FINAL JEE-MAIN EXAMINATION - APRIL, 2024

(Held On Monday 08th April, 2024)

TIME: 3:00 PM to 6:00 PM

MATHEMATICS

SECTION-A

- If the image of the point (-4, 5) in the line 1. x + 2y = 2 lies on the circle $(x + 4)^2 + (y-3)^2 = r^2$, then r is equal lo:
 - (1) 1

- (2)2
- (3)75
- (4) 3

Ans. (2)

Sol. Image of point (-4, 5)

$$\frac{x - x_1}{a} = \frac{y - y_1}{b} = -2\left(\frac{ax_1 + by_1 + c}{a^2 + b^2}\right)$$

Line: x + 2y - 2 = 0

$$\frac{x+4}{1} = \frac{y-5}{2} = -2\left(\frac{-4+10-2}{1^2+2^2}\right)$$
$$= \frac{-8}{5}$$

$$x = -4 - \frac{8}{5} = -\frac{28}{5}$$

$$y = -\frac{16}{5} + 5 = \frac{9}{5}$$

Point lies on circle $(x + 4)^2 + (y - 3)^2 = r^2$

$$\frac{64}{25} + \left(\frac{9}{5} - 3\right)^2 = r^2$$

$$\frac{100}{25} = r^2, \boxed{r=2}$$

- Let $\vec{a} = \hat{i} + 2\hat{i} + 3\hat{k}$, $\vec{b} = 2\hat{i} + 3\hat{i} 5\hat{k}$ and 2. $\vec{c}=3\hat{i}-\hat{j}+\lambda\hat{k}$ be three vectors. Let \vec{r} be a unit vector along $\vec{b} + \vec{c}$. If $\vec{r} \cdot \vec{a} = 3$, then 3λ is equal to:

 - (1)27
- (2)25
- (3)25
- (4) 21

Ans. (2)

TEST PAPER WITH SOLUTION

Sol. $\vec{r} = k(\vec{b} + \vec{c})$

 $\vec{r} \cdot \vec{a} = 3$

 $\vec{r} \cdot \vec{a} = k(\vec{b} \cdot \vec{a} + \vec{c} \cdot \vec{a})$

 $3 = k(2+6-15+3-2+3\lambda)$

 $3 = k(-6 + 3\lambda)$...(1)

 $\vec{r} = k(5\hat{i} + 2\hat{i} - (5 - \lambda)\hat{k})$

 $|\vec{r}| = k\sqrt{25 + 4 + 25 + \lambda^2 - 10\lambda} = 1$...(2)

 $k = \frac{3}{-6+3\lambda} = \frac{1}{-2+\lambda}$ put in (2)

 $4 + \lambda^2 - 4\lambda = 54 + \lambda^2 - 10\lambda$

 $6\lambda = 50$

 $3\lambda = 25$

- If $\alpha \neq a$, $\beta \neq b$, $\gamma \neq c$ and $\begin{vmatrix} \alpha & b & c \\ a & \beta & c \\ a & b & \gamma \end{vmatrix} = 0$, then
 - $\frac{a}{\alpha a} + \frac{b}{\beta b} + \frac{\gamma}{\gamma c}$ is equal to :
 - (1) 2

(2) 3

(3)0

(4) 1

Ans. (3)

Sol. $R_1 \rightarrow R_1 - R_2, R_2 \rightarrow R_2 - R_3$

$$\begin{vmatrix} \alpha - a & b - \beta & 0 \\ 0 & \beta - b & c - \gamma \\ a & b & \gamma \end{vmatrix} = 0$$

 $(\alpha - a) (\gamma(\beta - b) - b(c - \gamma)) - (b - \beta) (-a(c - \gamma)) = 0$

 $\gamma(\alpha - a)(\beta - b) - b(\alpha - a)(c - \gamma) + a(b - \beta)(c - \gamma)$

 $\frac{\gamma}{\gamma - c} + \frac{b}{\beta - b} + \frac{a}{\alpha - a} = 0$

- 4. In an increasing geometric progression of positive terms, the sum of the second and sixth terms is $\frac{70}{3}$ and the product of the third and fifth terms is
 - 49. Then the sum of the 4th, 6th and 8th terms is :-
 - (1)96
- (2)78

- (3)91
- (4) 84

Ans. (3)

Sol.
$$T_2 + T_6 = \frac{70}{3}$$

$$ar + ar^5 = \frac{70}{3}$$

$$T_3 \cdot T_5 = 49$$

$$ar^2 \cdot ar^4 = 49$$

$$a^2r^6 = 49$$

$$ar^3 = +7, \ a = \frac{7}{r^3}$$

$$ar(1+r^4) = \frac{70}{3}$$

$$\frac{7}{r^2}(1+r^4) = \frac{70}{3}, r^2 = t$$

$$\frac{1}{t}(1+t^2) = \frac{10}{3}$$

$$3t^2 - 10t + 3 = 0$$

$$t=3,\frac{1}{3}$$

Increasing G.P. $r^2 = 3$, $r = \sqrt{3}$

$$T_4 + T_6 + T_8$$

$$= ar^3 + ar^5 + ar^7$$

$$= ar^3(1 + r^2 + r^4)$$

$$=7(1+3+9)=91$$

- 5. The number of ways five alphabets can be chosen from the alphabets of the word MATHEMATICS, where the chosen alphabets are not necessarily distinct, is equal to:
 - (1) 175
- (2) 181
- (3) 177
- (4) 179

Ans. (4)

- **Sol.** AA, MM, TT, H, I, C, S, E
 - (1) All distinct

$$^{8}C_{5} \rightarrow 56$$

(2) 2 same, 3 different

$$^{3}C_{1} \times ^{7}C_{3} \rightarrow 105$$

(3) 2 same Ist kind, 2 same 2nd kind, 1 different

$${}^{3}C_{2} \times {}^{6}C_{1} \rightarrow 18$$

$$Total \rightarrow 179$$

6. The sum of all possible values of $\theta \in [-\pi, 2\pi]$, for which $\frac{1 + i\cos\theta}{1 - 2i\cos\theta}$ is purely imaginary, is equal

to

- $(1) 2\pi$
- (2) 3π
- $(3) 5\pi$
- $(4) 4\pi$

Ans. (2)

Sol.
$$Z = \frac{1 + i\cos\theta}{1 - 2i\cos\theta}$$

$$Z = -\overline{Z} \Rightarrow \frac{1 + i\cos\theta}{1 - 2i\cos\theta} = -\left(\frac{\overline{1 + i\cos\theta}}{1 - 2i\cos\theta}\right)$$

$$(1+i\cos\theta)(\overline{1-2i\cos\theta}) = (1-2i\cos\theta)(\overline{1+i\cos\theta})$$

$$(1+i\cos\theta)(1+2i\cos\theta) = -(1-2i\cos\theta)(1-i\cos\theta)$$

$$1 + 3i\cos\theta - 2\cos^2\theta = -(1 - 3i\cos\theta - 2\cos^2\theta)$$

$$2 - 4\cos^2\theta = 0$$

$$\Rightarrow \cos^2\theta = \frac{1}{2} \Rightarrow \theta = -\frac{\pi}{4}, -\frac{3\pi}{4}, \frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}$$

$$sum = 3\pi$$

- 7. If the system of equations $x + 4y z = \lambda$, $7x + 9y + \mu z = -3$, 5x + y + 2z = -1 has infinitely many solutions, then $(2\mu + 3\lambda)$ is equal to:
 - (1) 2

(2) -3

- (3) 3
- (4) -2

Ans. (2)

Sol.
$$\Delta = \begin{vmatrix} 1 & 4 & -1 \\ 7 & 9 & \mu \\ 5 & 1 & 2 \end{vmatrix} = 0$$

$$\Rightarrow$$
 $(18-\mu) - 4(14-5\mu) - (7-45) = 0 \Rightarrow \mu = 0$

$$\Delta = \Delta_x = \Delta_y = \Delta_z = 0$$
 (For infinite solution)

$$\Delta_{x} = \begin{vmatrix} \lambda & 4 & -1 \\ -3 & 9 & \mu \\ -1 & 1 & 2 \end{vmatrix} = 0$$

$$\lambda(18 - \mu) - 4(-6 + \mu) - 1(-3 + 9) = 0$$

$$18\lambda + 24 - 6 = 0 \implies \lambda = -1$$

8. If the shortest distance between the lines

$$\frac{x-\lambda}{2} = \frac{y-4}{3} = \frac{z-3}{4}$$
 and

$$\frac{x-2}{4} = \frac{y-4}{6} = \frac{z-7}{8}$$
 is $\frac{13}{\sqrt{29}}$, then a value

of λ is:

$$(1) - \frac{13}{25}$$

(2)
$$\frac{13}{25}$$

$$(4) - 1$$

Ans. (3)

Shortest dist. =
$$\frac{\left|\overline{b} \times (\overline{a}_2 - \overline{a}_1)\right|}{|b|} = \frac{13}{\sqrt{29}}$$

$$\frac{\left| \left(2\hat{i} + 3\hat{j} + 4\hat{k} \right) \times \left((2 - \lambda)\hat{i} + 4\hat{k} \right) \right|}{\sqrt{29}} = \frac{13}{\sqrt{29}}$$

$$\left| -8\hat{j} - 3(2 - \lambda)\hat{k} + 12\hat{i} + 4(2 - \lambda)\hat{j} \right| = 13$$

$$\left| 12\hat{\mathbf{i}} - 4\lambda\hat{\mathbf{j}} + (3\lambda - 6)\hat{\mathbf{k}} \right| = 13$$

$$144 + 16 \lambda^2 + (3\lambda - 6)^2 = 169$$

$$16\lambda^2 + (3\lambda - 6)^2 = 25 = \lambda \Rightarrow = 1$$

9. If the value of
$$\frac{3\cos 36^\circ + 5\sin 18^\circ}{5\cos 36^\circ - 3\sin 18^\circ}$$
 is $\frac{a\sqrt{5} - b}{c}$,

where a, b, c are natural numbers and gcd(a, c) = 1, then a + b + c is equal to:

