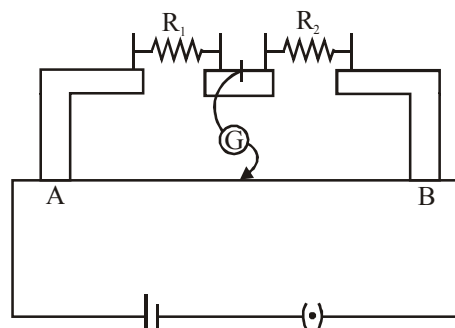
**Ans. (2)**

**Sol.**  $2.5 = 1 \times 5 \sin \theta$

$$\sin \theta = 0.5 = \frac{1}{2}$$

$$\theta = \frac{\pi}{6}$$

- 27.** In the experimental set up of metre bridge shown in the figure, the null point is obtained at a distance of 40 cm from A. If a 10Ω resistor is connected in series with R<sub>1</sub>, the null point shifts by 10 cm. The resistance that should be connected in parallel with (R<sub>1</sub> + 10)Ω such that the null point shifts back to its initial position is



- (1) 40 Ω                      (2) 60 Ω                      (3) 20 Ω                      (4) 30 Ω

**Ans. (2)**

**Sol.**  $\frac{R_1}{R_2} = \frac{2}{3} \dots\dots(i)$

$$\frac{R_1 + 10}{R_2} = 1 \Rightarrow R_1 + 10 = R_2 \dots\dots(ii)$$

$$\frac{2R_2}{3} + 10 = R_2$$

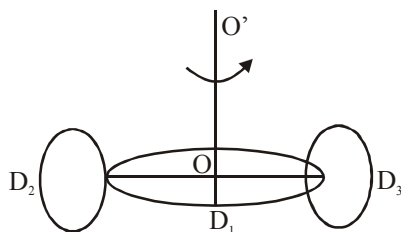
$$10 = \frac{R_2}{3} \Rightarrow R_2 = 30\Omega$$

$$\& R_1 = 20\Omega$$

$$\frac{30 \times R}{30 + R} = \frac{2}{3}$$

$$R = 60\Omega$$

- 28.** A circular disc  $D_1$  of mass  $M$  and radius  $R$  has two identical discs  $D_2$  and  $D_3$  of the same mass  $M$  and radius  $R$  attached rigidly at its opposite ends (see figure). The moment of inertia of the system about the axis  $OO'$ , passing through the centre of  $D_1$ , as shown in the figure, will be:-



- (1)  $3MR^2$  (2)  $\frac{2}{3}MR^2$   
(3)  $MR^2$  (4)  $\frac{4}{5}MR^2$

**Ans. (1)**

**Sol.**  $I = \frac{MR^2}{2} + 2\left(\frac{MR^2}{4} + MR^2\right)$   

$$= \frac{MR^2}{2} + \frac{MR^2}{2} + 2MR^2$$
  

$$= 3MR^2$$

- 29.** A copper wire is wound on a wooden frame, whose shape is that of an equilateral triangle. If the linear dimension of each side of the frame is increased by a factor of 3, keeping the number of turns of the coil per unit length of the frame the same, then the self inductance of the coil :

- (1) Decreases by a factor of  $9\sqrt{3}$   
 (2) Increases by a factor of 3  
 (3) Decreases by a factor of 9  
 (4) Increases by a factor of 27

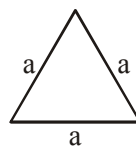
**Ans. (2)**

**Sol.** Total length  $L$  will remain constant

$$L = (3a) N \quad (N = \text{total turns})$$

and length of winding =  $(d) N$

( $d$  = diameter of wire)



$$\text{self inductance} = \mu_0 n^2 A \ell$$

$$= \mu_0 n^2 \left( \frac{\sqrt{3} a^2}{4} \right) dN$$

$$\propto a^2 N \propto a$$

So self inductance will become 3 times

- 30.** A particle of mass  $m$  and charge  $q$  is in an electric and magnetic field given by

$$\vec{E} = 2\hat{i} + 3\hat{j} ; \quad \vec{B} = 4\hat{j} + 6\hat{k}.$$

The charged particle is shifted from the origin to the point  $P(x = 1 ; y = 1)$  along a straight path.

The magnitude of the total work done is :-

- (1)  $(0.35)q$  (2)  $(0.15)q$   
 (3)  $(2.5)q$  (4)  $5q$

**Ans. (4)**

**Sol.**  $\vec{F}_{\text{net}} = q\vec{E} + q(\vec{v} \times \vec{B})$   

$$= (2q\hat{i} + 3q\hat{j}) + q(\vec{v} \times \vec{B})$$

$$W = \vec{F}_{\text{net}} \cdot \vec{S}$$

$$= 2q + 3q$$

$$= 5q$$