

Closed-loop Matters: Dual Regression Networks for Single Image Super-Resolution

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Abstract

Deep neural networks have exhibited promising performance in image super-resolution (SR) by learning a non-linear mapping function from low-resolution (LR) images to high-resolution (HR) images. However, there are two underlying limitations to existing SR methods. First, learning the mapping function from LR to HR images is typically an ill-posed problem, because there exist infinite HR images that can be downsampled to the same LR image. As a result, the space of the possible functions can be extremely large, which makes it hard to find a good solution. Second, the paired LR-HR data may be unavailable in real-world applications and the underlying degradation method is often unknown. For such a more general case, existing SR models often incur the adaptation problem and yield poor performance. To address the above issues, we propose a dual regression scheme by introducing an additional constraint on LR data to reduce the space of the possible functions. Specifically, besides the mapping from LR to HR images, we learn an additional dual regression mapping estimates the down-sampling kernel and reconstruct LR images, which forms a closed-loop to provide additional supervision. More critically, since the dual regression process does not depend on HR images, we can directly learn from LR images. In this sense, we can easily adapt SR models to real-world data, e.g., raw video frames from YouTube. Extensive experiments with paired training data and unpaired real-world data demonstrate our superiority over existing methods.

1. Introduction

Deep neural networks (DNNs) have been the workhorse of many real-world applications, including image classification [18, 14, 9, 15, 27, 13], video understanding [46, 45,

Figure 1. Performance comparison of the images produced by the state-of-the-art methods for $8\times$ SR. Our dual regression scheme is able to produce sharper images than the baseline methods.

44, 6] and many other applications [7, 50, 52, 11, 20]. Recently, image super-resolution (SR) has become an important task that aims at learning a nonlinear mapping to reconstruct high-resolution (HR) images from low-resolution (LR) images. Based on DNNs, many methods have been proposed to improve SR performance [51, 26, 10, 12, 49]. However, these methods may suffer from two limitations.

First, learning the mapping from LR to HR images is typically an ill-posed problem since there exist infinitely many HR images that can be downsampled to obtain the same LR image [36]. Thus, the space of the possible functions that map LR to HR images becomes extremely large. As a result, the learning performance can be limited since learning a good solution in such a large space is very hard. To improve the SR performance, one can design effective models by increasing the model capacity, e.g., EDSR [26], DBPN [16], and RCAN [51]. However, these methods still suffer from the large space issue of possible mapping functions, resulting in the limited performance without producing sharp textures [24] (See Figure 1). Thus, how to reduce the possible space of the mapping functions to improve the training of SR models becomes an important problem.

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Second, it is hard to obtain a promising SR model when the paired data are unavailable [43, 54]. Note that most SR methods rely on the paired training data, i.e., HR images with their Bicubic-degraded LR counterparts. However, the paired data may be unavailable and the unpaired data often dominate the real-world applications. Moreover, the real-world data do not necessarily have the same distribution to the LR images obtained by a specific degradation method (e.g., Bicubic). Thus, learning a good SR model for real-world applications can be very challenging. More critically, if we directly apply existing SR models to real-world data, they often incur a severe adaptation problem and yield poor performance [43, 54]. Therefore, how to effectively exploit the unpaired data to adapt SR models to real-world applications becomes an urgent and important problem.

In this paper, we propose a novel dual regression scheme that forms a closed-loop to enhance SR performance. To address the first limitation, we introduce an additional constraint to reduce the possible space such that the super-resolved images can reconstruct the input LR images. Ideally, if the mapping from LR \rightarrow HR is optimal, the super-resolved images can be downsampled to obtain the same input LR image. With such a constraint, we are able to estimate the underlying downsampling kernel and hence reduce the space of possible functions to find a good mapping from LR to HR (See theoretical analysis in Remark 1). Thus, it becomes easier to obtain promising SR models (See the comparison in Figure 1). To address the second limitation, since the regression of LR images does not depend on HR images, our method can directly learn from the LR images. In this way, we can easily adapt SR models to the real-world LR data, e.g., raw video frames from Youtube. Extensive experiments on the SR tasks with paired training data and unpaired real-world data demonstrate the superiority of our method over existing methods.

Our contributions are summarized as follows:

- We develop a dual regression scheme by introducing an additional constraint such that the mappings can form a closed-loop and LR images can be reconstructed to enhance the performance of SR models. Moreover, we also theoretically analyze the generalization ability of the proposed scheme, which further confirms its superiority to existing methods.
- We study a more general super-resolution case where there is no corresponding HR data w.r.t. the real-world LR data. With the proposed dual regression scheme, deep models can be easily adapted to real-world data, e.g., raw video frames from YouTube.
- Extensive experiments on both the SR tasks with paired training data and unpaired real-world data demonstrate the effectiveness of the proposed dual regression scheme in image super-resolution.