Ans. (3)

Sol.
$$\frac{3(\sqrt{5}+1)}{4} + 5(\frac{\sqrt{5}-1}{4}) = \frac{8\sqrt{5}-2}{2\sqrt{5}+8}$$
$$= \frac{4\sqrt{5}-1}{\sqrt{5}+4} \times \frac{\sqrt{5}-4}{\sqrt{5}-4}$$

$$= \frac{20 - 16\sqrt{5} - \sqrt{5} + 4}{-11}$$
$$= \frac{17\sqrt{5} - 24}{11} \implies a = 17, b = 27, c = 11$$

a+b+c=52

0. Let y = y(x) be the solution curve of the differential equation secy $\frac{dy}{dx} + 2x\sin y = x^3\cos y$,

y(1) = 0. Then $y(\sqrt{3})$ is equal to :

$$(1) \frac{\pi}{3}$$

(2)
$$\frac{\pi}{6}$$

(3)
$$\frac{\pi}{4}$$

(4)
$$\frac{\pi}{12}$$

Ans. (3)

Sol. $\sec^2 y \frac{dy}{dx} + 2x\sin y \sec y = x^3 \cos y \sec y$

$$\sec^2 y \frac{dy}{dx} + 2x \tan y = x^3$$

$$tany = t \implies sec^2 y \frac{dy}{dx} = \frac{dt}{dx}$$

$$\frac{dt}{dx} + 2xt = x^3$$
, If $= e^{\int 2x dx} = e^{x^2}$

$$te^{x^2} = \int x^3 \cdot e^{x^2} dx + c$$

$$x^{2} = Z \implies t.e^{Z} = \frac{1}{2} \int e^{Z}.ZdZ = \frac{1}{2} [e^{Z}.Z - e^{Z}] + c$$

$$2 \tan y = (x^2 - 1) + 2ce^{-x^2}$$

$$y(1) = 0 \implies c = 0 \implies y(\sqrt{3}) = \frac{\pi}{4}$$

11. The area of the region in the first quadrant inside the circle $x^2 + y^2 = 8$ and outside the pnrabola $y^2 = 2x$ is equal to:

(1)
$$\frac{\pi}{2} - \frac{1}{3}$$

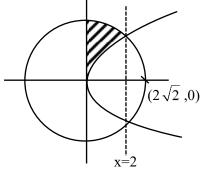
(2)
$$\pi - \frac{2}{3}$$

(3)
$$\frac{\pi}{2} - \frac{2}{3}$$

(4)
$$\pi - \frac{1}{3}$$

Ans. (2)

Sol.



Required area = Ar(circle from 0 to 2) - ar(para from 0 to 2)

$$= \int_{0}^{2} \sqrt{8 - x^{2}} \, dx - \int_{0}^{2} \sqrt{2x} \, dx$$

$$= \left[\frac{x}{2} \sqrt{8 - x^{2}} + \frac{8}{2} \sin^{-1} \frac{x}{2\sqrt{2}} \right]_{0}^{2} - \sqrt{2} \left[\frac{x\sqrt{x}}{3/2} \right]_{0}^{2}$$

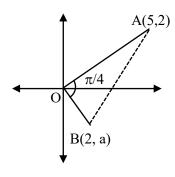
$$= \frac{2}{2} \sqrt{8 - 4} + \frac{8}{2} \sin^{-1} \frac{2}{2\sqrt{2}} - \frac{2\sqrt{2}}{3} (2\sqrt{2} - 0)$$

$$\Rightarrow 2 + 4 \cdot \frac{\pi}{4} - \frac{8}{3} = \pi - \frac{2}{3}$$

12. If the line segment joining the points (5, 2) and (2, a) subtends an angle π/4 at the origin, then the absolute value of the product of all possible values of a is:

Ans. (4)

Sol.



$$m_{OA} = \frac{2}{5}$$

$$m_{OB} = \frac{a}{2}$$

$$\tan\frac{\pi}{4} = \left| \frac{2}{5} - \frac{a}{2} \right|$$

$$1 = \left| \frac{4 - 5a}{10 + 2a} \right|$$

$$4 - 5a = \pm (10 + 2a)$$

$$4 - 5a = 10 + 2a$$

$$4 - 5a = -10 - 2a$$

$$\Rightarrow$$
 7a + 6 = 0

$$3a = 14$$

$$\Rightarrow a = -\frac{6}{7}$$

$$a = +\frac{14}{2}$$

$$-\frac{6}{7} \times \frac{14}{3} = -4$$

13. Let $\vec{a} = 4\hat{i} - \hat{j} + \hat{k}$, $\vec{b} = 11\hat{i} - \hat{j} + \hat{k}$ and \vec{c} be

a vector such that

$$(\vec{a} + \vec{b}) \times \vec{c} = \vec{c} \times (-2\vec{a} + 3\vec{b}).$$

If $(2\vec{a} + 3\vec{b}) \cdot \vec{c} = 1670$, then $|\vec{c}|^2$ is equal to:

Ans. (2)

Sol.
$$(\vec{a} + \vec{b}) \times \vec{c} - \vec{c} \times (-2\vec{a} + 3\vec{b}) = 0$$

$$(\vec{a} + \vec{b}) \times \vec{c} + (-2\vec{a} + 3\vec{b}) \times \vec{c} = 0$$

$$\Rightarrow (\vec{a} + \vec{b}) - 2\vec{a} + 3\vec{b}) \times \vec{c} = 0$$

$$\Rightarrow \vec{c} = \lambda(4\vec{b} - \vec{a})$$

$$\Rightarrow = \lambda \left(44\hat{i} - 4\hat{j} + 4\hat{k} - 4\hat{i} + \hat{j} - \hat{k} \right)$$

$$= \lambda \left(40\hat{i} - 3\hat{j} + 3\hat{k} \right)$$

Now

$$(8\hat{i} - 2\hat{j} + 2\hat{k} + 33\hat{i} - 3\hat{j} + 3\hat{k}) \cdot \lambda(40\hat{i} - 3\hat{j} + 3\hat{k}) = 1670$$

$$\Rightarrow (41\hat{i} - 5\hat{j} + 5\hat{k}).(40\hat{i} - 3\hat{j} + 3\hat{k}) \times \lambda = 1670)$$

$$\Rightarrow$$
 $(1640 + 15 + 15)\lambda = 1670 \Rightarrow \lambda = 1$

so
$$\vec{c} = 40\hat{i} - 3\hat{j} - 3\hat{k}$$

$$\Rightarrow |\vec{c}|^2 = 1600 + 9 + 9 = 1618$$

- If the function $f(x) = 2x^3 9ax^2 + 12a^2x + 1$, a > 014. has a local maximum at $x = \alpha$ and a local minimum $x = \alpha^2$, then α and α^2 are the roots of the equation:
 - (1) $x^2 6x + 8 = 0$ (2) $8x^2 + 6x 8 = 0$
 - (3) $8x^2 6x + 1 = 0$ (4) $x^2 + 6x + 8 = 0$

Ans. (1)

Sol. $f(x) = 6x^2 - 18ax + 12a^2 = 0$

$$\alpha + \alpha^2 = 3a \& \alpha \times \alpha^2 = 2a^2$$

$$(\alpha + \alpha^2)^3 = 27a^3$$

$$\Rightarrow$$
 2a² + 4a⁴ + 3(3a) (2a²) = 27a³

$$\Rightarrow 2 + 4a^2 + 18a = 27a$$

$$\Rightarrow 4a^2 - 9a + 2 = 0$$

$$\Rightarrow 4a^2 - 8a - a + 2 = 0$$

$$\Rightarrow$$
 $(4a-1)(a-2)=0 \Rightarrow a=2$

so
$$6x^2 - 36x + 48 = 0$$

$$\Rightarrow x^2 - 6x + 8 = 0 \tag{1}$$

If we take $a = \frac{1}{4}$ then $\alpha = \frac{1}{2}$ which is not possible

- 15. There are three bags X, Y and Z. Bag X contains 5 one-rupee coins and 4 five-rupee coins; Bag Y contains 4 one-rupee coins and 5 five-rupee coins and Bag Z contains 3 one-rupee coins and 6 five-rupee coins. A bag is selected at random and a coin drawn from it at random is found to be a one-rupee coin. Then the probability, that it came from bag Y, is:
 - $(1) \frac{1}{3}$

- (2) $\frac{1}{2}$
- $(3) \frac{1}{4}$
- $(4) \frac{5}{12}$

Ans. (1)

Sol.

5 one & 4 five 4 one & 5 five 3 one & 6 five

$$P = \frac{4/9}{5/9 + 4/9 + 3/9} = \frac{4}{12} = \frac{1}{3}$$

Let $\int_{-1}^{\log_e 4} \frac{dx}{\sqrt{e^x - 1}} = \frac{\pi}{6}$. Then e^{α} and $e^{-\alpha}$ are the **16.**

roots of the equation:

(1)
$$2x^2 - 5x + 2 = 0$$
 (2) $x^2 - 2x - 8 = 0$

(2)
$$x^2 - 2x - 8 = 0$$

(3)
$$2x^2 - 5x - 2 = 0$$
 (4) $x^2 + 2x - 8 = 0$

(4)
$$x^2 + 2x - 8 = 0$$

Ans. (1)

$$\textbf{Sol.} \quad \int\limits_{\alpha}^{\log_e 4} \frac{dx}{\sqrt{e^x - 1}} = \frac{\pi}{6}$$

Let
$$e^x - 1 = t^2$$

$$e^x dx = 2t dt$$

$$= \int \frac{2dt}{t^2 + 1}$$

$$= 2 \tan^{-1} t$$

$$= 2 \tan^{-1} \left(\sqrt{e^x - 1} \right) \Big|_{\alpha}^{\log_e^4}$$

$$= 2 \Big[\tan^{-1} \sqrt{3} - \tan^{-1} \sqrt{e^{\alpha} - 1} \Big] = \frac{\pi}{6}$$

$$=\frac{\pi}{3}-\tan^{-1}\sqrt{e^{\alpha}-1}=\frac{\pi}{12}$$

$$\Rightarrow \tan^{-1} \sqrt{e^{\alpha} - 1} = \frac{\pi}{4}$$

$$e^{\alpha} = 2$$
 $e^{-\alpha} = \frac{1}{2}$

$$x^2 - \left(2 + \frac{1}{2}\right)x + 1 = 0$$

$$2x^2 - 5x + 2 = 0$$

17. Let
$$f(x) = \begin{cases} -a & \text{if } -a \le x \le 0 \\ x + a & \text{if } 0 < x \le a \end{cases}$$

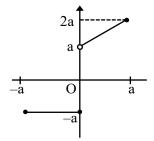
where a > 0 and g(x) = (f|x|) - |f(x)|/2.

Then the function $g: [-a, a] \rightarrow [-a, a]$ is

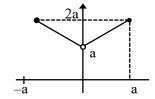
- (1) neither one-one nor onto.
- (2) both one-one and onto.
- (3) one-one.
- (4) onto

Ans. (1)

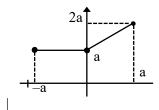
Sol. y = f(x)



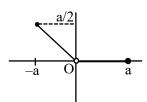
$$y = f|x|$$



$$y = |f(x)|$$



$$g(x) = \frac{f(|x|) - |f(x)|}{2}$$



- 18. Let $A=\{2,3,6,8,9,11\}$ and $B=\{1,4,5,10,15\}$ Let R be a relation on $A\times B$ define by (a,b)R(c,d)if and only if 3ad-7bc is an even integer. Then the relation R is
 - (1) reflexive but not symmetric.
 - (2) transitive but not symmetric.
 - (3) reflexive and symmetric but not transitive.
 - (4) an equivalence relation.

Ans. (3)

Sol. $A = \{2, 3, 6, 8, 9, 11\}$ (a, b)R (c, d) $B = \{1, 4, 5, 10, 15\}$ 3ad – 7bc Reflexive: (a, b) R(a, b) \Rightarrow 3ab – 7ba = – 4ab always even so it is reflexive.

Symmetric : If 3ad - 7bc = Even

Case-I : odd odd Case-II : even even

 $(c, d) R(a, b) \Rightarrow 3bc - 3ab$

Case-II: odd odd Case-II: even even

so symmetric relation

Transitive:

Set (3, 4)R (6, 4) Satisfy relation

Set (6, 4)R(3, 1) Satisfy relation

but (3, 4) R(3, 1) does not satisfy relation so not transitive.

19. For a, b > 0, let

$$f(x) = \begin{cases} \frac{\tan((a+1)x) + b \tan x}{x}, & x < 0 \\ \frac{3}{\sqrt{ax + b^2 x^2} - \sqrt{ax}}, & x > 0 \end{cases}$$

be a continuous function at x = 0. Then $\frac{b}{a}$ is equal

to

(1) 5

(2)4

(3) 8

(4) 6

Ans. (4)

Sol. $\lim_{x\to 0} f(x) = f(0) = 3$

$$\lim_{x \to 0^+} \frac{\sqrt{ax + b^2x^2} - \sqrt{ax}}{b\sqrt{a} \ x\sqrt{x}} = 3$$

$$\lim_{x \to 0^+} \frac{ax + b^2 x^2 - ax}{b \sqrt{a} \, x^{3/2} \left(\sqrt{ax + b^2 x^2} + \sqrt{ax} \right)}$$

$$\lim_{x \to 0^+} \frac{b^2}{b\sqrt{a}\left(\sqrt{a+b^2x} + \sqrt{a}\right)}$$

$$\frac{b}{\sqrt{a}.2\sqrt{a}} \Rightarrow \frac{b}{2a} = 3 \Rightarrow \frac{b}{a} = 6$$

20. If the term independent of x in the expansion of

$$\left(\sqrt{ax^2 + \frac{1}{2x^3}}\right)^{10}$$
 is 105, then a^2 is equal to :

(1)4

(2)9

(3)6

(4)2

Ans. (1)

Sol.
$$\left(\sqrt{a}x^2 + \frac{1}{2x^3}\right)^{10}$$

General term =
$${}^{10}C_r \left(\sqrt{a}x^2\right)^{10-r} \left(\frac{1}{2x^3}\right)^r$$

$$20 - 2r - 3r = 0$$

$$r = 4$$

10
C₄a³. $\frac{1}{16}$ = 105

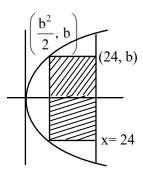
$$a^3 = 8$$

$$a^2 = 4$$

SECTION-B

Let A be the region enclosed by the parabola 21. $y^2 = 2x$ and the line x = 24. Then the maximum area of the rectangle inscribed in the region A is

Sol.



$$A = 2\left(24 - \frac{b^2}{2}\right).b$$

$$\frac{dA}{db} = 0$$
 \Rightarrow $b = 4$

$$A = 2(24 - 8)4$$

$$= 128$$

22. If
$$\alpha = \lim_{x \to 0^+} \left(\frac{e^{\sqrt{\tan x}} - e^{\sqrt{x}}}{\sqrt{\tan x} - \sqrt{x}} \right)$$
 and

 $\beta = \lim_{x \to 0} (1 + \sin x)^{\frac{1}{2} \cot x}$ are the roots of the quadratic equation $ax^2 + bx - \sqrt{e} = 0$, then 12

log_e(a + b) is equal to _____

Ans. (6)

Sol.
$$\alpha = \lim_{x \to 0^+} e^{\sqrt{x}} \frac{\left(e^{\sqrt{\tan x} - \sqrt{x}} - 1\right)}{\sqrt{\tan x} - \sqrt{x}}$$

$$\beta = \lim_{x \to 0} (1 + \sin x)^{\frac{1}{2}\cot x}$$
$$= e^{1/2}$$

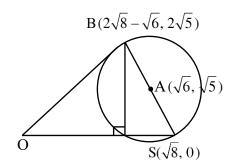
$$x^{2} - (1 + \sqrt{e}) + \sqrt{e} = 0$$
$$ax^{2} + bx - \sqrt{e} = 0$$

$$a = -1, b = \sqrt{e} + 1$$

$$12 \ \ell n(a+b) = 12 \times \frac{1}{2} = 6$$

Let S be the focus of the hyperbola $\frac{x^2}{3} - \frac{y^2}{5} = 1$, 23. on the positive x-axis. Let C be the circle with its centre at $A(\sqrt{6}, \sqrt{5})$ and passing through the point S. if O is the origin and SAB is a diameter of C then the square of the area of the triangle OSB is equal to -

Sol.

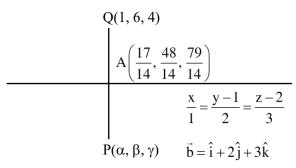


Area =
$$\frac{1}{2}$$
 (OS) h = $\frac{1}{2}\sqrt{8} \ 2\sqrt{5} = \sqrt{40}$

24. Let $P(\alpha, \beta, \gamma)$ be the image of the point Q(1, 6, 4) in the line $\frac{x}{1} = \frac{y-1}{2} = \frac{z-2}{3}$. Then $2\alpha + \beta + \gamma$ is equal to ______.

Ans. (11)

Sol.



$$\begin{aligned} & \underbrace{A(t, 2t+1, 3t+2)} \\ & \overline{QA} = (t-1)\hat{i} + (2t-5)\hat{j} + (3t-2)\hat{k} \\ & \overline{QA} \cdot \vec{b} = 0 \\ & (t-1) + 2(2t-5) + 3(3t-2) = 0 \\ & 14t = 17 \\ & \alpha = \frac{20}{14} \qquad \beta = \frac{12}{14} \qquad \gamma = \frac{102}{14} \\ & 2\alpha + \beta + \gamma = \frac{154}{14} = 11 \end{aligned}$$

25. An arithmetic progression is written in the following way

The sum of all the terms of the 10th row is ______
Ans. (1505)

Sol. 2, 5, 11, 20,

$$General\ term = \frac{3n^2 - 3n + 4}{2}$$

$$T_{10} = \frac{3(100) - 3(10) + 4}{2}$$

= 137

10 terms with c.d. = 3

$$sum = \frac{10}{2} (2(137) + 9(3))$$
$$= 1505$$

26. The number of distinct real roots of the equation |x + 1| |x + 3| - 4 |x + 2| + 5 = 0, is _____.

Ans. (2)

ol. |x + 1| |x + 3| - 4|x + 2| + 5 = 0

case-1

$$x \le -3$$

$$(x + 1) (x + 3) + 4(x + 2) + 5 = 0$$

$$x^2 + 4x + 3 + 4x + 8 + 5 = 0$$

$$x^2 + 8x + 16 = 0$$

$$(x+4)^2=0$$

$$x = -4$$

case-2

$$-3 \le x \le -2$$

$$-x^2 - 4x - 3 + 4x + 8 + 5 = 0$$

$$-x^2 + 10 = 0$$

$$x = \pm \sqrt{10}$$

case-3

$$-2 \le x \le -1$$

$$-x^2 - 4x - 3 - 4x - 8 + 5 = 0$$

$$-x^2 - 8x - 6 = 0$$

$$x^2 + 8x + 6 = 0$$

$$x = \frac{-8 \pm 2\sqrt{10}}{2} = -4 \pm \sqrt{10}$$

case-4

$$x \ge -1$$

$$x^2 + 4x + 3 - 4x - 8 + 5 = 0$$

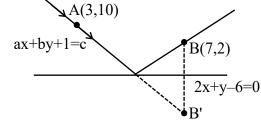
$$x^2 = 0$$

$$\mathbf{x} = \mathbf{0}$$

No. of solution = 2

27. Let a ray of light passing through the point (3, 10) reflects on the line 2x + y = 6 and the reflected ray passes through the point (7, 2). If the equation of the incident ray is ax + by + 1 = 0, then $a^2 + b^2 + 3ab$ is equal to .