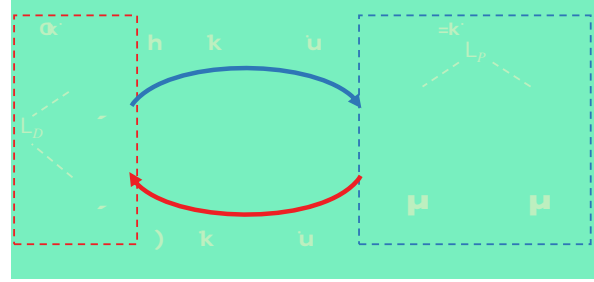


Figure 2. Dual regression training scheme, which contains a primal regression task for super-resolution and a dual regression task to project super-resolved images back to LR images. The primal and dual regression tasks form a closed-loop.

2. Related Work

Supervised super-resolution. Many efforts have been made to improve the performance of SR, including the interpolation-based approaches [19] and reconstruction-based methods [16, 25, 51]. Haris et al. [16] propose a back-projection network (DBPN) that consists of several up- and down-sampling layers to iteratively produce LR and HR images. Zhang et al. [51] propose the channel attention mechanism to build a deep model called RCAN to further improve the performance of SR. However, these methods still have a very large space of the possible mappings which makes it hard to learn a good solution.

Unsupervised super-resolution. There is an increasing interest in learning super-resolution models without paired data in the unsupervised setting [43, 54]. Based on CycleGAN [56], Yuan et al. [43] propose a CinCGAN model to generate HR images without paired data. Recently, some blind SR methods [2, 55] were proposed to learn the unknown degradation methods. However, these methods often totally discard the paired synthetic data, which can be obtained very easily and used to boost the training. On the contrary, our dual regression scheme seeks to adapt SR models to new LR data by exploiting both the real-world LR data and the paired synthetic data.

Dual learning. Dual learning methods [17, 40, 41, 53] contain a primal model and a dual model to learn two opposite mappings simultaneously to enhance the performance of language translation. Recently, this scheme has also been used to perform image translation without paired training data, e.g., CycleGAN [56] and DualGAN [42]. Specifically, a cycle consistency loss is proposed to avoid the mode collapse issue of GAN methods [56, 4, 5] and help minimize the distribution divergence. However, these methods cannot be directly applied to the standard SR problem. By contrast, we use the closed-loop to reduce the space of possible functions of SR. Moreover, we consider learning asymmetric mappings and provide a theoretical guarantee on the rationality and necessity of using a cycle.

3. Proposed Method

We propose a dual regression scheme to deal with both the paired and unpaired training data for super-resolution (SR). The overall training scheme is shown in Figure 2.

3.1. Dual Regression Scheme for Paired Data

Existing methods only focus on learning the mapping from LR to HR images. However, the space of the possible mapping functions can be extremely large, making the training very difficult. To address this issue, we propose a dual regression scheme by introducing an additional constraint on LR data. Specifically, besides learning the mapping LR → HR, we also learn an inverse/dual mapping from the super-resolved images back to the LR images.

Let $x \in X$ be LR images and $y \in Y$ be HR images. We simultaneously learn the primal mapping P to reconstruct HR images and the dual mapping D to reconstruct LR images. Note that the dual mapping can be regarded as the estimation of the underlying downsampling kernel. Formally, we formulate the SR problem into the dual regression scheme which involves two regression tasks.

Definition 1 (Primal Regression Task) We seek to find a function $P: X \rightarrow Y$, such that the prediction $P(x)$ is similar to its corresponding HR image y .

Definition 2 (Dual Regression Task) We seek to find a function $D: Y \rightarrow X$, such that the prediction of $D(y)$ is similar to the original input LR image x .

The primal and dual learning tasks can form a closed-loop and provide informative supervision to train the models P and D . If $P(x)$ was the correct HR image, then the down-sampled image $D(P(x))$ should be very close to the input LR image x . With this constraint, we can reduce the function space of possible mappings and make it easier to learn a better mapping to reconstruct HR images. To verify this, we provide a theoretical analysis in Section 4.2.