Sol.



For B'
$$\frac{x-7}{2} = \frac{y-2}{1} = -2\left(\frac{14+2-6}{5}\right)$$
$$\frac{x-7}{2} = \frac{y-2}{1} = -4$$
$$x = -1 \quad y = -2 \quad B'(-1, -2)$$

incident ray AB'

$$M_{AB'} = 3$$

$$y + 2 = 3(x + 1)$$

$$3x - y + 1 = 0$$

$$a = 3 \ b = -1$$

$$a^2 + b^2 + 3ab = 9 + 1 - 9 = 1$$

28. Let a, b, $c \in N$ and a < b < c. Let the mean, the mean deviation about the mean and the variance of the 5 observations 9, 25, a, b, c be 18, 4 and $\frac{136}{5}$, respectively. Then 2a + b - c is equal to

Ans. (33)

Sol.
$$a, b, c \in N$$

$$\overline{x} = mean = \frac{9 + 25 + a + b + c}{5} = 18$$

$$a + b + c = 56$$

Mean deviation =
$$\frac{\sum |x_i - \overline{x}|}{n} = 4$$

$$= 9 + 7 + |18 - a| + |18 - b| + |18 - c| = 20$$

$$= |18 - a| + |18 - b| + |18 - c| = 4$$

Variance =
$$\frac{\sum |x_i - \overline{x}|^2}{n} = \frac{136}{5}$$

$$= 81 + 49 + |18 - a|^2 + |18 - b|^2 + |18 - c|^2 = 136$$

$$= (18 - a)^2 + (18 - b)^2 + (18 - c)^2 = 6$$

Possible values $(18-a)^2 = 1$, $(18-b)^2 = 1$ $(18-c)^2 = 4$ a < b < c

so

a + b + c = 56

$$2a + b - c$$
 $34 = 19 - 20 = 33$

29. Lei $\alpha |x| = |y|e^{xy-\beta}$, α , $\beta \in N$ be the solution of the differential equation xdy - ydx + xy(xdy+ydx) = 0, y(1) = 2. Then $\alpha + \beta$ is equal to _

Ans. (4)

Sol.
$$a|x| = |y| e^{yx-\beta}$$
, $a, b \in N$
 $xdy - ydx + xy(xdy + ydx) = 0$

$$\frac{\mathrm{d}y}{y} - \frac{\mathrm{d}x}{x} + (x\mathrm{d}y + y\mathrm{d}x) = 0$$

$$\ell n|\mathbf{y}| - \ell n|\mathbf{x}| + \mathbf{x}\mathbf{y} = \mathbf{c}$$

$$y(1) = 2$$

$$\ell n|2| - 0 + 2 = c$$

$$c = 2 + \ell n2$$

$$\ell n|y| - \ell n|x| + xy = 2 + \ell n2$$

$$\ell n|x| = \ell n \left| \frac{y}{2} \right| - 2 + xy$$

$$|\mathbf{x}| = \left| \frac{\mathbf{y}}{2} \right| e^{\mathbf{x}\mathbf{y} - 2}$$

$$2|x| = |y|e^{xy-2}$$

$$\alpha = 2$$
 $\beta = 2$ $\alpha + \beta = 4$

30. If
$$\int \frac{1}{\sqrt[5]{(x-1)^4 (x+3)^6}} dx = A \left(\frac{\alpha x - 1}{\beta x + 3} \right)^B + C$$
,

where C is the constant of integration, then the value of $\alpha + \beta + 20AB$ is

Ans. (7)

Sol.
$$\int \frac{1}{\sqrt[5]{(x-1)^4 (x+3)^6}} dx = A \left(\frac{\alpha x - 1}{\beta x + 3} \right)^B + C$$

$$I = \int \frac{1}{(x-1)^{4/5} (x+3)^{6/5}} dx$$

$$I = \int \frac{1}{\left(\frac{x-1}{x+3}\right)^{4/5} (x+3)^2} dx$$

$$\left(\frac{x-1}{x+3}\right) = t \quad \Rightarrow \frac{4}{(x+3)^2} dx = dt \qquad t^{-4/5+1}$$

$$I = \frac{1}{4} \int \frac{1}{t^{4/5}} dt = \frac{1}{4} \frac{t^{1/5}}{1/5} + c$$

$$I = \frac{5}{4} \left(\frac{x-1}{x+3} \right)^{1/5} + C$$

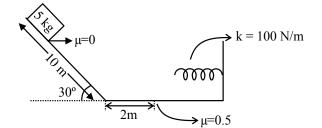
$$A = \frac{5}{4} \qquad \alpha = \beta = 1 \qquad B = \frac{1}{5}$$

$$\alpha + \beta + 20AB = 2 + 20 \times \frac{5}{4} \times \frac{1}{5} = 7$$

PHYSICS

SECTION-A

31.



A block is simply released from the top of an inclined plane as shown in the figure above. The maximum compression in the spring when the block hits the spring is:

- (1) $\sqrt{6}$ m
- (2) 2 m
- (3) 1 m
- (4) $\sqrt{5}$ m

Ans. (2)

Sol.
$$W_g + W_{Fr} + W_s = \Delta KE$$

$$5 \times 10 \times 5 - 0.5 \times 5 \times 10 \times x - \frac{1}{2} Kx^2 = 0 - 0$$

$$250 = 25 x + 50 x^2$$

$$2x^2 + x - 10 = 0$$

$$x = 2$$

32. In a hypothetical fission reaction

$$_{92}X^{236} \rightarrow _{56}Y^{141} + _{36}Z^{92} + 3R$$

The identity of emitted particles (R) is:

- (1) Proton
- (2) Electron
- (3) Neutron
- (4) γ -radiations

Ans. (3)

Sol.
$$Z$$
 in LHS = 92

$$Z \text{ in RHS} = 56 + 36 = 92$$

A in LHS
$$= 236$$

A in RHS =
$$141 + 92 = 233$$

So 3 neutrons are released.

TEST PAPER WITH SOLUTION

33. If \in_0 is the permittivity of free space and E is the electric field, then $\in_0 E^2$ has the dimensions:

- (1) $[M^0 L^{-2} T A]$
- (2) $[M L^{-1} T^{-2}]$
- (3) $[M^{-1} L^{-3} T^4 A^2]$
- (4) $[M L^2 T^{-2}]$

Ans. (2)

Sol.
$$E = \frac{KQ}{R^2}$$

$$E = \frac{Q}{4\pi\epsilon_{o}R^{2}}$$

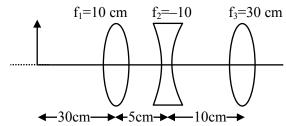
$$\varepsilon_{\rm o} = \frac{\rm Q}{4\pi {\rm R}^2 {\rm E}}$$

Now,
$$\varepsilon_0 E^2 = \frac{Q}{4\pi R^2 E} . E^2 = \frac{Q}{4\pi R^2} . E$$

$$[\epsilon_o E^2] = \left[\frac{QE}{R^2}\right] = \frac{[Q][E]}{[R^2]} = \frac{[Q]}{[R^2]} \frac{[W]}{[Q][R]}$$

$$=\frac{[W]}{[R^3]}=\frac{ML^2T^{-2}}{L^3}\,=\,ML^{-1}T^{-2}$$

34. The position of the image formed by the combination of lenses is:



- (1) 30 cm (right of third lens)
- (2) 15 cm (left of second lens)
- (3) 30 cm (left of third lens)
- (4) 15 cm (right of second lens)

Ans. (1)

Sol. For lens 1:
$$f_1 = 10$$
, $u = -30$, $v = ?$

$$v = \frac{uf}{u+f} = \frac{-30 \times 10}{-30 + 10} = 15$$

For lens 2: $f_1 = -10$, u = 10, v = ?

$$v = \frac{uf}{u+f} = \frac{10 \times -10}{10 - 10} = \infty$$

For lens 3: f = 30, $u = -\infty$, v = ?So v will be 30.

- 35. A plane progressive wave is given by $y = 2 \cos 2\pi (330 t x)$ m. The frequency of the wave is:
 - (1) 165 Hz
- (2) 330 Hz
- (3) 660 Hz
- (4) 340 Hz

Ans. (2)

Sol.
$$y = 2 \cos 2\pi (330 t - x) m$$

$$y = A\cos(\omega t - kx)$$

by comparing $\omega = 2\pi \times 330$

$$2\pi f = 2\pi \times 330$$

$$f = 330$$

- 36. A thin circular disc of mass M and radius R is rotating in a horizontal plane about an axis passing through its centre and perpendicular to its plane with angular velocity ω . If another disc of same dimensions but of mass $\frac{M}{2}$ is placed gently on the first disc co-axially, then the new angular velocity of the system is :
 - $(1) \frac{4}{5} \omega$
- $(2) \frac{5}{4} \omega$
- $(3) \frac{2}{3}\omega$
- $(4) \frac{3}{2}\omega$

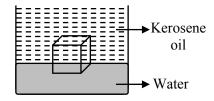
Ans. (3)

Sol.
$$I_1\omega = I_2\omega_2$$

$$\frac{MR^2}{2}\omega = \frac{3}{2}\left(\frac{MR^2}{2}\right)\omega_2$$

$$\omega_2 = \frac{2}{3} \omega$$

37. A cube of ice floats partly in water and partly in kerosene oil. The radio of volume of ice immersed in water to that in kerosene oil (specific gravity of Kerosene oil = 0.8, specific gravity of ice = 0.9)



- (1)8:9
- (2)5:4
- (3)9:10
- (4) 1:1

Ans. (4)

- **Sol.** $v_1 = \text{volume immersed in water.}$
 - v_2 = volume immersed in oil.

$$v_1 \rho_w g + v_2 \rho_0 g = (v_1 + v_2) \rho_c g$$

$$v_1 + \frac{v_2 \rho_o}{\rho_w} = (v_1 + v_2) \frac{\rho_c}{\rho_w}$$

$$= v_1 + 0.8 v_2 = 0.9 v_1 + 0.9 v_2$$

$$= 0.1 v_1 = 0.1 v_2$$

$$v_1 : v_2 = 1 : 1$$

38. Given below are two statements:

Statement (I): The mean free path of gas molecules is inversely proportional to square of molecular diameter.

Statement (II): Average kinetic energy of gas molecules is directly proportional to absolute temperature of gas.

In the light of the above statements, choose the correct answer from the option given below:

- (1) **Statement I** is false but **Statement II** is true.
- (2) **Statement I** is true but **Statement II** is false.
- (3) Both Statement I and Statement II are false
- (4) Both **Statement I** and **Statement II** are true.

Ans. (4)

Sol.
$$\lambda = \frac{RT}{\sqrt{2}\pi d^2 N_{\Delta} P}$$

$$KE = \frac{f}{2}nRT$$

- **39.** Two satellite A and B go round a planet in circular orbits having radii 4 R and R respectively. If the speed of A is 3v, the speed of B will be:
 - $(1) \frac{4}{3}v$
- (2) 3*v*
- (3) 6v
- (4) 12v

Ans. (3)

Sol.
$$\mathbf{v} = \sqrt{\frac{GM}{R}}$$

$$\frac{v_A}{v_B} = \sqrt{\frac{R_B}{R_A}} = \sqrt{\frac{R}{4R}} = \frac{1}{2}$$

$$v_B = 2v_A = 6v$$

- 40. A long straight wire of radius a carries a steady current I. The current is uniformly distributed across its cross section. The ratio of the magnetic field at $\frac{a}{2}$ and 2a from axis of the wire is:
 - (1)1:4
- (3)1:1
- (4) 3:4

Ans. (3)

- $B_1 2\pi \frac{a}{2} = \mu_0 \frac{1}{4}$ Sol.
 - $B_1 = \frac{\mu_o I}{4\pi a}$
 - $B_2 2\pi 2a = \mu_a I$
 - $B_2 = \frac{\mu_0 I}{4\pi a}$
- 41. The angle of projection for a projectile to have same horizontal range and maximum height is:
 - $(1) \tan^{-1} (2)$
- $(2) \tan^{-1} (4)$
- (3) $\tan^{-1} \left(\frac{1}{4} \right)$ (4) $\tan^{-1} \left(\frac{1}{2} \right)$

Ans. (2)

- **Sol.** $\frac{u^2 \sin 2\theta}{g} = \frac{u^2 \sin^2 \theta}{2g}$
 - $4\sin\theta\cos\theta = \sin^2\theta$
 - $4 = \tan \theta$
- 42. Water boils in an electric kettle in 20 minutes after being switched on. Using the same main supply, the length of the heating element should be to times of its initial length if the water is to be boiled in 15 minutes.
 - (1) increased, $\frac{3}{4}$
- (2) increased, $\frac{4}{3}$
- (3) decreased, $\frac{3}{4}$ (4) decreased, $\frac{4}{3}$

Ans. (3)

- **Sol.** $P = \frac{V^2}{R}, R = \frac{\rho \ell}{\Delta}$
 - $\mathbf{P} \propto \frac{1}{a}$
 - $\frac{P_1}{P_2} = \frac{t_2}{t_1} = \frac{15}{20} = \frac{\ell_2}{\ell_1}$
 - $\ell_2 = \frac{3}{4} \ell_1$

- A capacitor has air as dielectric medium and two 43. conducting plates of area 12 cm² and they are 0.6 cm apart. When a slab of dielectric having area 12 cm² and 0.6 cm thickness is inserted between the plates, one of the conducting plates has to be moved by 0.2 cm to keep the capacitance same as in previous case. The dielectric constant of the slab is: (Given $\epsilon_0 = 8.834 \times 10^{-12} \text{ F/m}$)
 - (1) 1.50
- (2) 1.33
- (3) 0.66
- (4) 1

Ans. (1)

Sol. $\frac{A\varepsilon_o}{d} = \frac{A\varepsilon_o}{\left(0.2 + \frac{d}{k}\right)}$

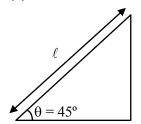
$$0.6 = 0.2 + \frac{0.6}{k}$$

$$k = \frac{3}{2}$$

- A given object takes n times the time to slide down 44. 45° rough inclined plane as it takes the time to slide down an identical perfectly smooth 45° inclined plane. The coefficient of kinetic friction between the object and the surface of inclined plane is:
 - (1) $1 \frac{1}{n^2}$
- (3) $\sqrt{1-\frac{1}{n^2}}$

Ans. (1)

Sol.



Case-1: No friction $a = g \sin\theta$

$$\ell = \frac{1}{2}(g\sin\theta)t_1^2$$

$$t_1 = \sqrt{\frac{2\ell}{g\sin\theta}}$$

$$a = g \sin\theta - \mu g \cos\theta$$

$$\ell = \frac{1}{2}(g\sin\theta - \mu g\cos\theta)t_2^2$$

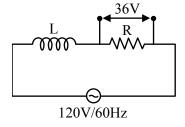
$$\sqrt{\frac{2\ell}{g\sin\theta - \mu g\cos\theta}} = n\sqrt{\frac{2\ell}{g\sin\theta}}$$

$$\mu = 1 - \frac{1}{n^2}$$

- A coil of negligible resistance is connected in 45. series with 90 Ω resistor across 120 V, 60 Hz supply. A voltmeter reads 36 V across resistance. Inductance of the coil is:
 - (1) 0.76 H
- (2) 2.86 H
- (3) 0.286 H
- (4) 0.91 H

Ans. (1)

Sol.



$$36 = I_{rms} R$$

$$36 = \frac{120}{\sqrt{X_1^2 + R^2}} \times R$$

$$R = 90 \Omega \Rightarrow 36 = \frac{120 \times 90}{\sqrt{X_L^2 + 90^2}}$$

$$\sqrt{X_L^2 + 90^2} = 300$$

$$X_L^2 = 81900$$

$$X_L = 286.18$$

$$\omega L = 286.18$$

$$L = \frac{286.18}{376.8}$$

$$L = 0.76 H$$

- 46. There are 100 divisions on the circular scale of a screw gauge of pitch 1 mm. With no measuring quantity in between the jaws, the zero of the circular scale lies 5 divisions below the reference line. The diameter of a wire is then measured using this screw gauge. It is found the 4 linear scale divisions are clearly visible while 60 divisions on circular scale coincide with the reference line. The diameter of the wire is:
 - (1) 4.65 mm
- (2) 4.55 mm
- (3) 4.60 mm
- (4) 3.35 mm

Ans. (2)

Sol. Least count =
$$\frac{1}{100}$$
 mm = 0.01mm

zero error = +0.05 mm

Reading = $4 \times 1 \text{ mm} + 60 \times 0.01 \text{ mm} - 0.05 \text{ mm}$ = 4.55 mm

- 47. A proton and an electron have the same de Broglie wavelength. If K_p and K_e be the kinetic energies of proton and electron respectively. Then choose the correct relation:
 - (1) $K_p > K_e$
- (2) $K_p = K_e$
- (3) $K_n = K_e^2$
- $(4) K_{\rm p} < K_{\rm e}$

Ans. (4)

Sol. De Broglie wavelength of proton & electron = λ

$$\therefore \lambda = \frac{h}{p}$$

$$p_{proton} = p_{electron}$$

$$\therefore$$
 KE = $\frac{p^2}{2m}$

$$\therefore KE_{proton} < KE_{electron}$$

$$[K_p < K_e]$$

Least count of a vernier caliper is $\frac{1}{20N}$ cm. The

value of one division on the main scale is 1 mm. Then the number of divisions of main scale that coincide with N divisions of vernier scale is:

$$(1)\left(\frac{2N-1}{20N}\right)$$

$$(1)\left(\frac{2N-1}{20N}\right) \qquad (2)\left(\frac{2N-1}{2}\right)$$

$$(3)(2N-1)$$

$$(4)\left(\frac{2N-1}{2N}\right)$$

- **Sol.** Least count of vernier calipers = $\frac{1}{20N}$ cm
 - \therefore Least count = 1 MSD 1 VSD

let x no. of divisions of main scale coincides with N division of vernier scale, then

$$1 \text{ VSD} = \frac{x \times 1 \text{mm}}{N}$$

$$\therefore \frac{1}{20N} cm = 1 mm - \frac{x \times 1mm}{N}$$

$$\frac{1}{2N}mm = 1mm - \frac{x}{N}mm$$

$$x = \left(1 - \frac{1}{2N}\right) N$$

$$x = \frac{2N - 1}{2}$$

49. If M_0 is the mass of isotope ${}_{5}^{12}B$, M_p and M_n are the masses of proton and neutron, then nuclear binding energy of isotope is:

$$(1) (5 M_p + 7 M_n - M_o)C^2$$

$$(2) (M_o - 5M_p)C^2$$

$$(3) (M_o - 12M_n)C^2$$

(4)
$$(M_o - 5M_p - 7M_n)C^2$$

Ans. (1)

Sol. B.E. = ΔmC^2

$$(5 M_p + 7M_n - M_o)C^2$$

- **50.** A diatomic gas ($\gamma = 1.4$) does 100 J of work in an isobaric expansion. The heat given to the gas is :
 - (1) 350 J
- (2) 490 J
- (3) 150 J
- (4) 250 J

Ans. (1)

For Isobaric process

$$w = P\Delta v = nR\Delta T = 100 J$$

$$Q = \Delta u + w$$

$$\Delta Q = \frac{F}{2}nR\Delta T + nR\Delta T$$

$$\left(\frac{f}{2}+1\right)$$
nR Δ T

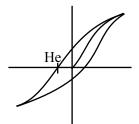
$$\left(\frac{5}{2} + 1\right) 100 = 350 \text{ J}$$

SECTION-B

51. The coercivity of a magnet is 5×10^3 A/m. The amount of current required to be passed in a solenoid of length 30 cm and the number of turns 150, so that the magnet gets demagnetised when inside the solenoid isA.