By jointly learning these two learning tasks, we propose to train the super-resolution models as follows. Given a set of N paired samples $S_P = \{(x_i, y_i)\}_{i=1}^N$, where x_i and y_i denote the i -th pair of low- and high-resolution images in the set of paired data. The training loss can be written as

$$\sum_{i=1}^N \underbrace{L_P(P(x_i), y_i)}_{\text{primal regression loss}} + \sum_{i=1}^N \underbrace{L_D(D(P(x_i)), x_i)}_{\text{dual regression loss}}, \quad (1)$$

where L_P and L_D denote the loss function (ℓ_1 -norm) for the primal and dual regression tasks, respectively. Here, λ controls the weight of the dual regression loss (See the sensitivity analysis of λ in Section 6.2).

Actually, we can also add a constraint on the HR domain, i.e., downscaling and upscaling to reconstruct the original

Algorithm 1: Adaptation Algorithm on Unpaired Data.

Input: Unpaired real-world data: S_U ;
 Paired synthetic data: S_P ;
 Batch sizes for S_U and S_P : m and n ;
 Indicator function: $1_{S_P}(\cdot)$.

- 1 Load the pretrained models P and D .
- 2 while not convergent do
- 3 Sample unlabeled data $\{x_i\}_{i=1}^m$ from S_U ;
- 4 Sample labeled data $\{(x_i, y_i)\}_{i=m+1}^{m+n}$ from S_P ;
- 5 // Update the primal model
- 6 Update P by minimizing the objective:
- 7 $\sum_{i=1}^{m+n} 1_{S_P}(x_i) L_P(P(x_i), y_i) + L_D(D(P(x_i)), x_i)$
- 8 // Update the dual model
- 9 Update D by minimizing the objective:
- 10 $\sum_{i=1}^{m+n} L_D(D(P(x_i)), x_i)$
- 11 end

HR images. However, it greatly increases the computation cost (approximately $2\times$ of the original SR model) and the performance improvement is very limited (See results in supplementary). In practice, we only add the dual regression loss on LR data, which significantly improves the performance while preserving the approximately the same cost to the original SR model (See discussions in Section 4.1).

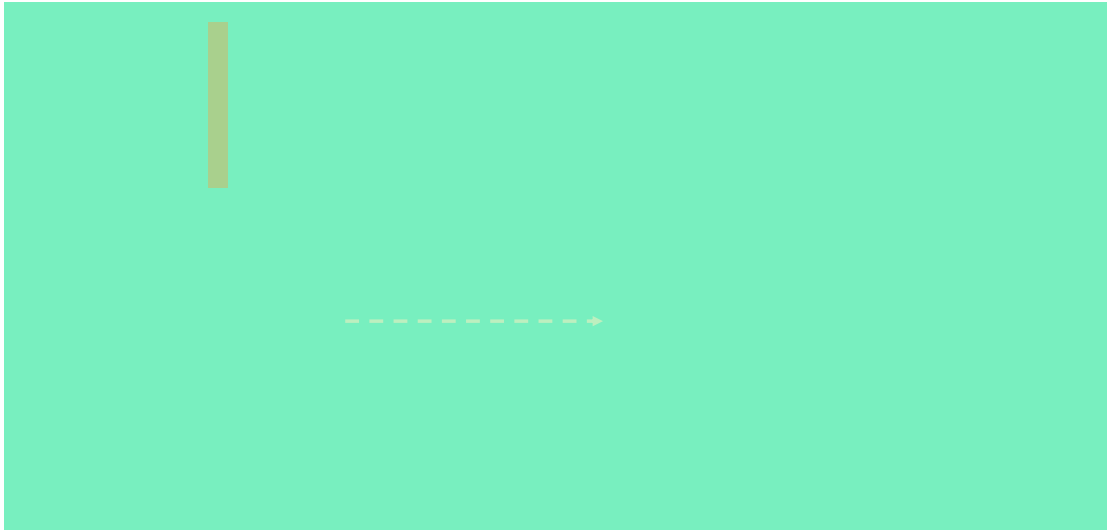
3.2. Dual Regression for Unpaired Data

We consider a more general SR case where there is no corresponding HR data w.r.t. the real-world LR data. More critically, the degradation methods of LR images are often unknown, making this problem very challenging. In this case, existing SR models often incur the severe adaptation problem [43, 54]. To alleviate this issue, we propose an efficient algorithm to adapt SR models to the new LR data. The training algorithm is shown in Algorithm 1.

Note that the dual regression mapping learns the underlying degradation methods and does not necessarily depend on HR images. Thus, we can use it to directly learn from the unpaired real-world LR data to perform model adaptation. To ensure the reconstruction performance of HR images, we also incorporate the information from paired synthetic data that can be obtained very easily (e.g., using the Bicubic kernel). Given M unpaired LR samples and N paired synthetic samples, the objective function can be written as:

$$\sum_{i=1}^{M+N} 1_{S_P}(x_i) L_P(P(x_i), y_i) + L_D(D(P(x_i)), x_i), \quad (2)$$

where $1_{S_P}(x_i)$ is an indicator function that equals 1 when $x_i \in S_P$, and otherwise the function equals 0.



We design a dual network to produce the down-sampled LR images from the super-resolved ones (See red lines in Figure 3). Note that the dual task aims to learn a down-sampling operation, which is much simpler than the primal task for learning the upscaling mapping. Thus, we design the dual model with only two convolution layers and a LeakyReLU activation layer [28], which has much lower computation cost than the primal model but works well in practice (See results in Section 5).

4.2. Theoretical Analysis

We theoretically analyze the generalization bound for the proposed dual regression scheme on paired data. Since the case with unpaired data is more complicated, we will investigate the theoretical analysis method in the future. Due to the page limit, all the definitions, proofs, and lemmas are put in the supplementary.

The generalization error of the dual regression scheme is to measure how accurately the algorithm predicts the unseen test data in the primal and dual tasks. Let $E(P, D) = E[L_P(P(x), y) + L_D(D(P(x)), x)]$ and $\hat{E}(P, D)$ is its empirical loss, we obtain a generalization bound of the proposed model using Rademacher complexity [30].

Theorem 1 Let $L_P(P(x), y) + L_D(D(P(x)), x)$ be a mapping from $X \times Y$ to $[0, C]$ with the upper bound C , and the function space H_{dual} be infinite. Then, for any error $\epsilon > 0$, with probability at least $1 - \epsilon$, the generalization error $E(P, D)$ (i.e., expected loss) satisfies for all $(P, D) \in H_{\text{dual}}$:

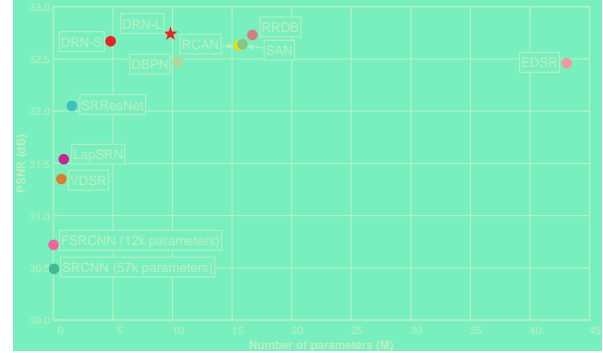
$$E(P, D) \leq \hat{E}(P, D) + 2\hat{R}_Z^{\text{DL}}(H_{\text{dual}}) + 3C \sqrt{\frac{1}{2N} \log \frac{1}{1-\epsilon}},$$

where N is the number of samples and \hat{R}_Z^{DL} is the empirical Rademacher complexity of dual learning. Let $B(P, D)$ be the generalization bound of the dual regression SR, i.e. $B(P, D) = 2\hat{R}_Z^{\text{DL}}(H_{\text{dual}}) + 3C \sqrt{\frac{1}{2N} \log \frac{1}{1-\epsilon}}$, we have

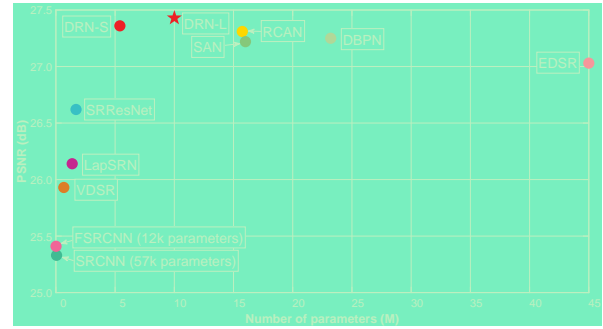
$$B(P, D) \leq B(P),$$

where $B(P)$, $P \in H$ is the generalization bound of the supervised learning w.r.t. the Rademacher complexity $\hat{R}_Z^{\text{SL}}(H)$.

This theorem shows the generalization bound of the dual regression scheme relies on the Rademacher complexity of a function space H_{dual} . From Theorem 1, the dual regression SR scheme has a smaller generalization bound than traditional SR method, and thus it helps to achieve more accurate SR predictions. More discussions can be referred to Remark 1. We highlight that the derived generalization bound of the dual regression scheme, where the loss function is bounded by $[0, C]$, is more general than [40]. Moreover, this generalization bound is tight when training data is sufficient, and the primal and dual models are powerful enough.