Ans. (10)

Sol.



$$H_c = \frac{\mu_o ni}{\mu_o}$$

$$5 \times 10^3 = \frac{150}{30} \times 100 \times i$$

$$\frac{50}{5} = i$$

$$I = 10$$

Ans. (40)

Sol. m = mass of small drop

M = mass of bigger drop

$$V_{t} = \frac{2}{9} \frac{R^{2}(\rho - \sigma)g}{n}$$

$$8 \propto m = M$$

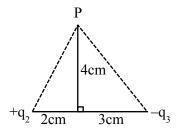
$$8r^3 = R^3 \Rightarrow R = 2R$$

as $V_t \times R^2 \ \ \because$ Radius double so V_t becomes 4 time

$$\therefore 4 \times 10 = 40 \text{ cm/s}$$

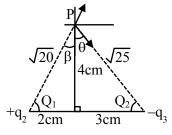
53. If the net electric field at point P along Y axis is zero, then the ratio of $\left| \frac{q_2}{q_2} \right|$ is $\frac{8}{5\sqrt{x}}$,

where x =



Ans. (5)

Sol.



$$\frac{Kq_2}{20}\cos\beta = \frac{Kq_3}{25}\cos\theta$$

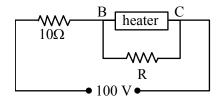
$$\frac{Kq_2}{20} \frac{4}{\sqrt{20}} = \frac{Kq_3}{25} \frac{4}{\sqrt{25}}$$

$$\frac{q_2}{q_3} = \frac{20}{25} \sqrt{\frac{20}{25}} = \frac{8}{5\sqrt{x}}$$

$$\Rightarrow \sqrt{x} = \frac{8 \times 25\sqrt{25}}{5 \times 20\sqrt{20}}$$

$$x = 5$$

54. A heater is designed to operate with a power of 1000 W in a 100 V line. It is connected in combination with a resistance of 10 Ω and a resistance R, to a 100 V mains as shown in figure. For the heater to operate at 62.5 W, the value of R should be Ω .



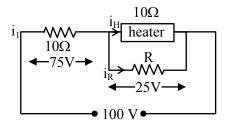
Ans. (5)

Sol.
$$R_{heater} = \frac{V^2}{P} = \frac{(100)^2}{1000} = 10\Omega$$

For heater
$$P = \frac{V^2}{R} \Rightarrow V = \sqrt{PR}$$

$$V = \sqrt{62.5 \times 10}$$

$$V = 25 \text{ v}$$



$$i_1 = \frac{75}{10} = 7.5 A$$
, $i_H = \frac{25}{10} = 2.5 A$.

$$i_R = i_1 - i_H = 5$$

$$V = IR$$

$$R = \frac{25}{5} = 5\Omega$$

Ans. (22)

Sol.
$$C = 2\mu f$$
; $E = 110\sqrt{2} \sin(100 t)$

$$X_C = \frac{1}{\omega c} = \frac{1}{100 \times 2 \times 10^6}$$

$$= \frac{10000}{2} = 5000\Omega$$

$$i_0 = \frac{110\sqrt{2}}{5000}$$

$$i_{rms} = \frac{110\sqrt{2}}{5000\sqrt{2}}$$

$$=\frac{110}{5}\text{mA}$$

$$= 22 \text{ mA}$$

Ans. (2)

Sol. $d = 1 \text{ mm}, D = 1 \text{ m}, \lambda = 500 \text{ nm}$

$$10 \left(\frac{\lambda D}{d} \right) = \frac{2\lambda D}{a}$$

$$\mathbf{a} = \frac{d}{5}$$

$$= \frac{10 \times 10^{-4} \text{ m}}{5}$$

$$= 2 \times 10^{-4}$$

57. An object of mass 0.2 kg executes simple harmonic motion along x axis with frequency of $\left(\frac{25}{\pi}\right)$ Hz. At the position x = 0.04 m the object has kinetic energy 0.5 J and potential energy 0.4 J.

The amplitude of oscillation is cm.

Ans. (6)

Sol. Total energy = K.E. + P.E.

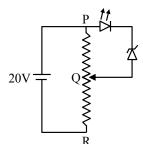
at
$$x = 0.04$$
 m, T.E. $= 0.5 + 0.4 = 0.9$ J

$$T.E = 1 \text{ m}\omega^2 A^2 = 0.9$$

$$= \frac{1}{2} \times 0.2 \left(2\pi \times \frac{25}{\pi} \right)^2 \times A^2 = 0.9$$

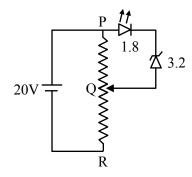
$$\Rightarrow$$
 A = 0.06 m

$$A = 6 \text{ cm}$$



Ans. (5)

Sol.



$$PR = 20 \text{ cm}$$

$$V_{PQ} = \frac{1}{4} \times R_{PR}$$

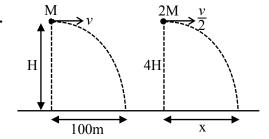
$$\ell_{\min}(PQ) = \frac{1}{4} \times 20$$

= 5 cm

59. A body of mass M thrown horizontally with velocity v from the top of the tower of height H touches the ground at a distance of 100m from the foot of the tower. A body of mass 2M thrown at a velocity $\frac{v}{2}$ from the top of the tower of height 4H will touch the ground at a distance ofm.

Ans. (100)

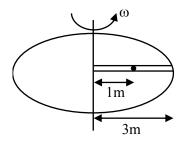
Sol.



$$100 = v\sqrt{\frac{2H}{g}}; \quad x = \frac{v}{2}\sqrt{\frac{2(4H)}{g}} = v\sqrt{\frac{2H}{g}}$$

$$\Rightarrow$$
 x = 100

60. A circular table is rotating with an angular velocity of ω rad/s about its axis (see figure). There is a smooth groove along a radial direction on the table. A steel ball is gently placed at a distance of 1m on the groove. All the surface are smooth. If the radius of the table is 3 m, the radial velocity of the ball w.r.t. the table at the time ball leaves the table is $x\sqrt{2}\omega$ m/s, where the value of x is......



Ans. (2)

Sol. $a_c = \omega^2 x$

$$\frac{v dv}{dx} = \omega^2 x$$

$$\int_{0}^{V} v dv = \int_{1}^{3} \omega^{2} x dx$$

$$\frac{v^2}{2} = \omega^2 \left[\frac{x^2}{2} \right]$$

$$\frac{\mathbf{v}^2}{2} = \frac{\omega^2}{2} \left[3^2 - 1^2 \right]$$

$$v = 2\sqrt{2}\omega$$

$$x = 2$$

CHEMISTRY

SECTION-A

- 61. In qualitative test for identification of presence of phosphorous, the compound is heated with an oxidising agent. Which is further treated with nitric acid and ammonium molybdate respectively. The yellow coloured precipitate obtained is:
 - (1) Na₃PO₄.12MoO₃
 - $(2) (NH_4)_3 PO_4.12(NH_4)_2 MoO_4$
 - (3) (NH₄)₃ PO₄.12MoO₃
 - (4) MoPO₄.21NH₄NO₃

Ans. (3)

Sol.
$$PO_4^{3-} + (NH_4)_2MoO_4 \xrightarrow{H^+} (NH_4)_3PO_4.12MoO_3 \downarrow$$

Or HPO_4^- Ammonium Canary yellow ppt. (Ammonium phopho molybdate)

62. For a reaction $A \xrightarrow{K_1} B \xrightarrow{K_2} C$

If the rate of formation of B is set to be zero then the concentration of B is given by:

- $(1) K_1 K_2 [A]$
- $(2) (K_1 K_2)[A]$
- $(3) (K_1 + K_2)[A]$
- $(4) (K_1/K_2)[A]$

Ans. (4)

Sol. Rate of formation of B is

$$\frac{d[B]}{dt} = k_1[A] - k_2[B]$$

$$0 = k_1[A] - k_2[B]$$

$$\left(\frac{\mathbf{k}_1}{\mathbf{k}_2}\right) [\mathbf{A}] = [\mathbf{B}]$$

- 63. When ψ_A and Ψ_B are the wave functions of atomic orbitals, then σ^* is represented by :
 - (1) $\psi_A 2\psi_B$
- (2) $\psi_A \psi_B$
- (3) $\psi_{A} + 2\psi_{B}$
- (4) $\psi_A + \psi_B$

Ans. (2)

TEST PAPER WITH SOLUTION

Sol. Antibonding molecular orbitals are formed by destructive interference of wave functions.