(a) Performance vs. model size for $4 \times$ SR.



(b) Performance vs. model size for $8 \times$ SR.

Figure 4. Comparisons of the performance and the number of parameters among different $4 \times$ SR models on the Set5 dataset.

Remark 1 Based on the definition of the Rademacher complexity, the capacity of the function space $H_{\text{dual}}: P \times D$ is smaller than the capacity of function space $H: P$ or $H: D$ in traditional supervised learning, i.e., $\hat{R}_Z^{\text{DL}} \leq \hat{R}_Z^{\text{SL}}$, where \hat{R}_Z^{SL} is the Rademacher complexity defined in supervised learning. In other words, the dual regression scheme has smaller generalization bound than the primal feed-forward scheme and the proposed dual regression scheme helps the primal model to achieve more accurate SR predictions.

5. Experiments

We extensively evaluate the proposed method on the image super-resolution tasks under the scenarios with paired Bicubic data and unpaired real-world data. All implementations are based on PyTorch.¹

5.1. Results on Supervised Image Super-Resolution

In this section, we first show an illustrated comparison in terms of performance and model size for $4 \times$ and $8 \times$ SR in Figure 4. Then, we provide a detailed comparison for $4 \times$ and $8 \times$ SR. In the experiments, we propose two models, namely a small model DRN-S and a large model DRN-L. We obtain the results of all the compared methods from their pretrained models, released code, or their original paper.

¹The source code is available at <https://github.com/guoyongcs/DRN>.

Table 1. Performance comparison with state-of-the-art algorithms for $4\times$ and $8\times$ image super-resolution. The bold number indicates the best result and the blue number indicates the second best result. "-" denotes the results that are not reported.

| Algorithms | Scale | #Params (M) | Set5 | Set14 | BSDS100 | Urban100 | Manga109 |
|-----------------|-------|-------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|
| | | | PSNR / SSIM | PSNR / SSIM | PSNR / SSIM | PSNR / SSIM | PSNR / SSIM |
| Bicubic | 4 | - | 28.42 / 0.810 | 26.10 / 0.702 | 25.96 / 0.667 | 23.15 / 0.657 | 24.92 / 0.789 |
| ESPCN [33] | | - | 29.21 / 0.851 | 26.40 / 0.744 | 25.50 / 0.696 | 24.02 / 0.726 | 23.55 / 0.795 |
| SRResNet [24] | | 1.6 | 32.05 / 0.891 | 28.49 / 0.782 | 27.61 / 0.736 | 26.09 / 0.783 | 30.70 / 0.908 |
| SRGAN [24] | | 1.6 | 29.46 / 0.838 | 26.60 / 0.718 | 25.74 / 0.666 | 24.50 / 0.736 | 27.79 / 0.856 |
| LapSRN [23] | | 0.9 | 31.54 / 0.885 | 28.09 / 0.770 | 27.31 / 0.727 | 25.21 / 0.756 | 29.09 / 0.890 |
| SRDenseNet [35] | | 2.0 | 32.02 / 0.893 | 28.50 / 0.778 | 27.53 / 0.733 | 26.05 / 0.781 | 29.49 / 0.899 |
| EDSR [26] | | 43.1 | 32.48 / 0.898 | 28.81 / 0.787 | 27.72 / 0.742 | 26.64 / 0.803 | 31.03 / 0.915 |
| DBPN [16] | | 10.4 | 32.42 / 0.897 | 28.75 / 0.786 | 27.67 / 0.739 | 26.38 / 0.794 | 30.90 / 0.913 |
| RCAN [51] | | 15.6 | 32.63 / 0.900 | 28.85 / 0.788 | 27.74 / 0.743 | 26.74 / 0.806 | 31.19 / 0.917 |
| SAN [8] | | 15.9 | 32.64 / 0.900 | 28.92 / 0.788 | 27.79 / 0.743 | 26.79 / 0.806 | 31.18 / 0.916 |
| RRDB [37] | | 16.7 | 32.73 / 0.901 | 28.97 / 0.790 | 27.83 / 0.745 | 27.02 / 0.815 | 31.64 / 0.919 |
| DRN-S | | 4.8 | 32.68 / 0.901 | 28.93 / 0.790 | 27.78 / 0.744 | 26.84 / 0.807 | 31.52 / 0.919 |
| DRN-L | | 9.8 | 32.74 / 0.902 | 28.98 / 0.792 | 27.83 / 0.745 | 27.03 / 0.813 | 31.73 / 0.922 |
| Bicubic | 8 | - | 24.39 / 0.657 | 23.19 / 0.568 | 23.67 / 0.547 | 20.74 / 0.515 | 21.47 / 0.649 |
| ESPCN [33] | | - | 25.02 / 0.697 | 23.45 / 0.598 | 23.92 / 0.574 | 21.20 / 0.554 | 22.04 / 0.683 |
| SRResNet [24] | | 1.7 | 26.62 / 0.756 | 24.55 / 0.624 | 24.65 / 0.587 | 22.05 / 0.589 | 23.88 / 0.748 |
| SRGAN [24] | | 1.7 | 23.04 / 0.626 | 21.57 / 0.495 | 21.78 / 0.442 | 19.64 / 0.468 | 20.42 / 0.625 |
| LapSRN [23] | | 1.3 | 26.14 / 0.737 | 24.35 / 0.620 | 24.54 / 0.585 | 21.81 / 0.580 | 23.39 / 0.734 |
| SRDenseNet [35] | | 2.3 | 25.99 / 0.704 | 24.23 / 0.581 | 24.45 / 0.530 | 21.67 / 0.562 | 23.09 / 0.712 |
| EDSR [26] | | 45.5 | 27.03 / 0.774 | 25.05 / 0.641 | 24.80 / 0.595 | 22.55 / 0.618 | 24.54 / 0.775 |
| DBPN [16] | | 23.2 | 27.25 / 0.786 | 25.14 / 0.649 | 24.90 / 0.602 | 22.72 / 0.631 | 25.14 / 0.798 |
| RCAN [51] | | 15.7 | 27.31 / 0.787 | 25.23 / 0.651 | 24.96 / 0.605 | 22.97 / 0.643 | 25.23 / 0.802 |
| SAN [8] | | 16.0 | 27.22 / 0.782 | 25.14 / 0.647 | 24.88 / 0.601 | 22.70 / 0.631 | 24.85 / 0.790 |
| DRN-S | | 5.4 | 27.41 / 0.790 | 25.25 / 0.652 | 24.98 / 0.605 | 22.96 / 0.641 | 25.30 / 0.805 |
| DRN-L | | 10.0 | 27.43 / 0.792 | 25.28 / 0.653 | 25.00 / 0.606 | 22.99 / 0.644 | 25.33 / 0.806 |