(ABMO)
$$\sigma^* = \psi_A - \psi_B$$

- **64.** Which one the following compounds will readily react with dilute NaOH?
 - $(1) C_6H_5CH_2OH$
- (2) C₂H₅OH
- (3) (CH₃)₃COH
- $(4) C_6H_5OH$

Ans. (4)

Sol.
$$\bigcirc OH \qquad \bigcirc O^-Na^+$$

$$+ NaOH \rightarrow \bigcirc O^-Na^+$$

Stronger ACID than H₂O

- **65.** The shape of carbocation is :
 - (1) trigonal planar
- (2) diagonal pyramidal
- (3) tetrahedral
- (4) diagonal

Ans. (1)

66. Given below are two statements :

Statement (I): $S_N 2$ reactions are 'stereospecific', indicating that they result in the formation only one stereo-isomers as the product.

Statement (II): $S_N 1$ reactions generally result in formation of product as racemic mixtures. In the light of the above statements, choose the **correct** answer from the options given below:

- (1) Statement I is true but Statement II is false
- (2) Statement I is false but Statement II is true
- (3) Both Statement I and Statement II is true
- (4) Both Statement I and Statement II is false

Ans. (3)

Sol. $SN^2 \rightarrow Inversion$

 $SN^1 \rightarrow Racemisation$

67. Match List-I with List-II.

List-I List-II (Reactions) (Products) NH_2 **CHO** (II) COOH OH

Choose the **correct** answer from the options given below:

- (1) (A)-(III), (B)-(II), (C)-(I), (D)-(IV)
- (2) (A)-(IV), (B)-(II), (C)-(III), (D)-(I)
- (3) (A)-(I), (B)-(IV), (C)-(II), (D)-(III)
- (4) (A)-(II), (B)-(IV), (C)-(I), (D)-(III)

68. Match List-I with List-II.

List-I		List-II	
(Test)		(Identification)	
(A)	Bayer's test	(I)	Phenol
(B)	Ceric ammonium	(II)	Aldehyde
	nitrate test		
(C)	Phthalein due test	(III)	Alcoholic-OH

- (C) Phthalein dye test group
- (D) Schiff's test (IV) Unsaturation Choose the **correct** answer from the options given below:

$$(1)$$
 (A) - (III) , (B) - (I) , (C) - (IV) , (D) - (II)

$$(2) (A)-(II), (B)-(III), (C)-(IV), (D)-(I)$$

$$(3)$$
 (A)-(IV), (B)-(I), (C)-(II), (D)-(III)

$$(4) (A)-(IV), (B)-(III), (C)-(I), (D)-(II)$$

Ans. (4)

Sol. (A) Bayer's test \rightarrow Unsaturation

- (B) Ceric ammonium nitrate test \rightarrow Alcoholic-OH group
- (C) Phthalein dye test \rightarrow Phenol
- (D) Schiff's test \rightarrow Aldehyde
- 69. Identify the **incorrect** statements about group 15 elements:
 - (A) Dinitrogen is a diatomic gas which acts like an inert gas at room temperature.
 - (B) The common oxidation states of these elements are -3, +3 and +5.
 - (C) Nitrogen has unique ability to form $p\pi-p\pi$ multiple bonds.
 - (D) The stability of +5 oxidation states increases down the group.
 - (E) Nitrogen shows a maximum covalency of 6. Choose the **correct** answer from the options given below.

Ans. (4)

Sol. (D) Due to inert pair effect lower oxidation state is more stable.

> (E) Nitrogen belongs to 2nd period and cannot expand its octet.

70. IUPAC name of following hydrocarbon (X) is:

$$\begin{array}{ccccc} CH_{3}-CH-CH_{2}-CH_{2}-CH-CH-CH_{2}-CH_{3}\\ & & | & & | \\ CH_{3} & (X) & CH_{3} & CH_{3} \end{array}$$

- (1) 2-Ethyl-3,6-dimethylheptane
- (2) 2-Ethyl-2,6-diethylheptane
- (3) 2,5,6-Trimethyloctane
- (4) 3,4,7-Trimethyloctane

Ans. (3)

2,5,6-Trimethyloctane

- 71. The equilibrium $Cr_2O_7^{2-} \rightleftharpoons 2CrO_4^{2-}$ is shifted to the right in :
 - (1) an acidic medium
 - (2) a basic medium
 - (3) a weakly acidic medium
 - (4) a neutral medium

Ans. (2)

Sol.
$$\operatorname{Cr}_2\operatorname{O}_7^{2-} \xrightarrow{\operatorname{OH}^-} 2\operatorname{CrO}_4^{2-}$$

72. Given below are two statements:

Statement (I): A Buffer solution is the mixture of a salt and an acid or a base mixed in any particular quantities.

Statement (II): Blood is naturally occurring buffer solution whose pH is maintained by H_2CO_3 / HCO_3° concentrations.

In the light of the above statements, choose the **correct** answer from the options given below.

- (1) Statement I is false but Statement II is true
- (2) Both Statement I and Statement II is true
- (3) Both **Statement I** and **Statement II** is false
- (4) **Statement I** is true but **Statement II** is false

Ans. (1)

Sol. Buffer solution is a mixture of either weak acid / weak base and its respective conjugate.

Blood is a buffer solution of carbonic acid H₂CO₃ and bicarbonate HCO₃

Statement 1 is false but Statement II is true.

73. The correct sequence of acidic strength of the following aliphatic acids in their decreasing order is:

CH₃CH₂COOH, CH₃COOH, CH₃CH₂CH₂COOH, HCOOH

- (1) HCOOH > CH₃COOH > CH₃CH₂COOH > CH₃CH₂CCOOH
- (2) HCOOH > CH₃CH₂CH₂COOH > CH₃CH₂COOH > CH₃COOH
- (3) CH₃CH₂CH₂COOH > CH₃CH₂COOH > CH₃COOH > HCOOH
- (4) CH₃COOH > CH₃CH₂COOH > CH₃CH₂CH₂COOH > HCOOH

Ans. (1)

Sol. CH₃CH₂COOH, CH₃COOH, CH₃CH₂CH₂COOH, HCOOH

The correct order is:

HCOOH > CH₃COOH > CH₃CH₂COOH > CH₃CH₂COOH

74. Given below are two statements:

Statement (I): All the following compounds react with p-toluenesulfonyl chloride.

 $C_6H_5NH_2$ $(C_6H_5)_2NH$ $(C_6H_5)_3N$

Statement (II): Their products in the above reaction are soluble in aqueous NaOH.

In the light of the above statements, choose the **correct** answer from the options given below.

- (1) Both **Statement I** and **Statement II** is false
- (2) Statement I is true but Statement II is false
- (3) Statement I is false but Statement II is true
- (4) Both **Statement I** and **Statement II** is true

Ans. (1)

Sol. Hinsberg test given by 1° amine only.

75. The emf of cell $T1 \begin{vmatrix} T1^+ \\ (0.001M) \end{vmatrix} \begin{vmatrix} Cu^{2+} \\ (0.01M) \end{vmatrix}$ Cu is 0.83 V at

298 K. It could be increased by:

- (1) increasing concentration of T1⁺ ions
- (2) increasing concentration of both T1⁺ and Cu²⁺ ions
- (3) decreasing concentration of both T1⁺ and Cu²⁺ ions
- (4) increasing concentration of Cu²⁺ ions

Ans. (4)

Sol.

$$\begin{split} &\text{Anodic Reaction} & \left[T\ell_{(s)} \! \to \! T\ell^+_{(aq)} + e^- \right] 2 \\ & \text{Cathodic Reaction} & \text{Cu}^{+2}_{(aq)} \! + \! 2e^- \! \to \! \text{Cu}_{(s)} \\ & \\ & \text{Overall Redox Reaction} & 2T\ell_{(s)} \! + \! \text{Cu}^{+2}_{(aq)} \! \to \! 2T\ell^+_{(aq)} \! + \! \text{Cu}_{(s)} \end{split}$$

$$E_{cell} = E_{cell}^{o} - \frac{0.0591}{2} log \frac{\left[T\ell^{+}\right]^{2}}{\left[Cu^{+2}\right]}$$

 E_{cell} increases by increasing concentration of $[Cu^{+2}]$ ions.

- **76.** Identify the correct statements about p-block elements and their compounds.
 - (A) Non metals have higher electronegativity than metals.
 - (B) Non metals have lower ionisation enthalpy than metals.
 - (C) Compounds formed between highly reactive nonmetals and highly reactive metals are generally ionic.
 - (D) The non-metal oxides are generally basic in nature.
 - (E) The metal oxides are generally acidic or neutral in nature.
 - (1) (D) and (E) only (2) (A) and (C) only
 - (3) (B) and (E) only (4) (B) and (D) only

Ans. (2)

Sol. As electronegativity increases non-metallic nature increases.

Along the period ionisation energy increases.

High electronegativity difference results in ionic bond formation.

Oxides of metals are generally basic and that of non-metals are acidic in nature.

77. Given below are two statements:

Statement (I): Kjeldahl method is applicable to estimate nitrogen in pyridine.

Statement (II): The nitrogen present in pyridine can easily be converted into ammonium sulphate in Kjeldahl method.

In the light of the above statements, choose the **correct** answer from the options given below.

- (1) Both **Statement I** and **Statement II** is false
- (2) Statement I is false but Statement II is true
- (3) Both Statement I and Statement II is true
- (4) Statement I is true but Statement II is false

Ans. (1)

Sol. Nitrogen present in pyridine can not be estimated by Kjeldahl method as the nitrogen present in pyridine can not be easily converted into ammonium sulphate.