(a) Visual comparison for $4\times$ super-resolution.

(b) Visual comparison for $8\times$ super-resolution.

Figure 5. Visual comparison of different methods for (a) $4\times$ and (b) $8\times$ image super-resolution.

5.2. Datasets and Implementation Details

We compare different methods on five benchmark datasets, including SET5 [3], SET14 [47], BSDS100 [1], URBAN100 [21] and MANGA109 [29]. Two commonly used image quality metrics are adopted as the metrics, such as PSNR and SSIM [38]. Following [37], we train our models on DIV2K [34] and Flickr2K [26] datasets.

5.2.1 Comparison with State-of-the-art Methods

We compare our method with state-of-the-art SR methods in terms of both quantitative results and visual results. For

quantitative comparison, we compare the PSNR and SSIM values of different methods for $4\times$ and $8\times$ super-resolution. From Table 1, our DRN-S with about 5M parameters yields promising performance. Our DRN-L with about 10M parameters yields comparable performance with the considered methods for $4\times$ SR and yields the best performance for $8\times$ SR. For quality comparison, we provide visual comparisons for our method and the considered methods (See Figure 5). For both $4\times$ and $8\times$ SR, our model consistently produces sharper edges and shapes, while other baselines may give more blurry ones. The results demonstrate the effectiveness of the proposed dual regression scheme in gen-

Table 2. Adaptation performance of super-resolution models on images with different degradation methods for $8\times$ SR.