78. The reaction;

$$\frac{1}{2}H_{2(g)}^{} + AgCl_{(s)}^{} \longrightarrow H_{(aq)}^{^{+}} + Cl_{(aq)}^{^{-}} + Ag_{(s)}^{}$$

occurs in which of the following galvanic cell:

(1)
$$Pt \left| H_{2(g)} \right| HCl_{(soln.)} \left| AgCl_{(s)} \right| Ag$$

(2)
$$Pt|H_{2(g)}|HCl_{(soln)}|AgNO_{3(ag)}|Ag$$

(3)
$$Pt |H_{2(g)}| KCl_{(soln.)} |AgCl_{(s)}| Ag$$

(4)
$$Ag|AgCl_{(s)}|KCl_{(soln.)}|AgNO_{3(aq.)}|Ag$$

Ans. (3)

Sol. Anodic half cell

Gas – gas ion electrode

$$\frac{1}{2}H_{2(g)} \to H^{+}_{(aq)} + e^{-}$$

Cathodic Reaction

Metal-metal insoluble salt anion electrode

$$Ag^{+}_{(aq)} + e^{-} \rightarrow Ag_{(s)}$$

$$AgCl_{(s)} \mathop{\Longrightarrow}\limits_{} Ag^{^{+}}_{\;\; (aq)} + Cl^{^{-}}_{\;\; (aq)}$$

$$AgCl_{(s)} + e^{-} \rightarrow Ag_{(s)} + Cl_{(aq)}^{-}$$

Overall redox reaction

$$\frac{1}{2}H_{2(g)} + AgCl_{(s)} \to H^{+}_{(aq)} + Cl^{-}_{(aq)} + Ag_{(s)}$$

Cell Representation

$$Pt \mid H_{2(g)} \mid kCl_{(sol)} \mid AgCl_{(s)} \mid Ag$$

79. Given below are two statements:

Statement (I): Fusion of MnO₂ with KOH and an oxidising agent gives dark green K₂MnO₄.

Statement (II): Manganate ion on electrolytic oxidation in alkaline medium gives permanganate ion.

In the light of the above statements, choose the **correct** answer from the options given below.

- (1) Both **Statement I** and **Statement II** is true
- (2) Both **Statement I** and **Statement II** is false
- (3) Statement I is true but Statement II is false
- (4) Statement I is false but Statement II is true

Ans. (1)

Sol.
$$MnO_2 + 4KOH + O_2 \xrightarrow{fused} 2K_2MnO_4 + 2H_2O$$

Dark green

Electrolytic oxidation in alkaline medium:

At anode:

$$MnO_4^{2-} \rightarrow MnO_4^- + e^-$$

80. Match List-I with List-II.

List-I

List-II

(Complex ion)

(Spin only magnetic

moment in B.M.)

(A)
$$[Cr(NH_3)_6]^{3+}$$

(B)
$$[NiCl_4]^{2-}$$

(C)
$$[CoF_6]^{3-}$$

$$(III)$$
 0.0

(D)
$$[Ni(CN)_4]^{2-}$$

Choose the **correct** answer from the options given below:

$$(1) (A)-(I), (B)-(IV), (C)-(II), (D)-(III)$$

Ans. (3)

Sol. (A)
$$[Cr(NH_3)_6]^{3+}$$

$$Cr^{3+} \cdot 3d^3$$

n = 3 (unpaired electrons)

$$\mu \simeq 3.87 \text{ B.M. (II)}$$

(B) $[NiCl_4]^{2-}$

$$Ni^{2+}: 3d^8$$

$$n = 2$$

$$\mu \simeq 2.83$$
 B.M. (IV)

(C) $[CoF_6]^{3-}$

$$Co^{3+}: 3d^6$$

$$n = 4$$

$$\mu \simeq 4.90 \text{ B.M.} (I)$$

(D) $[Ni(CN)_4]^{2-}$

$$Ni^{2+}: 3d^8$$

$$n = 0$$

$$\mu = 0$$
 B.M. (III)

SECTION-B

81. $\Delta_{\text{vap}} \text{H}^{\odot}$ for water is +40.49 kJ mol⁻¹ at 1 bar and 100°C. Change in internal energy for this vapourisation under same condition is _____ kJ mol⁻¹. (Integer answer)

(Given R = 8.3 JK⁻¹ mol⁻¹)

Ans. (38)

Sol.
$$H_2O(\ell) \rightleftharpoons H_2O(g)$$
 $\Delta H_{vap}^0 = 40.79 \, kJ \, / \, mole$ $\Delta H_{vap}^0 = \Delta U_{vap}^0 + \Delta n_g RT$ $40.79 = \Delta U_{vap}^0 + \frac{1 \times 8.3 \times 373.15}{1000}$ $\Delta U_{vap}^0 = 40.79 - 3.0971$ $= 37.6929$ $\Delta U_{vap}^0 \approx 38$

Number of molecules having bond order 2 from the following molecule is ______.C₂, O₂, Be₂, Li₂, Ne₂, N₂, He₂

Ans. (2)

Sol. C_2

(12e⁻):
$$\sigma 1s^2$$
, $\sigma *1s^2$, $\sigma 2s^2$, $\sigma *2s^2$ $\left[\pi 2p_x^2 = \pi 2p_y^2\right]$
B.O. = $\frac{8-4}{2} = 2$

 O_2

$$(16e^{-})$$
: $\sigma 1s^{2}, \sigma^{*}1s^{2}, \sigma 2s^{2}, \sigma^{*}2s^{2}, \sigma 2pz^{2}$

$$\[\pi 2p_x^2 = \pi 2p_y^2\] \[\pi * 2p_x^1 = \pi * 2p_y^1\]$$

B.O. =
$$\frac{10-6}{2}$$
 = 2

Be

$$(8e^{-})$$
: $\sigma 1s^{2}, \sigma * 1s^{2}, \sigma 2s^{2}, \sigma * 2s^{2}$

B.O. =
$$\frac{4-4}{2}$$
 = 0

 Li_2

$$(6e^{-})$$
: $\sigma 1s^{2}, \sigma * 1s^{2}, \sigma 2s^{2}$

B.O. =
$$\frac{4-2}{2}$$
 = 1

Ne

$$(20e^{-})$$
: $\sigma 1s^{2}, \sigma * 1s^{2}, \sigma 2s^{2}, \sigma * 2s^{2}, \sigma 2pz^{2}$

$$\left[\pi 2 p_{x}^{2} = \pi 2 p_{y}^{2}\right] \left[\pi^{*} 2 p_{x}^{2} = \pi^{*} 2 p_{y}^{2}\right] \sigma^{*} 2 p_{z}^{2}$$

B.O. =
$$\frac{10-10}{2}$$
 = 0

Na

$$(14e^{-}):\sigma 1s^{2},\sigma^{*}1s^{2},\sigma 2s^{2},\sigma^{*}2s^{2} \bigg\lceil \pi 2p_{x}^{2}=\pi 2p_{y}^{2} \bigg\rceil \ \sigma 2p_{z}^{2}$$

B.O. =
$$\frac{10-4}{2}$$
 = 6

He₂

$$(4e^{-})$$
: $\sigma 1s^{2}, \sigma * 1s^{2}$

B.O. =
$$\frac{2-2}{2}$$
 = 0

83. Total number of optically active compounds from the following is _____.

Ans. (1)

Sol.
$$CH_3 - CH_2 - CH - CH_3$$

 $C1$

84. The total number of carbon atoms present in tyrosine, an amino acid, is _____.

Ans. (9)

Sol. Tyrosine

$$HO$$
 NH_2 OH

Number of carbon atoms = 9

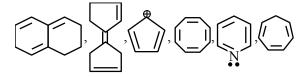
85. Two moles of benzaldehyde and one mole of acetone under alkaline conditions using aqueous NaOH after heating gives x as the major product. The number of π bonds in the product x is

Ans. (9)

Sol.
$$\begin{array}{c} Ph & O \\ H & C = O + CH_3 - C - CH_3 + O = C \\ \hline & & \\ NaOH/\Delta \\ \hline & Ph & \\ H & C = CH - C - CH = C \\ \hline & \\ H & \\ \end{array}$$

$$\begin{array}{c} Ph \\ Aldol \\ condensation \\ reaction \\ \hline \end{array}$$

86. Total number of aromatic compounds among the following compounds is _____.



Ans. (1)

87. Molality of an aqueous solution of urea is 4.44 m. Mole fraction of urea in solution is $x \times 10^{-3}$. Value of x is ______. (integer answer)

Ans. (74)

Sol. Molality of urea is 4.44 m, that means 4.44 moles of urea present in 1000 gm of water.

$$\therefore X_{urea} = \frac{4.44}{4.44 + \frac{1000}{18}}$$

= 0.0740

OR

$$74 \times 10^{-3}$$

$$X = 74$$

88. Total number of unpaired electrons in the complex ion $[Co(NH_3)_6]^{3+}$ and $[NiCl_4]^{2-}$ is

Ans. (2)

Sol.
$$Co^{+3}: 3d^6 \quad t_{2g}^{2,2,2} e_g^{0,0}$$

Unpaired $e^- = 0$
 $Ni^{+2}: 3d^8 \quad e^{2,2} t_2^{2,1,1}$
Unpaired $e^- = 2$

89. Wavenumber for a radiation having 5800 Å wavelength is $x \times 10 \text{ cm}^{-1}$. The value of x is

Ans. (1724)

Sol.
$$\overline{v}$$
 (wave no.) = $\frac{1}{\lambda} = \frac{1}{5800 \times 10^{-8} \text{ cm}} = 17241$
OR

$$1724 \times 10 \,\mathrm{cm}^{-1} \Rightarrow x = 1724$$

90. A solution is prepared by adding 1 mole ethyl alcohol in 9 mole water. The mass percent of solute in the solution is _____ (Integer Answer) (Given: Molar mass in g mol⁻¹ Ethyl alcohol: 46, water: 18)

Ans. (22)

Sol. Mass percent of Alcohol $= \frac{\text{Mass of ethyl alcohol}}{\text{Total mass of solution}} \times 100$ $= \frac{1 \times 46}{1 \times 46 + 9 \times 18} \times 100 = \frac{4600}{208}$ = 22.11 Or 22