| Algorithms | Degradation | Set5 | Set14 | BSDS100 | Urban100 | Manga109 |
|--------------|-------------|---------------|---------------|---------------|---------------|---------------|
| | | PSNR / SSIM | PSNR / SSIM | PSNR / SSIM | PSNR / SSIM | PSNR / SSIM |
| Nearest | Nearest | 21.22 / 0.560 | 20.11 / 0.485 | 20.64 / 0.471 | 17.76 / 0.454 | 18.51 / 0.594 |
| EDSR [26] | | 19.56 / 0.580 | 18.24 / 0.498 | 18.53 / 0.479 | 15.68 / 0.435 | 17.22 / 0.598 |
| DBPN [16] | | 18.80 / 0.541 | 17.36 / 0.461 | 17.94 / 0.456 | 15.07 / 0.400 | 16.67 / 0.550 |
| RCAN [51] | | 18.33 / 0.534 | 17.11 / 0.436 | 17.67 / 0.444 | 14.73 / 0.380 | 16.25 / 0.525 |
| CinCGAN [43] | | 21.76 / 0.648 | 20.64 / 0.552 | 20.89 / 0.528 | 18.21 / 0.505 | 18.86 / 0.638 |
| DRN-Adapt | BD | 23.00 / 0.715 | 21.52 / 0.561 | 21.98 / 0.539 | 19.07 / 0.518 | 19.83 / 0.613 |
| EDSR [26] | | 23.54 / 0.702 | 22.13 / 0.594 | 22.71 / 0.567 | 19.70 / 0.551 | 20.64 / 0.700 |
| DBPN [16] | | 23.05 / 0.693 | 21.65 / 0.586 | 22.50 / 0.565 | 19.28 / 0.538 | 20.16 / 0.689 |
| RCAN [51] | | 22.23 / 0.678 | 21.01 / 0.567 | 21.85 / 0.552 | 18.36 / 0.509 | 19.34 / 0.659 |
| CinCGAN [43] | | 23.39 / 0.682 | 22.14 / 0.581 | 22.73 / 0.554 | 20.36 / 0.538 | 20.29 / 0.670 |
| DRN-Adapt | | 24.62 / 0.719 | 23.07 / 0.612 | 23.59 / 0.583 | 20.57 / 0.591 | 21.52 / 0.714 |

erating more accurate and visually promising HR images. More results are put in the supplementary.

We also compare the number of parameters in different models for $4\times$ and $8\times$ SR. Due to the page limit, we only show the results for $4\times$ SR and put the $8\times$ SR in the supplementary. From Figure 4, our DRN-S obtains promising performance with a small number of parameters. When we increase the number of channels and layers, the larger model DRN-L further improves the performance and obtains the best results. Both the empirical results and the theoretical analysis in Theorem 1 show the effectiveness of the proposed dual regression scheme for image super-resolution.

5.3. Adaptation Results on Unpaired Data

In this experiment, we apply the proposed method to a variety of real-world unpaired data. Different from the supervised setting, we first consider a toy case where we evaluate SR models on the LR images with different degradation methods (e.g., Nearest and BD [48]). During training, we can only access the LR images but not their corresponding HR images. Then, we also apply our method to LR raw video frames from YouTube.

5.3.1 Datasets and Implementation Details

In this experiment, we obtain the paired synthetic data by downsampling existing images. Considering the real-world SR applications, all the paired data belong to a different domain from the unpaired data (See more discussions in supplementary). Following [32], we randomly choose 3k images from ImageNet (called ImageNet3K) and obtain LR images using different degradation methods, including Nearest and BD. We adopt DIV2K (Bicubic) as the paired synthetic data² and ImageNet3K LR images with different degradations as the unpaired data. Note that ImageNet3K HR images are not used in our experiments. For the SR task

²We can also use other degradation methods to obtain the paired synthetic data. We put the impact of degradation methods in supplementary.

Figure 6. Visual comparison of model adaptation to real-world video frames (from YouTube) for $8\times$ SR.

on video, we collect 3k raw video frames as the unpaired data to train the models. In this section, we use our DRN-S model to evaluate the proposed adaptation algorithm and call the resultant model DRN-Adapt. More details can be found in supplementary.

5.3.2 Comparison on Unpaired Synthetic Data

To evaluate the adaptation performance on unpaired data, we compare our DRN-Adapt and the baseline methods on synthetic data. We report the PSNR and SSIM values of different methods for $8\times$ super-resolution in Table 2.

From Table 2, DRN-Adapt consistently outperforms the supervised methods on all the datasets. For CycleGAN based method, CinCGAN achieves better performance than the supervised learning methods but still cannot surpass our method due to the inherent limitations mentioned before. Note that, for Nearest LR data, we also report the recovering results of the Nearest kernel, which is the same as the degradation method. Our method also yields a large performance improvement over this baseline. These results demonstrate the effectiveness of the proposed adaptation algorithm.

5.3.3 Comparison on Unpaired Real-world Data

We apply our method to YouTube raw video frames, which are more challenging owing to the complicated and unknown degradation in real-world scenarios. Since there are

Table 3. The impact of the proposed dual regression scheme on super-resolution performance in terms of PSNR score on the five benchmark datasets for $4 \times$ SR.

| Model | Dual | Set5 | Set14 | BSDS100 | Urban100 | Manga109 |
|-------|------|-------|-------|---------|----------|----------|
| DRN-S | | 32.53 | 28.76 | 27.68 | 26.54 | 31.21 |
| | | 32.68 | 28.93 | 27.78 | 26.84 | 31.52 |
| DRN-L | | 32.61 | 28.84 | 27.72 | 26.77 | 31.39 |
| | | 32.74 | 28.98 | 27.83 | 27.03 | 31.73 |

Table 4. Effect of the hyper-parameter α in Eqn. (1) on the performance of DRN-S (testing on Set5) for $4 \times$ SR.

| | 0.001 | 0.01 | 0.1 | 1.0 | 10 |
|--------------|-------|-------|-------|-------|-------|
| PSNR on Set5 | 32.57 | 32.61 | 32.67 | 32.51 | 32.37 |

no ground-truth HR images, we only provide the visual comparison. From Figure 6, the generated frames from three supervised baselines (i.e., EDSR, DBPN, and RCAN) contain numerous mosaics. For CinCGAN, the SR results are distorted and contain a lot of noise due to the sensitivity to data differences between unpaired LR and HR images. By contrast, our DRN-Adapt produces visually promising images with sharper and clearer textures. Due to the page limit, we put more visual results in the supplementary.

6. Further Experiments

6.1. Ablation Study on Dual Regression Scheme

We conduct an ablation study on the dual regression scheme and report the results for $4 \times$ SR in Table 3. Compared to the baselines, the models equipped with the dual regression scheme yield better performance on all the datasets. These results suggest that the dual regression scheme can improve the reconstruction of HR images by introducing an additional constraint to reduce the space of the mapping function. We also evaluate the impact of our dual regression scheme on other models, e.g., SRResNet [24] based network (See more details in the supplementary).

6.2. Effect of α on DRN

We conduct an experiment to investigate the impact of the hyper-parameter α in Eqn. (1). From Table 4, when we increase α from 0.001 to 0.1, the dual regression loss gradually becomes more important and provides powerful supervision. If we further increase α to 1 or 10, the dual regression loss term would overwhelm the original primal regression loss and hamper the final performance. To obtain a good tradeoff between the primal and dual regression, we set $\alpha = 0.1$ in practice.

6.3. Effect of β on Adaptation Algorithm

We investigate the effect of β on the proposed adaptation algorithm. We compare the performance when we change the data ratio of unpaired data β and show the corresponding training curves in Figure 7. From Figure 7, when we set

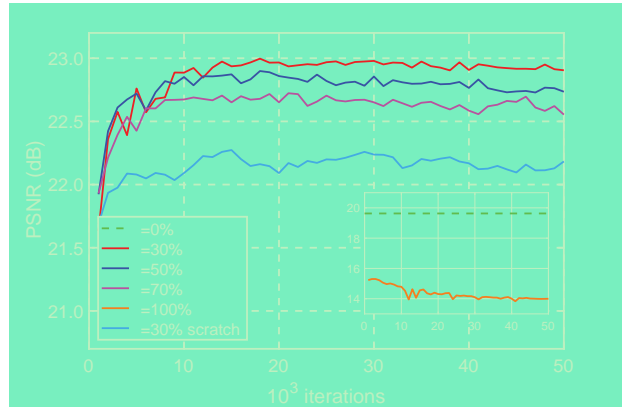


Figure 7. Comparisons of the performance on unpaired data with Nearest degradation (testing on Set5) for $4 \times$ SR.

$\beta \in \{30\%, 50\%, 70\%\}$, the resultant models obtain better performance than the baseline model, i.e., with $\beta = 0\%$. In practice, we set $\beta = 30\%$ to obtain the best performance. We also compare the models with and without the pretrained parameters. From Figure 7, the model trained from scratch yields slightly worse result but still outperforms the baseline model without adaptation. These results demonstrate the effectiveness of the proposed adaptation algorithm.

7. Conclusion

In this paper, we have proposed a novel dual regression scheme for paired and unpaired data. On the paired data, we introduce an additional constraint by reconstructing LR images to reduce the space of possible functions. Thus, we can significantly improve the performance of SR models. Furthermore, we also focus on the unpaired data and apply the dual regression scheme to real-world data, e.g., raw video frames from YouTube. Extensive experiments on both paired and unpaired data demonstrate the superiority of our method over the considered baseline methods.

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